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Nonlinear Decoupling of Torque and Field Amplitude in an Induction Motor

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Abstract - A novel approach to control of induction motors, based on nonlinear state feedback, is presented. The resulting scheme gives a linearized input-output decoupling of the torque and the amplitude of the field. The proposed approach is used to design controllers for the field amplitude and the motor torque. The method is tested both by simulation and by experiments on a motor drive.

NOMENCLATURE

a	complex spatial operator $e^{j2\pi/3}$
$i_{sA,B,C}$	stator phase currents A,B and C
$u_{sA,B,C}$	stator phase voltages A,B and C
\bar{i}_s	stator current complex space vector
\bar{u}_s	stator voltages complex space vector
R_s, R_r	resistances of a stator and rotor phase winding
L_s, L_r	self inductance of the stator and the rotor
L_m	magnetizing inductance
T_r	rotor time constant ($T_r = L_r/R_r$)
σ	leakage factor ($1 - L_m^2/(L_s L_r)$)
R_r'	referred rotor resistance ($R_r' = (L_m/L_r)^2 R_r$)
L_s'	referred stator inductance ($L_s' = \sigma L_s$)
L_m'	referred magnetizing inductance ($L_m' = (1 - \sigma)L_s$)
p	time derivative operator ($p \equiv d/dt$)
Z_p	number of pole pair
ω_{mech}	angular speed of the rotor
ω_{mR}	angular speed of the rotor flux
i_{mR}	rotor magnetizing current
ρ	rotor flux angle
c_m	torque factor ($c_m = 1.5Z_p L_m'$)

I. INTRODUCTION

The development of the design of high-performance controllers for drives using an induction motor as an actuator is shortly stated by Leonhard [7] as "30 Years Space Vectors, 20 Years Field Orientation and 10 Years Digital Signal Processing with Controlled AC-drives". The relevance of field oriented control is witnessed by a large numbers of investigations carried out both from a theoretical and a practical point of view [6]. The scheme works with a controller which approximately linearizes and decouples the relation between input and output variables by using the simplifying hypothesis that the actual motor flux is kept constant and equal to some desired value.

In the last 10 years with digital signal processing, significant advances have been made in the theory of nonlinear state feedback control [4], and particular feedback linearization and input-output decoupling techniques have been successfully applied for control of induction motor drives [8],[5],[1][2][9][10].

In De Luca [8], a simplified model is used, i.e. only the electromagnetic part is modeled assuming the speed as a slowly varying parameter. Exact decoupling in the control of electric torque and flux amplitude using the amplitude and frequency of the voltage supply as inputs is obtained by a static state feedback compensator. The resulting nonlinear feedback is quite complex due to the fact that the formulation adopted to carry out the decoupling is based on a reference frame rotating with the stator flux vector. Krzeminski [5] took advantage from the intrinsic decoupling connected with the rotor field orientation, but in his paper the decoupled system does not end up with a double integrator, but with a second order system depending on the motor parameters. Bellini [1] presents a different approach for decoupling of flux and speed, which yields a simple linearized model, constituted by two lines of double integrators, without requiring particular complex computations to determine the components of the motor supply voltage. Because of the mechanical equation for speed the load torque has to be known or estimated.

Flux and speed is also decoupled in Frick et. all. [2] and Marino et. all [9]. Marino propose an adaptive method but it is not obvious how limitation of the motor currents influence the method. By proposing a nonlinear controller based on a two-step input-output decoupling Frick et. all. [2] obtain precise limitation of motor currents and voltages which is indispensable in all applications demanding maximum torque production.

The method of most of the above references uses adaptation of the load torque. However this is a limiting factor to the servo performance because adaptation of the load torque is slow. In order to circumvent this problem torque and flux are decoupled in this paper assuming speed as a measured parameter.

