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Published in:
IEEE Transactions on Power Electronics

DOI (link to publication from Publisher):
10.1109/TPEL.2017.2714342

Publication date:
2018

Document Version
Version created as part of publication process; publisher's layout; not normally made publicly available

Link to publication from Aalborg University

Citation for published version (APA):
A Decentralized Current-Sharing Controller Endows Fast Transient Response to Parallel DC-DC Converters

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Abstract—This paper proposes a decentralized current-sharing control strategy to endow fast transient response to paralleled DC-DC converters systems, such as DC microgrids or distributed power systems. The proposed controller consist of two main control loops: an external voltage droop control for current-sharing proposes and an internal current loop. The external droop control loop is designed as a voltage loop with embedded virtual impedance, which avoids the use of a slow voltage loop and a separate extra virtual impedance loop that may limit the system bandwidth. The internal current loop, thanks to the external control loop simplification, plays a major role in the system bandwidth, so that an adaptive PI controller is proposed for this matter. In the paper, two different droop control methods have been modeling, designed, simulated, and tested: the conventional virtual-impedance-loop based V-I droop and the proposed embedded-virtual-impedance based I-V droop. In order to compare the dynamic response performances between two droop controllers, their state-space models have been developed and analyzed in this paper. The results show that the dynamic response of the I-V droop control is faster than that of the conventional V-I droop control. Furthermore, by analyzing the effects from I-V droop control parameters, the errors can be reduced faster by enlarging the proportional terms, but with no fluctuations, and then completely eliminated by restoring back to small proportional values. Meanwhile, there exists a trade-off phenomenon between the fast dynamic response and good steady-state performance, thus an adaptive PI controller is proposed to both improve dynamic response and guarantee good steady-state performance simultaneously. Experimental results are shown to verify the accuracy of the models and the effectiveness of the proposed control framework.

Index Terms—Paralleled DC-DC converters, droop control, dynamic response, large-signal model, adaptive PI control

I. INTRODUCTION

THE CONCEPT of dc microgrid (MG) provides a promising solution to integrate renewable energy sources (RESs) into the power grid [1]-[3]. In an islanded dc MG, energy storage system (ESS) need to be installed in the system to provide the voltage support and guarantee the stable operation [4-6]. Due to the capacity extending and distributed configuration of dc MG, multi batteries are usually connected to the common bus by using paralleled converters [7], [8]. Another application for multiple dc-dc converters connected in parallel giving voltage support and current-sharing at the same time, are the distributed power systems (DPS). In a DPS, a number of multiple busses with different voltages are interconnected by multiple paralleled dc-dc converters.

In the aforementioned applications, the droop control is often used by imposing virtual resistance in order to achieve autonomous (communication-less) current sharing among paralleled converters [9]-[11]. When using droop control methods, also named primary control, the major concern of previous works are focused on the secondary and tertiary control levels inside the hierarchical control structure according to voltage deviations caused by line impedance [12]-[16], state of charge (SoC) for battery management systems [17]-[19], power losses [19]-[22], and communication algorithms [16], [22]-[23]. Major part of those methods are based on an adaptive droop control with the virtual impedance or the voltage reference able to adjust those values according to the signals sent by the superior control levels (secondary/tertiary). However, the dynamical process of the droop control to reach a new steady-state operation point has not been studied so much in previous works. Slow response performance can elongate the recovery time of voltage and current, which has adverse effect on the power quality of the system. In addition, due to the load and generation power flows, converters output currents oscillations may exist when dynamic response performances are poor and thus, bus voltage fluctuations may attempt system stability [24].

For the improvement of dynamic characteristics of ac MGs, a small signal state-space model of the whole MG including the droop controller, network and loads is proposed in [25], and the root locus method is used to analyze the dynamic characteristics. On the other hand, the dynamic characteristics of a current-fed converter developed from the corresponding voltage-fed converter by applying the duality-transformation method are investigated in [26], which is based on the photovoltaic generator. In [27], a feed-forward control based on dual-loop constant voltage PI control for three-phase interleaved dc-dc converter in dc MG is proposed, which is used to increase the output current reference of the converter.
when a load change occurs, then the response speed can be improved, but this method is applicable to dc MG that has only one dc-dc converter. In addition, until now there are no reports dealing with the comparison of dynamic response performances between the different droop controls. To fill this gap, this paper presents a comparison of dynamic response performances between two droop control methods, named V-I and I-V droop controllers, showing that the dynamic response of the I-V droop control is faster.

