Stationary Frame Current Control Evaluations for Three-Phase Grid-Connected Inverters with PVR-based Active Damped LCL Filters

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Abstract

Grid-connected inverters (GCIs) with LCL output filter have the ability of attenuating high-frequency (HF) switching ripples. However, by using only grid-current control, the system is prone to resonances if it is not properly damped, and the current distortion would be amplified significantly under highly distorted grid conditions. In this paper, a synchronous reference frame equivalent proportional-integral (SRF-EPI) controller in αβ stationary frame using the parallel virtual resistance-based active damping (PVR-AD) strategy for grid-interfaced distributed generation (DG) systems to suppress the LCL resonance is proposed. Although both proportional-resonant (PR) controller in αβ stationary frame and PI controller in dq synchronous frame achieve zero steady-state error, the amplitude- and phase-frequency characteristics differ greatly from each other except for the reference tracking at fundamental frequency. Therefore, an accurate SRF-EPI controller in αβ stationary frame is established to achieve precise tracking accuracy. Moreover, the robustness, harmonic rejection capabilities, and influence of control delay are investigated by the Nyquist stability criterion when the PVR-based AD method is adopted. Furthermore, the grid voltage feed-forward and multiple PR controllers are integrated in the current loop to mitigate the current distortion introduced by the grid background distortion. Besides, the parameters design guidelines are presented to show the feasibility and effectiveness of the proposed strategy. Finally, simulation and experimental results are provided to validate the feasibility of the proposed control approach.

Key words: Synchronous frame equivalent PI, active damping, stability, LCL filter, PVR-AD scheme

I. INTRODUCTION

Recently, distributed generation (DG) systems based on renewable energy systems, such as photovoltaics and wind turbines, are attracting more and more attention. These renewable energy sources are usually installed in a distributed way and as an interface between DGs and the network, a grid-connected inverter (GCI) plays an important role in ensuring high-quality power to be injected to the grid [1-4].

In a GCI, an L filter or an LCL filter is usually used as an interface between the inverter and the grid. However, if only an inductor is used, high-frequency (HF) switching is needed to ensure that no excessive switching ripples are generated from the pulse-width modulation (PWM) process, which would be accompanied by undesirable problems of excessive switching losses and electromagnetic interference (EMI), especially in high-power applications [5]. Compared to the classical L filter, an LCL filter has better attenuation capacity of the switching harmonics and better dynamic characteristics,
which usually yields to a lower volume and cost [6]. However, the LCL filter is a three-order system and instability problems may occur at the resonant frequency, thus proper damping solutions are mandatory to stabilize the whole system [7].

The ways to damp the resonance problems can be classified into passive damping (PD) and active damping (AD) methods. PD is achieved by inserting an additional resistor in series or parallel with the filter inductor or filter capacitor [8]. The PD scheme by adding a resistor in series with the filter capacitor has been widely adopted for its simplicity and highly reliability. However, the additional resistor will result in power loss and decrease the attenuation of the LCL filter [9]. In order to overcome these drawbacks, the concept of virtual resistor was proposed, which is called AD method [10], [11]. An interesting control strategy based on the feedback of the splitting capacitor current was proposed in [12]. With this method, the injected current is not controlled directly and the damping capability relies on the LCL parameters. Therefore, among the AD methods, the method involving feedback of the capacitor current has attracted considerable attention due to its simple implementation and wide application [2], [13-17].

Another interesting approach, which is the main focus of this work, is to consider the current controller implementation so that a better performance is ensured. It is well-known that the proportional integral (PI) controller has an infinite gain for dc component, thus guarantees a precise tracking for dc references without steady-state error. However, for ac references, the PI controller would lead to steady-state error due to the finite gain at the selected frequency [18], [19]. The proportional resonant (PR) controller can provide infinite gain at the selected resonant frequency to suppress the effect of the unwanted harmonics, thus ensuring zero steady-state error when tracking an ac reference at the selected frequency [20-22]. On the other hand, by applying PI controller in dq synchronous frame, one can ensure zero steady-state error, since the ac signal is transformed into dc signal, thus infinite gain is achieved by the PI controller at the dc component [23], [24]. However, the synchronous frame PI control scheme requires accurate phase synchronization of the grid voltage by using a phase-locked-loop (PLL), which may deteriorate the tracking performance under grid disturbances [24]. Moreover, the straightforward analysis method which is named PI model, i.e., to replace the PI controller in dq synchronous frame with PI plus resonant controller in abc stationary frame. However, the approximation is not accurate and the coupling terms are ignored, either [25]. In [26], an accurate synchronous frame equivalent PI (SRF-PI) in stationary frame with L filter was presented, which shows robust performance under a wide frequency range. However, the system with the LCL resonance is not considered and the effects of the power-stage parameter deviations and the grid background distortion were not taken into account, and the discrete model and the control delay effect were also neglected.

