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MULTI-PITCH ESTIMATION OF AUDIO RECORDINGS USING A CODEBOOK-BASED APPROACH

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ABSTRACT

In this paper, a method for multi-pitch estimation of single-channel mixtures of harmonic signals is presented. Using the method, it is possible to resolve amplitudes of overlapping harmonics, which is otherwise an ill-posed problem. The method is based on the extended invariance principle (EXIP), and a codebook consisting of realistic amplitude vectors. A nonlinear least squares (NLS) cost function is formed based on the observed signal and a parametric model of the signal, for a set of fundamental frequency candidates. For each of these, amplitude estimates are computed. The magnitudes of these estimates are quantized according to a codebook, and an updated cost function is used to estimate the fundamental frequencies of the sources. The performance of the proposed estimator is evaluated using synthetic and real mixtures, and the results show that the proposed method is able to estimate multiple pitches in a mixture of sources with overlapping harmonics.

Index Terms— Multi-pitch estimation, amplitude estimation, vector quantization, music information retrieval.

1. INTRODUCTION

The pitch, or fundamental frequency, is a key feature of harmonic signals, such as short segments of music and speech signals. Music signals often contain multi-pitch signals, e.g., when multiple instruments are playing simultaneously. Pitch estimation has applications in problems such as separation [1], enhancement [2], automatic music transcription [3], and source localization [4].

Two common types of pitch estimation methods exist, i.e., non-parametric methods, and parametric, model-based methods. Examples of single-pitch methods in the former category include methods based on auto-correlation [5, 6]. Auto-correlation based methods have also been used for multi-pitch estimation, an example is [7], which is based on the enhanced summary autocorrelation function (ESACF). However, those methods are sub-optimal from a statistical point of view. Examples of single-pitch methods in the latter category include those based on maximum likelihood (ML) [8, 9] (see [10] for further examples). Parametric multi-pitch methods also exist, and one that uses ML estimation iteratively is the expectation-maximization (EM) algorithm [11], while another is known as the harmonic matching pursuit [12] (see also [10]).

Multipitch estimation becomes difficult when the pitches have overlapping harmonics, for instance in a mixture of two sources where the fundamental frequencies are 300 Hz and 450 Hz. A strong peak would occur at 150 Hz if using, e.g., the NLS estimator, which would result in wrong pitch estimates. A solution might be to map the amplitude estimates to realistic amplitudes in a codebook, e.g., using vector quantization [13]. Vector quantization has previously been applied in parameter estimation of music and speech signals, some notable references include source separation [14], and speech enhancement [15]. Harmonic amplitude information has been used previously in fields such as instrument recognition [16], where the aim is to provide instrument labels for frames with concurrent instruments playing, and automatic music transcription [17, 18], where the aim is to output the discrete pitches being played, along with onset times and note durations. Discrete pitch estimates, however, are not useful when estimating the pitch of an instrument played with vibrato, or for the purpose of tuning an instrument.

In this paper, we propose a method for multi-pitch estimation of mixtures of harmonic signals, such as recordings of musical instruments, where harmonics might overlap. In this work, the mixtures are single-channel. The method is based on the extended invariance principle (EXIP) [19, 20], and a codebook of naturally occurring amplitude vectors, trained using amplitude vectors of signals similar to those of interest. The fundamental frequencies are estimated iteratively for each source, and the amplitudes are quantized according to the codebook. The idea is to investigate whether some crude knowledge about the spectral envelope of the components of the mixture signals is beneficial for multi-pitch estimation of musical signals. It should be noted that we are here estimating continuous pitch of the instruments.

The remainder of the paper is organized as follows. In Section 2, the signal model is introduced. The proposed
multi-pitch estimator is described in Section 3. The experimental setup and results are presented in Section 4, and the work is concluded in Section 5.

2. SIGNAL MODEL

Consider a complex-valued single-channel mixture of $M$ harmonic signals embedded in noise at time instant $n$. The data can be represented by the snapshot $x \in \mathbb{C}^N$, i.e.,

$$x = [x(0) \ x(1) \ \cdots \ x(N-1)]^T.$$  

A complex signal model is used because it leads to simpler expressions, and lower computational complexity. It should be noted that although the signal model is complex, it can be used with real signals by applying the Hilbert transform. The entries in the data vector are linear superpositions of $M$ sources, i.e.,

$$x(n) = \sum_{m=1}^{M} s_m(n) + e(n),$$  

where

$$s_m(n) = \sum_{i=1}^{L_m} \alpha_{m,i} e^{j\omega_{0,m,ln}},$$  

where $\omega_{0,m}$ is the fundamental frequency, $L_m$ the model order (assumed known here, but can be estimated using, e.g., the MAP method, see [10]), and, $l = 1, \ldots, L_m$ is the harmonic index of the $m$th source, and

