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Absorption Cycle Heat Pump Model for Control Design

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Abstract—Heat pumps have recently received increasing interest due to green energy initiatives and increasing energy prices. In this paper, a nonlinear dynamic model of a single-effect LiBr-water absorption cycle heat pump is derived for simulation and control design purposes. The model is based on an actual heat pump located at a larger district heating plant. The model is implemented in Modelica and is based on energy and mass balances, together with thermodynamic property functions for LiBr and water and staggered grid representations for heat exchangers. Model parameters have been fitted to operational data and different scenarios are simulated to investigate the operational stability of the heat pump. Finally, this paper provides suggestions and examples of derivation of lower order linear models for control design.

I. INTRODUCTION

Energy consumption in residential, commercial and industrial buildings has received increasing attention in recent years due to the rising demand for efficient energy use and higher comfort standards. In industrial buildings, in particular, energy efficiency is becoming more and more important in order to avoid waste. Due to their attractive properties, heat pumps of various types are seeing extensive use in modern buildings, see for instance \cite{1}, \cite{2}, and many others. Furthermore, applying heat pumps together with other technologies at modern combined heat and power (CHP) plants and using them in combination with district heating, can yield significant economical and practical benefits, as described in e.g. \cite{3}, \cite{4}, \cite{5}, \cite{6}, and \cite{7}.

The town of Sønderborg in the southern part of Denmark is one such case, where two suppliers, Sønderborg Fjernvarme (SFJV) A.m.b.a. and Sønderborg Kraftvarmeværk I/S, collaborate to provide district heating to a fairly large number of commercial and private consumers in the local area. Together, the two suppliers incorporate burning of waste, natural gas, wood-chips and, of highest relevance to the present paper, four interconnected absorption cycle heat pumps primarily driven by geothermal heat.

As can be expected, day-to-day operation needs to be adjusted to consumer load changes, weather, fuel prices, etc. In order to operate complex plants under such dynamic conditions, it is necessary to have good knowledge of the dynamic behavior and constraints of individual units. However, while absorption cycle heat pumps have received some attention in terms of modeling for the purpose of design and operation under steady state conditions, the literature is quite limited when it comes to modeling for control purposes. \cite{8} and \cite{9} provides an overview of the technology, but does not consider dynamic operation; \cite{10}, \cite{11}, and \cite{12} all provide steady-state models of absorption cycle heat pumps of varying degree of detail, but also do not consider dynamics. \cite{13} and \cite{14} both present models that include dynamics (mass storage and thermal inertia), but the main focus remains on steady-state operation.

In this paper, we present a single-effect absorption cycle heat pump model for the specific purpose of investigating control design issues. In our model, the main heat transport is carried out by a chemical absorption/desorption cycle involving a mixture of water and Lithium-bromide (LiBr), and we consider both mass storage and heat transfer. The model is implemented as interconnected components in the simulation tool Dymola using the open-source and object-oriented modeling language Modelica \cite{15}. The component models of the absorber and generator are formulated based on the aforementioned modeling papers, while the evaporator and condenser models are inspired by \cite{16}. Heat exchangers are modeled using staggered grid models, e.g., see \cite{11}, while LiBr properties are modeled according to \cite{17}. Model parameters are then fitted using actual plant data.

The outline of the paper is as follows. Section II gives an overview of the heat pump process. Section III presents the main model components, whereupon Section IV presents the results of parameter fitting. Next, Section V shows simulations with external water flow control, Section VI discusses linearization of the model, and Section VII sums up the work. Finally, it should be pointed out that a companion paper, \cite{18}, presents an analysis of different control loop configurations based on the model presented here.