This paper proposes a novel parallel virtual resistance (PVR)-based AD method integrated with the SRF-PI control strategy in abc stationary frame for three-phase grid-connected inverter with an LCL filter. The multiple PR controllers and the grid voltage feed-forward loop for improving tracking precision under background grid distortion conditions are investigated when the proposed strategy is used. Moreover, the SRF-PI, PI and PR controllers are analyzed, designed and compared, which show the feasibility and effectiveness of the proposed strategy.

This paper is organized as follows. In Section II, the system description and the proposed control scheme are presented. The damping characteristics of the various PD schemes, the series virtual resistance (SVR)- and PVR-based AD strategies are analyzed, and the use of the SRF-PI, PI and PR controllers are compared in the stationary frame. Section III presents the parameters design guidelines. The impact of LCL-parameter variations based on the SRF-PI controller in the stationary frame is studied as well. Section IV presents the simulation and experimental results of a 2.2 kVA three-phase DG system. Finally, Section V concludes this paper.

Fig. 1. System topology and control strategy of the three phase grid-connected inverters with LCL filter.
II. SYSTEM DESCRIPTION AND CONTROL SCHEME

Fig. 1 shows the topology of three-phase grid-connected voltage source inverter (VSI) based on the LCL filter, where the inductor parasitic resistances are neglected. In addition, the switch is used to choose the current controllers and $G_{ref}(s)$, $G_{eq}(s)$, and $G_{ref}(s)$ correspond to the PI controller, the SRF-EPI controller, and the PR controller, respectively. To achieve a good filtering performance, the resonance frequency of LCL filter should be in the range of $10f_0 < f_{res} < f_s/2$, where $f_0$ denotes the fundamental frequency, $f_{res}$ represents the resonance frequency, and $f_s$ is the switching frequency [7], [18], [27]. Based on these guidelines, the parameters of the power-stage are given in Table I.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Quantity</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$U_{dc}$</td>
<td>Input voltage amplitude</td>
<td>650 V</td>
</tr>
<tr>
<td>$u_g$</td>
<td>Grid voltage</td>
<td>311 V</td>
</tr>
<tr>
<td>$T_s$</td>
<td>Sampling and switching period</td>
<td>100 μs</td>
</tr>
<tr>
<td>$\omega_0$</td>
<td>Fundamental angular frequency</td>
<td>$100\pi$ rad/s</td>
</tr>
<tr>
<td>$C$</td>
<td>Capacitor</td>
<td>10 μF</td>
</tr>
<tr>
<td>$L$</td>
<td>Converter-side inductor</td>
<td>1.8 mH</td>
</tr>
<tr>
<td>$L_g$</td>
<td>Grid-side inductor</td>
<td>1.8 mH</td>
</tr>
</tbody>
</table>

A. Stationary Frame SRF-EPI, PI and PR Controllers

A major objective for ac current regulators is to achieve zero phase and magnitude errors. Here, the synchronous reference frame equivalent PI (SRF-EPI) controller in the stationary frame was presented as an alternative solution for fundamental frequency reference signal tracking purposes [26], [28].

The synchronous reference frame equivalent integral controller is $F(\theta)$, and $n<0$ means the signal is in negative sequence.

$$ F = \begin{cases} \infty & n=1 \\ \frac{2k_i}{\omega_0 |n|} & n \neq 1 \end{cases}, \quad \theta = \begin{cases} 0^\circ & n=1 \\ -90^\circ (n>1) \cup (n<0) \\ 90^\circ & 0<n<1 \end{cases} \quad (1) $$

The proportional (P) controller in $dq$ synchronous frame is the same as the $P$ controller in the $a\beta$ frame. Then, the SRF-EPI controller transfer function is $G_v(s) = k_p + F(\theta) = k_p + F \cos \theta + jF \sin \theta \quad (2)$

Compared with the SRF-EPI controller, the integral and resonant models of PI and PR models are given by

$$ F_i = \begin{cases} \infty & n=0 \\ \frac{k_i}{\omega_0 |n|} & n \neq 0 \end{cases}, \quad \theta_i = -90^\circ \quad (3) $$

$$ F_r = \begin{cases} \infty & n=1 \\ \frac{2k_i}{\omega_0 (n^2 + 1)} & n \neq 1 \end{cases}, \quad \theta_r = \begin{cases} 0^\circ & n=1 \\ -90^\circ & n>1 \\ 90^\circ & n<1 \end{cases} \quad (4) $$

The PI and PR current controller are obtained by substituting (3) and (4) into (2), respectively.

