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Graugaard-Jensen, J.; Brincker, Rune; Hjelm, H. P.; Munch, K.

Published in:
Structural Dynamics EURODYN 2005

Publication date:
2005

Document Version
Publisher's PDF, also known as Version of record

[Link to publication from Aalborg University](#)

Citation for published version (APA):
Graugaard-Jensen, J., Brincker, R., Hjelm, H. P., & Munch, K. (2005). Modal Based Fatigue Monitoring of Steel Structures. In C. Soize, & G. I. Schuëller (Eds.), *Structural Dynamics EURODYN 2005: Proceedings of 6th International Conference on Structural Dynamics, Paris, France, 4-7 september 2005* (pp. 305-310). Millpress.

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Modal based fatigue monitoring of steel structures

J. Graugaard-Jensen

Structural Vibration Solutions A/S, Denmark

R. Brincker

Department of Building Technology and Structural Engineering Aalborg University, Denmark

H.P. Hjelm

Structural Vibration Solutions A/S, Denmark

K. Munch

Structural Vibration Solutions A/S, Denmark

ABSTRACT: In this paper it is shown how the accumulated fatigue in steel structures can be estimated with high accuracy by continuously measuring the accelerations in a few points of the structure. First step is to obtain a good estimate of the mode shapes by performing a natural input modal analysis. The so obtained mode shapes are then used to calibrate a Finite Element model of the structure and to obtain the modal coordinates of the active modes by inverting the mode shape matrix. If the number of active modes is smaller than the number of measurement points, then the problem is solved by regression. If the number of active modes is larger than the number of measurement points, then the number of active modes is reduced by band pass filtering. Once the modal coordinates are identified and thus the complete response is established in the modal domain, then the information is mapped to the physical domain by applying the mode shapes of the calibrated Finite Element model and strains are obtained using the shape functions for the actual elements. The technique has been applied on a model frame structure in the laboratory and on a wind loaded lattice pylon structure. In both cases the estimated stresses has been compared with direct strain gauge measurements and it appears that the difference between the strains measured by strain gauges and the strains estimated by the presented technique is quite small. Looking at the fatigue of the lattice pylon it appears that the estimated damage is significantly smaller than the damage forecasted by commonly accepted design rules. This points to possibilities of significantly increasing the fatigue lives of structures by performing continuous monitoring

1 NOCLAMENTURE

Φ	Mode shape matrix.
$\Delta\sigma$	Stress range.
D	Damage.
f	Natural frequency.
N	Number of stress cycles.
$\mathbf{q}(t)$	Time depend modal coordinate vector.
$\mathbf{y}(t)$	Time depend displacement vector.
exp	Experimental determined value.
FE	Numerical (finite element) determined value.

2 INTRODUCTION

Determination of stress histories in dynamic sensitive structures is usual assigned with large uncertainty, since a conventional determination of stress

histories requires information about e.g. the load history and transfer function – both assigned with some uncertainty. Minimizing these uncertainties can simply be done by determine the stresses experimentally. Experimentally determined stresses are normally determined from strains measured with strain gauges, but fatigue sensitive joints are often located in sections where mounting of strain gauges are difficult or even impossible, e.g. below water on offshore structures. Furthermore strain gauges are not reliable for long time measurements and are, for this reason, not at reliable tool for determination of the stress histories.

By determining the stress histories in structures by natural input modal analysis two important advantages are introduced. First, the method is based on measurements with accelerometers, which are

known as reliable for long time measurements. Second, by introducing a finite element model, the stress history can be calculated in any arbitrary point of a structure when accelerations are measured in only a few points of the structure.

The theory of determination of stress histories by natural input analysis is explained in details and validated through experiments in Graugaard-Jensen et al. (2004).

3 THEORY

The accelerations of a structure, exposed to a stochastic loading, are measured in a few easily accessible points of the structure. A modal identification is performed to obtain the natural frequencies f_{exp} and mode shapes Φ_{exp} of the structure. The identification may be performed by e.g. Stochastic Subspace Identification (SSI), cf. Van Overschee and De Moor (1996), or Frequency Domain Decomposition (FDD), cf. Brincker et al. (2001). The FDD is used in this paper as implemented in the ARTEMIS Extractor software. The FDD is based on calculation of Spectral Density Matrices of the measured data series by discrete Fourier transformation. For each frequency line the Spectral Density Matrix is decomposed into auto spectral functions corresponding to a single degree of freedom system (SDOF). A finite element model is calibrated to obtain

$$\Phi_{\text{exp}} = \mathbf{A} \Phi_{\text{FE}} \quad (1)$$

where \mathbf{A} is an observation matrix containing zeros and ones.