II. DISTRICT HEATING HEAT PUMP SETUP

At the highest level of abstraction, a part of the district heating supply system at SFJV is structured as shown in Fig. 1. The main sources of heat are a wood-chip fired boiler (high-value heat) and a geothermal reservoir (low-value heat). These two main heat sources supply heat to the district heating system via four absorption cycle heat pumps interconnected in a fairly complex way that permits one or more of the individual heat pumps (of different size) to be disengaged from the heat supply operation. In the following, we will limit our focus to the largest heat pump (HP1).
The heat pump in question was delivered by Hope Deep-blue Air-conditioner Manufacture Corp., Ltd., and has an operational weight of 67 ton [19]. An illustration of the heat pump is provided in Fig. 2. The basic absorption cycle works similarly to the standard vapor compression cycle except that the compressor is replaced by an absorber and a generator, and the working fluid in an absorption refrigeration system is a binary solution consisting of refrigerant and absorbent—in this case, water and LiBr, respectively. This solution is pumped from the absorber to the generator by an electrical pump (1−3). High temperature water from the wood-chip burner is supplied to the generator (11−12) and used to vaporize refrigerant from the solution. The refrigerant and absorbent are chemically separated as the refrigerant vaporizes, leaving a liquid solution with a high absorbent concentration in the generator, which is gradually returned to the absorber (4) when the generator overflows. A u-tube mechanism then helps maintain a pressure difference between the generator and absorber (5−6), see [13] for further explanation of the u-tube design. The refrigerant vapor from the generator is led to a condenser (7), where a standard condensation occurs, expelling heat to the surroundings (15−16), which in this case is district heating water. Saturated refrigerant is fed to an evaporator through another u-tube overflow mechanism (8−9), where it evaporates, consuming heat from the surroundings (17−18). Actually, in this case, heat is taken from the district heating water, but this water is reheated by geothermal water, which can be considered as a cheap energy source. An evaporator pump is used to continuously circulate liquid refrigerant across the heat exchanger pipes. Finally, the vapor is led to the absorber (10), where the solution absorbs refrigerant vapor at low pressure; this absorption process is an exothermic process. This means that it must reject heat to the surroundings (13−14), which again is district heating water. A solution heat exchanger (HEX) allows the solution from the absorber (2) to be preheated before entering the generator (3) by using the heat from the hot solution leaving the generator (4−5). As a consequence, less hot water from the wood-chip burner is required in the generator. Moreover, the size of the absorber can be reduced as less heat is rejected. The system also has a water HEX located after the condenser, which transfers heat from the refrigerant to the district heating water (19−20) before it enters the evaporator.

Fig. 2. Illustration of the absorption cycle heat pump at SFJV. The numbers indicate thermodynamic state points used in the model (adopted from [8]).

Fig. 3. Dühring chart illustration of different state points in the absorption cycle. The four colored dots indicate the initial conditions of the liquid content of the evaporator, absorber, generator, and condenser for the data presented in Section V.

Fig. 1. Bird’s eye view of a district heat supply system at SFJV with indication of typical water flow temperatures.

III. ABSORPTION CYCLE HEAT PUMP MODEL

A sketch of a single-effect LiBr-water absorption cycle heat pump model is shown in Fig. 4. The individual components are drawn in a temperature-pressure diagram to illustrate the relative operating conditions in the four main components (evaporator, absorber, generator, and condenser).
The model is based on the heat pump system shown in Fig. 2. However, for simplicity, the evaporator with evaporator pump is replaced by an evaporator model without the pump, where the heat exchanger pipes are submerged in the liquid water. The overflow pipes from the generator and the condenser together with the u-tube design can alternatively be replaced by controlled electronic expansion valves. Valve models are therefore used, where control loops start to open the valves, when the level in the generator or the condenser exceeds a predefined upper bound (nominal level).

The dynamic model of the absorption cycle used in this work is based on mass and energy balances and thermodynamic property functions. Further, the model is implemented in the Modelica modeling language. This allows reuse of the standard Fluid and Media libraries and encourages object-oriented programming. Fluid flow between individual component models in thermodynamic systems are also standardized using the stream connector implementation, see [20], which is also adopted here.

