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CHAPTER 94

ASSESSMENT OF THE RELIABILITY PROFILES FOR CONCRETE BRIDGES 1

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ABSTRACT

In this paper, calculation of reliability profiles is discussed. ULS as well as SLS limit states are formulated. Corrosion due to chloride penetration is the considered deterioration mechanism. Three models for corrosion are formulated. A definition of service lifetime for concrete bridges is presented and discussed. The proposed method of calculating reliability profiles is illustrated on an existing UK bridge.

1. INTRODUCTION

This paper is based on research performed for the Highways Agency, London, UK under the project DPU/9/44 "*Revision of Bridge Assessment Rules Based on Whole Life Performance: Concrete Bridges*". It contains details of a methodology which can be used to generate Whole Life (WL) reliability profiles. These WL reliability profiles may be used to establish revised rules for Concrete Bridges. The paper is based on Thoff-Christensen et al. [1], Thoff-Christensen et al. [2] and Thoff-Christensen [3],[4],[5].

2. LIMIT STATES

Four limit states are selected for the reliability analysis:

- two ultimate limit state (ULS): collapse limit state (using yield line analysis) shear failure limit state,
- two serviceability limit state (SLS): crack width limit state deflection limit state.

¹ Engineering Structures, Vol. 20, 1998, pp. 1004-1009.

2.1 Collapse (yield line) limit state

The following safety margin is used

$$Z = V E_D - W_D \tag{1}$$

where V is a model uncertainty variable, E_D is the energy dissipated in yield lines, and W_D is the work done by the applied loads.

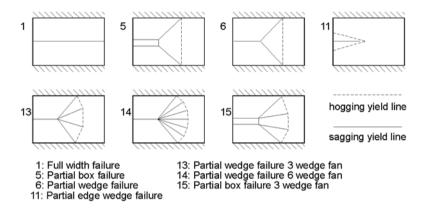


Figure 1. Failure modes for simply supported slab bridges.

The plastic collapse analysis and estimation of the load are performed using the COBRAS program, Middleton 6]. The reliability analysis (element and system) is done using RELIAB01 [7] and RELIAB02 [8]. The RELIAB and COBRAS programs have been interfaced and an optimisation algorithm has been included to determine the optimal yield line pattern for each iteration of the reliability analysis, see also Thoft-Christensen [9]. The estimation of the deterioration of the steel reinforcement is based on the program CORROSION [10]. COBRAS supports 16 different types of failure mode, 7 are used in this bridge slab analysis; see figure 1. The basic variables used in the yield line ULS are: thickness of slab, cube strength of concrete, density of concrete, depth of reinforcement, yield strength of reinforcement, and two load parameters.

2.2 Shear failure limit state

Shear failure is modelled using a model applicable to reinforced concrete beams; see Imperial College [11], which may be written as

$$M_2: g_2(\cdot) = Z_2 V_{j,ult} - V_j$$
(2)

where V_j is the shear force from external loads, $V_{j,ult}$ is the ultimate shear strength, v_c is the design shear stress, and ξ_s is the depth factor defined as, where b is the width of the beam and d is the depth of the beam

$$V_{u} = \xi_{s} v_{c} b d \quad , \quad v_{c} = 0.24 \left(\frac{100 A_{s}}{b d}\right)^{1/3} f_{c}^{1/3} \quad , \quad \xi_{s} = \left(\frac{500}{d}\right)^{1/4} \tag{3}$$

The stochastic variables used in the shear limit state are: thickness of slab, cover on reinforcement, concrete cube strength, yield stress of reinforcement, initial area of the reinforcement, density of concrete, static load factor, dynamic load factor, model uncertainty variable, and variables related to the chloride induced corrosion.

2.3 CRACK WIDTH LIMIT STATE

Cracking shall be limited to a level that will not impair the proper functioning of the structure or cause its appearance to be unacceptable. The design crack width may be obtained from; see Eurocode [12]

$$w_k = \beta s_{rm} \varepsilon_{sm} \tag{4}$$

where w_k is the design crack width, s_{rm} is the average final spacing, ε_{sm} is the mean strain allowing, under the relevant combination of loads, for the effects of tension stiffening, shrinkage, etc., and β is a coefficient relating the average crack width to the design value. The value of ε_{sm} may be calculated from

$$\varepsilon_{sm} = \frac{\sigma_s}{E_s} (1 - \beta_1 (\frac{\sigma_{sr}}{\sigma_s})^2)$$
(5)

where σ_s is the stress in the reinforcement calculated on the basis of a cracked section. σ_{sr} is the stress in the reinforcement calculated on the basis of a cracked section under the loading conditions causing first cracking. β_1 is a coefficient which takes account of the bond properties of the bars.