The measured accelerations are integrated twice to obtain the displacements $\mathbf{y}_{\text{exp}}(t)$. The integration is performed by use of Simpson's Rule, cf. Kreyszig (1998), and the resulting numerical drift is removed by digital high-pass filtering, e.g. by use of Butterworth filters.

The obtained displacements $\mathbf{y}_{\text{exp}}(t)$ are expanded in modal coordinates $\mathbf{q}(t)$ by use of either the experimental mode shapes Φ_{exp}

$$\mathbf{y}_{\text{exp}}(t) = \Phi_{\text{exp}} \mathbf{q}(t) \quad (2)$$

or numerical mode shapes Φ_{FE}

$$\mathbf{y}_{\text{exp}}(t) = \mathbf{A} \Phi_{\text{FE}} \mathbf{q}(t) \quad (3)$$

From the modal coordinates and the numerical mode shapes, the response $\mathbf{y}_{\text{FE}}(t)$ in any arbitrary point of the structure is simply calculated by

$$\mathbf{y}_{\text{FE}}(t) = \Phi_{\text{FE}} \mathbf{q}(t) \quad (4)$$

and the strains and far field stresses can be calculated in any point of the structure by traditional finite element calculations. The hot spot stresses are calculated by applying the finite element relationship between the far field stresses and the hot spot stresses.

Use of the experimental mode shapes in the modal expansion may seem as the most obvious, since the response is experimental determined, but in some cases equation (1) cannot be fulfilled. If e.g. the structure is symmetric, repeated poles may occur resulting in a theoretical case where individual modes cannot be defined, and an experimental case where the corresponding mode shapes may be unstable and the direction may differ from the numerical mode shapes. In such a case, the modal expansion must be performed by use of the numerical mode shapes. However, it is important that the FE-model is always correct calibrated. The calibration is checked by comparison the experimental and numerical natural frequencies and by calculating the Modal Assurance Criteria (MAC) between the experimental and numerical mode shapes. The MAC between Φ_{exp} and Φ_{FE} should generally be high to obtain accurate results, unless the Φ_{exp} is unstable.

If the number of mode shapes of the system equals the measured degrees of freedom, then equation (2) or (3) is solved directly. If the number of measured degrees of freedom exceeds the number of mode shapes, the equation is over determined and is solved by linear regression, e.g. the Least Square method.

If the number of mode shapes exceeds the number of measured degrees of freedom the equation is under determined and must be divided into sub-systems. The dividing into sub-systems may be performed by digital filtering or directly in frequency domain by considering the same problem frequency range by frequency range. The division into sub-systems shall furthermore ensure that mode shapes with high correlation is not included in the same sub-system. High correlated mode shapes included in the same sub-system may result in error on the calculated modal coordinates, resulting in large errors on the following calculation of the stress history, cf. Graugaard-Jensen et al. (2004).

4 INTRODUCTION TO EXPERIMENTS

Two experiments are performed; an experiment on a laboratory structure and an experiment on a lattice pylon, cf. Figure 1. The laboratory structure is a 2 m high cantilever beam with a mounted beam and weight on the top to induce torsion modes. The purpose of the experiment is to demonstrate that the stress history in the structure can be calculated in any point with sufficient accuracy. This is demon-

strated by simultaneous measuring strains in two sections on the lower part of the structure and accelerations on the upper part of the structure. The stresses in the lower part of the structure are subsequently calculated from the strain gauge measurements and from the acceleration measurements and the stress histories are compared.

For simplicity, in the rest of this paper the stress calculations based on the strain gauges measurements are referred to as “measured stresses”, and the stress calculations based on the acceleration measurements (natural input analysis) are referred to as “calculated stresses”.

The lattice pylon, located near the Structural Research Laboratory of Aalborg University, is a 20 m high welded structure with a constant width of 0.9 m. Plywood plates are mounted on the upper 1.5 m of the structure to increase the wind load. The purpose of the experiment on the lattice pylon is to verify that the method produces satisfying results on a real structure exposed to stochastic loading. Strains and accelerations are measured using same approach as used for the laboratory structure and the measured and calculated stresses are compared. Furthermore, the uncertainty on the calculated stress history is defined by comparison of the measured and calculated stress histories.