The key items in this paper are

- a model assuming the speed as a parameter
- rotor field orientation
- decoupling of torque and rotor field amplitude based on nonlinear state feedback
- two independent decoupled systems

II. INDUCTION MOTOR MODEL

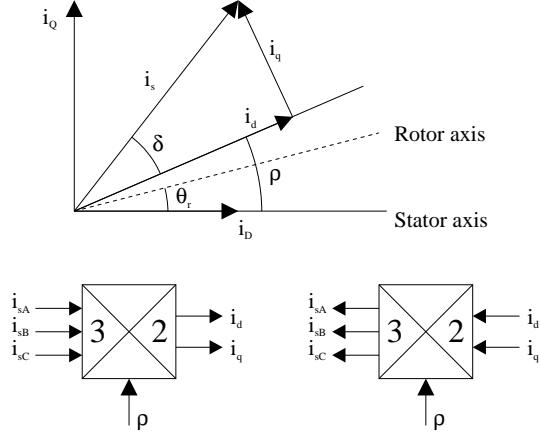


Fig.1. Definitions of transformation angles and symbols

If the currents in the stator coordinates (i_{sA}, i_{sB}, i_{sC}) and the field angle ρ are known, then the following equations based on the angle definition given in Fig. 1 give the transformation from stator coordinates to field coordinates:

$$\vec{i}_s = \frac{2}{3}(i_{sA} + ai_{sB} + a^2i_{sC})e^{-j\rho}$$

In a reference frame fixed to the *rotor magnetizing current*, we have with the angular definitions given in Fig. 1, the d-axis in the direction of the rotor magnetizing current $i_{mR}e^{j\rho}$ and the q-axis orthogonal to the d-axis. Defining the synchronous speed $\omega_{mR} = \frac{d\rho}{dt}$ and

$$\begin{aligned} f_1 &= (-R_s i_{sd} + \omega_{mR} L'_s i_{sq} - R'_r (i_{sd} - i_{mR}))/L'_s \\ f_2 &= (-R_s i_{sq} - \omega_{mR} L'_s i_{sd} - \omega_{mR} L'_m i_{mR})/L'_s \\ f_3 &= (i_{sd} - i_{mR})/T_r \\ f_4 &= Z_p \omega_{mech} + i_{sq}/(i_{mR} T_r) = \omega_{mR} \end{aligned}$$

the motor model is given by:

$$\frac{d}{dt} \begin{Bmatrix} i_{sd} \\ i_{sq} \\ i_{mR} \\ \rho \end{Bmatrix} = \begin{Bmatrix} f_1 \\ f_2 \\ f_3 \\ f_4 \end{Bmatrix} + \begin{Bmatrix} \frac{1}{L'_s} \\ 0 \\ 0 \\ 0 \end{Bmatrix} u_{sd} + \begin{Bmatrix} 0 \\ \frac{1}{L'_s} \\ 0 \\ 0 \end{Bmatrix} u_{sq} \quad (1)$$

with the developed electrical torque given by:

$$m_e = \frac{3}{2} Z_p L'_m i_{mR} i_{sq} = c_m i_{mR} i_{sq} \quad (2)$$

III. NONLINEAR DECOUPLING

The input-output decoupling problem is to find a state feedback such that the transformed system is input-output decoupled, i.e. one input influence one output only. Detailed information on input-output decoupling can be found in [4].

Using the definitions

$$x = \{i_{sd}, i_{sq}, i_{mR}, \rho\}^T \quad u_1 = u_{sd} \quad u_2 = u_{sq}$$

$$\begin{aligned} f_1 &= \frac{1}{L'_s} (-R_s x_1 + (Z_p \omega_{mech} + \frac{x_2}{x_3 T_r}) L'_s x_2 - R'_r (x_1 - x_3)) \\ f_2 &= \frac{1}{L'_s} (-R_s x_2 - (Z_p \omega_{mech} + \frac{x_2}{x_3 T_r}) (L'_s x_1 + L'_m x_3)) \\ f_3 &= \frac{1}{T_r} (x_1 - x_3) \\ f_4 &= Z_p \omega_{mech} + \frac{x_2}{x_3 T_r} \end{aligned}$$

$$f = \{f_1, f_2, f_3, f_4\}^T$$

$$g_1 = \{1/L'_s, 0, 0, 0\}^T$$

$$g_2 = \{0, 1/L'_s, 0, 0\}^T$$

the induction motor equations (1) are given by

$$\dot{x} = f(x) + g_1 u_1 + g_2 u_2$$

and the torque equation (2) is

$$m_e = c_m x_2 x_3$$

This system can be linearized by a state space transformation and a nonlinear state feedback, if and only if the following conditions are satisfied in an open set U of R^4 , as shown by Isidori [4]:

$$G_0 = \text{span}(g_1, g_2)$$

must be involutive and have constant dimension in U and

$$G_1 = \text{span}(g_1, g_2, [f, g_1], [f, g_2])$$

must have the same dimension as the state vector in U . The Lie bracket $[f, g]$ used is defined by

$$[f, g] = \frac{\partial g}{\partial x} f - \frac{\partial f}{\partial x} g$$

For x_3 not equal to zero both conditions are easily verified. It is therefore possible to find $\dim(G_1) - \dim(G_0) = 2$ output functions allowing the linearization of the system.

The two output functions are denoted by $y_1 = h_1(x)$ and $y_2 = h_2(x)$. If the two functions satisfy the conditions:

$$\begin{aligned} L_{g_1} h_1(x) &= 0 \\ L_{g_1} h_2(x) &= 0 \\ L_{g_2} h_1(x) &= 0 \\ L_{g_2} h_2(x) &= 0 \end{aligned} \quad (3)$$

where $L_h \lambda(x)$ is the Lie derivative of the function $\lambda(x)$ along the vector field $h(x)$, defined by

$$L_h \lambda(x) = \sum_i \frac{\partial \lambda(x)}{\partial x_i} h_i(x)$$

Because the relative degree r_1 and r_2 associated with each output is greater than one the total relative degree $r = r_1 + r_2$ is less than or equal to the degree of the state vector $n = 4$. The conditions (3) then lead to a total relative degree $r = n$. This means that no zero dynamics have to be considered. Equation (3) leads to

$$\frac{\partial h_1}{\partial x_1} = \frac{\partial h_2}{\partial x_1} = \frac{\partial h_1}{\partial x_2} = \frac{\partial h_2}{\partial x_2} = 0$$

giving output functions only depending on x_3 and x_4 . The two simplest functions satisfying this are $y_1 = h_1(x_3, x_4) = x_3$ and $y_2 = h_2(x_3, x_4) = x_4$ leading to a decoupling of the flux amplitude and the flux angle. In the field weakening region where both field amplitude and torque are varied a more interesting result would be decoupling of torque and field amplitude. This means that candidates for output functions are

$$\begin{aligned} h_1(x) &= x_3 \\ h_2(x) &= x_2 x_3 \end{aligned}$$

if the zero dynamics of the resulting uncontrollable state is stable.

The approach to obtain the input-output linearization of the system is to take the time derivative of the output functions until the input appears.

$$\begin{aligned} \dot{y}_1 &= L_f h_1 + L_{g_1} h_1 u_1 + L_{g_2} h_1 u_2 = L_f h_1 \\ \ddot{y}_1 &= L_f^2 h_1 + L_{g_1} L_f h_1 u_1 + L_{g_2} L_f h_1 u_2 \\ \dot{y}_2 &= L_f h_2 + L_{g_1} h_2 u_1 + L_{g_2} h_2 u_2 \end{aligned}$$

After some calculations the following equations are obtained for $x_3 \neq 0$

$$\begin{aligned} \dot{y}_1 &= f_3 \\ \ddot{y}_1 &= \frac{1}{T_r L'_s} (u_1 + L'_s (f_1 - f_3)) \\ \dot{y}_2 &= \frac{x_3}{L'_s} (u_2 + L'_s (f_2 + \frac{x_2}{x_3} f_3)) \end{aligned}$$

New inputs defined by

$$\begin{aligned} \nu_1 &= \frac{1}{T_r L'_s} (u_1 + L'_s (f_1 - f_3)) \\ \nu_2 &= \frac{x_3}{L'_s} (u_2 + L'_s (f_2 + \frac{x_2}{x_3} f_3)) \end{aligned}$$

lead to the following decoupled outputs for a field amplitude different from zero

$$\begin{aligned} \ddot{y}_1 &= \nu_1 \\ \dot{y}_2 &= \nu_2 \end{aligned}$$

The inputs u_1 and u_2 are then given by the nonlinear equations

$$\begin{aligned} u_1 &= T_r L'_s \nu_1 - L'_s (f_1 - f_3) \\ u_2 &= \frac{L'_s}{x_3} \nu_2 - L'_s (f_2 + \frac{x_2}{x_3} f_3) \end{aligned} \quad (4)$$