In order to analyze the dynamic response performances of the two droop control methods, mathematic models need to be first built. As a typical method, average-value modeling for converters has been studied in many publications [28], [29]. Average-value modeling method, whose objective is to replace the discontinuous switching cells with continuous blocks that represent the averaged behavior of the switching cell within a prototypical switching interval, can be derived using state-space averaging or circuit averaging methods [30-32]. Considering the inductor-diode-MOSFET switching cell as a simplified variable current source feeding output RC circuit, a model is proposed based on the average injected inductor current in [33]. In [34], instead of using traditional small or linear ripple approximations the model is developed by using the correction coefficients which can account for the current and voltage nonlinear waveforms. The concept of input-output stability is applied to estimate the large-signal stability region via the small-signal feedback control loops in [35], by which the effect of the small-signal loop gains on the large-signal stability region can be also revealed. In this paper, based on the average-value modeling theory, the state-space models of the two droop controls for the analysis of the dynamic characteristics are built. The variation of the load current is set as the input of the model, so that the relations of all the variables in the model are linear. The state variables of the model include the variations of converter’s output current and bus voltage caused by load changes, so that the model can be used to analyze the dynamic response performances of the system. This model has universal applicability for the analysis of dynamic process from one to another steady-state condition for paralleled dc-dc converters.

Although the I-V droop controller is faster than the V-I droop controller, this paper investigates whether there is a room for the further improvement of the I-V droop control transient response, and a novel adaptive PI control is proposed according to the analysis. Authors in [36] propose a parameter tuning algorithm to enable an adaptive PI controller to learn to control a changing process by merely observing the process output errors, which is devised to guarantee the stability of the system. In [37], the adaptive PI controllers are used for the current and voltage control loops of three phase ac-dc PWM converter by automatically adjusting PI control gains via the current and voltage error signals to improve the converters’ tracking performance. In [38], a stable adaptive PI control is designed for the output voltage regulation of a quadratic boost converter, and the identification of a large class of converters that can be stabilized via adaptive PI control is the main contribution. Since abrupt changes of proportional parameters of current PI controllers have adverse effects on the dynamic performances of paralleled dc-dc converters, in this paper, a compensate term is added into the output duty ratio, which is indispensable for the realization of the proposed adaptive PI control.

This paper presents a comparison of dynamic response performances between the V-I and I-V droop controllers. When a load change occurs, the dynamical process to reach a new steady-state point is analyzed and improved. First, the modeling method, which is used for the dynamic analysis of the two droop controllers, is proposed. Second, the root locus methods are used to compare the dynamic response performances between the two droop controllers. The proposed models and the comparative analysis are verified by means of experimental results. Third, the influence of I-V droop control parameters on the dynamic response performances is analyzed and a novel adaptive PI controller is proposed to further improve its dynamic response performances. Finally, experiments are performed to verify the proposed control.

This paper is structured as follows. In Section II, the models of the two droop controllers are built. In Section III, the comparison of dynamic response performances between two droop control methods is presented and verified by experiments. In Section IV, the adaptive PI control to improve the dynamic response of I-V droop control is proposed and verified by experiments. Section V concludes this paper.