Fig. 2 shows the bode plots of the equivalent model $G_{eq}(s)$, the resonant and integral controllers for the fundamental frequency signal tracking. It can be seen that the models show remarkable differences from each other in the low frequency range, thus the direct implementation of the PR or PI model to predict system performance would lead to inaccurate result. As for the phase characteristic, equivalent PI controller $G_{eq}(s)$ in positive sequence shows the same phase characteristic with resonant model, while $G_{eq}(s)$ in the negative sequence shows the same phase-frequency characteristic with integral model.

![Fig. 2. Bode plots of the integral controller, resonant controller, and equivalent integrator controller in positive and negative sequences.](image)

B. Passive Damping under Grid Current Feedback

As shown in Fig. 3, the grid current is conventionally used as a feedback variable of the current controller to regulate the current injected into the grid. An amplitude peak exists at the resonant frequency of the LCL filter, which would limit the design procedure of the current control-loop [6], [29].

Fig. 3. Block diagram of various PD methods under grid current control for the three-phase inverter with LCL output filter.

The direct way to damp the LCL filter resonance is to insert a passive resistor in the inductor or capacitor of the LCL filter. In this case, the open-loop transfer functions of the grid current feedback control algorithm with various passive damping (PD) methods can be obtained as

$$ G_{Series - L}(s) = \frac{G_p(s)G_{in}(s)}{s^2LLC + sCLR_{dL} + s(L + L_g) + R_{dL}} \quad (5) $$

$$ G_{Parallel - L}(s) = \frac{G_p(s)G_{in}(s)(sL + R_{dL})}{s^2LLC + sCLR_{dL} + s(L + L_g) + R_{dL}} \quad (6) $$
where $G_m(s)=U_{dc}/U_{in}$ is the gain of the PWM inverter, $U_{dc}$ is the inverter dc voltage, and $U_{in}=1$ is the carrier amplitude. $G_{Series-C}$ and $G_{Series-Lg}$ represent the open-loop transfer functions from $i_{ref,αβ}$ to $i_{g,αβ}$ when damping resistor is connected in series with $L$ and $L_{ig}$, respectively. $G_{Parallel-C}$ and $G_{Parallel-Lg}$ represent the open-loop transfer functions when the damping resistor is connected in parallel with $L$ and $L_{ir}$, respectively. $G_{Series-C}$ and $G_{Parallel-C}$ are the open-loop transfer functions when damping resistor is connected in series and parallel with $C$, respectively.

Fig. 4 shows the bode plots of the open-loop transfer functions with various PD schemes using the parameters in Table I when a PI current regulator is used. As shown in Fig. 4(a), the LCL filter with PD methods has less attenuation in the low frequency (LF) region when a series resistor is connected with $L$ or $L_{ig}$. The less attenuation is caused in the HF region when a parallel resistor is connected with $L$ or $L_{ir}$ which is shown in Fig. 4(b). As shown in Fig. 4(c), it can be seen that the less attenuation is also caused when a series resistor is connected with $C$. As shown in Fig. 4(d), there is no impact on the LF and HF regions when a parallel resistor is connected with $C$. However, an excessive power loss is always existing among the various PD schemes.

C. Virtual Resistance based Active Damping (AD) Strategy

Compared with PD method, active damping (AD) strategy is more flexible and more efficient, which adopts virtual resistor to eliminate power loss and can be easily incorporated to the existing control algorithm. The block diagram transformation of traditional virtual resistor in series with capacitor is derived in Fig. 5. It is reported that, the series virtual resistance based AD (SVR-based AD) needs to introduce differential element and it will cause noise amplification problems and the system can be unstable due to HF interference [17].

![Diagram showing block diagram transformation of virtual resistor in series with capacitor.](image)

Fig. 5. Block diagram transformation of virtual resistor in series with capacitor. (a) Passive damping of capacitor series with resistor. (b) Equivalent SVR-based AD.

Therefore, an effective parallel virtual resistance based active damping (PVR-based AD) method in parallel with capacitor for LCL filter is proposed in this paper, which avoids the LCL resonance problems, and the satisfactory stability and robustness can be achieved. The principle diagram and its block diagram transformations of PVR-based AD are shown in Fig. 6.

The transfer function of the PVR-based AD describing the grid current $i_{g,αβ}$ as a function of voltage $u_{g,αβ}$ is given by

$$G_{active-αβ}(s) = \frac{i_{g,αβ}(s)}{u_{g,αβ}(s)} = \frac{1}{s(L_{ir}C_{r}^2 + R_{d,eq}L_{ir}C_{r} + (L + L_{ir}))}$$

where $R_{d,eq}$ is an equivalent proportional term, $R_{d,eq} = L/C_{r}$.