The average final crack spacing (in mm) for members subjected dominantly to flexure or tension can be calculated from the equation

$$s_{rm} = 50 + 0.25k_1k_2\phi / \rho_r \tag{6}$$

where ϕ is the bar size in use (or the average bar size). ρ_r is the effective reinforcement ratio, $A_s / A_{c.eff}$, where A_s is the area of reinforcement contained within the effective tension area, $A_{c.eff}$. k_1 is a coefficient which takes account of the bond properties of the bar. k_2 is a coefficient which takes account of the strain distribution.

The crack width limit state can then be formulated by

$$g(\cdot) = w_{\max} - z_c w_k \tag{7}$$

where z_c is a model uncertainty stochastic variable. The stochastic variables used in the crack SLS are: concrete cover, distance between reinforcement bars, diameter of reinforcement bars, thickness of slab, elastic modulus of reinforcement bars, tensile strength of concrete, external bending moment, and one model uncertainty variable.

2.4 DEFLECTION LIMIT STATE

The following deflection limit state is used

$$g(\cdot) = w_{\max} - z_c w_k \tag{8}$$

where d_{max} is the maximum allowable deflection, d_k is the deflection estimated by linear elastic analysis, and z_d is a model uncertainty variable.

3. DETERIORATION

Corrosion initiation period refers to the time during which the passivation of steel is destroyed and the reinforcement starts to corrode actively. Practical experience of bridges in wetter countries shows that chloride ingress is far bigger a problem that carbonation. The rate of chloride penetration into concrete, as a function of depth from the concrete surface and time, can be represented by Fick's law of diffusion as follows:

$$\frac{\delta c}{\delta t} = D_C \frac{\delta^2 c}{\delta x^2} \tag{9}$$

where *c* is the chloride ion concentration, as % of the weight of cement, at distance *x* cm from the concrete surface after *t* seconds of exposure to the chloride source. D_c is the chloride diffusion coefficient expressed in cm²/sec. The solution of the differential equation (8) is

$$C(x,t) = C_0 \left\{ 1 - \operatorname{erf}\left(\frac{x}{2\sqrt{D_c \cdot t}}\right) \right\}$$
(10)

where C_0 is the equilibrium chloride concentration on the concrete surface, as % of the weight of cement, x is the distance from the concrete surface in cm, t is the time in sec, erf is the error function, D_c is the diffusion coefficient in cm²/sec and C(x,t) is the chloride concentration at any position x at time t. In a real structure, if C(x,t) is assumed to be the chloride corrosion threshold and x is the thickness of concrete cover, then the corrosion initiation period T_I can be calculated based on a knowledge of the parameters C_0 and D_c . The time T_I to initiation of reinforcement corrosion is

$$T_{I} = \frac{\left(d_{1} - D_{1} / 2\right)^{2}}{4D_{C}} \left(erf^{-1}\left(\frac{C_{cr} - C_{0}}{C_{i} - C_{0}}\right)\right)^{-2}$$
(11)

where C_i is the initial chloride concentration, C_{cr} is the critical chloride concentration at which corrosion starts, and $d_1 - D_1 / 2$ is the concrete cover. When corrosion has started then the diameter $D_1(t)$ of the reinforcement bars at time t is modelled by

$$D_{I}(t) = D_{1} - C_{Corr} i_{corr} t \tag{12}$$

where D_1 is the initial diameter, C_{corr} is a corrosion coefficient, and i_{corr} is the rate of corrosion.

Based on a survey three models for chloride penetrations are proposed (the initial chloride is assumed to be zero): low deterioration, medium deterioration and high deterioration. The deterioration parameters for these three levels are (N(a,b) is a normal distribution with the mean a and the standard deviation b, Uniform [a,b] is a uniform distribution in the interval [a; b]) :

LOW:	
Diffusion coefficient D_C :	N(25.0, 2.5) [mm ² /year]
Chloride concentration , surface C_0 :	N(0.575, 0.038) [%]
Corrosion density i_{corr} :	Uniform[1.0, 2.0] [mA/cm ²]
Medium:	
Diffusion coefficient D_C :	N(30.0, 2.5) [mm ² /year]
Chloride concentration , surface C_0 :	N(0.650, 0.038) [%]
Corrosion density i_{corr} :	Uniform[1.5, 2.5] [mA/cm ²]
<u>High:</u>	
Diffusion coefficient D_C :	N(35.0, 2.5) [mm ² /year]
Chloride concentration , surface C_0 :	N(0.725, 0.038) [%]
Corrosion density i_{corr} :	Uniform[2.0, 3.0] [mA/cm ²]