II. MODELING FOR TWO DROOP CONTROL SCHEMES

A typical structure of a dc MG consisted of paralleled dc-dc converters with multiple energy storage systems (ESS) is shown in Fig. 1. The ESS can support the bus voltage by using droop control on islanded operation mode. The V-I droop control method for paralleled dc-dc converters is achieved by linearly reducing the voltage reference when the output current increases as shown in Fig. 2(a). In this method, also known as virtual resistance loop, the voltage reference can be obtained by emulating a droop characteristic as

\[ u_{ref} = U_{rate} - ri \]  \hspace{1cm} (1)

where \( u_{ref} \) is the voltage reference, \( U_{rate} \) is the no load voltage of the source, \( r \) is the virtual resistance (VR) and \( i \) is the average inductor current (namely the output current). By reversing the reference output from the droop characteristic, the I-V droop control can be obtained as shown in Fig. 2(b), which is achieved by linearly increasing the current reference when the bus voltage decreases. The current reference can be computed as

\[ i_{ref} = \frac{1}{r} (U_{rate} - u) \]  \hspace{1cm} (2)

where \( i_{ref} \) is the current reference and \( u \) is the bus voltage. For \( n \) paralleled dc-dc converters based on either droop control, the total load current can be shared by converters in proportion to their reciprocals of VRs at steady-state:

\[ i_{ref1} = i_{ref2} = \cdots = i_{refn} \]  \hspace{1cm} (3)

where \( i_k \) \( (k=1, 2, \ldots , n) \) is the output current, \( r_k \) \( (k=1, 2, \ldots , n) \) is the VR, and \( n \) is the number of parallel-connected converters.
derivative, (5) can be rewritten as
\[
\frac{di_d(t)}{dt} = \frac{d_\text{avg}(t)L}{L} = \frac{d_\text{avg}(t)L}{L}.
\] (7)

In addition, since \(i_{\text{dc}} = i_0\) at steady-state, the following equation can be obtained as
\[
\frac{d[u_\text{ref} + u_d(t)]}{dt} = \frac{d[u_\text{ref} + u_d(t)]}{dt} = \frac{i_0 + i_d(t) - i_{\text{dc}} - i_{\text{AVG}}}{C} = \frac{i_d(t) - i_{\text{dc}}}{C}
\] (8)

where \(C\) is the dc bus capacitance. According to (1), at steady-state, the voltage reference can be obtained as
\[
u_{\text{ref}} = u_0 = U_{\text{ref}} - r_0 t.
\] (9)

And expressed in the same form, considering steady-state values and variations:
\[
u_{\text{ref}} + u_{\text{dc}} = U_{\text{ref}} - r_0 t + i_0(t).
\] (10)

Let \(k_{\text{pu}}\) and \(k_{\text{ii}}\) represent the proportional and integral terms of the voltage PI controller, respectively, so that the increment of the current reference can be computed as
\[
i_{\text{AVG}} = k_{\text{ii}} \left[ [u_{\text{ref}} + u_{\text{dc}}] - [u_0 + u_d(t)] \right] + k_{\text{pu}} \int [u_{\text{ref}} + u_{\text{dc}}] - [u_0 + u_d(t)] \right] dt.
\] (11)

Calculating the time derivative of (11) and by considering (7)-(10), then (11) can be rewritten as
\[
\frac{d[i_{\text{AVG}}]}{dt} = \frac{-k_{\text{pu}} \left( i_{\text{AVG}} - i_{\text{dc}} \right)}{C} - \frac{r_{\text{pu}} U_{\text{in}}}{L} \frac{d_\text{avg}(t)}{dt}.
\] (12)

Let \(k_{\text{pu}}\) and \(k_{\text{ii}}\) represent the proportion and integral terms of current PI controller, respectively, so that the increment of duty ratio can be computed as
\[
d_\text{avg}(t) = k_{\text{ii}} \left[ [u_{\text{ref}} + i_{\text{dc}}] - [i_0 + i_d(t)] \right] + k_{\text{pu}} \int [u_{\text{ref}} + i_{\text{dc}}] - [i_0 + i_d(t)] \right] dt.
\] (13)

In steady-state, \(i_{\text{ref}} = i_0\), so that calculating the time derivative of (13) and by considering (7) and (12), then (13) can be rewritten as
\[
\frac{dd_\text{avg}(t)}{dt} = \frac{-r_{\text{pu}} k_{\text{ii}} i_{\text{dc}} + r_{\text{pu}} k_{\text{ii}} i_{\text{dc}}}{C} - \frac{r_{\text{pu}} k_{\text{ii}} E + r_{\text{pu}} U_{\text{in}}}{L} \frac{d_\text{avg}(t)}{dt}.
\] (14)