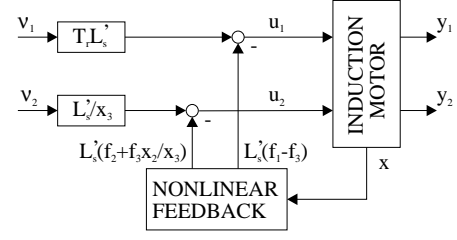


Fig. 2. Nonlinear state feed-back giving two decoupled linear systems $\ddot{y}_1 = \nu_1$ and $\dot{y}_2 = \nu_2$

IV. ZERO-DYNAMICS

Due to the fact that the relative degree $r = 2 + 1 < n = 4$ the input-output decoupling leaves one uncontrollable state to be analyzed for stability. Based on the coordinates giving output decoupling the following coordinates

$$\eta = \{h_1, L_f h_1, h_2, x_4\}^T = \left\{ x_3, \frac{1}{T_r} (x_1 - x_3), x_2 x_3, x_4 \right\}^T$$

defines a diffeomorphism for $x_3 \neq 0$ because the Jacobian

$$\frac{\partial \eta}{\partial x} = \begin{Bmatrix} 0 & 0 & 1 & 0 \\ \frac{1}{T_r} & 0 & -\frac{1}{T_r} & 0 \\ 0 & x_3 & x_2 & 0 \\ 0 & 0 & 0 & 1 \end{Bmatrix}$$

is nonsingular for $x_3 \neq 0$.

The zero-dynamics of a MIMO nonlinear system is the dynamics of the system when the outputs are constrained to be constant.

Since the constraint that the outputs identically is equal to constants implies that all the derivatives of the outputs are zero we have $\dot{y}_1 = \ddot{y}_1 = 0$ and $\dot{y}_2 = 0$. Because $y_1 = h_1$, $\dot{y}_1 = L_f h_1$ and $y_2 = h_2$ we have $\dot{\eta}_1 = \dot{\eta}_2 = \dot{\eta}_3 = 0$.

Since $\dot{\eta}_1 = 0$ gives $x_3(t) = x_3^0$, $\dot{\eta}_2 = 0$ gives $x_2(t) = x_3(t) = x_3^0$ and $\dot{\eta}_3 = 0$ leads to $\dot{x}_2(t) x_3^0 = 0$ giving $x_2(t) = x_2^0$ we have in the original coordinates, that when the system operates in zero-dynamics, the system states evolves on the surface $x_2(t) = x_3(t) = x_3^0$ and $x_2(t) = x_2^0$ with $x_3^0 \neq 0$.

The zero-dynamics is then given by

$$\dot{\eta}_4 = Z_p \omega_{mech} + \frac{x_2^0}{x_3^0 T_r}$$

with the physical explanation that $\omega_{mR} = \dot{\eta}_4$ is constant as expected in a steady state situation.

V. TORQUE AND FIELD AMPLITUDE CONTROL

A. Field Amplitude Controller.

The output $y_1 = h_1(x) = x_3$ with the decoupled dynamics $\ddot{y}_1 = \nu_1$ is controlled by the following PD-controller:

$$\nu_1 = K_1 (i_{mR,ref} - y_1 - K_a \dot{y}_1)$$

giving the closed loop transfer function:

$$y_1 = \frac{1}{\frac{1}{K_1}p^2 + K_a p + 1} i_{mR,ref}$$

Defining α_1 as a design parameter and using $K_1 = 1/(\alpha_1 T_r)^2$ and $K_a = 2\alpha_1 T_r$ the following transfer function from $i_{mR,ref}$ to $i_{mR} = y_1$ is obtained:

$$\hat{i}_{mR} = \frac{1}{(1 + \alpha_1 T_r p)^2} i_{mR,ref}$$

Differentiation is avoided by using $T_r \dot{y}_1 = T_r \dot{x}_3 = x_1 - x_3$ i.e. the controller for the field amplitude is given by

$$\nu_1 = K_1 (i_{mR,ref} - x_3 - K_a/T_r (x_1 - x_3))$$

together with the nonlinear transformation equation (4).