Low

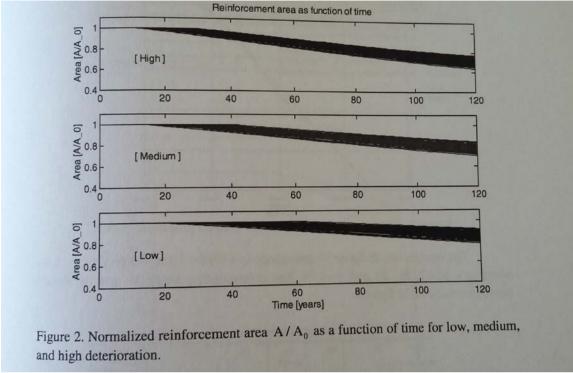


Figure 2 shows sample realisations of the history of the reinforcement area for all tree deterioration models.

4. SERVICE LIFE

In Thoft-Christensen [5] the service life is defined as the initiation time T_I , see equation (11), for corrosion of the reinforcement. This is a rational definition from a life-cycle cost of view since repair of corroded reinforced elements is a major contributor to the life-cycle cost. It is relatively inexpensive to repair a structural element by replacing some part of the concrete instead of waiting until corrosion has taken place.

Based on equation (11) outcomes of the corrosion initiation time T_I have been obtained by simple Monte Carlo simulation (1000 simulations) of the following data using the software program Corrosion [10]:

Initial chloride concentration:	0%
Surface chloride concentration:	Normal (0.650;0.038)
Diffusion coefficient:	Normal (30;5)
Critical concentration:	Normal (0.3;0.05)
Cover:	Normal (40;8)
Number of samples:	1000

The simulated values are plotted on Weibull probability paper in figure 3. In the same figure is shown that a Weibull distribution can be used to approximate the distribution of the simulated data.

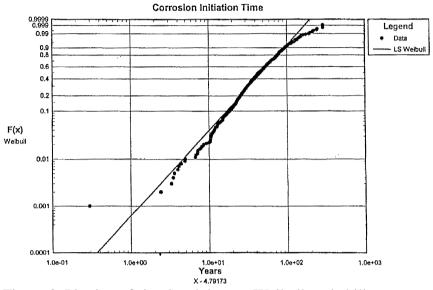


Figure 3. Plotting of simulated data on Weibull probability paper.

The straight line in figure 3 corresponds to a Weibull distribution $W(x; \mu, k, \varepsilon)$, where $\mu = 63.67$, k=1.81 and $\varepsilon = 4.79$. The corresponding histogram and the density function are shown in figure 4.

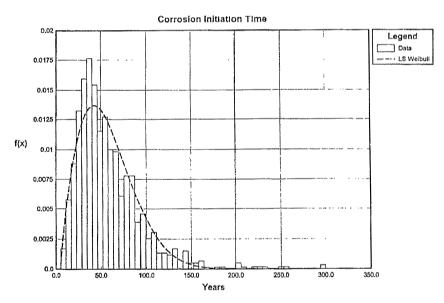


Figure 4. Density function of the corrosion initiation time.

5. RELIABILITY PROFILES

This example is used to illustrate the proposed methodology. The example is based on an existing UK bridge, but some limitations and simplifications are made. The bridge was built in 1975. The bridge was designed for 45 units HB load. The bridge has a span of 9.755 m, the width is 2 times 13.71 m, and the slab thickness is 550 mm (see figure 5). Based on the corrosion data shown in table 1 the expected area of the reinforcement as a function of time can be calculated, see figure 6.

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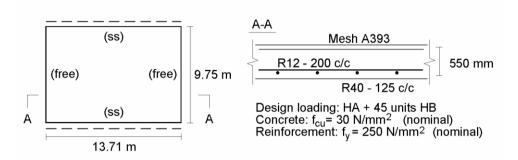
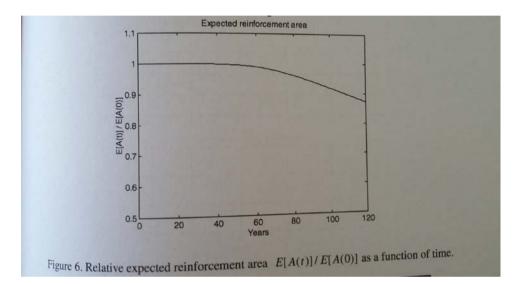


Figure 5. Bridge data.