$$\alpha_{m,i} = A_{m,i} e^{j\phi_{m,i}}$$  

is the complex amplitude, where $A_{m,i}$ is the real amplitude of the $i$th harmonic for the $m$th source, $\phi_{m,i}$ its phase, and $e(n)$ is assumed to be white Gaussian noise. It is assumed that the signal is stationary during the interval $n = 0, \ldots, N - 1$. A vector signal model can be stated as

$$x = \sum_{m=1}^{M} Z_m(\omega_{0,m}) \alpha_m + e,$$  

where $Z_m(\omega_{0,m})$ is a Vandermonde matrix, i.e.,

$$Z_m(\omega_{0,m}) = [z_{m,1}(\omega_{0,m}) \ \cdots \ z_{m,L_m}(\omega_{0,m})],$$  

where $z_{m,i}(\omega_{0,m}) = [1 \ e^{j\omega_{0,m}i} \ \cdots \ e^{j\omega_{0,m}(N-1)}]^T$. The vector of complex amplitudes is

$$\alpha_m = [\alpha_{m,1} \ \cdots \ \alpha_{m,L_m}]^T,$$  

and

$$e = [e(0) \ e(1) \ \cdots \ e(N-1)]^T.$$  

The likelihood function of the observed signal, parametrized by

$$\theta = [\omega_{0,1} \ \alpha_1^T \ \cdots \ \omega_{0,M} \ \alpha_M^T]^T,$$  

can be written as

$$p(x; \theta).$$  

Here, we are concerned with estimating the set of fundamental frequencies $\omega_0 = [\omega_{0,1} \ \cdots \ \omega_{0,M}]^T$.

3. PROPOSED METHOD

We will now derive the proposed multi-pitch estimator. For the signal model at hand, we wish to find the parameters of the multi-pitch mixture, i.e.,

$$\hat{\theta} = \arg\max_\theta \ln p(x; \theta).$$  

(11)

For white Gaussian noise, this can be solved using the NLS method, i.e.,

$$\hat{\omega}_0 = \arg\min_{\omega_{0,m} \in \Omega} \norm{x - \sum_{m=1}^{M} Z_m \alpha_m}^2_2,$$  

(12)

where $\Omega$ is the set of possible frequencies. However, this is a complicated problem to solve for all $\omega_{0,m}$ at once. One possible approach for estimating the parameters is to use an iterative approach, such as the harmonic matching pursuit [12, 10], which we will use. It is based on a residual for iteration $i$, defined as

$$r^{(i)}(n) = x(n) - \sum_{m=1}^{i} \sum_{l=1}^{L_m} \alpha_{m,l} e^{j\omega_{0,m,ln}},$$  

(13)

which for $i = 1, \ldots, M$ can be written as

$$r^{(i)}(n) = r^{(i-1)}(n) - \sum_{l=1}^{L_i} \alpha_i l e^{j\omega_{0,i,ln}},$$  

(14)

and is used to estimate the model parameters iteratively for each source. The method is initialized using the observed signal, i.e., $r^{(0)}(n) = x(n)$. The parameters, for sources $m = 1, \ldots, M$, are then estimated by solving

$$\hat{\omega}_{0,m} = \arg\min_{\omega_{0,m}, \alpha_m} \norm{r^{(i-1)} - Z_m \alpha_m}^2_2,$$  

(15)

where $r^{(i)}$ is a vector containing the residual. It should be noted that the cost function is multi-modal, and we therefore perform the minimization using a grid search. The LS estimates of the amplitudes $\alpha_m$ are [21]

$$\hat{\alpha}_m = \left( Z_m^H Z_m \right)^{-1} Z_m^H r^{(i-1)}.$$  

(16)

The estimate of $\omega_{0,m}$ is found by substituting the above into (15), i.e.,

$$\hat{\omega}_{0,m} = \arg\min_{\omega_{0,m}} \norm{r^{(i-1)} - Z_m \left( Z_m^H Z_m \right)^{-1} Z_m^H r^{(i-1)}}^2_2.$$  

(17)

The fundamental frequencies and amplitudes of the $M$ sources are then obtained by computing the residual (14) and estimating the fundamental frequency using (17) and the amplitudes using (16). However, estimating the amplitudes
of overlapping harmonics is an ill-posed problem. To solve this, we propose to make use of the EXIP [19, 20], and to map the vector $\hat{\mathbf{A}}_m$, where each entry is the magnitude of the corresponding entry in $\hat{\alpha}_m$ to entries in a codebook of realistic amplitudes using a vector quantizer, i.e.,

$$\hat{\mathbf{A}}_m \rightarrow \tilde{\mathbf{A}}_m \in \mathcal{C}.$$ \hfill (18)

In this work, the mapping of amplitudes $\tilde{\alpha}_m$ to codebook entries is done by solving

$$\tilde{\mathbf{A}}_m = \arg \min_{\tilde{\mathbf{A}}_m \in \mathcal{C}} \| \hat{\mathbf{A}}_m - \tilde{\mathbf{A}}_m \|^2_2. \hfill (19)$$

