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## **Co-optimized Bidding Strategy of an Integrated Wind-Thermal-Photovoltaic System in Deregulated Electricity Market under Uncertainties**

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1 Co-optimized Bidding Strategy of an Integrated  
2 Wind-Thermal-Photovoltaic System in Deregulated  
3 Electricity Market Under Uncertainties

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15 **Abstract**

16 Clean Energy sources, such as wind and solar, have become an inseparable  
17 part of today's power grids. However, the intermittent nature of these sources  
18 has become the greatest challenge for their owners, which makes the bidding  
19 in the restructured electricity market more challenging. Hence, the main goal  
20 of this paper is to propose a novel multi-objective bidding strategy framework  
21 for a wind-thermal-photovoltaic system in the deregulated electricity market for  
22 the first time. Contrary to the existing bidding models, in the proposed mod-  
23 el, two objective functions are taken into account that the first one copes with  
24 profit maximization while the second objective function concerns with emis-  
25 sion minimization of thermal units. The proposed multi-objective optimization  
26 problem is solved using the weighted sum approach. The uncertainties associ-  
27 ated with electricity market prices and the output power of renewable energy  
28 sources are characterized by a set of scenarios. Ultimately, in order to select  
29 the best-compromised solution among the obtained Pareto optimal solutions,

30 two diverse approaches are applied. The proposed bidding strategy problem is  
 31 being formulated and examined in various modes of joint and disjoint opera-  
 32 tion of dispatchable and non-dispatchable energy sources. Simulation results  
 33 illustrate that not only the integrated participation of these resources increases  
 34 the producer's expected profit, but also decreases the amount of the produced  
 35 pollution by the thermal units.

36 *Keywords:* Integrated operation, bidding strategy, Multi-objective  
 37 optimization, Wind-thermal-Photovoltaic system, weighted-sum technique,  
 38 Emission trading

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## Nomenclature

### *Indices*

t	time index.
g	Index for thermal units.
$\omega$	Scenario index.
b	Index for blocks of the generation cost curve and emission curve of thermal units.

### *Constants*

$\pi_\omega$	Probability of occurrence of scenario $\omega$
$P^{W,Max}$	Rated wind power output, MW.
$P^{PV,Max}$	Rated PV power output, MW.
$STUC(g)$	Start-up cost of every thermal unit, €/each start-up.
$MDT(g)$	Minimum down-time of every thermal unit, hr.
$MUT(g)$	Minimum up-time of every thermal unit, hr.
$RUR(g)$	Ramp-up rate of every thermal unit, MW/hr.
$RDR(g)$	Ramp-down rate of every thermal unit, MW/hr.
$E^{EQ}$	Emission quota of power producer, lbs.

$P^{Maxb}(b, g)$	Maximum power output of every thermal unit in $b$ th block of the piecewise linear cost function, MW.
$P^{Max}(g)$	Maximum power output of every thermal unit, MW.
$P^{Min}(g)$	Minimum power output of every thermal unit, MW.
$PS^{Max}(g)$	Maximum capacity of every thermal unit for participating in the spinning reserve market, MW.
$NC(g)$	No-load generating cost of every thermal unit, €/hr.
$IC(b, g)$	Incremental generating cost of $b$ th block of unit $g$ , €/MWhr.
$E(q, b, g)$	Slope of block $b$ in emission group $q$ of every thermal unit, lbs/MWhr.
$EMG$	Emission group including $NO_X$ and $SO_2$ .
$STURL(g)$	Start-up ramp bound of every thermal unit, MW/hr.
$STDRL(g)$	Shut-down ramp bound of every thermal unit $g$ , MW/hr.
$a_g, b_g, c_g$	Coefficients of thermal generation cost function.
$\alpha_g, \beta_g, \gamma_g$	Emission coefficients of thermal unit $g$ .
$N_T$	Number of periods.
$N_G$	Number of thermal units.
$N_\Omega$	Number of scenarios.
$N_b$	Number of segments of the production cost and emission curve.
$\lambda^{EM}$	Emission market price, €/lbs.
<b>Variables</b>	
$\lambda^E(t, \omega)$	Price of day-ahead energy market, €/MW.
$\lambda^S(t, \omega)$	Price of spinning reserve market, €/MW.
$P^{th,S}(t, \omega)$	Optimal bid of thermal units in the spinning reserve market, MW.
$P^{th,E}(t, \omega)$	Optimal bid of thermal units in the day-ahead energy market, MW.
$P^W(t, \omega)$	Optimal bid of wind power plant in the day-ahead energy market, MW.
$P^{PV}(t, \omega)$	Optimal bid of PV system in the day-ahead energy market, MW.
$P^{th,Ac}(t, \omega)$	Actual power output of thermal units, MW.
$P^{W,F}(t, \omega)$	Realized power output of wind power plant, MW.
$P^{PV,F}(t, \omega)$	Realized power output of PV system, MW.
$P^C(t, \omega)$	Joint energy offer of the all energy resources in the day-ahead energy market, MW.

$\Delta^+(t, \omega)$	Imbalance-up, MW.
$\Delta^-(t, \omega)$	Imbalance-down, MW.
$STU(g, t, \omega)$	Start-up cost of every thermal unit, €.
$C(g, t, \omega)$	Generation cost of every thermal unit, €.
$EG(b, g, t, \omega)$	Produced power of thermal units through the $b$ th block of the piecewise linear cost function for participating in the day-ahead energy market, MW.
$ES(g, t, \omega)$	Power offer of every thermal unit in the spinning reserve market, MW.
$ET(g, t, \omega)$	Total power offer by every thermal unit in all selected markets, MW.
$u(g, t, \omega)$	Binary variable which indicates acceptance situation of every thermal unit in the day-ahead energy market.
$x(g, t, \omega)$	Binary variable which indicates start-up situation of thermal units in the day-ahead energy market.
$y(g, t, \omega)$	Binary variable which indicates shut-down situation of thermal units in the day-ahead energy market.
$r^+(t, \omega)$	Imbalance penalty for over-generation as multiplier of energy price
$r^-(t, \omega)$	Imbalance penalty for under-generation as multiplier of energy price