5 LABORATORY EXPERIMENT

5.1 Test Program for Laboratory Experiment

Accelerations are measured in four sections on the upper part of the structure. In each section the measurements are performed in three points, making it possible to determine rigid-body motion and torsion. The strains are measured in two sections on the lower part of the structure with single 120 Ω complimentary gauges. The strain gauges are mounted on each of the four sides of the profile 0.2 m and 0.7 m above the support, measuring in the axial direction of the profile.

The pilot experiment is performed in two stages. In stage one the modal properties of the structure is determined and only accelerations are measured. Accelerations are sampled with 512 Hz in 500 sec in two sections (six channels) at a time. In stage two both accelerations (six channels) and strains (eight channels) are sampled with 512 Hz in one operation in approximately 10 sec. These measurements are subsequently used for comparison of measured and calculated stresses.

The structure is modeled in the finite element program ANSYS by 20-node isoparametric elements

with three degrees of freedom (d.o.f.) per node. The model is calibrated by applying springs in the joints in the model, so that the numerical mode shapes Φ_{FE} correspond reasonably well to the experimental mode shapes Φ_{exp} .



Figure 1. (Top left) Laboratory structure, (top right) lattice pylon, (bottom) base of lattice pylon. Red and blue circles indicate location of strain gauges and accelerometers respectively.

5.2 Data Processing and Results of Laboratory Experiment

In Figure 2 the results of the modal identification by FDD is plotted. Nine modes are identified. In Table 1 the experimental and numerical determined natural frequencies are listed and compared, and Modal Assurance Criteria (MAC) between Φ_{FE} and Φ_{exp} are

calculated. The high values of MAC indicate that the FE-model is well calibrated.

The modal decomposition is performed using Φ_{exp} , cf. equation (2), and the response is calculated in the finite elements holding the coordinates to the strain gauges by use of equation (4). The stresses in these elements are subsequently calculated by traditional finite element calculations, cf. Cook et al. (2002).

The numerical drift resulting from the integration is removed by an 8th order 1 Hz low-pass Butterworth filter. Since nine modes are present, but accelerations are measured in only six channels at a time, the equation system is under determined and must be divided into two or more sub-systems. The system of equations is divided into four sub-systems at 10, 50, 100 Hz using 8th order Butterworth filters.

In Figure 3 an example of a stress history for one channel is shown. As seen the calculated and measured stresses correspond very well. The two time series have different length since the accelerations and strains are sampled by two separate data acquisition systems and thus not started and stopped at the same time.

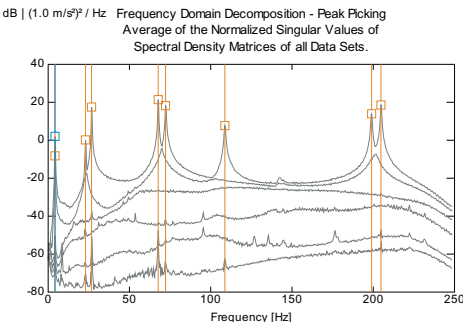


Figure 2. Frequency Domain Decomposition of measurements on laboratory structure. Mean of normalized singular values of spectral density matrices, 1024 frequency lines.

Table 1. Experimental and numerical determined natural frequencies, percentage deviation and MAC-values for pilot experiment.

Φ [-]	f_{exp} [Hz]	f_{FE} [Hz]	Deviation [%]	MAC [-]
1	4.25	4.28	0.7	0.9941
2	4.25	4.29	0.9	0.9816
3	23.00	23.14	0.6	0.9917
4	26.75	27.00	0.9	0.9984
5	67.75	67.70	-0.1	0.9979
6	72.25	71.72	-0.7	0.9976
7	108.80	109.74	0.9	0.9915
8	199.00	195.66	-1.7	0.9846
9	204.80	202.12	-1.3	0.9962

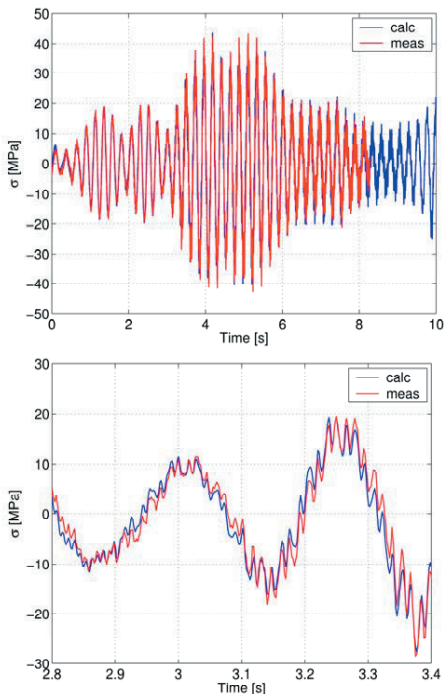


Figure 3 Example of measured and calculated stress history. (Top) Entire time series, (bottom) zoom in on 2.8–3.4 s.