According to Fig. 6(b), the open-loop transfer function of the PVR-based AD is given by
\[ G_{\text{open}}(s) = \frac{G_c(s)G_{\text{inv}}(s)}{LLC_s^2 + R_{d,eq}L_sCs^2 + (L + L_s)s} \] (10)

Fig. 6. Block diagram transformations of the PVR-based AD method. (a) PD scheme using parallel-connected resistor across capacitor. (b) Block transformation of PD control strategy in (a). (c) The block diagram of parallel virtual resistance active damping.

Fig. 7. Bode plots of the open-loop transfer function with PVR-based AD strategy.

From (10), it shows that there is no unstable open-loop poles, i.e., \( P=0 \). If the PI current controller is used, by using the parameters in Table I, the bode plots of the open-loop transfer function \( G_{\text{open}}(s) \) with AD method when \( R_{d,eq} = 0, 8 \) and 26 is illustrated in Fig. 7, respectively. The corresponding parallel virtual resistor \( R_d \) is \( \infty \), 22.5 \( \Omega \) and 6.9 \( \Omega \), respectively. According to Nyquist stability criterion [7], the system is stable if \( Q=0 \)

\[ Q = P + N_c - N \] (11)

where \( P \) is the number of unstable open-loop poles, \( N_c \) and \( N \) are the number of times that the path crosses the line in the clockwise and counter-clockwise directions. Hence, there is a one-to-one correspondence between positive half of Nyquist plot and the open-loop bode plot, and the \( N_c \) and \( N \) are two times the numbers of positive (from lower to upper) and negative (from upper to lower) crossings of \( (2k+1)\pi \) \( (k \) is an integer) in the open-loop bode plot in the frequency range with gains above 0 dB. For minimum phase system, i.e., \( P=0 \), the system is stable if \( N_c=N \) [29], [30].

1) When \( R_{d,eq}=0 \), the \( PH-F \) contour cross -180° from upper to lower at \( f_{ref} \) (in \( Mag>0 \) dB region). Thus, when \( P=0, N=0, N_c=2, \) and \( Q=2 \), the system is unstable.

2) When the feedback gain \( R_{d,eq} \) increases, the \( PH-F \) contour cross -180° outside the \( Mag>0 \) dB region if the value of \( R_{d,eq} \) is appropriate. Thus, when \( P=0, N=0, N_c=0, \) and \( Q=0 \), the system is stable. The case for \( R_{d,eq} =0, 8, 26 \) is shown in Fig. 8, respectively.

In order to intuitively show variation tendency of system stability when \( R_{d,eq} \) varies, the discrete pole-zero map for feedback gains \( R_{d,eq} \) increases from 0 to 36 is illustrated in Fig. 8 by using the ZOH method. It can be seen that the system stability changes along with delay time. The discrete open-loop transfer function of current controller using PVR-based AD scheme is

\[ G_{\text{open}}(z) = G_c(z) \times \left[ 1 - e^{-zT_s} \right] \times \frac{1}{GC(s)G_{\text{inv}}(s)} \]

(12)

(13)

where \( G_c(s) \) represents the delay in digital control, \( T_s \) is delay time and it is related with analog-digital sampling process, PWM generation process, and hardware filtering [6], [26], [30]. The PWM switching frequency and the sampling frequency of the digital current controller are both selected to be 10 kHz.

Fig. 8. Pole-zero map for close-loop transfer function with PVR-based AD strategy. (a) No delay. (b) 3/2\( T_s \) delay
Fig. 9. Bode plots of PVR-based AD scheme compared with PD and no damping strategies.

Fig. 10. Step response of the PVR-based AD scheme with different $R_{d,eq}$.

Fig. 11. Block diagram transformation of the PVR-based AD control algorithm with the grid voltage feed-forward loop.

The block diagram transformation of the PVR-based AD algorithm with the grid voltage feed-forward loop is shown in Fig. 11, and the current injected into the grid can be derived as

$$i_{q,eq}(s) = \frac{W(s)}{1+W(s)} - G_s(s)G_1(s) = \frac{1}{1+W(s)} G_s(s)u_{q,ref}(s)$$

where

$$G_s(s) = \frac{G_r(s)G_m(s)}{s^2LC + sCR_{d,eq} + 1}$$

and $W(s) = G_1(s)G_2(s)$.

The transfer function from the grid voltage to the grid side current with PVR-based AD is derived as

$$u_{q,eq}(s) = \frac{s^2LC + sCR_{d,eq} + 1}{G_c(s)G_m(s) + s^2LLCL + s^2CL_{R_{d,eq}} + s(L + L_c)}$$

Fig. 12. Bode plots comparison of disturbance voltage to grid current of the harmonic admittance without the feed-forward of grid voltage.