B. Torque Controller.

The output $y_2 = h_2(x) = x_2 x_3$ with the decoupled dynamics $\dot{y}_2 = \nu_2$ is controlled by the following P-controller:

$$\nu_2 = K_2 \left(\frac{1}{c_m} m_{e,ref} - y_2 \right)$$

giving the following closed loop transfer function:

$$y_2 = \frac{1}{1 + p/K_2} \frac{1}{c_m} m_{e,ref}$$

Defining T_2 as a design parameter and using

$$K_2 = \frac{1}{T_2}$$

the closed loop transfer function from $m_{e,ref}$ to $m_e = c_m y_2$ is obtained

$$m_e = \frac{1}{1 + T_2 p} m_{e,ref}$$

the controller for the torque is therefore given by

$$\nu_2 = K_2 \left(\frac{1}{c_m} m_{e,ref} - x_2 x_3 \right)$$

together with the nonlinear transformation equation (4).

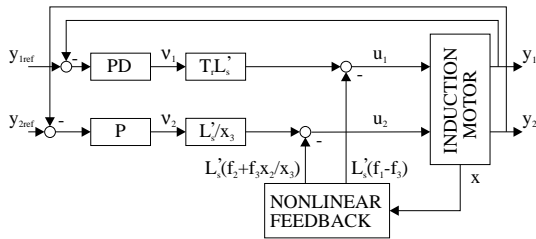


Fig.3. Decoupled torque and field amplitude control

The P and PD controllers for the decoupled torque and field amplitude is shown in Fig. 3 together with the nonlinear decoupling.

VI. SIMULATION

Because the measurements only give the stator currents (i_{sd}, i_{sq}) and θ_{mech} an estimate of the flux has to be performed based on these measurements. Many observers for the flux may of cause be used. The most simple is based on the motor current equations and leads to

$$\begin{aligned} \hat{i}_{mR}(t) &= \frac{1}{1+pT_r} i_{sd}(t) \\ \hat{\rho}(t) &= Z_p \theta_{mech} + \int_0^t \frac{i_{sq}(\tau)}{T_r \hat{i}_{mR}(\tau)} d\tau \end{aligned}$$

defined for $i_{mR} \neq 0$. This means that the state vector $x = \{i_{sd}, i_{sq}, i_{mR}, \rho\}$ is replaced by the estimate $\hat{x} = \{i_{sd}, i_{sq}, \hat{i}_{mR}, \hat{\rho}\}$.

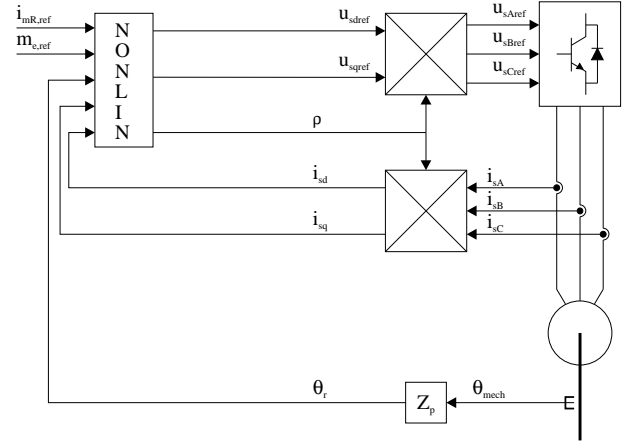


Fig.4. Field Oriented Control System with decoupling of torque and field amplitude

Fig. 4 shows a field oriented control system with speed controller and field weakening function omitted.