It should be noted that the amplitude vectors should be scaled, to limit the size of the codebook. The codebook amplitudes $\tilde{\mathbf{A}}_m$ are combined with the phases of the amplitude estimates $\hat{\alpha}_m$ to result in the amplitude estimates

$$\tilde{\alpha}_m = [\hat{A}_{1,m} e^{j \hat{\alpha}_{1,m}} \ldots \hat{A}_{L_m,m} e^{j \hat{\alpha}_{L_m,m}}]^T.$$ \hfill (20)

These amplitudes can be substituted in (15), i.e.,

$$\omega_{0,m} = \arg \min_{\omega_{0,m}} \| e^{(1-1) \cdot l} - Z_m \tilde{\alpha}_m \|^2_2. \hfill (21)$$

As an example of what we want to avoid, the magnitude of the amplitude of the fundamental frequency should not be allowed to evolve non-smoothly over time. Using the approach proposed here, the magnitudes of the harmonic amplitudes are constrained to have values that would be considered realistic.

The method proposed in this section, which is based on the harmonic matching pursuit [12], could be used to initialize an EM algorithm, where the superimposed signals are harmonic sources [11] (see also [10]).

4. EXPERIMENTS

We now present the experimental evaluation of the proposed multi-pitch estimator. In the initial, proof-of-concept experiment, the data is synthetically generated using the multi-pitch harmonic signal model (2). The synthetic signal contained two sources, i.e., $M = 2$ with fundamental frequencies $f_{0,1} = 260$ Hz and $f_{0,2} = 390$ Hz, and refined cost function according to (21) (solid).

Fig. 1. Spectrum of synthetic signal used for evaluation of the proposed method.

Fig. 2. Initial cost function according to (12) (dotted), where $f_{0,1} = 260$ Hz and $f_{0,2} = 390$ Hz, and refined cost function according to (21) (solid).
A codebook of amplitudes is trained using ten recordings of different woodwind instruments playing a succession of notes, ranging from C4 (262 Hz) to B4 (494 Hz), i.e., 12 notes. The recordings are single-channel with $f_s = 44.1$ kHz, however, they are downsampled to $f_s = 8$ kHz. The approximate NLS joint pitch and model order estimator in [10] has been used to jointly estimate the pitch and model order for segments of length $N = 240$ samples. The pitch and model order estimates are then used to form LS estimates of the amplitudes (16) for each frame of each signal, resulting in 11544 amplitude vectors. The amplitudes are scaled such that the norm of each amplitude vector equals one before vector quantization. The chosen codeword is then scaled to match the original amplitudes. The codebook has been trained using the $K$-means clustering algorithm [22], where the first 10 harmonics of the woodwind signals are considered. If the estimated model order is less than 10, the remaining values are set equal to zero for the corresponding codebook entry. Different choices of the number of clusters for the training of the codebooks have been considered, varying from 1 to 100 clusters. Empirically, a suitable number of codewords was found to be 10, which is the number of clusters used in this experiment. Examples of codebook entries are shown in Figure 4. For test data, a multi-pitch mixture was created by mixing two single note recordings of a Bb trumpet (with vibrato) and a French horn, playing the notes C4 (262 Hz), and F#4 (370 Hz), respectively (it should be noted that the training and test data are disjoint). White noise was added to result in an SNR of 20 dB. A spectrogram of the mixture and the multi-pitch estimates obtained using the proposed method are shown in Figure 3. Each pitch estimate is obtained by performing a grid search from 100 Hz to $f_s/4 = 2000$ Hz, with a spacing of 0.5 Hz, and the results are compared to results obtained using the usual NLS cost function. The results on real data are similar to the results on synthetic data. When the amplitudes are estimated using LS, the estimates for one of the notes are half of what they should be. Using the proposed method of mapping the estimated amplitudes to codebook entries, it is possible to correctly estimate the fundamental frequencies in the mixture.

5. DISCUSSION

In this paper, a method for multi-pitch estimation of mixtures of harmonic signals has been proposed. The method is based on the harmonic matching pursuit [12], where an initial cost function, and amplitude estimates for each candidate fundamental frequency are formed. These initial amplitudes are then mapped to entries in a codebook. The codebook has been trained using recordings of woodwind instruments, while the mixture consists of recordings of brass instruments. The results show that by using the proposed multi-pitch estimator it is possible to estimate the pitches of multiple sources in a mixture of harmonic signals. The results of the estimator could be used to initialize the EM algorithm [11, 10], and the method could be used in automatic music transcription, enhancement, and separation systems. Future work includes investigating the choice of the number of harmonic amplitudes to include in the codebook, e.g., by using a technique such as variable-dimension vector quantization (VDVQ) [23]. Furthermore it should be investigated whether the amplitudes can be modeled statistically instead of using a codebook approach, which involves training, e.g., by using linear prediction [24].
6. REFERENCES


