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PITCH AND TDOA-BASED LOCALIZATION OF ACOUSTIC SOURCES WITH DISTRIBUTED ARRAYS
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ABSTRACT
In this paper, a method for acoustic source localization using distributed microphone arrays based on time-differences of arrival (TDOAs) is presented. The TDOAs are used to estimate the location of an acoustic source using a recently proposed method, based on a 4D parameter space defined by the 3D location of the source, and the TDOAs. The performance of the proposed method for acoustic source localization is compared to the performance of a method based on generalized cross-correlation with phase transform (GCC-PHAT) using synthetic and speech signals with varying source position. Results show a decrease in the error of the estimated position when the proposed method is used.

Index Terms— Acoustic source localization, distributed microphone arrays, TDOA estimation, pitch estimation.

1. INTRODUCTION
Microphone arrays are found in many modern-day devices such as hearing aids, smartphones, smart TVs, laptops, game consoles and robots. These microphone arrays facilitate beamforming [1] and direction of arrival (DOA) estimation, and can be used for, e.g., video teleconferencing [2]. When multiple microphones are available, it is possible to perform acoustic source localization, where the range and DOA of the acoustic source are estimated jointly.

For the problem of source localization, several classes of methods exist, like multilateration [3], TDOA-based source localization [4], maximum likelihood source localization [5] and energy-based source localization [6]. Some of the earliest work is for SONAR applications, an example being [7]. In [4], a method based on range differences (RDs) is used to estimate the position of an acoustic source using a single array. In [8–10], source localization strategies are reviewed and categorized, and time-delay estimation (TDE) and source-detection is considered. More recent work takes advantage of distributed microphone arrays. In [11], distributed microphone arrays are used to localize an acoustic source, by using hyperbolic constraints. TDOAs are estimated using GCC-PHAT [12]. A class of geometric methods for acoustic source localization based on TDOAs is described in [13]. In the paper, two categories of solutions to the acoustic source localization problem using TDOAs are described, based on maximum likelihood (ML) and least squares (LS) criteria. If multiple independent microphone arrays are distributed in an environment, these are likely not to be synchronized. This aspect can be of great importance when estimating TDOAs, and in [14] a solution to the problem of synchronization between independent microphone arrays is presented.

It appears from the above that many localization methods are based on TDOA estimation, which is often done using GCC-PHAT. Examples can be found in [15,16]. Another possible solution is to jointly estimate the TDOAs and the pitch, since many audio signals have a harmonic structure that could be exploited. The latter approach can be used to get statistically efficient estimates, which is generally not possible with correlation based methods such as GCC-PHAT [17]. This is the approach taken herein, although we assume the pitches to be known, since pitch estimation is not the main topic of this paper.

In this paper, we propose an acoustic source localization scheme for distributed, unsynchronized uniform linear arrays (ULAs) of microphones, that uses the cone-based localization method of [13, 14]. The method is based on ML TDOA estimation for each channel. We propose to estimate the TDOAs of the sensor signals individually for each array using a maximum likelihood approach, inspired by [17], instead of the often used GCC-PHAT method. In this paper, the locations of the microphone arrays and the sensors are assumed to be known. If the locations of the microphone arrays are unknown, they can be estimated using a method for automatic microphone localization, like the one in [18].

The paper is organised as follows. In Section 2, the signal model is introduced. In Section 3, the proposed method of using ML TDOA estimation in cone-based localization for acoustic source localization with distributed microphone arrays is described. Section 4 presents the experimental setup and results, and the work is concluded in Section 5.
2. SIGNAL MODEL

We will now introduce the signal model for each microphone array. Consider a single, quasi-periodic source, such as speech, being sampled spatially by a microphone array, consisting of $N_s$ sensors at time $n_t$. For simplicity, we will assume that the microphones are arranged as a uniform linear array (ULA). If the input signal is denoted $x(n_t)$, the output at sensor $n_s$ in each array is

$$y_{n_s}(n_t) = x_{n_s}(n_t) + w_{n_s}(n_t),$$  

with $x_{n_s}(n_t) = s(n_t - f_s \tau_{n_s})$, where $\tau_{n_s}$ is the TDOA between the reference sensor and sensor $n_s$, $f_s$ is the sampling frequency, $s(n_t - f_s \tau_{n_s})$ is the delayed signal and $w_{n_s}(n_t)$ is the noise recorded by sensor $n_s$. It is assumed that the distance between sensors is small, such that there is no attenuation between channels. The signal is assumed to be harmonic, thus it can be modelled as a sum of complex sinusoids

$$s(n_t) = \sum_{l=1}^{L} a_l e^{j \omega_0 n_t},$$  

where $L$ is the model order, $a_l = A_l e^{j \phi_l}$, where $A_l > 0$ is the real amplitude, and $\phi_l$ is the phase of the $l$th harmonic. It should be noted that the model (2) can be used for all periodic signals by careful selection of $L$ and $\omega_0$. The model can be applied to real data by using the Hilbert transform. Using (2), the signal at sensor $n_s$ is

$$s(n_t - f_s \tau_{n_s}) = \sum_{l=1}^{L} a_l e^{j \omega_0 n_t} e^{-j \omega_l n_s},$$  