The control values are given by (4) which for $i_{mR} \neq 0$ leads to

$$\begin{aligned} \nu_1 &= \frac{1}{\alpha_1^2 T_r^2} (i_{mR,ref} - \hat{i}_{mR} - 2\alpha_1 (i_{sd} - \hat{i}_{mR})) \\ \nu_2 &= \frac{1}{T_2} \left(\frac{m_{e,ref}}{c_m} - i_{sq} \hat{i}_{mR} \right) \\ u_{s,d,ref} &= T_r L_s' \nu_1 + R_s i_{sd} - \omega_{mR} L_s' i_{sq} \\ &\quad + \left(R_r' + \frac{L_r'}{T_r} \right) (i_{sd} - \hat{i}_{mR}) \\ u_{s,q,ref} &= \frac{L_s'}{\hat{i}_{mR}} \nu_2 + R_s i_{sq} + \omega_{mR} (L_s' i_{sd} + L_m' \hat{i}_{mR}) \\ &\quad - \frac{L_s' i_{sq}}{T_r \hat{i}_{mR}} (i_{sd} - \hat{i}_{mR}) \end{aligned}$$

The load is simulated as

$$J \frac{d\omega_{mech}}{dt} = m_e - f_0 \omega_{mech}$$

and the resulting curves show i_{mR} , m_e and ω_{mech} for the following reference values:

$$\begin{aligned} i_{mR,ref} &= \begin{cases} 0 & \text{for } t < 0 \\ 0.8 & \text{for } 0 \leq t < 1 \\ 0.4 & \text{for } 1 \leq t \end{cases} \\ m_{e,ref} &= \begin{cases} 0 & \text{for } t < 0.5 \\ 0.4 & \text{for } 0.5 \leq t \end{cases} \end{aligned}$$

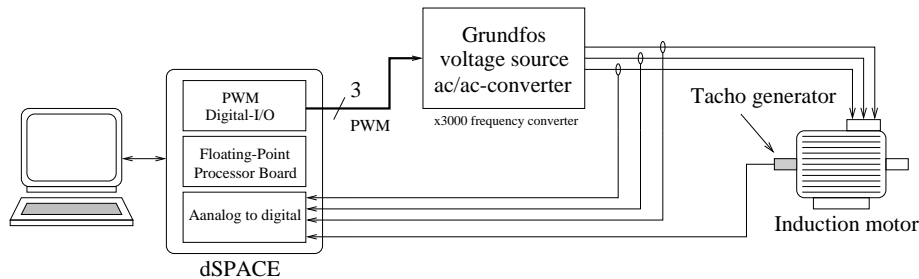


Fig. 5. Computer interface to the motor drive system

The parameters used for simulation are $R_s = 9.2$, $R_r' = 6.56$, $L_m' = 0.447$, $L_s' = 0.014$, $J = 0.00056$, $Z_p = 1$, $\alpha_1 = 0.04$, $T_2 = 0.00005$.

The small deviation from ideal performance as seen from Fig. 6.a, 6.c and 6.e are caused by the first order approximation of the closed loop response for the direct and quadrature current.

VII. EXPERIMENTS

The interface to the motor drive used for experiments is shown in Fig. 5. A standard board with simultaneous sample/hold and direct memory access (DMA) to the computer makes up the analog to digital conversion of the phase currents and the DC-link voltage. The PWM generator is a counter/timer board with port interface to the computer.

The experimental curves 6.b, 6.d and 6.f may be compared with 6.a, 6.c and 6.e. The decoupling between magnetizing current and torque is not perfect mainly due to delay in the digital control system. The deviation between simulated and experimental curves of the magnetizing current may be explained by the inverter nonlinearity and are overcome by adding integral action to the controller.

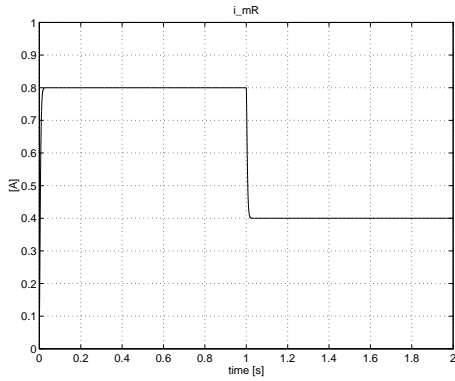
VIII. CONCLUSION

A new and improved method based on nonlinear control theory has been developed and verified by simulations and experimental studies. Compared to other strategies evolving from the nonlinear control theory reported in the literature this method do not need an adaptation of the motor load. Elimination of this need for adaptation implies that servo performance is present even at momentary load torque changes. Unfortunately the developed strategies is very sensitive to motor parameter variations, more specifically wrong assumptions on rotor resistance and saturation of the main inductance spoils the essential decoupling. Compared to field oriented control strategies uncertainties are not here weakened or eliminated by high gain current controllers. The impact of saturation can be improved by developing a nonlinear strategy on the basis of a dynamic