6 EXPERIMENT ON LATTICE PYLON

6.1 Test Program for Lattice pylon

The vibration monitoring system, composed of six Shaevitz accelerometers and eight single 120 Ω complimentary gauges, was installed on the lattice pylon for one month in the spring 2004. Three accelerometers were mounted at the top of the structure, three accelerometers near the middle of the structure and eight strain gauges were mounted near the support of the pylon; six strain gauges on the legs 0.4 m above the support and two strain gauges on diagonals 1.3 m above the support. All strain gauges were measuring in the direction of the profiles.

The monitoring system was initially setup to sample continuously one hour every forth hour, and during periods with high wind speed the monitoring was running continuously in several hours. In all, 223 hours of measurements was recorded. All measurements were sampled with 100 Hz.

The structure is modeled in the finite element program StaadPro using beam elements with six d.o.f.

per node. The model is calibrated by applying springs in the support of the model.

6.2 Data Processing and Results of Experiments on Lattice pylon

Eight modes are identified from 20 minutes measurement series. In Figure 4 the results of the modal identification by FDD is plotted. In Table 2 the experimental and numerical determined natural frequencies are listed and compared, and MAC between Φ_{FE} and Φ_{exp} are calculated. In Figure 8 the mode shapes are plotted.

The modal identification is performed on different 20 minutes measurements series with different wind speeds and wind directions. By comparison the identified mode shapes from the different series, it is found that mode shape 1 and 2 are not stable. For this reason, the MAC between the experimental and numerical mode shape 1 and 2 are low, and the modal expansion must be done using the numerical mode shapes. The numerical drift resulting from the integration is removed by a 5th order 0.2 Hz low-pass Butterworth filter.

It is important to include all the modes that contribute significantly to the fatigue damage. These modes are identified by calculating the damage vs. the number of modes. E.g. the modes of higher order are filtered out one by one (or in pairs) by low-pass filtering and for each filter step the accumulated damage is calculated.

In Figure 5 an example of a 10 min. stress history for channel 1 (leg) is shown, comparing the measured and calculated stresses. The figure shows that the stress histories have been calculated with great accuracy and it is verified that the modal expansion with use of the numerical mode shapes is applicable. Stress spectra are plotted and damage is calculated including all 223 hours of measurements. An example of such a stress spectrum is plotted for one channel (leg) in Figure 6, and in Table 3 the damage is listed for all eight channels. The damage is calculated with use of a linear SN-curve with the parameters $\log K = 16.786$ and $m = 5$ and without any cut-off limit, cf. DS410 (1998).

As comparison to the calculation traditional fatigue estimation by simulation of the pylon response by Monte Carlo simulation based on the turbulence spectrum is performed. In Table 3 the damage produced by the simulation is listed for all eight channels. By comparing the results of the calculation and the simulation the larger uncertainty of the traditional method is clearly demonstrated.

In inspection planning the uncertainty on the stress history is included in a Coefficient Of Variation (COV). For offshore jacket structures COV is typically ranging from 0.10 to 0.15, cf. Faber et al. (2003). It is found that COV is reduced to 0.03 for the results of the lattice pylon, illustrated in Figure 6 where COV is plotted by assuming that the uncertainty is modeled by a normal distributed 95% double-sided probability interval.