In the following it is assumed that the evaporator and absorber operate at the same low pressure, and that the generator and condenser operate at the same high pressure. Further, there are no heat losses to the ambient air and each of the four main components can be represented by a liquid control volume (subscript \( i \)) and a vapor control volume (subscript \( v \)). The overall mass balances are

\[
\text{Eva: } \frac{dM_a}{dt} = m_9 - m_{10}, \\
\text{Abs: } \frac{dM_a}{dt} = m_6 + m_{10} - m_1, \\
\text{Gen: } \frac{dM_g}{dt} = m_3 - m_4 - m_7, \\
\text{Con: } \frac{dM_c}{dt} = m_7 - m_8,
\]

where \( M \) is mass, \( V \) is volume, \( \rho \) is density, \( m \) correspond to mass flows illustrated with arrows in Fig. 4, \( i \in \{ e, a, g, c \} \) in (5) and (12) denote each component, and subscript \( \text{tot} \) denotes total. The LiBr mass balances are

\[
\begin{align*}
\text{Abs: } & \frac{d(X \nu_{\text{Gen}, \text{a}} \rho_{\text{a}, \text{c}})}{dt} = X_0 m_6 - X_1 m_1, \\
\text{Gen: } & \frac{d(X \nu_{\text{Gen}, \text{g}} \rho_{\text{g}, \text{c}})}{dt} = X_3 m_3 - X_4 m_4,
\end{align*}
\]

where \( X \) is mass fraction of LiBr. The energy balances are

\[
\begin{align*}
\text{Eva: } & \frac{dU_e}{dt} = m_9 h_0 - m_{10} h_{10} + Q_e, \\
\text{Abs: } & \frac{dU_a}{dt} = m_6 h_6 + m_{10} h_{10} - m_1 h_1 - Q_a, \\
\text{Gen: } & \frac{dU_g}{dt} = m_3 h_3 - m_4 h_4 - m_7 h_7 + Q_g, \\
\text{Con: } & \frac{dU_c}{dt} = m_7 h_7 - m_8 h_8 - Q_c,
\end{align*}
\]

where \( U \) is internal energy, \( Q \) is heat transfer rate, \( h \) is specific enthalpy, and \( p \) is pressure.

The water vapor flow out of the generator solution and the water vapor flow absorbed in the absorber are driven by the amount of heat transferred through the HEXs assuming that the solutions are always in a saturated state. It is also assumed (see [8]) that the solution that exits the absorber and generator, the water that exits the condenser, and the vapor that exits the evaporator, all are in a saturated state (same state as in the respective components). Additionally, the vapor from the generator interacts with the solution from the absorber in a counterflow way (sprayed in), such that the vapor at the outlet is superheated to the saturation temperature of the solution, see again [8].

The mass and energy balances are supplemented with thermodynamic property functions. E.g., to calculate enthalpy or density of water we would use a function of the form

\[ (h, p) = f(p, T), \]

since liquid-vapor equilibrium is assumed. The water property functions are part of the standard Modelica Media library and the LiBr-water solution property functions are implemented based on the formulations given in [17].

Since Modelica.Media does not provide an interface for incompressible solutions the LiBr-water solution properties have been implemented in a separate package with functions for pressure, \( p(T, X) \), density \( \rho(T, X) \), specific enthalpy \( h(T, X) \), entropy \( s(T, X) \) and heat capacity \( c_T(T, X) \). Their partial derivatives wrt. temperature, \( T \), and concentration, \( X \), have been symbolically deduced from the expressions in [17] and are also provided in the package.

The HEX in the four main components, the water HEX, and the solution HEX, illustrated in Fig. 4, are such that partial differential equations must be used in the description due to the distributed parameter nature. This is modeled using 1-dimensional dynamic staggered grid flow models with a finite volume model representation with \( N \) volumes elements (volume divided equally) and \( N + 1 \) flow elements in between the volumes, as shown in Fig. 5. Further, stream connectors are used to connect each element as indicated
Finally, the mass flow through the solution pump \( m_1 \) is related to the pump work \( W_p \) via the static equation

\[
\eta_p W_p = \Delta p_p \frac{m_1}{\rho_p},
\]

where \( \eta_p \) is a fixed pump efficiency and \( \rho_p \) is the density of the incompressible solution.