Thus, (7), (8), (12) and (14) can be rewritten in a state-space model as the following compact form:
B. Modeling for I-V Droop Control

Let \( i_{\text{ref}}, i_0, \) and \( d_0 \) represent the current reference, the average inductor current and the duty ratio in steady-state, \( i_{\text{det}}(t), i_d(t) \) and \( d_d(t) \) represent the variation of current reference, inductor current and duty ratio after load changing. According to (2), at steady-state, the current reference can be obtained as

\[
i_{\text{ref}} = i_0 = \frac{1}{r} (U_{\text{rate}} - u_0).
\]

And expressed in the same form, considering steady-state values and variations:

\[
i_{\text{ref}} + i_{\text{det}}(t) = \frac{1}{r} [U_{\text{rate}} - u_0 + u_d(t)].
\]

Calculating the time derivative of (13) and considering (16) and (17), (13) can be rewritten as

\[
\frac{dd_d(t)}{dt} = k_p \left[ \frac{-du_d(t)}{dt} - \frac{di_d(t)}{dt} \right] + k_i \left[ \frac{-u_d(t)}{r} - i_d(t) \right].
\]

Substituting (7) and (8) into (18), (18) can be rewritten as

\[
\frac{dd_d(t)}{dt} = \left( k_p \frac{1}{rC} + k_i \right) i_d(t) + \left( k_p \frac{U_{\text{in}}}{L} - \frac{1}{r} \right) i_{\text{det}}(t) - \frac{k_p}{rC} U_{\text{in}} d_d(t) + \frac{k_p}{rC} i_{\text{dref}}(t).
\]

Then (7), (8) and (19) can be rewritten in a state-space model as the following compact form:

\[
\begin{bmatrix}
i_d \\
d_d \\
i_{\text{dref}}
\end{bmatrix} = \begin{bmatrix}
0 & U_{\text{in}} & \frac{1}{L} \\
0 & \frac{k_p}{rC} + k_i & \frac{k_p}{L} - \frac{k_p}{r} \\
\frac{1}{C} & 0 & 0
\end{bmatrix} \begin{bmatrix}
i_d \\
d_d \\
i_{\text{dref}}
\end{bmatrix} + \begin{bmatrix}
0 \\
0 \\
0
\end{bmatrix} \cdot i_{\text{dref}}.
\]

III. DYNAMIC ANALYSIS FOR TWO DROOP SCHEMES

A. Dynamics Comparison for the Two Droop Controllers

By setting the average inductor current as the output, the root locus method has been employed to analyze the dynamic characteristics of the V-I and I-V droop controls. The parameters of electrical setup, current PI controller and VR of the two controls are listed in Table I. Setting the voltage loop integral parameter of the V-I droop control as \( I \) and by changing its proportional term value from 0.01 to 1, the pole shifting trajectories of the output current are shown in Fig. 3. Setting the voltage loop proportional term value of the V-I droop control as 0.1 and by changing its integral term value from 0.1 to 10, the pole shifting trajectories of the output current are shown in Fig. 4.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>( U_{\text{in}} )</td>
<td>Input Voltage</td>
</tr>
<tr>
<td>( L )</td>
<td>Converter Inductance</td>
</tr>
<tr>
<td>( C )</td>
<td>DC bus Capacitance</td>
</tr>
<tr>
<td>( r )</td>
<td>Virtual Resistance</td>
</tr>
<tr>
<td>( k_p )</td>
<td>Current Loop Proportional Term</td>
</tr>
<tr>
<td>( k_i )</td>
<td>Current Loop Integral Term</td>
</tr>
<tr>
<td>( U_{\text{bus}} )</td>
<td>Rated Bus Voltage</td>
</tr>
</tbody>
</table>

From the pole shifting trajectories of two droop controls it can be seen that during the dynamical process, higher frequency oscillation can be caused by both the two droop controls, which attenuates rapidly. The low frequency oscillation which attenuates much more slowly can be caused by the V-I droop control due to the two poles closer to imaginary axis no matter how much the voltage loop
parameters are.