## 39 1. Introduction

### 40 1.1. Motivation and Aim

41 Nowadays, a wide range of power system issues is affected by the presence of  
42 renewable energy resources. With the growth of industries and communities, the  
43 request for supplying customers demand is rising day-to-day [1]. In this regard,  
44 conventional energy sources such as coal, gas and nuclear, as well as renewable  
45 energy sources, e.g., hydro, wind and solar, are the two main options for gov-  
46 ernments to supply the required electricity of communities [2]. Generally, the  
47 rising cost of fossil fuels and attention to environmental concerns can be men-  
48 tioned as the main reasons for the desire of diverse communities to augment the  
49 penetration of renewable energy sources [3]. Briefly, sustainability, environmen-  
50 tally friendly, reducing fossil fuel consumption, and low maintenance costs are

51 among the reasons for increasing the interest of various communities in renew-  
52 able energy sources [4]. Despite many subsidies that governments have devoted  
53 to renewable energy developers, we will witness a significant increase in invest-  
54 ments in this sector [5]-[6]. On the other hand, the existence of subsidies will not  
55 guarantee the profits of investors. Hence, the deregulated electricity market lay  
56 the groundwork for both producers and consumers to devise the best possible  
57 strategy for themselves. Consequently, renewable energy sources owned by gen-  
58 eration companies (GenCos)/large consumers must design the most profitable  
59 bidding strategy by participating in various electricity markets.

## 60 1.2. Literature Review

61 The problem of optimal bidding strategy/self-scheduling has attracted the  
62 attention of many researchers so far [7]-[22]. A bidding structure based on the  
63 joint implementation of stochastic and robust uncertainty modeling approach-  
64 es for an industrial consumer has been addressed in [7]. Likewise, in [8], the  
65 authors conducted a stochastic-robust optimization-based framework for a bid-  
66 ding strategy of a large consumer in a deregulated electricity market. In both  
67 papers [7] and [8], the uncertainty of load is addressed by the specified range,  
68 and the uncertainty related to renewable productions and market prices are  
69 modeled via independent scenarios. A self-scheduling model for the participa-  
70 tion of a sample microgrid containing plug-in electric vehicles, wind turbines,  
71 and fuel cell units has been developed in [9]. In [10], authors have proposed  
72 a coordinated self-production and load-scheduling framework for an industrial  
73 plant in joint electricity and carbon emission markets. A hybrid probabilistic-  
74 possibilistic technique has been employed in [11] to cope with the uncertainties  
75 in the self-scheduling of thermal units. In [12], authors have focused on pre-  
76 senting a bi-objective self-scheduling structure for a typical factory as a large  
77 consumer. In [13], a risk-constrained self-scheduling model for a real virtual  
78 power plant in Iran has been suggested.

79 Integrated energy resources scheduling is one of the most challenging prob-  
80 lems in the electrical power system which has attracted much attention. Wind

81 power generation as one of the most favorite organ of integrated energy re-  
82 sources has been widely considered alongside other production resources such  
83 as thermal, hydro, solar, and pumped storage power plants. In [14], the authors  
84 present an integrated self-scheduling model for a wind-pumped-storage system  
85 while the uncertainty of wind power generation is modeled by a neural network  
86 based technique. Authors illustrated that presenting a coordinated bidding s-  
87 trategy of both resources can remarkably raise their profitability. A critical  
88 shortage of this work is that the authors have not modeled the uncertainty  
89 associated with electricity market prices. Authors in [15], presented a linear  
90 programming framework for self-scheduling of a hydro-thermal system, whereas  
91 the electricity market prices and forced outages of generating units have been  
92 considered as uncertain sources. Likewise, the investigation of integrated wind  
93 and thermal energy sources in the context of the bidding strategy problem have  
94 been accomplished in [16]-[18]. The ultimate goal of all these three works is  
95 to prove the profitability of integrated scheduling compared to non-integrated  
96 one. In [19], a risk-based bidding framework for a wind-thermal-pumped storage  
97 system is presented.

98 Contrary to the mentioned studies, the bi-objective scheduling of integrated  
99 energy systems with the aim of minimizing pollution emission has also been con-  
100 sidered by researchers [20]-[21]. In [20], a bi-objective microgrid self-scheduling  
101 model is presented in which the microgrid cost and emission minimizations are  
102 taking into account. A multi-objective self-scheduling model for a hydro-thermal  
103 system considering joint energy and ancillary services markets is proposed in  
104 [21]. In [22], a multi-objective economic dispatch model for pumped-hydro-  
105 thermal systems is presented in which the normal boundary intersection is uti-  
106 lized to achieve the Pareto optimal solutions. The taxonomy of reviewed papers  
107 [7]-[22] based on different aspects of their works has been listed in Table 1.

108

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Table 1 is placed here

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109

110

111 *1.3. Contributions*

112 According to the reviewed papers in subsection 1.2 and the specified char-  
113 acteristics for each paper in Table 1, this paper focuses on presenting a novel  
114 bi-objective bidding strategy of a wind-thermal-photovoltaic system in the en-  
115 ergy and spinning reserve markets. To the best of authors' knowledge, this work  
116 proposes the most comprehensive study in the context of multi-objective and  
117 single-objective coordinated bidding strategy of wind, thermal and photovoltaic  
118 units in the literature, so the major contributions of this paper are:

- 119 • A comprehensive coordinated mathematical formulation is presented for  
120 the multi-objective bidding strategy of all existing sources.
- 121 • A novel bi-objective bidding strategy is proposed for a wind-thermal-  
122 photovoltaic (WTPV) system participating in the energy and spinning  
123 reserve markets. The process of profit maximization and emission mini-  
124 mization are concurrently accomplished while the uncertainty arising from  
125 day-ahead energy, spinning reserve, and imbalance prices along with the  
126 output power of renewable energy resources are addressed in the proposed  
127 framework.
- 128 • An efficient solution method, namely, the hybrid weighted sum method  
129 and fuzzy satisfying approach, is introduced as the solution methodology  
130 of the bi-objective bidding strategy problem
- 131 • A decision-making scheme based on the preferences of decision-maker is  
132 suggested in the bidding strategy problem to select the most favored so-  
133 lution.
- 134 • An additional pattern based on the emission trading concept is proposed  
135 for an emission-constrained WTPV power producer to select the best pos-  
136 sible strategy.