where $\omega_l = \omega_0 f_s \tau_1$ is the spatial frequency. It is assumed that the ULA is placed in the far-field of the source, and that the recording environment is anechoic. A spatio-temporal vector signal model of the signal in (1) can then be defined as

$$y = x + w = Z \alpha + w,$$  

where $y = [y_0(n_t) \cdots y_{N_s-1}(n_t) \cdots y_0(n_0 - N_t + 1) \cdots y_{N_s-1}(n_t - N_t + 1)]^T$, with similar definitions for $x$ and $w$, and

$$Z = [z(\omega_0, \omega_s) \cdots z(L \omega_0, L \omega_s)],$$

$$z(l \omega_0, l \omega_s) = z_s(l \omega_0) \otimes z_s(l \omega_s),$$

$$\alpha = [a_1 e^{j \omega_0} \cdots a_L e^{j \omega_0}]^T,$$

$$z_s(\omega_s) = [1 \ e^{-j \omega_s} \cdots e^{-j (N_s-1) \omega_s}]^T,$$

$$z_l(\omega_0) = [1 \ e^{-j \omega_0} \cdots e^{-j (N_t-1) \omega_0}]^T,$$

where $\otimes$ denotes the Kronecker product. With the signal model in place, we can proceed to the estimation of the TDOAs for each array and the proposed localization scheme that takes into account the TDOAs for multiple arrays.

3. PROPOSED METHOD

The proposed method for source localization is based on the cone-based localization method of [13, 14]. In this paper, however, a maximum likelihood (ML) TDOA estimator, inspired by [17], is used to estimate TDOAs instead of the standard approach of using GCC-PHAT.

In the case of white Gaussian noise, with equal variance on all channels, the ML estimator for TDOA estimation is asymptotically equivalent to the non-linear least squares (NLS) method [17]. The NLS TDOA estimates for each array are found by solving

$$\hat{\alpha} = (Z^H Z)^{-1} Z^H y,$$  

If (11) is inserted into (10), we find

$$\hat{\tau} = \arg \max_{\tau \in \mathbb{T}} y^H Z \alpha.$$

Using the above estimator, we can estimate the TDOA $\tau_{n_s}$ of a quasi-periodic signal, with known pitch and model order, sampled by each ULA. Because of the nonlinear nature of the cost function (12), a grid search is used to evaluate the cost function. In this paper, the pitch $\omega_0$ of the signal is assumed to be known. It can easily be estimated in practice, e.g., using the fast, multichannel, FFT-based method in [19].

Equipped with the TDOA estimates $\hat{\tau}_{n_s}$ for each sensor in each of the arrays, we proceed by using the source localization method [13]. In this localization method, an extended coordinate system is formed by adding a range difference coordinate to the coordinates of the source. Each point $p = [x, y, s]^T$ is hereby mapped onto the 4D space-range $[p^T, w]^T$, where $w$ is the range coordinate. Consider a ULA with $N_s$ sensors, placed at $m_{n_s} = [x_{n_s}, y_{n_s}, z_{n_s}]^T$, where $n_s = 0, \ldots, N_s-1$. The range difference between the source and the $n_s$-th microphone and between the source and the reference microphone is

$$w_{n_s} = c \tau_{n_s,0} = \|p_s - m_{n_s}\| - \|p_s - m_0\|,$$  

where $m_0$ is the reference sensor, $p_s$ is the position of the source, and $\tau_{n_s,0}$ is found using (12). The microphones $m_{n_s}$ can be represented by cones with apex $[m_{n_s}, w_{n_s}]^T$. With noiseless measurements, $p_s$ should fall in the intersection of all such cones (see [13] for further details). Because of noisy measurements, the source location is found as the point $\hat{p}_s$ with minimum distance to the surface of the cones, i.e.,

$$\hat{p}_s = \arg \min_{p_s \in P_s} ||e(p_s)||^2,$$  

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where $\mathbf{P}_s$ is a set of candidate array source positions,

$$e(\mathbf{p}_s) = [e_0(\mathbf{p}_s) \cdots e_{N_s-1}(\mathbf{p}_s)]^T,$$

(15)

and $e_{n_s}(\mathbf{p}_s) = (x_s - x_{n_s})^2 + (y_s - y_{n_s})^2 + (z_s - z_{n_s})^2 - (w_s - w_{n_s})^2$. If the microphones in the arrays are not synchronized, the $z$-axis does not correspond to the reference microphone. To address synchronization in the case of $N_s$ distributed arrays, a difference between the distance from the source to the reference and to the local reference of the $n_s$th array is defined as [14]

$$\Delta^2 z(n_s) = \sqrt{\Delta^2 x_{n_s} + \Delta^2 y_{n_s} + \Delta^2 z_{n_s}} - \sqrt{\Delta^2 x_0 + \Delta^2 y_0 + \Delta^2 z_0},$$

(16)

where $\Delta x_{n_s} = x_{0,n_s} - x_s$, $x_{0,n_s}$ is the position of the reference sensor in the $n_s$th array. By adding the displacements (16) to the cone errors in (14), the range difference estimates refer to a single global reference microphone. It should be noted that array placement is an important factor to consider. In this paper, since 3D localization is considered, the environment must contain arrays that estimate the position in three dimensions, in order to estimate the position of an acoustic source in 3D. For further details, see [13].