The comparison between the two droop controls shows that when the system current is changed due to either generation or consumption, the system with the I-V droop control will reach steady-state more rapidly compared with the V-I droop controller, so that the dynamic response of the I-V droop control is faster.

B. Verification for Model and Analysis

The islanded experimental dc MG setup, which consists of four 0.7 kW dc-dc converters, a battery, a real-time dSPACE1006 platform and resistance loads, has been built as shown in Fig. 5. The switching frequency is set to 10 kHz. The parameters of electrical setup, current PI controller and VR of the two droop controls are listed in Table I as well. The proportional and integral term values of the voltage PI controller are set as 0.1 and 1, respectively. The tests of step response for output current based on V-I droop control and I-V droop control have been obtained by using the obtained models and contrasted with the experimental results.

Putting into 100W load, the experimental waveform of the output current obtained by using the V-I droop control is shown in Fig. 6(a), which is identical with that from the model, as shown in Fig. 6(b). Fig. 7(a) shows the experimental waveform of the output current obtained by using I-V droop control, which is identical with that from the model as shown in Fig. 7(b). It can be seen that the models are accurate and the low frequency fluctuation attenuating much slowly can be caused by the V-I droop control, cannot be obtained by using the I-V droop control, which is consistent with the analysis.

IV. ADAPTIVE PI CONTROL AND EXPERIMENT VERIFICATION

Section III has shown that the dynamic response performance of the I-V droop control is faster than that of the V-I droop control. However, the dynamic response performance of I-V droop control can be influenced by other factors as well. According to the state-space model, it can be found that the factors influencing the dynamic performance of the I-V droop control include the input voltage, the converter inductance, the bus capacitance, the virtual resistance and the proportional and integral parameters of current PI controller. However, the virtual resistance and the electrical setup parameters can hardly be changed, so it is more practical to improve the dynamic characteristics by adjusting PI controller parameters, which will be further studied in this Section.

A. Analysis of the Dynamic Response Performance

For $n$ dc-dc converters, let $I_d$ and $D_d$ represent the variations of the average inductor currents and the duty ratios, respectively, where

$$I_d = [i_{d1} \ i_{d2} \cdots \ i_{dn}]^T, \ D_d = [d_{d1} \ d_{d2} \cdots \ d_{dn}]^T.$$

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Symbol</th>
<th>Description</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Electrical setup parameters</td>
<td>$U_m$</td>
<td>Input Voltage</td>
<td>230 V</td>
</tr>
<tr>
<td></td>
<td>$L$</td>
<td>Converter Inductance</td>
<td>1.8 mH</td>
</tr>
<tr>
<td></td>
<td>$C$</td>
<td>DC Bus Capacitance</td>
<td>8800 μF</td>
</tr>
<tr>
<td>Droop control parameters</td>
<td>$r_1$</td>
<td>Virtual Resistance of Converter 1</td>
<td>1 Ω</td>
</tr>
<tr>
<td></td>
<td>$r_2$</td>
<td>Virtual Resistance of Converter 2</td>
<td>1/2 Ω</td>
</tr>
<tr>
<td></td>
<td>$r_3$</td>
<td>Virtual Resistance of Converter 3</td>
<td>1/3 Ω</td>
</tr>
<tr>
<td></td>
<td>$r_4$</td>
<td>Virtual Resistance of Converter 4</td>
<td>1/4 Ω</td>
</tr>
<tr>
<td></td>
<td>$U_{bus}$</td>
<td>Rated Bus Voltage</td>
<td>100 V</td>
</tr>
</tbody>
</table>

