Small-Scale Testing of Laterally Loaded Non-Slender Monopiles in Sand

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Small-Scale Testing of Laterally Loaded Non-Slender Monopiles in Sand

K. Thomassen¹; H. R. Røesen¹; L. B. Ibsen²; and S. P. H. Sørensen³
Aalborg University, June 2010

Abstract
In current design of offshore wind turbines, monopiles are often used as foundation. The behaviour of the monopiles when subjected to lateral loading has not been fully investigated, e.g. the diameter effect on the soil response. In this paper the behaviour of two non-slender aluminium piles in sand subjected to lateral loading are analysed by means of small-scale laboratory tests. The six quasi-static tests are conducted on piles with diameters of 40 mm and 100 mm and a slenderness ratio, $L/D$, of 5. In order to minimise scale effects, the tests are carried out in a pressure tank at stress levels of 0 kPa, 50 kPa, and 100 kPa, respectively. From the tests load-deflection relationships of the piles at three levels above the soil surface are obtained. The load-deflection relationships reveal that the uncertainties of the results for the pile with diameter of 40 mm are large due to the small soil volume activated during failure. From the load-deflection relationships normalised as $H/(L^2D\gamma')$ and $y/D$ indicates that the lateral load, $H$, is proportional to the embedded length square times the pile diameter, $L^2D$. Furthermore, by comparing the normalised load-deflection relationships for different stress levels it is seen that small-scale tests with overburden pressure applied is preferable.

1 Introduction
In the design of laterally loaded monopiles the $p−y$ curve method given in the design regulations API (1993) and DNV (1992) is often used. For piles in sand the recommended $p−y$ curves are based on results from two slender, flexible piles with a slenderness ratio $L/D = 34.4$ where $L$ is the embedded length and $D$ is the diameter. Contrary to the assumption of flexible piles for these curves the monopile foundations installed today has a slenderness ratio $L/D < 10$, and behaves almost as rigid objects. The recommended curves does not take the effect of the slenderness ratio into account. Furthermore, the initial stiffness is considered independent of the pile properties such as the pile diameter. The research within the field of diameter effects gives contradictory conclusions. Different studies have shown the initial stiffness to be either independent, linearly dependent, or non-linear dependent on the pile diameter, cf. Brodåæk et al. (2009).

This paper evaluates the effects of the pile diameter on the soil resistance through six small-scale tests.

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2 Test Programme

Scale effects occur when conducting small-scale tests in sand at 1 g. At low stress levels the soil parameters, in particular the internal angle of friction, will vary strongly with the effective stresses. Therefore, it is an advantage to increase the effective stresses to a level where the internal angle of friction is independent of the stress variations. This increase in stresses will minimise the fluctuations of the measurements as well. To make the increase in stress level possible the tests are conducted in a pressure tank, cf. Fig. 1.

The tests are carried out at stress levels of 0 kPa, 50 kPa, and 100 kPa, and the results are presented in this paper. The tests are quasi-static tests on two closed-ended aluminium pipe piles with outer diameters of 40 mm and 100 mm and a slenderness ratio of 5, corresponding to embedded lengths of 200 mm and 500 mm, respectively. The wall thickness of the piles is 5 mm.

The test programme, cf. Tab. 1, is designed to investigate the soil resistance dependency of the pile diameter at different stress levels. The pile diameters in the test programme are chosen to supplement the tests described in Sørensen et al. (2009) where piles with diameters of 60 mm and 80 mm were tested. To some extent the results from these tests are included in this paper.