IV. MODEL PARAMETER FITTING AND COMPARISON WITH OPERATIONAL DATA

The heat pump model described in Section III contains multiple parameters that can represent the operational characteristics of a given system. Data from the heat pump described in Section II and a data sheet [19] are used to fit the parameters to HP1 (Fig. 1) located at SFJV. In addition to identification of parameters, it is necessary to implement and tune basic stabilizing control loops similar to the setup in SFJV, because the available data is obtained from closed-loop operation. However, once a basic control setup is found that provides a good fit to the closed-loop data it can be used as a benchmark for design of more advanced control.

The mass flow through the solution pump \( m_1 \) is used to control the LiBr concentration of the strong solution at the outlet of the generator, while the external water mass flow through the generator \( m_{11} \) is used to control the condenser pressure (same pressure as in the generator). The external water mass flow through the water HEX \( m_{19} \) is controlled to maintain a constant outlet temperature \( T_{20} \).

Decentralized PI control loops are used for each of the mass flows \((m_1, m_{11}, \text{and } m_{19})\) to provide simple setups that can be tuned manually. Note that the exact control algorithms in the heat pump at SFJV are unknown and the suggested control implementation is only one out of many possible ways to control the cycle, see [18] for further detail on potential control setups. However, the suggested controls have given the best agreement between data and simulation.

Finally, the external water mass flow through the evaporator, absorber, and condenser are controlled externally as described in Section V and the data presented in Fig. 6.
are used as input to the simulation, along with the initial conditions shown in Fig. 3.

Table I contains the most important model parameters. The volumes and HEX wall masses are based on information provided in the data sheet [19]. The relative sizes of the solution HEX and the water HEX are assumed to be 10% of the generator and condenser sizes, respectively. Furthermore, it is assumed that the nominal liquid filling (level) of the evaporator, absorber, and condenser is 15% of their respective total volumes. The generator has a slightly higher nominal liquid level of 20%. The resulting masses of HEX walls, water, solution, and miscellaneous equipment gives reasonable total shipment and fluid weight values, respectively 54.6 ton and 12.4 ton, when compared with data sheet values. The heat transfer parameters and the control parameters were found through manual iteration from an initial guess to give a good visual fit in steady state operation and in the transient behavior during the ramp change in capacity utilization during the 20 hours of operation (see Fig. 6). In addition, 7 volume elements and 8 flow elements are used to discretize the HEX tubes, which is a trade-off between model accuracy and complexity (the improvement in accuracy is negligible with more elements).

The simulation result using the manually tuned model parameters is compared with operational data from SFJV in Fig. 7. Only four measurements are available internally in the heat pump cycle ($T_4$, $T_5$, $T_{10}$, and $X_4$). This means that the initial absorber concentration has also been an iteration variable in the model tuning process and it was set to 55.5% in the presented simulation result. A potential set point reference for the concentration $X_{4,ref}$ used at SFJV is unknown and the control loop in the simulation has therefore been set to follow the measured concentration at SFJV as reference. However, the reference for the condenser pressure control loop is kept fixed at the initial pressure.

Changes in all temperatures are observed when the capacity is ramped up at around 7 hours. The system settles again a couple of hours after the ramping period ends at around 11 hours. All the temperatures show good qualitative agreement with measurement data. The largest offsets are seen in the temperatures associated with the generator and absorber. These models are relatively simple, where the temperature of the solution is assumed to be the same across the entire HEX wall. Models with higher fidelity could be used; however, this will increase the model order and the obtained model detail is considered adequate for control design.

V. SIMULATION OF EXTERNAL WATER FLOW CONTROL

The external evaporator water mass flow $m_{17}$ is used to determine the desired capacity utilization of the heat pump. Higher external mass flow through the evaporator generates more steam, which in turn requires a higher absorber flow to absorb the steam and a higher condenser flow to generate enough condensate for the evaporator. Higher condensation rate in the condenser lowers the pressure and the internal control will thus generate more steam in the generator and pump more solution from the absorber to maintain a suitable LiBr concentration in the generator. The heat pump located at SFJV is specified to operate with external absorber and condenser mass flows as a scaling of the evaporator mass flow with minimum and maximum margins;

$$0.95k_am_{17} \leq m_{13} \leq 1.6k_am_{17},$$  
$$0.85k_cm_{17} \leq m_{15} \leq 1.15k_cm_{17},$$

with nominal absorber flow scaling $k_a = 1.591$ and nominal condenser flow scaling $k_c = 1.078$.