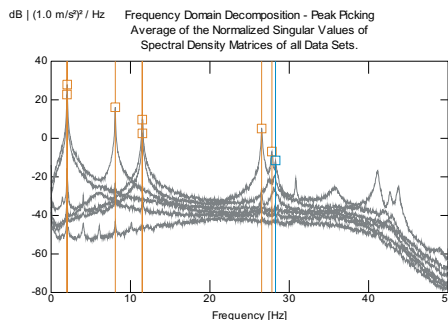
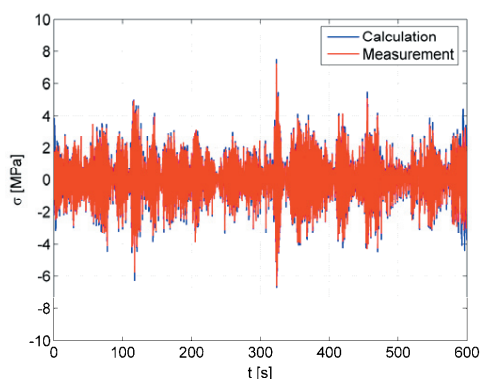


Figure 4. Frequency Domain Decomposition of measurements on lattice pylon. Mean of normalized singular values of spectral density matrices, 2048 frequency lines.

Table 2. Experimental and numerical determined natural frequencies, percentage deviation and MAC-values for experiment on lattice pylon.

Φ [-]	f_{exp} [Hz]	f_{FE} [Hz]	Deviation [%]	MAC [-]
1	2.00	2.01	0.5	0.7428
2	2.02	2.02	-0.3	0.7448
3	8.08	7.87	-2.5	0.9791
4	11.47	11.40	-0.6	0.9618
5	11.49	11.54	0.4	0.9671
6	26.51	25.75	-2.9	0.8289
7	27.80	29.49	6.1	0.8714
8	28.27	30.35	7.4	0.8520



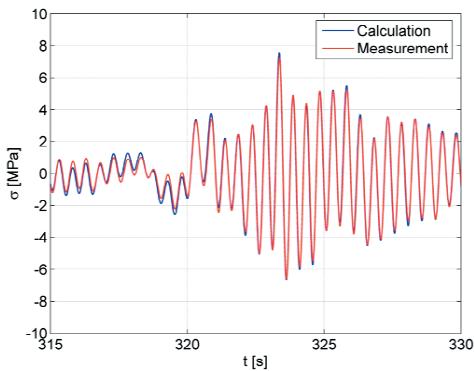


Figure 5 Example of measured and calculated stress history. (top) Entire time series, (bottom) zoom in on 315-330 s.

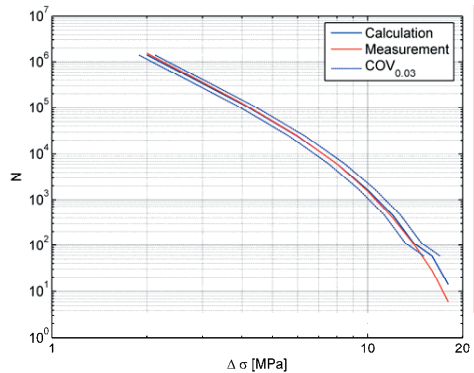


Figure 6 Example of stress spectrum (channel 1, leg).

Table 3. Comparison of measured damage with simulated and calculated damage. Damage is calculated based on Rainflow counting. The \pm values indicates the 95% probability intervals for COV = 0.15 (simulation) and COV = 0.03 (calculation).

Ch.	D_{meas} 1 · 10 ⁻⁶	D_{sim} 1 · 10 ⁻⁶	D_{calc} 1 · 10 ⁻⁶
1	3.53	1.44 +3.79/-1.19	3.54+1.17/-0.93
2	3.55	1.58 +4.12/-1.30	3.43+1.14/-0.89
3	4.52	1.58+4.13/-1.30	3.43+1.14/-0.89
4	0.88	0.79+2.22/-0.64	0.73+0.24/-0.19
5	0.86	0.84+2.18/0.64	0.72+0.24/-0.19
6	3.38	1.44+3.76/-1.19	3.54+1.17/-0.92
7	2.31	8.29+18.94/-6.97	2.74+0.90/-0.72
8	2.22	8.27+18.92/-6.96	2.22+0.74/-0.58

7 CONCLUSION

It has been shown that it is possible to calculate stress histories in any point of a structure with great accuracy by combining natural input modal analysis with finite element modeling. The advantage of the method is that the accelerations of the structure only

have to be measured in few easily accessible points of the structure, and the stresses can be calculated in any arbitrary point of the structure. In this manner the calculated stress histories can replace strain gauge measurements in many cases and it allows for an accurate estimation of fatigue damage.

The coefficient of variation (COV) on the stress history is lowered to below 0.05. The result is that if the method is applied on e.g. offshore structures, the number of inspections can be reduced significantly, since the number of these directly depends on the uncertainty on the stress history, cf. Graugaard-Jensen et al. (2004).

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