137 **2. Problem formulation**

138 The multi-objective bidding strategy problem of a WTPV system is formu-  
 139 lated as a stochastic mixed integer programming (MIP) which maximizing the  
 140 expected profit of WTPV system and minimizing the expected emission aris-  
 141 ing from thermal units are considered as two distinct objective functions of the  
 142 decision-maker. In the following subsections, separate objective functions of the  
 143 bi-objective bidding strategy problem will be thoroughly explained.

144 *2.1. First objective function: Maximizing expected profit*

145 The primary purpose of the WTPV system is to maximize its profits through  
 146 participation in diverse electricity markets in the 24-hour scheduled horizon. In  
 147 the coordinated bidding structure, a single offering package will be offered to  
 148 the energy market from all existing energy resources while the offering package  
 149 of power producer in the spinning reserve market exclusively contains the par-  
 150 ticipation of thermal units in this market. The first objective function of the  
 151 power producer for the coordinated operation of all resources is formulated as  
 152 follows:

$$\begin{aligned}
 \text{Max } F_1^C = & \sum_{\omega=1}^{N_\Omega} \pi_\omega \times \left[ \sum_{t=1}^T (\lambda^E(t, \omega) P^{th,E}(t, \omega) + \lambda^E(t, \omega) P^W(t, \omega) \right. \\
 & + \lambda^E(t, \omega) P^{PV}(t, \omega) + \lambda^S(t, \omega) P^{th,S}(t, \omega) \\
 & + \lambda^E(t, \omega) r^+(t, \omega) \Delta^+(t, \omega) - \lambda^E(t, \omega) r^-(t, \omega) \Delta^-(t, \omega) \left. \right] \\
 & - \sum_{\omega=1}^{N_\Omega} \pi_\omega \times \left[ \sum_{t=1}^T \sum_{g=1}^{N_G} C(g, t, \omega) - \sum_{t=1}^T \sum_{g=1}^{N_G} (STU(g, t, \omega)) \right] \quad (1)
 \end{aligned}$$

153 where the first two lines of (1) represent the expected income of power pro-  
 154 ducer from participating in the day-ahead energy and spinning reserve markets  
 155 while the third line relates to the imbalances of power producer in the balancing  
 156 market, finally, the last line refers to the costs of operating and start-up costs  
 157 of the thermal units. The constraints of the objective function (1) would be  
 158 presented as follows:

$$0 \leq EG(b, g, t, \omega) \leq P^{Maxb}(b, g), \quad \forall b, \forall g, \forall t, \forall \omega \quad (2)$$

$$P^{Min}(g)u(g, t, \omega) \leq \sum_{b=1}^{N_b} EG(b, g, t, \omega) \leq P^{Max}(g)u(g, t, \omega), \quad \forall g, \forall t, \forall \omega \quad (3)$$

$$0 \leq ES(g, t, \omega) \leq PS^{Max}(g)u(g, t, \omega), \quad \forall g, \forall t, \forall \omega \quad (4)$$

$$P^{Min}(g)u(g, t, \omega) \leq ET(g, t, \omega) \leq P^{Max}(g)u(g, t, \omega), \quad \forall g, \forall t, \forall \omega \quad (5)$$

$$0 \leq P^W(t, \omega) \leq P^{W,Max}, \quad \forall t, \forall \omega \quad (6)$$

$$0 \leq P^{PV}(t, \omega) \leq P^{PV,Max}, \quad \forall t, \forall \omega \quad (7)$$

$$0 \leq STU(g, t, \omega) \geq STUC(g)x(g, t, \omega), \quad \forall g, \forall t, \forall \omega \quad (8)$$

$$\sum_{n=t-MUT(g)+1}^t x(g, t, \omega) \leq u(g, t, \omega), \quad \forall g, \forall t, \forall \omega \quad (9)$$

$$u(g, t, \omega) + \sum_{n=t-MDT(g)+1}^t y(g, t, \omega) \leq 1, \quad \forall g, \forall t, \forall \omega \quad (10)$$

$$\begin{aligned} \sum_{b=1}^{N_b} EG(b, g, t, \omega) &\leq \sum_{b=1}^{N_b} EG(b, g, t-1, \omega) + RUR(g)u(g, t-1, \omega) \\ &+ STURL(g)x(g, t, \omega), \quad \forall g, \forall t > 1, \forall \omega \end{aligned} \quad (11)$$

$$\begin{aligned} \sum_{b=1}^{N_b} EG(b, g, t-1, \omega) &\leq \sum_{b=1}^{N_b} EG(b, g, t, \omega) + RDR(g)u(g, t, \omega) \\ &+ STDRL(g)y(g, t, \omega), \quad \forall g, \forall t > 1, \forall \omega \end{aligned} \quad (12)$$

$$0 \leq \Delta^+(t, \omega) \leq P^{PV,F}(t, \omega) + P^{W,F}(t, \omega) + P^{th,Ac}(t, \omega), \quad \forall t, \forall \omega \quad (13)$$

$$0 \leq \Delta^-(t, \omega) \leq P^{PV,Max} + P^{W,Max} + \sum_{g=1}^{N_G} P^{Max}(g)u(g, t, \omega), \quad \forall t, \forall \omega \quad (14)$$