<table>
<thead>
<tr>
<th>Test</th>
<th>$D_{[mm]}$</th>
<th>$L/D$</th>
<th>$P_0$ [kPa]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Test 1</td>
<td>100</td>
<td>6</td>
<td>0</td>
</tr>
<tr>
<td>Test 2</td>
<td>100</td>
<td>5</td>
<td>50</td>
</tr>
<tr>
<td>Test 3</td>
<td>100</td>
<td>5</td>
<td>100</td>
</tr>
<tr>
<td>Test 4</td>
<td>40</td>
<td>5</td>
<td>0</td>
</tr>
<tr>
<td>Test 5</td>
<td>40</td>
<td>5</td>
<td>50</td>
</tr>
<tr>
<td>Test 6</td>
<td>40</td>
<td>5</td>
<td>100</td>
</tr>
</tbody>
</table>
3 Tests in Pressure Tank

The tests are carried out in a pressure tank installed in the Geotechnical Engineering Laboratory at Aalborg University, Denmark, cf. Fig. 1. The tank has a height of 2.5 m and a diameter of 2.1 m. The tank is placed in a load-frame on a reinforced foundation separated from the rest of the floor in the laboratory.

3.1 Test Setup

Inside the tank a 0.58 m thick layer of fully saturated sand with a layer of highly permeable gravel underneath was located. A cross sectional view of the pressure tank and test setup can be seen in Fig. 2.

The test piles were installed in the sand layer, cf. Fig. 3. A lateral load was applied by means of a wire connected in series to a hydraulic piston through a force transducer. The deflection of the piles was measured by displacement transducers attached in three different levels above soil surface, cf. Fig. 4 and Fig. 5. Thereby, three load-deflection relationships were obtained. To make the soil preparation and pile installation possible the platform mounted on top of the pressure tank, cf. Fig. 1, was used.

3.2 Increase of the Effective Stresses

The increase of the effective stresses in the soil was obtained by placing an elastic, rubber membrane on the soil surface. The membrane was sealed around the pile and against the side of the tank causing the fully saturated soil to be sealed from the air in the upper part of the tank, cf. Fig. 6. Water was poured in on top of the membrane to ensure fully saturated sand even if there were small gabs in the membrane or in the sealing between membrane and tank. Moreover, the dynamic viscosity of water is approximately 55 times greater than of air, and thereby the water minimised the flow through gaps.
The effective stresses were then increased by closing the openings in the tank, as shown in Fig. 7, and applying an air pressure of 50 kPa and 100 kPa, respectively. Because the pressure in the upper part of the tank made the membrane resemble an applied surface load, a homogeneous increase of the effective stresses was obtained.

### 3.3 Hydrostatic Pore Pressure

To maintain a hydrostatic pore pressure in the soil, an ascension pipe was connected to the tank and, thereby, the water flowing through the gaps was led out of the tank. This way the soil remained fully saturated and the stresses were applied as effective stresses only. The variation of the effective vertical stresses in the soil layer is shown in Fig. 8, where $P_0$ denotes the applied overburden pressure. The ascension pipe can be seen in Fig. 9.

### 4 Measuring System

The hydraulic piston used to actuate the pile was controlled by a predefined displacement and it acted at a vertical eccentricity of 370 mm above the soil surface, cf. Fig. 4. The force transducer connecting the wire and the hydraulic system in series, cf. Fig. 2 (a), was a HBM U2B 10 kN for tests on the 40 mm pile and a HBM U2B 20 kN for the 100 mm pile.
The displacement transducers, cf. Fig. 2 (2), were of the type WS10-1000-R1K-L10 from ASM Gmbh. For measuring the pressure in the tank a HBM P6A 10 bar absolute pressure transducer was employed in the first test, and a HBM P3MBA 5 bar absolute pressure transducer was employed in the remaining tests reducing the fluctuations of the measurements. The sampling frequency was 10 Hz.

5 Soil conditions

The sand used in the tank was Baskarp Sand No. 15. The material properties for Baskarp Sand No. 15 are well-defined from previous tests in the laboratory at Aalborg University. A representative distribution of the grains found by sieve analysis is shown in Fig. 10. The uniform grading of the grains makes it possible to obtain a homogeneous compaction of the soil. The hydraulic conductivity is $k \approx 6 \cdot 10^{-5}$ m/s. The loading velocity was $1 \cdot 10^{-5}$ m/s, thus, the soil was considered drained during the tests. The material properties are given in Tab. 2.