Let $I_d$ represent the $n$-order vector with all elements 1. Since all the modules share the common part of capacitor and load, (7) and (8) can be respectively rewritten as
\[
\frac{dI_a(t)}{t} = [D_a(t)U_{in} - u_d(t)I]^T, \quad (21)
\]
\[
\frac{du_d(t)}{dt} = \frac{1}{C}[I_a(t)I^T - i_{kh}(t)] \quad (22)
\]
where
\[
U_{in} = \begin{bmatrix}
U_{in1} & 0 & \cdots & 0 \\
0 & U_{in2} & \cdots & 0 \\
\vdots & \vdots & \ddots & \vdots \\
0 & 0 & \cdots & U_{inn}
\end{bmatrix},
L = \begin{bmatrix}
L_1 & 0 & \cdots & 0 \\
0 & L_2 & \cdots & 0 \\
\vdots & \vdots & \ddots & \vdots \\
0 & 0 & \cdots & L_n
\end{bmatrix}.
\]

Considering the current PI controller, (18) can be rewritten as
\[
\frac{dD_a(t)}{dt} = [-\frac{dI_a(t)}{dt}IR^1 - \frac{dI_a(t)}{dt}]K_{pi} + [-u_d(t)IR^1 - I_d(t)]K_{ii} \quad (23)
\]
where
\[
R = \begin{bmatrix}
r_1 & 0 & \cdots & 0 \\
0 & r_2 & \cdots & 0 \\
\vdots & \vdots & \ddots & \vdots \\
0 & 0 & \cdots & r_n
\end{bmatrix},
K_{pi} = \begin{bmatrix}
k_{p1} & 0 & \cdots & 0 \\
0 & k_{p2} & \cdots & 0 \\
\vdots & \vdots & \ddots & \vdots \\
0 & 0 & \cdots & k_{pi}\n
K_{ii} = \begin{bmatrix}
k_{i1} & 0 & \cdots & 0 \\
0 & k_{i2} & \cdots & 0 \\
\vdots & \vdots & \ddots & \vdots \\
0 & 0 & \cdots & k_{ii}
\end{bmatrix}
\]

Substituting (21) and (22) into (23), (23) can be rewritten as
\[
\frac{dD_a(t)}{dt} = -I_a(t) \cdot \frac{1}{C} I^T K_{pi} R^1 + K_{ii} - D_a(t) \cdot K_{pi} L^T U_{in} + u_d(t) \cdot (K_{pi} L^1 - K_{ii} R^1) + i_{kh}(t) \cdot \frac{IK_{pi} R^3}{C} \quad (24)
\]
where
\[
K_{pi} = \begin{bmatrix}
k_{p1} & 0 & \cdots & 0 \\
0 & k_{p2} & \cdots & 0 \\
\vdots & \vdots & \ddots & \vdots \\
0 & 0 & \cdots & k_{pi}\n
K_{ii} = \begin{bmatrix}
k_{i1} & 0 & \cdots & 0 \\
0 & k_{i2} & \cdots & 0 \\
\vdots & \vdots & \ddots & \vdots \\
0 & 0 & \cdots & k_{ii}
\end{bmatrix}
\]

In order to analyze a general paralleled module system consisting of \( n \) converters, (21), (22) and (24) can be rewritten in a more compact state-space model defined as
\[
\dot{x} = A \cdot x + B \cdot y \quad (25)
\]
where
\[
A = \begin{bmatrix}
0 & L^1 U_{in} & -L^1 I^T \\
-\frac{K_{pi} R^1 I^T I}{C} - K_{ii} & -K_{pi} L^1 U_{in} & K_{pi} L^1 I^T - K_{ii} R^1 I^T \\
\frac{1}{C} I & 0 & 0
\end{bmatrix},
B = \begin{bmatrix}
IK_{pi} R^1 C \cdot -\frac{1}{C} I^T \\
\end{bmatrix},
\]
\[
\dot{x} = [I_a(t) \quad D_a(t) \quad u_d(t)]^T, \quad y = i_{kh}(t).
\]

In the state-space model, there are two state variables in each converter and one common state variable from the capacitor and load part. Thus, in the system with \( n \) converters, the total number of state variables is \((2n+1)\). Taking four paralleled converters as an example, the root locus method is used based on the model shown in (25) to analyze the dynamic response of the system by shifting different control parameters. The electrical setup and VR parameters which are kept constant are shown in Table II.