$$P^C(t, \omega) \leq P^C(t, \tilde{\omega}), \quad \forall \omega, \tilde{\omega} : [\lambda^E(t, \omega) \leq \lambda^E(t, \tilde{\omega})], \quad \forall t \quad (15)$$

$$P^{th,S}(t, \omega) \leq P^{th,S}(t, \tilde{\omega}), \quad \forall \omega, \tilde{\omega} : [\lambda^S(t, \omega) \leq \lambda^S(t, \tilde{\omega})], \quad \forall t \quad (16)$$

$$P^C(t, \omega) = P^C(t, \tilde{\omega}), \quad \forall \omega, \tilde{\omega} : [\lambda^E(t, \omega) = \lambda^E(t, \tilde{\omega})], \quad \forall t \quad (17)$$

$$P^{th,S}(t, \omega) = P^{th,S}(t, \tilde{\omega}), \quad \forall \omega, \tilde{\omega} : [\lambda^S(t, \omega) = \lambda^S(t, \tilde{\omega})], \quad \forall t \quad (18)$$

$$C(g, t, \omega) = NC(g)u(g, t, \omega) + \sum_{b=1}^{N_b} IC(b, g)EG(b, g, t, \omega), \quad \forall t, \forall \omega \quad (19)$$

$$\sum_{g=1}^{N_G} \sum_{b=1}^{N_b} EG(b, g, t, \omega) = P^{th,E}(t, \omega), \quad \forall t, \forall \omega \quad (20)$$

$$\sum_{g=1}^{N_G} ES(g, t, \omega) = P^{th,S}(t, \omega), \quad \forall t, \forall \omega \quad (21)$$

$$ET(g, t, \omega) = \sum_{b=1}^{N_b} EG(b, g, t, \omega) + ES(g, t, \omega), \quad \forall g, \forall t, \forall \omega \quad (22)$$

$$P^C(t, \omega) = P^{th,E}(t, \omega) + P^W(t, \omega) + P^{PV}(t, \omega) \quad \forall t, \forall \omega \quad (23)$$

$$\Delta(t, \omega) = P^{PV,F}(t, \omega) + P^{W,F}(t, \omega) + P^{th,Ac}(t, \omega) - P^C(t, \omega), \quad \forall t, \forall \omega \quad (24)$$

$$\Delta(t, \omega) = \Delta^+(t, \omega) - \Delta^-(t, \omega), \quad \forall t, \forall \omega \quad (25)$$

$$u(g, t - 1, \omega) - u(g, t, \omega) + x(g, t, \omega) - y(g, t, \omega) = 0, \quad \forall g, \forall t, \forall \omega \quad (26)$$

159 Inequalities (2) and (3) restrict the generated power of thermal units within  
 160 their minimum and maximum bounds while constraint (4) is implemented to  
 161 limit the spinning reserve offer of generation facility within their maximum capa-  
 162 bility in providing upward spinning reserve. Constraint (5) is fulfilled to restrict  
 163 the total bids of thermal units in the day-ahead energy and spinning reserve  
 164 market within their limited operating areas. Constraints (6) and (7) represent  
 165 the upper and lower bounds of the scheduled power of renewable energy sources.  
 166 Constraints (8) is fulfilled to calculate the start-up costs incurred by thermal  
 167 units during the scheduling horizon. Other technical restrictions of thermal u-  
 168 nits, as well as the minimum up/down time are enforced by constraints (9)-(10).  
 169 The ramp-up and ramp-down limitations, considering the shut-down and start-  
 170 up ramps of thermal units are modeled by constraints (11)-(12). Restriction (13)  
 171 limits the positive energy deviations of power producer within the total actual  
 172 power output of all three sources while constraint (14) ensures that the negative  
 173 energy deviations should not exceed the maximum capacity of renewable ener-  
 174 gy sources plus the maximum available capacity of thermal units. Constraints  
 175 (15)-(16) and (17)-(18) are the non-decreasing and non-anticipativity settings  
 176 for the offering packages in the energy and spinning reserve markets, respec-  
 177 tively. The generation cost of thermal units for energy delivery is computed  
 178 through constraint (19). The quadratic cost curve of thermal units makes the  
 179 problem nonlinear. In order to overcome this issue, many researchers have been  
 180 approximated this cost curve using various piecewise blocks [20]. In the current  
 181 paper, these piecewise linearized segments are indexed by letter  $b$ . Constraint  
 182 (20) represents the total bid of thermal units in the energy market. Equation  
 183 (21) calculates total bid of thermal units in the spinning reserve market while  
 184 equation (22) computes the total bid of thermal units in energy and spinning  
 185 reserve markets. Coordinated operation constraints: Constraint (23) calculates  
 186 the final bid of power producer that should be offered to the energy market.  
 187 Constraints (24) and (25) model the imbalances of the power producer in the

188 balancing market. Finally, the logical relationship between the various status  
 189 of thermal units is enforced by equality (26).

190 *2.2. Second objective function: Minimizing expected emission*

191 The second objective function of the power producer in the proposed struc-  
 192 ture is emission minimization. In fact, due to the worldwide rising concerns  
 193 about environmental issues, minimizing the produced pollution by thermal u-  
 194 nits is consistently considered as one of the objective functions of the power  
 195 producers in the optimization process. The linear form of this objective func-  
 196 tion would be as follows:

$$\text{Min } F_2^{th} = \sum_{\omega=1}^{N_\Omega} \pi_\omega \times \left[ \sum_{q=1}^{EMG} \sum_{g=1}^{N_G} \sum_{b=1}^{N_b} E(q, b, g) EG(b, g, t, \omega) \right] \quad (27)$$

197 It is worth to note that in order to take advantage of linear programming in  
 198 the proposed structure, the emission functions of thermal units, which generally  
 199 have a quadratic form, are approximated by some piecewise linearized blocks.  
 200 In the current paper, the  $SO_2$  and  $NO_X$  are taken into consideration as the  
 201 primary sources of emission [21].