<table>
<thead>
<tr>
<th>Property</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Specific grain density $d_s$</td>
<td>2.64</td>
</tr>
<tr>
<td>Maximum void ratio $e_{\text{max}}$</td>
<td>0.858</td>
</tr>
<tr>
<td>Minimum void ratio $e_{\text{min}}$</td>
<td>0.549</td>
</tr>
<tr>
<td>$d_{50}$ = 50%-quantile [mm]</td>
<td>0.14</td>
</tr>
<tr>
<td>$U = d_{60}/d_{10}$</td>
<td>1.78</td>
</tr>
</tbody>
</table>

5.1 Soil preparation

Prior to each test the soil was loosened by an upward gradient of 0.9. Hereafter, it was vibrated mechanically to ensure fully saturated soil and a homogeneous compaction.

The pile was installed in the centre of the tank. During installation, a gradient of 0.9 was applied to minimise the pressure on the closed end of the pile. Hereby, the toe resistance and the skin friction along the pile were minimised. After installation the soil was vibrated mechanically, cf. Fig. 12, to minimise disturbances in the soil emerged from the pile installation. While vibrating the pile was secured in its upright position by means of the hydraulic piston mounted through the top hatch of the tank, cf. Fig. 2 (1) and Fig. 11.

To control the homogeneity and the compaction of the soil, cone penetration tests (CPT) were conducted. The setup of the CPT-device can be seen in Fig. 13. A total
of six CPT’s were conducted prior to each test. Four were conducted in a distance of 500 mm from the centre of the pile, cf. Fig. 14. The remaining two CPT’s were conducted 160 mm and 200 mm from the pile centre for the 40 mm and the 100 mm pile, respectively. Both were conducted on the neutral side of the pile. The probe diameter of the CPT-device was 15 mm.

In Fig. 15 the cone resistance of the CPT’s conducted prior to test 5 shows a homogeneous compaction of the soil. Fig. 16 shows the mean value of the cone resistance, $q_c$, prior to each of the six tests described in this paper and those obtained prior to the tests described in Sørensen et al. (2009). The figure shows that $q_c$ of the soil was approximately the same for the six tests conducted on the 40 mm pile and the 100 mm pile. Though, compared to the CPT’s conducted in Sørensen et al. (2009) they were higher.

In Tab. 3 the soil parameters derived on basis of the CPT’s are presented. The parameters are derived in accordance to Ibsen et al. (2009), cf. Eqs. 1 to 5, which are derived empirically for Baskarp Sand No. 15. The formulation for the tangential modulus of elasticity, $E_0$ cf. Eq. 6, is given by Brinkgreve and Swolfs (2007).

\[
\varphi_{tr} = 0.152 \cdot I_D + 27.39 \cdot \sigma'_3^{-0.2807} + 23.21 \\
\psi_{tr} = 0.195 \cdot I_D + 14.86 \cdot \sigma'_3^{-0.9764} - 9.946 \\
I_D = c_2 \left( \frac{\sigma'_1}{(q_c)^{c_3}} \right)^{c_3} \\
\gamma' = \frac{d_s - 1}{1 + e_{in-situ}} \gamma_w \\
E_{50} = (0.6322 \cdot I_D^{2.507} + 10920) \cdot \left( \frac{c \cdot \cos \varphi_{tr} + \sigma'_3 \cdot \sin \varphi_{tr}}{c \cdot \cos \varphi_{tr} + \sigma'_3 \cdot \sin \varphi_{tr}} \right)^{0.58} \\
E_0 = \frac{2 \cdot E_{50}}{2 - R_f} 
\]
\( \varphi_{tr} \) is the internal angle of friction, \( I_D \) is the identity index, \( \sigma_3' \) and \( \sigma_1' \) are the effective horizontal and vertical stresses, respectively, and \( \psi_{tr} \) is the dilation angle. \((c_1, c_2, c_3) = (0.75, 5.14, -0.42)\), \( \gamma' \) is the effective unit weight of the soil, \( d_s \) is the relative density of the soil, \( e_{in-situ} \) is the in-situ void ratio, and \( \gamma_w \) is the unit weight of water. \( E_0 \) is the secant modulus of elasticity, \( c \) is the cohesion, and \( R_f \) is the failure ratio, which is normally set to 0.9.