![Fig. 8. Root locus analysis for all converters with proportional terms changing.](image1)

![Fig. 9. Root locus analysis for all converters with integral terms changing.](image2)

The integral term values for four converters are initialized as 0.01, respectively. Then changing the proportional term values of all the converters from 0.00001 to 0.1, the pole shifting trajectories of all converters’ average inductor current are shown in Fig. 8, which demonstrates that the system can be unstable when all the proportional terms are too small. When the four converters’ proportional term values are initialized as 0.001, changing the integral term values of all the converters from 0.0001 to 1, respectively, the pole shifting trajectories of four converters’ output currents can be observed as shown in Fig. 9. According to the pole shifting trajectories, the result can be obtained that increasing integral terms can enlarge current fluctuations during dynamical process, but the errors can be eliminated more rapidly. Specifically, Fig. 9 shows that the system can be unstable when all the integral terms are too large.

**B. The Proposed Adaptive PI Control**

According to the preceding analysis it can be seen that integral terms can be hardly optimized to improve the current sharing speed without fluctuations, so optimizing the proportional terms is the most effective way to improve the dynamic response performance. During dynamical process, the errors can be rapidly reduced by large proportional terms with no fluctuations and then completely eliminated under small proportional terms as shown in Fig. 11. In addition, the disturbances of duty ratios will be greater in steady-state because of large proportional terms, which results in stronger...
fluctuating inductor currents against the steady-state characteristics [27]. Therefore, an adaptive PI controller with a compensator is proposed to improve the dynamic response of I-V droop control and guarantee good steady-state performance simultaneously.

Fig. 10. Step response of output current under different proportional terms.

Let $e_k(t)$ be the absolute error between current reference and average inductor current of the $k$-th converter, then

$$e_k(t) = \left| -\frac{1}{r_k}u_k(t) - i_{\text{in}}(t) \right|. \quad (26)$$

In steady-state, the error between current reference and the average inductor current is zero, but during dynamical process, the error can be changed. When the $e_k(t)$ reaches the specific threshold value, the proportional term should be increased to improve the speed of error reduction. In steady-state, let $\Delta u_{\text{max}}$ represent the max fluctuation amplitude of the bus voltage ripple, $\Delta i_{\text{max}}$ represent the max ripple fluctuation amplitude of the average inductor current which is sampled by the $k$-th converter. In order to guarantee the proportional term constant in steady-state, this threshold value $e_{1k}$ should satisfy the following condition as

$$e_{1k} > \frac{\Delta u_{\text{max}}}{r_k} + \Delta i_{\text{max}}. \quad (27)$$

In order to prevent the frequent switching of the proportional term, the hysteresis loop needs to be used as shown in Fig. 11, so the follows can be obtained

$$\begin{cases} 
\Delta k_{pk} = 0 & e_k(t) < e_{2k} \\
\Delta k_{pk} = k_{pk} & e_k(t) > e_{2k} \\
\Delta k_{pk} \text{ is kept unchanging} & e_{1k} < e_k(t) < e_{2k}
\end{cases} \quad (28)$$

where $\Delta k_{pk}$ means the variation of proportional term of the $k$-th converter, and $k_{pk}$ needs to be increased to $k_{pk}$ to improve the response speed when the absolute error increases to $e_{2k}$. As the absolute error is less than $e_{1k}$, $k_{pk}$ returns to zero to eliminate the error rapidly and guarantee good steady-state performance. According to (3), the relationship between the $n$ converters’ threshold values can be obtained as

$$\begin{cases} 
e_{11}r_1 = e_{12}r_2 = \cdots = e_{1n}r_n \\
e_{21}r_1 = e_{22}r_2 = \cdots = e_{2n}r_n \\
\Delta k_{pk} \text{ is kept unchanging} & e_{1k} \leq \Delta u_{\text{max}} / r_k + \Delta i_{\text{max}}, \quad \text{k} = 1, 2, \ldots, n
\end{cases} \quad (29)$$

However, since the difference between the average inductor current and current reference is not always zero at the very beginning of $\Delta k_{pk}$ restoring to zero, the output duty ratio of PI controller will change back at the falling edge of $\Delta k_{pk}$ to induce that the output current returns back, which can increase $\Delta k_{pk}$ to $k_{pk}$ again. Since the above processes can take place repeatedly, fluctuations of currents will be induced and the dynamic can be weaker.