202 In this paper, three different bidding strategies, including the coordinated  
 203 and uncoordinated operation of various energy sources, are considered to thor-  
 204 oughly examine the productivity of the proposed structure. Fig. 1 shows these  
 205 three different bidding strategies with their determinant constraints. These  
 206 three trading strategies are designed to exhaustively assess the multi-objective  
 207 bidding strategy problem based on the following modes of operation:

- 208 1. Uncoordinated operation of all three available energy resources.
- 209 2. Coordinated operation of two energy resources + Uncoordinated operation  
 210 of the last energy resources.
- 211 3. Coordinated operation of all three available energy resources.

212 Note that the authors have passed up to present the formulation of the first  
 213 and second trading strategies to avoid tautology in writing. It is notable that  
 214 the superscript numbers in the constraints of the second strategy point out two  
 215 distinct trading strategy in this case study.

216  
 217  
 218

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Fig. 1 is placed here

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219 *2.3. Solution method of the multi-objective optimization problem*

220 Most practical engineering issues are faced with more than one objective  
 221 function, which in many cases, these objective functions conflict with each other.  
 222 Multifarious techniques and methods have been employed in the literature  
 223 to solve multi-objective problems, which  $\epsilon$ -constraint technique [20] and the  
 224 weighted sum (WS) approach [24] are among these methods. In the present  
 225 paper, the weighted sum technique has been used to solve the multi-objective  
 226 bidding strategy of wind-thermal-photovoltaic energy resources. In the weight-  
 227 ed sum method, all objective functions with different weighting factors that  
 228 represent the relative significance of each objective function are put together in  
 229 a separate objective function according to the following equation:

$$\text{Min } [OF] = w_1 F_1' + w_2 F_2 \quad (28)$$

230 subject to

$$\begin{cases} w_1 + w_2 = 1 \\ F_1' = -F_1 \\ \text{All restrictions of the proposed problem} \end{cases} \quad (29)$$

231 where  $F_1$  and  $F_2$  stand for the two conflicting objective functions of the  
 232 proposed problem, i.e., profit maximization and emission minimization. One  
 233 of the difficulties faced by decision-makers in the weighted sum method is the  
 234 different scale of objective functions in (28). To this end, a fuzzy satisfying

235 approach is proposed to overcome this issue in the literature of multi-objective  
 236 programming problems [21]. Based on this approach, the objective functions in  
 237 (28) are normalized as follows:

$$F_{1,pu} = \frac{F_1 - F_1^{max}}{F_1^{max} - F_1^{min}} \quad (30)$$

$$F_{2,pu} = \frac{F_2^{max} - F_2}{F_2^{max} - F_2^{min}} \quad (31)$$

238 where  $F_{1,pu}$  and  $F_{2,pu}$  are the per unit values of objective functions  $F_1$  and  
 239  $F_2$ , respectively. In fact, the equations (30) and (31) map the objective functions  
 240  $F_1$  and  $F_2$  in the range 0 and 1.  $(F_1^{max}, F_2^{max})$  and  $(F_1^{min}, F_2^{min})$  represent the  
 241 obtained maximum and minimum values of each objective function through the  
 242 single objective optimization process, respectively. After normalizing each ob-  
 243 jective function, the objective function of the weighted sum method is rewritten  
 244 as follows:

$$\text{Min } [OF] = w_1 F'_{1,pu} + w_2 F_{2,pu} \quad (32)$$

#### 245 2.4. Decision-maker's approach to select the best compromise solution

246 After obtaining the Pareto solutions via the WS method, the most favored  
 247 solution among all set of solutions should be picked up. In the present paper,  
 248 the final selection of the best compromise solution is accomplished based on the  
 249 mindset, inclination, and preferences of decision-makers [25]. Indeed, decision-  
 250 makers ascertain the minimum and maximum permissible values for the objec-  
 251 tive functions based on insight, the experience of previous years, short-term and  
 252 long-term plans, and restrictions imposed by system operators. In this regard,  
 253 for the objective function of maximizing profit, the minimum acceptable profit  
 254 and for the objective function of minimizing emission, the maximum allowable  
 255 emission is determined by the decision-maker, and finally, the most favored  
 256 solution is selected based on these preconditions.

257 *2.5. Uncertainty characterization*

258 The uncertain sources in the optimal bidding strategy of a GenCo are gener-  
 259 ally divided into two groups: the price of various target markets and generation  
 260 power of renewable energy sources. The methodology for modeling the uncer-  
 261 tainties arising from electricity market prices and output power of renewable  
 262 energy sources will be explained in the following subsections.

263 *2.5.1. Market Prices uncertainty model*

264 In the proposed framework, the normal probability density function (PDF)  
 265 is utilized to model the three uncertain market prices: the day-ahead energy and  
 266 spinning reserve market prices along with the real-time market price. The PDF  
 267 of an electricity market price  $\lambda_{price}$  with mean  $\mu_{price}$  and standard deviation  
 268  $\sigma_{price}$  would be formulated as follows:

$$f_{price}(\lambda_{price}, \mu_{price}, \sigma_{price}) = \frac{1}{\sigma_{price}\sqrt{2\pi}} \exp \left[ -\frac{(\lambda_{price} - \mu_{price})^2}{2\sigma_{price}^2} \right] \quad (33)$$

269 *2.5.2. Wind power uncertainty model*

270 As it is evident, the production power of a wind turbine is not constant and  
 271 changes as a function of wind speed. In the current paper, the Weibull PDF  
 272 has been considered for modeling wind speed. The Weibull PDF of wind speed  
 273  $V$  with scale and shape factors  $c$  and  $k$  is defined as follows:

$$f_{wind}(V, c, k) = \frac{k}{c} \left( \frac{V}{c} \right)^{k-1} \exp \left[ -\left( \frac{V}{c} \right)^k \right] \quad (34)$$