Fig. 12 shows the bode plots of (18) under no damping, PD
and PVR-based AD cases without feed-forward of grid voltage. It can be observed that a voltage disturbance near the resonance frequency results in large input currents under no damping case. However, the PD and PVR-based AD schemes provide efficient resonance damping characteristics, and the PVR-based active damping scheme shows additional damping performance without causing additional power losses.

In order to mitigate the effect of the grid voltage on the quality of LCL-filter currents, a feed-forward loop of the grid voltage and the multiple resonant regulators at the harmonic frequencies of grid voltages are applied in the current loop. According to (15), setting \( 1-G_{\text{R}}(s)G_{i}(s) \) to zero and adopting approximate full compensation approach, the feed-forward function is derived as

\[
G_{\text{f}}(s) = \frac{1}{G_{i}(s)} = \frac{s^2LC + sCR_{\text{eq}} + 1}{G_{r}(s)G_{\text{m}}(s)} \tag{19}
\]

Considering that derivative functions are difficult to be implemented and mainly for middle- and higher-frequency harmonics, and the noise amplification problems would reduce the stability margin, hence (19) is approximated by a first order low pass filter, and the higher order differential terms are neglected to avoid high frequency instabilities \([29, 33]\). As shown in Fig. 11(a), if the feed-forward control lies behind the current controller, the feed-forward factor has a very simple form and the proportional feed-forward is adopted, and \( G_{\text{f}}(s)=1/G_{\text{m}}(s) \). Moreover, the multiple resonant controllers are achieved by paralleling several resonant blocks tuned to the desired harmonic frequencies to be compensated, which is expressed as

\[
G_{i}(s) = \sum_{k=5,7,11...}^{\infty} \frac{2K_{i0}^{*}s}{s^2 + (k\omega_0)^2} \tag{20}
\]

where \( h \) is the harmonic order to be compensated, \( \omega_0 \) represents the fundamental frequency, and \( K_{i0}^{*} \) represents the respective resonant gain, which should be tuned relatively high, but within the stability limits, for minimizing the steady-state error. The dynamics of the fundamental PI, PR and SRF-EPI controllers in the stationary frame is unaffected when the multiple resonant controllers are added, since the resonant controllers compensate only for frequencies that are very close to the selected resonant frequencies.

### III. DESIGN GUIDELINES

#### A. Stability of the SRF-EPI, PI and PR Controllers

The resonance damping and dynamic response have been taken into consideration for the aforementioned active damping design procedure. Thus, the current regulator \( G_{\text{c}}(s) \) is designed to maintain suitable PM, GM and cutoff frequency \( f_c \). Generally, PM in the range of 30°–60° and GM≥3–6 dB are adopted for a compromise among the stability, dynamic response and robustness \([10, 14]\).

The cutoff frequency \( f_c \) is typically restricted lower than \( f_r \) considering the effect of attenuating HF noise and \( f_c \) generally can be chosen lower than 1/10 of \( f_r \). Therefore, considering the frequency response of the system below the cutoff frequency, the influence of the capacitor of LCL filter can be ignored and \( G_{\text{open}}(s) \) can be approximated as

\[
G_{\text{open}}(s) \approx \frac{G_{c}(s)G_{\text{m}}(s)}{(L+L_{e})s} \tag{21}
\]

Here, PI controller is adopted to design the parameters for the PR controller and SRF-EPI controller for comparison. At the cutoff frequency, the magnitude-frequency characteristic of the open-loop system is zero, hence

\[
20\log |G(j2\pi f_c)| = 20\log \left| \frac{k_{g}G_{\text{m}}(s)}{(L+L_{e})j2\pi f_c} \right| = 0 \tag{22}
\]

Thus, the controller gain \( k_{g} \) is approximately represented as

\[
k_{g} \approx \frac{2\pi f_c(L+L_{e})}{G_{\text{m}}(s)} \tag{23}
\]

showing that \( f_c \) is approximately proportional to \( k_{g} \). Therefore, a larger \( k_{g} \) means a faster dynamic response and a larger loop gain at low frequencies.