Fig. 11. Adaptive PI controller based on droop control.

In order to solve this problem, the improved method for this adaptive PI controller is proposed. At the very beginning of $\Delta k_{pk}$ restoring back, the output duty ratio needs to be constant to hold the inductor current, so a compensate term need to be added into the output duty ratio at the falling edge of $\Delta k_{pk}$, which can be computed as

$$d_{pk} = k_{pk}[i_{\text{ref}}(t) - i_{\text{in}}(t)] \quad (30)$$

where $d_{pk}$ is the compensate value for the $k$-th converter. Due to this improvement, the repeated fluctuations of currents can be avoided, and the voltage and current can smoothly transit from the dynamic process to the steady-state. Thus, the dynamic response performances can be improved by the adaptive PI controller as shown in Fig. 11, and the steady characteristics can be guaranteed simultaneously.

C. Experiments of Adaptive PI Control

For the four converters whose parameters are listed in Table II, Fig. 8 shows that when all the integral term values are 0.01 and the proportional term values are not less than 0.001, there...
are no low-frequency fluctuating components, so that considering speeds of error elimination, the proportional term values can be initialized as 0.001. Putting into 350W load, the bus voltage and four output currents are illustrated in Fig. 12 which shows that even though there are no oscillations, the transient response performances are slow.

The experiments have been performed by using the adaptive PI controller without the compensator. Fig. 8 shows that increasing proportional term values to 0.008, the speeds of error reduction can be obviously improved at the beginning of the dynamic process and all the fluctuating components can be further suppressed. Thus, initializing proportional and integral term values as 0.001 and 0.01, respectively, \( k_{p,0} \) is set as 0.007.

Putting into 350W load, the bus voltage and four output currents are illustrated in Fig. 13, which shows that fluctuations of currents have been induced and transient response performances have not been enhanced.

With the compensator, the bus voltage and four output currents are illustrated in Fig. 14, which shows that the transient response performances have been obviously enhanced and the voltage sags are decreased as well. There are no huge oscillations or overshoots, and the voltage and current can smoothly transit from the dynamic process to the steady-state. The experimental results verify that the dynamic characteristics can be significantly improved by using the proposed adaptive PI controller.

![Fig. 12. The bus voltage and four output currents as \( k_p=0.001 \) and \( k_i=0.01 \).](image1.png)

![Fig. 13. The bus voltage and four output currents when the adaptive PI control is used without the compensator.](image2.png)

![Fig. 14. The bus voltage and four output currents when the adaptive PI control is used with the compensator.](image3.png)

V. CONCLUSION

Two models considering \( V-I \) droop and \( I-V \) droop have been built separately, based on which this paper presents a dynamic response comparison between two droop controllers. The results show that the dynamic response performance of \( I-V \) droop control method is much faster than that of the \( V-I \) droop control because two more poles always exist near the imaginary axis in the \( V-I \) droop-based model no matter how to change the parameters. Furthermore, an adaptive PI controller with a duty ratio compensator is proposed to further improve the transient response performances of \( I-V \) droop controller. The compensate term of duty ratio is added into the control to hold output currents at the falling edge of proportional terms, which is indispensable for the realization of the proposed adaptive PI control. Experiments in a dc microgrid system have been performed to verify the effectiveness of the proposed control framework.

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CM and signal average

This article has been accepted for publication in a future issue of this journal, but has not been fully edited. Content may change prior to final publication. Citation information: DOI 10.1109/TPEL.2017.2714342, IEEE Transactions on Power Electronics.
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