274 The generated power of a wind turbine in specified wind speed  $V$  has fully  
 275 corresponded to its technical specifications, namely, cut-out speed  $v_{co}$ , cut-in  
 276 speed  $v_{ci}$ , and rated speed  $v_r$ , which is calculated using the following equation:

$$P_{wind} = \begin{cases} 0, & 0 \leq V \leq v_{ci} \\ P_{rated} \times \left( \frac{V-v_{ci}}{v_r-v_{ci}} \right), & v_{ci} \leq V \leq v_r \\ P_{rated}, & v_r \leq V \leq v_{co} \end{cases} \quad (35)$$



278 *2.5.3. Solar power uncertainty model*

279 Solar irradiance is the most significant factor in determining the output  
 280 power of photovoltaic units, which is always confronted with uncertainties. In  
 281 this paper, the Beta PDF is utilized as an appropriate expression pattern of  
 282 solar irradiance. The Beta PDF of solar irradiance  $Si$  is expressed as follows:

$$f_{irr}(Si, \alpha, \beta) = \begin{cases} \frac{\Gamma(\alpha+\beta)}{\Gamma(\alpha)\Gamma(\beta)} \times (Si)^{\alpha-1} \times (1-Si)^{\beta-1}, & 0 \leq Si \leq 1, \alpha \geq 0, \beta \geq 0 \\ 0, & otherwise \end{cases} \quad (36)$$

283 Given the solar irradiance  $Si$  of photovoltaic units, their efficiency  $\eta^{PV}$  and  
 284 total area  $S^{PV}$ , the output power of PV units  $P_{PV}$  are calculated as follows  
 285 [23]:

$$P_{PV} = \eta^{PV} \times S^{PV} \times Si \quad (37)$$

286 Finally, By assigning appropriate probability density functions to each un-  
 287 certain parameter, scenarios associated with these parameters are constructed  
 288 by the roulette wheel mechanism [23].

289 **3. Emission trading**

290 In this paper, a solution fits the purchasing or selling emission quotas is pre-  
 291 sented for those occasions that taking advantage of emission trading is accessible  
 292 for GenCos/industrial consumers. In this regard, [26] and [27] have focused on  
 293 the detailed investigation of emission trading pattern in China's container ter-  
 294 minal and building materials industry, respectively. Based on this approach,  
 295 after solving the multi-objective bidding strategy problem, a specific strategy  
 296 for each Pareto optimal solution will be adopted. If the emission of thermal  
 297 units per Pareto exceeds the emission quota, the GenCo will have to purchase  
 298 additional emission quotas. However, if the emission of a GenCo in each Pareto  
 299 is less than the assigned emission quota, the Genco can sell its surplus emission  
 300 quota. As mentioned above, the total expected earnings of GenCo in every  
 301 Pareto optimal solution will be calculated as follows:

$$TPF = EPP + [\lambda^{EM} \times (E^{EQ} - EEG)] \quad (38)$$

302 where the TPF is net expected profit, EPP is the expected profit of Gen-  
 303 Co per Pareto,  $E^{EQ}$  is the assigned emission quota to GenCo,  $\lambda^{EM}$  refers to  
 304 emission price, and the EEG stands for the expected emission of GenCo per  
 305 Pareto. Ultimately, for each emission price, a Pareto with the maximum val-  
 306 ue of TEP is selected as the optimal Pareto solution of the proposed bidding  
 307 strategy problem.

## 308 4. Results and discussion

### 309 4.1. Input data

310 The proposed system under study comprises five thermal units, a wind farm,  
 311 and a PV site with the maximum capacity of 340 MW, 250 MW, and 150  
 312 MW for each, respectively. The economic and technical information on thermal  
 313 units is provided in Table 2 and Table 3. These data have been extracted with  
 314 some adjustments from [16]. Also, the data related to the emission curve of  
 315 thermal units are given in Table 4. It is worthwhile to mention again that  
 316 the quadratic cost and emission curves of thermal units are approximated by  
 317 three piecewise blocks. This action, along with the proper formulation of the  
 318 problem, leads to the absence of any nonlinear term in the proposed issue. On  
 319 the basis of previously published papers, the  $SO_2$  and  $NO_x$  are considered as the  
 320 fundamental origins of emission [21]. The expected values of forecasted wind  
 321 speed and solar irradiance [28] are portrayed in Fig. 2 while information on wind  
 322 turbines and PV site are provided in Table 5.

323

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Tables 2, 3, 4, and 5 are placed here

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326

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Figure 2 is placed here

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329 In the proposed model, GenCo only allows the thermal units to participate  
330 in the spinning reserve market, and since the offer of each unit in this market  
331 has to be ready to deliver in ten minutes, the maximum offer for each unit in  
332 this market is calculated using  $PS^{\text{Max}}(g) = \frac{1}{6} \times \text{RUR}(g)$  [29]. As outlined in  
333 subsection 2.5, five uncertainty sources exist in the proposed structure (day-  
334 ahead market, spinning reserve market, and imbalance prices as well as wind  
335 and PV generation). Based on the suggested model, for each parameter, the  
336 adequate number of scenarios based on the statistical analysis of [28] and [30] is  
337 constructed using roulette wheel mechanism, and with a common approach, i.e.,  
338 fast forward reduction technique [16] and [19], the initially generated scenarios  
339 for each parameter are reduced to three representative scenarios. Consequently,  
340 the final scenario set will contain  $3^5 = 243$  scenarios. The proposed structure  
341 is formulated based on the MIP and has been implemented in GAMS (general  
342 algebraic modeling system), with CPLEX as the solver.