The steady-state error of \( i_{e,q0}^{*} \) at fundamental frequency \( \omega_0 = 2\pi f_0 \) is an important index of the controller parameters design. As given by (15), assuming adoption of grid feed-forward control, the steady-state tracking error of grid current \( i_{e,q0}^{*} \) can be calculated as

\[
E_{e}(s) = \frac{i_{e1}(s) - i_{e0}(s)}{i_{e0}(s)} = \frac{W(s)}{1+W(s)} - 1 \tag{24}
\]

![Fig. 13. Bode plots of the open-loop transfer function with PVR-based AD strategy.](image)

The fundamental components of \( i_{e2} \) and \( u_{e,q0}^{*} \) are denoted by \( i_{e2}^{*} \) and \( u_{e}^{*} \), respectively. As the influence of the filter capacitor is negligible at fundamental frequency \( f_0 \), considering (18), \( i_{e2}^{*} \) can be approximated as

\[
i_{e2}^{*} \approx -\frac{u_{e}^{*}}{G_{\text{m}}G_{c}(j2\pi f_0)} \tag{25}
\]

Considering equation (21) and (25), \( I_{e2} \) can be derived as

\[
I_{e2} \approx \frac{U_{e}}{G_{\text{m}}[G_{c}(j2\pi f_{0})]} \approx \frac{U_{e}}{2\pi f_{0}[G_{\text{open}}(j2\pi f_{0})]} \tag{26}
\]

where \( I_{e2} \) and \( U_{e} \) are the root mean square (RMS) values of \( i_{e2}^{*} \) and \( u_{e}^{*} \), respectively.

According to (21) and the transfer function of PI controller, (26) can be rewritten as
According to (17) and (18), the PM of the system can be expressed as

$$PM = 180^\circ + \frac{G_{a}(s)G_{m}(s)}{L_{f}C_{s}^2 + R_{f}C_{s} + (L + L_{g})} \left( \frac{G_{a}(s)G_{m}(s)}{L_{f}C_{s}^2 + R_{f}C_{s} + (L + L_{g})} \right) \left( \frac{G_{a}(s)G_{m}(s)}{L_{f}C_{s}^2 + R_{f}C_{s} + (L + L_{g})} \right)$$

Substituting the transfer function of PI into (29), and

$$PM = \arctan \frac{2\pi L}{k_{p}} - \frac{k_{i}}{2\pi f_{c} k_{p}}$$

Then, (30) can be rewritten as

$$k_{i} = \frac{2\pi L}{k_{p}} - \frac{k_{i}}{2\pi f_{c} k_{p}}$$

Using parameters of Table I, the resonance frequency $f_{res}$ of LCL filter is equal to 1.68 kHz, and the value of the cutoff frequency $f_{c}$ is selected as 600 Hz. In addition, the PM is selected as 50 degrees. With the system parameters given in Table I, the SRF-EPI, PI and PR controller parameters are selected as $k_{p}=0.02$, $k_{i}=5.77$. The bode plots of the open-loop transfer function with PVR-based AD scheme of the SRF-EPI controller in the $\alpha\beta$ frame, the bode plots of the compensated loop gain considering the variations of the LCL filter parameters are given in Fig. 14. The grid impedance is considered as a part of the LSRF parameter $L_{g}$. It is found that, although $C$ varies from 7 to 13 $\mu$F (10 $\mu$F $\pm$ 30%), $L$ varies from 1.26 to 2.34 mH (1.8 mH $\pm$ 30%), or $L_{g}$ varies from 1.26 to 3.6 mH (1.8 mH - 30% - +100%), the lowest cutoff frequency is still higher than 417 Hz, the PM is larger than 37.7 degrees, the GM is larger than 9.84 dB. The frequency response characteristics in Fig. 14 verify that the designed system has a strong robustness.

IV. SIMULATION AND EXPERIMENTAL RESULTS

In order to verify the effectiveness of the proposed control strategies, the simulation and experimental results of the proposed control strategy are presented and compared. The simulation studies were implemented using Matlab/Simulink. As shown in Fig. 15, the experimental setup was built and tested, which consists of two 2.2 kW Danfoss inverters, one working as grid-connected inverter and the other controlled in voltage control mode to emulate the grid with distortion. The dSPACE1006 platform was used to implement the control algorithms. In order to provide effective comparison, all the control parameters are the same for the simulation and experiments. The system parameters are given in Table I and the SRF-EPI, PI and PR controllers parameters are selected as $k_{p}=0.02$, $k_{i}=5.77$. 