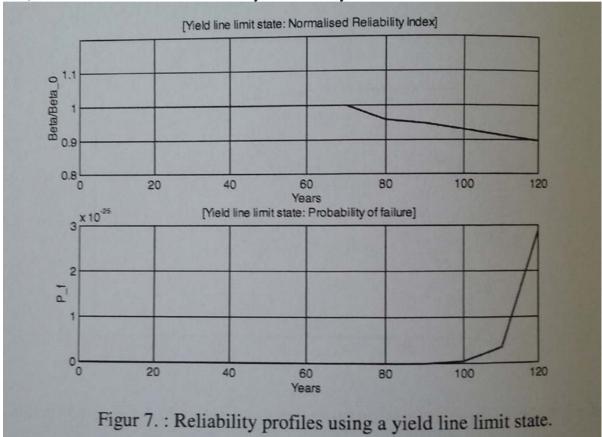
	chastic variables: Yield line limit state			
No	Туре	Par. 1	Par. 2	Description
1	Normal	550.0	10.0	Thickness of slab [mm]
2	LogNormal	30.0	6.0	Cube strength of concrete [MPa]
3	Normal	23.6	0.4	Density of concrete [kN/m3]
4	LogNormal	289.0	25.0	Yield strength: longitudinal reinforcement [MPa]
5	Normal	60.0	8.0	Cover on longitudinal reinforcement [mm]
6	LogNormal	289.0	25.0	Yield strength: transverse reinforcement [MPa]
7	Normal	86.0	8.0	Cover on transverse reinforcement [mm]
8	Fixed	10053.0	-	Longitudinal reinforcement area (initial) [mm2]
9	Fixed	565.0	-	Transverse reinforcement area (initial) [mm2]
10	Gumbel	0.352	0.026	Static load factor [-]
11	Normal	1.27	0.20	Dynamic load factor [-]
12	Normal	1.08	0.072	Chloride concentration on surface [%]
13	Fixed	0.0	-	Initial chloride concentration [%]
14	Normal	35.0	2.5	Diffusion Coefficient [cm2/sec]
15	Normal	0.4	0.05	Critical Chloride concentration [%]
16	Uniform	2.5	0.29	Corrosion parameter [-]
17	Normal	1.0	0.05	Model uncertainty variable [-]

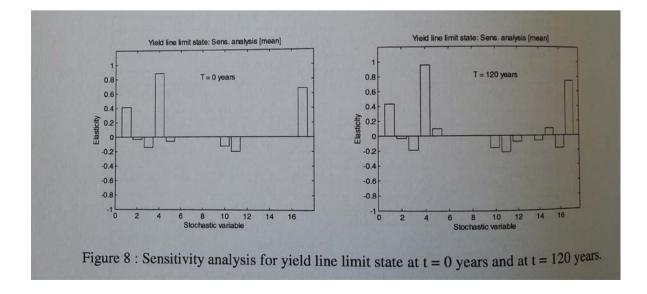
Table 1. Stochastic modelling used for the ULS.

Reliability profiles for the yield line limit state (ULS) are as an illustration calculated on the basis of the stochastic modelling shown in tables 1. The general traffic

highway load model in the Eurocode 1, Part 3 (ENV 1991-3:1995) for lane and axle load is applied. The load effects produced by the Eurocode model (lane and axle load) are multiplied by a static load factor (extreme type 1) and a dynamic load factor (normal).

The normalised reliability profile for the yield line ULS (full width failure) and the corresponding probability of failure profile are shown in figure 7. The reliability index at time t = 0 is $\beta_0 = 11.5$. Due to the size of the concrete cover (mean value 60 mm) the deterioration does not have any effect until year 70.





The results from the sensitivity analysis with regard to the mean values are shown for t = 0 years and t = 120 years in figure 8. The sensitivity measure shown is the reliability elasticity coefficient. The meaning of the elasticity coefficient e_p is the following. If a parameter p is changed 1 % then the reliability index is changed e_p %. The most important variables are, as expected, the thickness of the slab, the yield strength of the reinforcement, and the model uncertainty. Observe that the magnitude of sensitivity with regard to the cover changes from negative at time t = 0 years to positive at time t = 120 years due to the corrosion.

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