4. EXPERIMENTAL RESULTS

The performance of the proposed method of ML TDOA estimation, as described in Section 2, used for source location estimation, is compared to GCC-PHAT [12, 20]. Both methods have been evaluated using an anechoic synthetic harmonic signal, consisting of 10 harmonic complex sinusoids, with a sampling rate of $f_s = 8$ kHz. The speed of sound is assumed to be $c = 340$ m/s. The acoustic environment is set up using the Signal Generator for MATLAB [21], which is based on the image method [22]. The room dimensions are 4 m by 4 m by 4 m. Four microphone arrays each consisting of four microphones are used. The arrays are placed with their reference microphones at the middle of each side of the room, along the walls. The microphone spacing is 5 cm. Figure 1 shows the placement of the microphones. After generating a multichannel signal with the above-mentioned setup, a number of channels of diffuse white Gaussian noise, corresponding to the total number of microphones, is added to the signals received at the microphones, resulting in an SNR at the microphones, $\text{SNR}_m$. White Gaussian noise is added to the source signal, resulting in a varying SNR at the source position, $\text{SNR}_s$.

As mentioned earlier, TDOA estimation is performed using an ML TDOA estimation technique. The signals are processed individually for each array, since we are considering a distributed network of microphone arrays. The maximum possible TDOA corresponds to the distance between the sensors in the array. Because of this, the TDOAs are estimated using a grid ranging from $-0.1875$ to $0.1875$ ms, corresponding to a range of $-1.5$ to $1.5$ samples. The search grid spacing is $0.01$ samples. For GCC-PHAT the same TDOA grid was used. Furthermore, an FFT length of 512 samples was used, and in this method we integrate over frequencies in the range $f = [300, 4000]$ Hz [23].

Two experiments were conducted in order to assess the performance of the proposed method; one where the segment length $N_t$ was varied, and one where $\text{SNR}_m$ was varied. The data is obtained by conducting 500 Monte-Carlo simulations for each data point. In each simulation, the source position is randomly chosen, $x \in [1.0, 3.0]$, $y \in [1.0, 3.0]$ and $z \in [1.0, 2.0]$ with a search grid spacing of 1 cm in all directions. Furthermore, the fundamental frequency is sampled from the interval $f_0 \in [300, 4000]$ Hz, and the phase of each of the harmonics is randomized. Figure 2 shows the magnitude of the

**Fig. 1.** Microphone array and source positions.

**Fig. 2.** Average of the magnitude of localization error in m (top) and TDOA MSE (bottom) for varying segment lengths, using a synthetic signal.
localization error in meters, and the TDOA mean squared error (MSE), for segment lengths varying from 30 to 100 samples. The SNR of the signal emitted from the position of the acoustic source is \( SNR_s = 20 \) dB. The SNR of the signals received at the microphones is \( SNR_m = 10 \) dB. The model order is \( L = 10 \). The figure shows a decrease in the localization error, for both methods, when the segment length is increased. Furthermore, the error when using GCC-PHAT is approximately twice as large compared to when the ML TDOA estimation method is used. Figure 3 shows the magnitude of the localization error in m, for \( SNR_m \) varying from 0 to 30 dB. For this experiment, the segment length is \( N_t = 100 \) samples, \( SNR_s = 20 \) dB, and the model order is \( L = 10 \). The figure shows a decrease in the magnitude of the localization error in m, for both methods, when \( SNR_m \) is increased. Furthermore, the error when using GCC-PHAT is approximately twice as large compared to when ML TDOA estimation is used. In both experiments, the results show that using ML TDOA estimates results in smaller errors than GCC-PHAT.

Figure 4 shows the spectrogram of the speech signal, the estimated fundamental frequency for each frame and the localization error in m for each frame. The mean error for the ML TDOA method is 0.30 m, and 0.59 m for the GCC-PHAT method. This reduction in localization error is consistent with the results using synthetic signals.

5. DISCUSSION

In this paper, the problem of acoustic source localization based on TDOA estimation is considered. In particular, the method of using ML TDOA estimation, inspired by [17], is compared to using GCC-PHAT [12]. The considered scenario consists of multiple distributed microphone arrays. The performance of the source localization method when using ML TDOA estimation is compared to the performance when using GCC-PHAT for TDOA estimation. By using ML TDOA estimation, the accuracy of the acoustic source localization is increased, when compared to using GCC-PHAT, using both synthetic and real signals. This is expected, since the TDOA estimator is the maximum likelihood estimator, when the noise is white Gaussian, with the same variance on each channel, the environment is anechoic and the source is in the far-field. The results are of particular interest for localization of moving sources, since the ML TDOA estimation method results in small errors even at low segment lengths, which are required for moving sources, and low SNRs. Furthermore, an accurate estimate of the position of an acoustic source is important for enhancement purposes.
6. REFERENCES