Fig. 14. Bode plots of the system considering the variations of the LCL filter parameters with PVR-based AD strategy. (a) $C$: 10 $\mu$F $\pm$ 30%. (b) $L$: 1.8 mH $\pm$ 30%. (c) $L_{g}$: 1.8 mH -30% $\sim$ +100%.

$$G_{open}(f_{0}) = 20\log |G_{open}(j2\pi f_{0})| = 20\log \left| \frac{G_{m}(k_{p} + \frac{k_{i}}{j2\pi f_{0}(L + L_{g})}}}{j2\pi f_{0}(L + L_{g})} \right|$$

Substituting (23) into (27), the integration gain is derived as

$$k_{i} = \frac{4\pi^{2} f_{c}^{2}(L + L_{g})}{G_{m}} \left( 10^{\frac{G_{m}(f_{c}^{2} + f_{0}^{2})}{2\pi f_{c}^{2}}} - f_{c}^{2} \right)$$

$$G_{open}(f_{0}) = 20\log |G_{open}(j2\pi f_{0})| = 20\log \left| \frac{G_{m}(k_{p} + \frac{k_{i}}{j2\pi f_{0}(L + L_{g})}}}{j2\pi f_{0}(L + L_{g})} \right|$$

When tracking the fundamental frequency reference. Thus, the SRF-EPI controller has a better performance than the PI and PR controllers in all frequencies when they are used in stationary frame. Except for reference tracking at the fundamental frequency, the SRF-EPI controller in stationary frame is not equivalent to PI or PR controller in the $\alpha\beta$ frame. 

B. IMPACTS OF LCL-PARAMETER VARIATIONS

In fact, filter parameters drift away from the rated values due to the parasitic parameters variations, the operating conditions, temperature and grid impedance impact [10], [34]. To examine the robustness of the system with PVR-based AD scheme of the SRF-EPI controller in the $\alpha\beta$ frame, the bode plots of the compensated loop gain considering the variations of the LCL filter parameters are given in Fig. 14. The grid impedance is considered as a part of $L_{g}$. It is found that, although $C$ varies from 7 to 13 $\mu$F (10 $\mu$F $\pm$ 30%), $L$ varies from 1.26 to 2.34 mH (1.8 mH $\pm$ 30%), or $L_{g}$ varies from 1.26 to 3.6 mH (1.8 mH - 30% - +100%), the lowest cutoff frequency is still higher than 417 Hz, the PM is larger than 37.7 degrees, the GM is larger than 9.84 dB. The frequency response characteristics in Fig. 14 verify that the designed system has a strong robustness.
The simulation and experimental results of the steady-state waveforms for different controllers in stationary frame with the proposed PVR-based AD method are shown in Fig. 17 and Fig. 21, respectively. As shown in Fig. 17, the fundamental RMS value of $i_{\omega}$ (A phase) in Fig. 17(a), (b) and (c) are 1.63 A, 1.422 A and 1.42A with a reference value of 1.414 A (RMS). The measured steady-state errors in Fig. 17(a), (b) and (c) are 15.3%, 0.57% and 0.42% respectively and the total harmonic distortion (THD) are 1.22%, 1.16% and 1.12%, respectively. As shown in Fig. 21, the measured steady-state errors in Fig. 21(a), (b) and (c) are consistent with simulation results. However, the current THD are 1.28%, 4.8% and 4.75%, respectively. It is noted that the THDs of the experimental results with the PR and SRF-EPI controllers are worse than that of the PI controller because the current of the PI controller has a higher amplitude due to the effect of steady state error. Therefore, the sufficient accuracy can be achieved by using SRF-EPI controller, which is slightly better than the PR controller.

The simulation and experimental results of the transient responses when the reference steps up from 1.0 kW to 2.0 kW for different controllers in stationary frame with the PVR-based AD method are shown in Fig. 18 and Fig. 22, respectively. As shown in Fig. 18, good dynamic performances are achieved when the PR and SRF-EPI controllers in the a/β frame are adopted. Fig. 22 shows that the transient response of the SRF-EPI controller is slightly better than PR controller. The experimental results are consistent and in good agreement with the theoretical analysis and simulation results.

In order to evaluate the robustness of the SRF-EPI control scheme with the PVR-based AD method, the simulation and experimental results under different virtual parallel resistance in case of control delay and the effect of grid voltage harmonics are presented.

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Fig. 15 Experimental setup.

Fig. 16. Simulation result of the SRF-EPI control strategy when PVR-based AD strategy is disabled at 40ms.

Fig. 17. Steady-state simulation results under 50% load condition with the proposed PVR-based AD strategy. (a) The PI controller. (b) The PR controller. (c) The SRF-EPI controller.

Fig. 18. Transient responses when the reference of $i_{\omega}$ steps up from half-load to full-load with the proposed PVR-based AD strategy. (a) The PI controller. (b) The PR controller. (c) The SRF-EPI controller.
Fig. 19. Simulation results of different \( R_{d_{eq}} \) with the delay time \( T_{d}=1.5T_s \) when the SRF-EPI controller is used in the proposed PVR-based AD strategy. (a) \( R_{d_{eq}} = 26.8 \). (b) \( R_{d_{eq}} = 18.8 \). (c) \( R_{d_{eq}} = 6.8 \).