#### 343 4.2. Results

344 In order to assess the performance of the proposed structure, two different  
345 case studies are considered in this paper. In the first case study, we examine the  
346 single objective framework for the bidding strategy of the system under consid-  
347 eration, and in the second case study, the multi-objective bidding strategy of  
348 the wind-thermal-PV system is discussed. It is worth to note that in all case  
349 studies, the three trading strategies shown in Fig. 1 is fully explored. The first  
350 trading strategy appertained to the disjoint operation of all three energy sources  
351 in the electricity markets. The second trading strategy refers to the coordinated  
352 operation of wind and thermal units, while the PV system individually and in-  
353 dependently participates in the electricity market. Eventually, the third trading  
354 strategy relates to the coordinated operation of all available energy sources.

355 *4.2.1. Case study 1*

356 As already mentioned, this case study focuses on the single objective bidding  
357 strategy of the system under study. In other words, this case study focuses solely  
358 on maximizing producer's profit without having a program or goal to minimize  
359 emissions. The results of this case study have been exhibited in Table 6. It  
360 is necessary to mention that this table will allow us to compare the economic  
361 and environmental aspects of different trading strategies. According to the ob-  
362 tained results, trading strategy 1 has the lowest expected profit (€302434.636)  
363 and the highest imbalance cost (€25369.536) among all three trading strategies.  
364 In contrast, coordinated operations of all three resources (trading strategy 3)  
365 have resulted in the highest profitability and the lowest imbalance cost, which  
366 the obtained results are €304509.778 and €15278.357, respectively. Similar-  
367 ly, in the second trading strategy that includes the coordinated operation of  
368 wind and thermal resources, more profit (€303221.192) and fewer imbalance  
369 cost (€23037.277) are obtained compared to the first strategy. From a differ-  
370 ent point of view, coordinated operation of energy resources in the proposed  
371 bidding strategy not only increase the profitability of the power producer but  
372 also reduces the emission of thermal units. It has to be noted that the numeric  
373 percent for comparing the decreasing or increasing values related to expected  
374 profit, expected emission, and expected imbalance cost of trading strategies two  
375 and three will be presented later to check out the effectiveness of the proposed  
376 bidding strategy.

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Table 6 is placed here

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380 Fig. 3 shows the expected participation of WTPV system in the energy  
381 and spinning reserve markets for all trading strategies. According to Fig. 3a,  
382 it is observed that at almost most of the hours, trading strategy 1 has more  
383 participation in the energy market. This issue has led the trading strategy 1 to  
384 have the highest imbalance cost, which ultimately leads to more reduction in the

385 expected profit of WTPV system. Besides, it can be viewed that the difference  
386 in the participation of various trading strategies in the day-ahead energy market  
387 reflects more during high market prices. On the other hand, as shown in Fig. 3b,  
388 the participation of WTPV system in the spinning reserve market for trading  
389 strategies 2 and 3 are similar at most hours. Also, the high day-ahead market  
390 prices during hours 11-14 have led to a reduction in producer's participation  
391 in the spinning reserve market for the specified time interval. In other words,  
392 the producer will have a greater willingness to participate in the energy market  
393 instead of participating in the spinning reserve market to gain more profit in the  
394 aforementioned time interval. Finally, Fig. 4 presents the comparison between  
395 the share of thermal units from the entire participation of WTPV system in the  
396 energy market for all trading strategies. The share of thermal units in trading  
397 strategies 1 and 2 are lower than the first trading strategy, which leads to lower  
398 emission of power producer, as reported in Table 6. It is worth mentioning  
399 that Fig. 3 and Fig. 4 are demonstrated to unfold how the coordinated trading  
400 strategy of various available sources will alter the expected participation of the  
401 whole system and thermal units in the energy and spinning reserve markets,  
402 respectively.

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403  
404 Figures 3 and 4 are placed here  
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#### 406 *4.2.2. Case study 2*

407 This case study is designed to address the multi-objective bidding strategy  
408 of the wind-thermal-PV system. Contrary to the first case study, in this case  
409 study, minimizing the emission of thermal units is also added to one of the  
410 decision-maker's goals in the optimization process. As discussed in the previous  
411 sections, the weighted sum method is used to solve the multi-objective optimiza-  
412 tion problem. In this method, different weighting factors for objective functions  
413 (here,  $w_1$  and  $w_2$ ) are chosen subject to  $w_1 + w_2 = 1$ , and finally, the Pareto  
414 solutions of the proposed problem will be obtained. The results of Pareto for

415 trading Strategies 1, 2, and 3 are shown in Fig. 5, Fig. 6, and Fig. 7, respective-  
416 ly. Also, the normalized values of objective functions  $F1$  and  $F2$  in equations  
417 (30) and (31), i.e.,  $F_{1,pu}$  and  $F_{2,pu}$ , are reported in the aforementioned figures.  
418 These normalized values let us observe that the proposed bi-objective model can  
419 efficiently obtain various results in the range of 0 and 1 that do not agglutinate  
420 in a specific space and it is capable of covering almost any range of  $F_{1,pu}$  and  
421  $F_{2,pu}$ . After obtaining Pareto results, the proposed approach in subsection 2.4  
422 is implemented to select the most favored solution among all Pareto solutions.  
423 The minimum and maximum predetermined limits for the profit and emission  
424 are assumed to be  $20 \times 10^3$  lbs and  $\text{€ } 250 \times 10^3$ , respectively. It has to be not-  
425 ed that these limits are determined by the decision-maker (GenCo) to merely  
426 compare the results of different trading strategies under similar conditions and  
427 consequently, every other restriction can be imposed by the decision-maker. Ac-  
428 cordingly, the presented Pareto solutions in Fig. 5, Fig. 6, and Fig. 7 will let us  
429 pick the most favored solution under different predetermined restrictions. The  
430 summary results of different trading strategies in terms of the environmental  
431 and economic evaluation of the multi-objective bidding strategy have been pro-  
432 vided in Table 7. It is worth noting that the results of Table 7 correspond to the  
433 red box of Fig. 5, Fig. 6 and Fig. 7 ( $P14$ ) that obtained through the suggested  
434 approach in subsection 2.4.