By comparing the obtained parameters to the ones derived in Sørensen et al. (2009), given in Tab. 4, it can be seen that the identity indices, \( I_D \), derived for the present tests are approximately 10% higher. Because the internal angle of friction, \( \varphi_{tr} \), and the effective unit weight of the soil, \( \gamma' \), are dependent on \( I_D \) these parameters are slightly higher as well. The tangential modulus of elasticity, \( E_0 \), is not calculated for the tests without overburden pressure because the low stress level leads to large uncertainties in the determination.

### 6 Results

During the tests, prescribed displacements were applied to the pile and, thereby, the soil was brought to failure, then unloaded and reloaded. Hereby, an estimation of the ultimate soil resistance and the elastic behaviour of the soil can be obtained.
In Fig. 17 the load-deflection relationships for test 4 are shown. Firstly, it can be seen that, when unloading and reloading, the load-deflection curves reach the original curves. Secondly, the upper displacement transducer recorded the largest deflection, while the lower transducer recorded the smallest. This is in agreement with the expected results.

The normalised relationships between load, $H/H_{\text{max}}$, and deflection, $y/D$, at the level of the hydraulic piston ($x = -370$ mm) for test 1 to 3 are shown in Fig. 18. The test without overburden pressure gives a more curved graph than the tests with overburden pressures. This is caused by the low stress level, at which the dilation of the soil is larger.

**6.1 Plastic Response and Pile Capacity**

The plastic behaviour of the soil depends on the applied overburden pressure. For the case without overburden pressure the plastic deformation after the first unloading is approximately 85 % of the total deformation after the first loading. For the cases were overburden pressures of 50 kPa and 100 kPa were applied the plastic deformation is 50 % and 60 %, respectively, of the total deformation after the first loading, cf. Fig. 18.

In Fig. 18 it can be observed that several loading-reloading curves are present for the test at 50 kPa. The reason for this deviation compared to the remaining tests is that the test was run in three stages because of problems with the wire transferring the load to the pile. During the first run the wire was dragged out of its bracket. Therefore, the applied displacement was obtained in the extension of the wire, which resulted in very small deflections of the pile. During the second run the wire deformed, again leading to small deflections of the pile. A last run was conducted and the wanted deflection of the pile was obtained.

Figs. 19 and 20 present the dependency of the overburden pressure on the lateral load. As expected, the capacity of the soil increases with increasing overburden pressure. The difference between the lateral load for the tests without overburden pressure compared to the ones with overburden pressures of 50 kPa and 100 kPa, respectively, is determined for 10 mm de-
flection at the level of the hydraulic piston, i.e. $x = -370 \text{ mm}$. The lateral load increases with a factor of 17 for the 40 mm pile for 50 kPa and 15 for the 100 mm pile. For 100 kPa the load increases with a factor of 18 and 20 for the 40 mm pile and the 100 mm pile, respectively.

### 6.2 Uncertainties for the 40 mm Pile

Conducting tests on the 40 mm pile was difficult because little disturbance of the soil would cause large uncertainties for the obtained results due to the small soil volume activated during failure. Fig. 19 shows the load-deflections relationship for the 40 mm pile. The figure shows an unexpected appearance of the graph for the test at 100 kPa as the graph for the first loading describes nearly a straight line. Before this test the pile got stuck in the hydraulic piston and when releasing it the surrounding soil was disturbed. This disturbance might have caused a decrease of the strength in the soil. Thereby, the graph is straight till the point where the pile obtained a deflection large enough to activate the undisturbed soil further away from the pile. Therefore, the results from test 6 are not considered to represent the correct behaviour of an undisturbed soil.

### 6.3 Comparison of Test Results

In Fig. 21 the results for the tests without overburden pressure are compared to the results obtained by Sørensen et al. (2009) for 60 mm and 80 mm piles. As expected, the lateral load necessary to obtain a deflection of the pile increases with increasing pile diameter.