Fig. 20. Simulation results of the SRF-EPI controller with PVR-based AD strategy when grid voltages are highly distorted. (a) Without grid voltage feed-forward control. (b) With grid voltage feed-forward control. (c) Combine with resonant controllers and grid voltage feed-forward control.

Fig. 21. Steady-state experimental results under half-load condition with the proposed PVR-based AD strategy. (a) The PI controller. (b) The PR controller. (c) The SRF-EPI controller.

Fig. 22. Experimental transient waveforms when the reference of \( i_{sp} \) steps from half load to full load with the proposed PVR-based AD strategy. (a) The PI controller. (b) The PR controller. (c) The SRF-EPI controller.

Fig. 23. Experimental results of different \( R_{d_{eq}} \) with the delay time \( T_{d}=1.5T_s \) when the SRF-EPI controller is used in the proposed PVR-based AD strategy. (a) \( R_{d_{eq}} = 26.8 \). (b) \( R_{d_{eq}} = 18.8 \). (c) \( R_{d_{eq}} = 6.8 \).
Fig. 24. Experimental results of the SRF-EPI controller in stationary frame with the PVR-based AD strategy when the grid voltages are highly distorted. (a) The SRF-EPI controller without grid voltage feed-forward control. (b) The SRF-EPI controller with grid voltage feed-forward control. (c) The SRF-EPI controller combines with the resonant controllers and grid voltage feed-forward control.

Fig. 19 and Fig. 23 show the effect of the feedback gain $R_{d,eq}$ of the PVR-based AD method on the output current quality with the control delay time of $T_{d}=1.5T_{s}$ and $R_{d,eq}$ of the SRF-EPI controller is chosen to be 26.8, 18.8 and 6.8, respectively. The simulation and experimental results under different $R_{d,eq}$ with $T_{d}=1.5T_{s}$ are shown in Fig. 19 and Fig. 23, respectively. Although the system is stable, the harmonic content increases dramatically when the value of $R_{d,eq}$ increases and the current THDs (phase A) in Fig. 19 (a), (b) and (c) are 35.82%, 6.04%, and 2.95%, respectively. The current THDs (phase A) of the experimental results in Fig. 23(a), (b) and (c) are 45%, 6.5% and 3.6%, respectively. Therefore, it is necessary to optimize the value of $R_{d,eq}$ to ensure a sufficient stability margin and a good dynamic response when the control delay is introduced.

To validate the performance of the control algorithm in case of distorted grid conditions, the grid-emulator was distorted with 5th and 7th harmonics, with voltage THDs of 3% and 2%, respectively. The simulation and experimental results of the grid currents with the SRF-EPI controller in stationary frame under different control scenarios are shown in Fig. 20 and Fig. 24, respectively. The multiple resonant controllers tuned at 5th and 7th harmonic with $K_{a}=5$ for $h=5$ and 7 are added to the SRF-EPI controller in stationary frame with the proposed active damping method. The THDs of simulated grid current $i_{gq}$ under different control scenarios are shown in Fig. 20, which are 64.27%, 38.33%, and 3.22%, respectively. As shown in Fig. 24, the current THDs of the experimental results are about 54.38%, 29.12% and 3.92%, respectively. It shows that when only the SRF-EPI controller is used, the grid currents are highly distorted due to harmonic distortion of grid voltages. When the grid voltage feed-forward scheme is used in combination with proposed control strategies, the current distortion can be effectively suppressed. However, the THD of the grid current is still high and the distortion in grid currents cannot be rejected by the voltage feed-forward loop alone. However, when the SRF-EPI controller is adopted in combination with the grid voltage feed-forward loop and the multiple resonant controllers in the current loop, the sinusoidal waveforms are guaranteed in the grid currents.

V. CONCLUSIONS

In this paper, the stationary frame SRF-EPI control algorithm using PVR-based AD method is proposed for three-phase LCL type grid-connected DG system, which achieves a compromise between the resonance damping and the dynamic performance and makes it easier to stabilize the whole system. The accurate stationary frame of SRF-EPI controller is introduced to achieve a high closed-loop bandwidth and good robustness. It is found that the SRF-EPI controller is equivalent to the PR controller in stationary frame at fundamental frequency, but shows different phase characteristics at other frequency ranges compared to the PR or PI controller in the stationary frame.

In order to guarantee the quality of the grid currents under non-ideal grid conditions, the grid voltage feed-forward control with the multiple resonant controllers in harmonic frequencies is adopted, and the performance under no damping, PD and AD methods are compared. Furthermore, the design guidelines of whole system of the SRF-EPI, PI and PR controllers are presented. Finally, simulation and experimental results of a three-phase LCL-based grid-connected inverter are presented to validate the proposed control approach.

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