In order to keep the heat pump operable it is important that the liquid levels (mass distributions) in each of the four main components are kept within a reasonable range from their nominal values. It is also important that the concentration is controllable to be able to prevent potential crystallization.

Simulations of the four extreme situations in terms of absorber and condenser mass flows are shown in Fig. 8. The simulation conditions are the same as presented in Section II, except for the external absorber and condenser mass flows, which are set to be scaled according to Eq. (20) and (21).

The levels and concentration are kept within reasonable bounds during the 20 hour simulations in three out of four extreme cases. The situation with high condenser mass flow and low absorber mass flow exhibits potential problems in
terms of keeping the concentration at the reference and maintaining decent levels in the evaporator and the absorber. This is due to a too efficient condenser that overflows the evaporator with condensate, while the absorber does not absorb enough steam from the evaporator to maintain a healthy liquid level, which raises the concentration in the absorber and causes the concentration in the generator to raise as well. Note that generally in order to keep the evaporator and the absorber levels controlled at their nominal values (15%) it would be necessary to measure or estimate at least one of these levels, see [18]. However, the system is operable with suitable scaling of external mass flows.

VI. LINEARIZATION OF NONLINEAR MODEL FOR CONTROL DESIGN

The nonlinear heat pump model implemented in Modelica has the following states: four levels (4), temperature and concentration in absorber and generator (4), pressure and enthalpy for each volume element in the four main component HEXs (56), temperature of each volume element and each wall segment for the solution HEX (21, no pressure loss assumed), temperature of each wall segment and each volume element internally in the water HEX (14, no pressure loss assumed), pressure and enthalpy for each volume element externally in the water HEX (14). This gives 113 states.

A linear lower order model is often preferred for control design and Dymola has a built-in linearization functionality, which can linearize the nonlinear model in a given operating point. The output is a state space representation, where model order reduction can be performed on the high order model for the input/output set of interest, e.g., using the Matlab function balred. The linear model can be verified by perturbing the inputs of the nonlinear model with sinusoidal signals of different frequency and calculating the response in each output of interest. The test frequencies should be chosen around the desired control bandwidth as lower/higher frequencies are not as important for the control design.
The solution pump mass flow $m_1$ and the external generator water mass flow $m_{11}$ are two internal inputs in the heat pump model. These inputs are used to control the generator outlet LiBr concentration $X_4$ and the condensation temperature $T_c$ (or pressure) as described in Section IV. Fig. 9 shows the frequency response for the case with $m_1$ as input and $X_4$ as output and the case with $m_{11}$ as input and $T_c$ as output. Both full 113 order linear models, reduced order linear models (6. and 5. order, respectively), and test on the nonlinear model are shown for comparison.

The chosen orders gives a good fit for the presented frequency range, where only a small discrepancy in phase is observed for high frequencies (the *Matlab* function *hsvd* can also help indicate a suitable model order). The test also indicates that the linear model is a good approximation of nonlinear model, at least close to the chosen operating point (the amplitude of the sinusoidal perturbations are 5% of the nominal input at the operating point). However, note that any cross coupling effect from other inputs are lost, which means that either the chosen input should have a dominating effect on the chosen output or model reduction should be performed on a MIMO model with all inputs to the system.

**VII. CONCLUSION**

A nonlinear dynamic model of a single-effect absorption heat pump cycle has been derived for simulation and control design purposes and implemented in Modelica. The object oriented component modeling in Modelica makes it easy to extend the model and build more complex systems. A simple control setup for the heat pump is also provided, which is close to the control used in the plant at SFJV and can serve as a benchmark for more advanced control. Simulation using manually fitted model parameters have shown good agreement with 20 hours of closed-loop operational data in steady state and during a change in heat pump capacity utilization. Simulation of different scenarios of external water flow control revealed potential problems when the condenser flow is high and the absorber flow is low. Furthermore, the potential for deriving reduced order linear models for control design is demonstrated through examples with two interesting input-output control pairs. Finally, the model has been used in a companion paper to analyze different input-output pairings in terms of control potential.

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