Figs. 22, 23, and 24 shows the normalised relationships between the lateral load, $H$, and the deflection, $y$, determined at the level of the hydraulic piston for the three stress levels. The normalised formulation for the load, Eq. 7, is chosen because the load is assumed dependent on the soil volume activated during failure, and the stresses in the soil. This assumption provides the expression $LD\sigma'$ that can be rewritten to $LD\gamma' = L^2D\gamma'$.

\[
\text{Normalised load} = \frac{H}{L^2D\gamma'} \quad (7)
\]

\[
\text{Normalised deflection} = \frac{y}{D} \quad (8)
\]
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**Figure 21:** Load-deflection relationships for the four piles at $P_0 = 0$ kPa.

**Figure 22:** Normalised relationships between load ($H/H_{\text{max}}$) and deflection ($y/D$) measured at the level of the hydraulic piston for the tests at $P_0 = 0$ kPa.

**Figure 23:** Normalised relationships between load ($H/H_{\text{max}}$) and deflection ($y/D$) measured at the level of the hydraulic piston for the tests at $P_0 = 50$ kPa.

**Figure 24:** Normalised relationships between load ($H/H_{\text{max}}$) and deflection ($y/D$) measured at the level of the hydraulic piston for the tests at $P_0 = 100$ kPa.

Fig. 22 shows deviations between the normalised curves for the four piles without overburden pressure. The curves seems to be grouped in pairs. The 80 mm pile and the 100 mm pile are similar at the initial part of the curves, but deviates at larger deflections. The curves for the 40 mm and the 60 mm pile are similar, but this might be caused by the fact that the identity index for the soil was approximately 10 % larger for the test on the 40 mm pile than for the test on the 60 mm pile, cf. Tabs. 3 and 4.

The reason for the deviations could be the difference in the soil volume activated during failure and the different embedded lengths for the four piles, which causes deviations of the reached stress levels.

In Fig. 23 it can be seen that when applying an overburden pressure of 50 kPa the initial part of the graphs are almost similar. The smaller deviations indicate that the accuracy of the results increases when overburden pressure is applied. For the tests with overburden pressure of 100 kPa the curves are coinciding for the tests on
the 60 mm, 80 mm, and 100 mm piles. This implies that the accuracy of the test results increases with increasing overburden pressure. The deviation of the curve for the 40 mm pile is caused by the disturbance of the soil before the test.

In spite of the inaccurate results for the tests without overburden pressure and for the tests of the 40 mm pile, the normalised relationships indicate that the lateral load is proportional to the embedded length squared and the pile diameter, cf. Eq. 7. Furthermore, they indicate that the accuracy of small-scale testing increases with increasing overburden pressure. In future research it is therefore recommended to conduct similar tests with higher overburden pressure applied.

7 Conclusion

The paper presents results from six small-scale quasi-static tests on laterally loaded piles in sand. The aluminium piles had outer diameters of 40 mm and 100 mm, respectively, and a slenderness ratio, \(L/D\), of 5. The tests were conducted in a pressure tank with effective stress levels of 0 kPa, 50 kPa, and 100 kPa.

By increasing the effective stresses in the soil the problems with the non-linear yield surface for small stress levels were avoided. The increase of the effective stress levels were successfully obtained by separating the sand from the upper part of the tank by an elastic membrane.

The problems with the non-linear yield surface were seen in the results for the tests without overburden pressure, as the curves for the normalised relationships were not similar. The similarity for the normalised results were obtained for the tests with overburden pressure of 100 kPa, and it can be concluded that accuracy in small-scale testing increases with increasing overburden pressure. Therefore, in future research it is recommended to conduct small-scale tests with higher overburden pressure applied.

The uncertainties when conducting tests on the 40 mm pile were high, because small disturbances of the soil led to results in disagreement to the other test results. Thereby, it is difficult to draw reasonable conclusions from these tests. In further research small-scale tests should be conducted on piles with larger diameters.

Both the test results obtained for the 100 mm pile and the test results obtained by Sørensen et al. (2009) indicates that the lateral load acting on the pile is proportional to the embedded length squared times the pile diameter.

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Bibliography


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