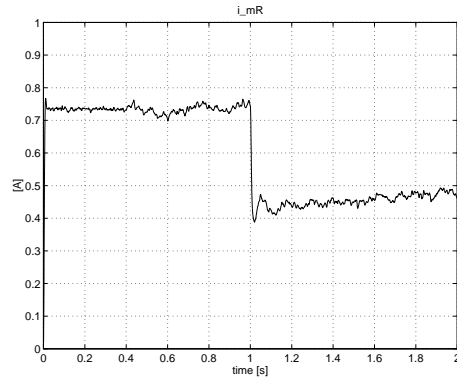
motor model containing saturation effects. This improvement will be an issue for further research together with a comparing study with the traditional field oriented control.

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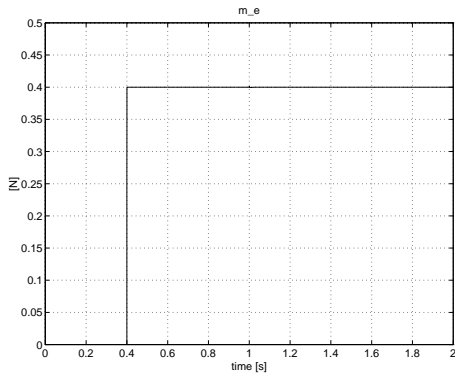
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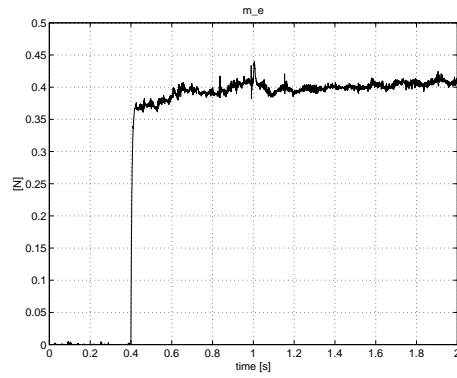
a) *Estimated magnetizing current i_{mR} (simulation)*



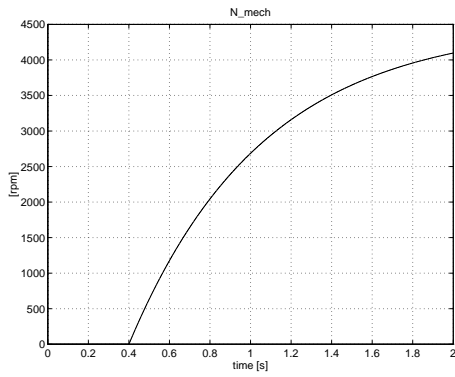
b) *Estimated magnetizing current i_{mR} (experiment)*



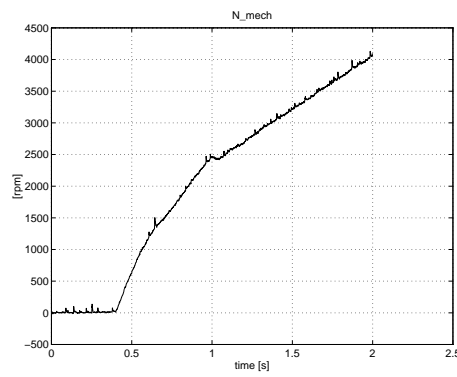
c) *Developed electrical torque m_e (simulation)*



d) *Estimated electrical torque m_e (experiment)*



e) *Rotor speed $N_{mech} = 60/(2\pi)\omega_{mech}$ (simulation)*



f) *Rotor speed $N_{mech} = 60/(2\pi)\omega_{mech}$ (experiment)*

Fig.6. Nonlinear decoupling of magnetizing current and developed electrical torque. Simulation curves (a), (c) and (e). Experiment on test set-up curves (b), (d) and (f).