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435  
436 Table 7 is placed here

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438  
439 Figures 5, 6 and 7 are placed here

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441 According to the provided results in Table 7, trading strategies 2 and 3 have  
442 also led to an increase in the producer's expected profit in the multi-objective  
443 bidding strategy. The expected profit for trading strategies one, two, and three  
444 is  $\text{€}253638.926$ ,  $\text{€}255566.283$ , and  $\text{€}256978.704$ , respectively. In this regard, the  
445 most expected profit is achieved via the third trading strategy ( $\text{€}256978.704$ )

446 Which is consistent with the results of the previous case study. Similar to the  
447 first case study, in the second case study, the trading strategies 2 and 3 also  
448 diminish the imbalance costs and emissions in comparison with the first trading  
449 strategy.

450 Similar to Fig. 3, Fig. 8 illustrates the expected bids of power producer  
451 that are going to be submitted in the energy and spinning reserve markets for  
452 all three trading strategies. The expected production bids in the energy market  
453 (Fig. 8a) follow the explanation given about Fig. 3a, with the difference that the  
454 rates of production bids are significantly reduced. Fig. 8b allows us to conclude  
455 that the power producer's bidding approach in the spinning reserve market for  
456 all trading strategies will not affect the producer's strategy in this market. This  
457 issue stems from the fact that the producer tends to utilize the maximum level  
458 of participation in the spinning reserve market to gain its expected profit in  
459 whole trading strategies while the pollution constraints restrict its production  
460 in the energy market. At the remaining hours, the rising level of GenCo's  
461 participation in the energy market, the GenCo's involvement in the spinning  
462 reserve also increases. Analogous to Fig. 4, the comparison between the portion  
463 of thermal units from the total participation of the WTPV system in the energy  
464 market for all trading strategies in the multi-objective optimization approach is  
465 captured in Fig. 9. In fact, this figure exposes how the emission of both trading  
466 strategies 2 and 3 will be reduced in comparison with the first trading strategy.  
467 In comparison with the first case study, a large portion of the thermal units'  
468 production bids has been reduced, which is more evident in time intervals with  
469 lower energy prices.

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471 Figures 8 and 9 are placed here

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473 In order to participate in diverse electricity markets, the producers should  
474 submit their bidding packages to each specific market. The bidding curves of the  
475 power producer in the energy market for hours 8 and 22 for both single-objective  
476 and bi-objective bidding approaches are captured in Fig. 10 and Fig. 11. It can

477 be noticed that in the coordinated operation of energy resources, for example,  
478 trading strategy 3, a bidding curve from all three energy resources is submit-  
479 ted to the day-ahead energy market. As can be seen from these curves, the  
480 coordinated operation of two or all units (strategy 2 or 3) leads to a change in  
481 the producer's bidding curve compared to the uncoordinated one (strategy 1).  
482 This is evident for both single objective and bi-objective bidding approaches.  
483 Moreover, the drop in bid volumes of bi-objective bidding approach compared  
484 to the single objective one is noticeable as can be seen from these figures.

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485  
486 Figures 10 and 11 are placed here  
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488 In this paper, along with the proposed approach in subsection 2.4, emission  
489 trading is also taken into consideration as a new scheme in the decision-making  
490 process of the power producer. Following the explanations given in section 3,  
491 after solving the multi-objective bidding strategy problem and obtaining corre-  
492 sponding Pareto solutions, this approach is implemented to select the optimal  
493 solution among all Pareto solutions. The maximum TPF obtained by equation  
494 (38) will be the optimal solution corresponding to each emission price. One of  
495 the superiorities and advantages of this method versus other techniques is that  
496 the emission quota of the power producer is implicitly included in the bidding  
497 process. In the current paper, in order to avoid tautology in the demonstration  
498 of results, only the results of emission quota arbitraging for trading strategy 3  
499 have been reported in Table 8. The emission quota of the power producer is  
500 considered  $20 \times 10^3$  lbs. The bold numbers in each column pertaining to emission  
501 prices indicate the optimal Pareto solution for that particular emission price.  
502 As can be seen from this table, the increase in the price of emission leads to a  
503 reduction in the expected net profit of the power producer.

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504  
505 Table 8 is placed here  
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507 The final investigation of this paper is dedicated to examining the effect of



508 the number of scenarios on the principal output variables of the problem, i.e.,  
509 expected profit and emission, and their standard deviation. To this end, dif-  
510 ferent analyses under the different number of scenarios of operating variables,  
511 namely, renewable power productions and electricity market prices, are carried  
512 out, and results will be compared. It has to be noted that these analyses are  
513 conducted on the third trading strategy because of two reasons: first, the coordi-  
514 nated operation of wind, thermal, and PV units is selected as the final preferred  
515 bidding strategy and second, the third trading strategy involves one optimiza-  
516 tion problem where all existing uncertainty sources are present and, as a result,  
517 all uncertainties affect the outputs of the problem. The considered analyses are  
518 as follows:

- 519 1. Analysis 1: two representative scenarios for each uncertain parameter is  
520 considered in the scenario reduction stage. Consequently, the total number  
521 of scenarios in this analysis would be  $2^5=32$ .
- 522 2. Analysis 2: three scenarios for each uncertain parameter is taken into  
523 account. The total number of scenarios is  $3^5=243$ . In fact, this analysis  
524 is the same as the one proposed in this paper.
- 525 3. Analysis 3: the reduced number of scenarios for each uncertain parameter  
526 is equal to four, so the entire scenario set includes  $4^5=1024$  scenarios.

527 It is worth mentioning that the reduced scenarios are obtained according to  
528 provided descriptions in subsection 4.1. Fig. 12 and Fig. 13 demonstrate the  
529 attained expected profit and emission versus their standard deviations in var-  
530 ious analyses. According to Fig. 12, raising the total number of scenarios will  
531 result in an increment in both expected profit and its standard deviation. On  
532 the contrary, based on Fig. 13, it can be observed that the expected emission  
533 of the system and its standard deviation will be reduced by moving toward  
534 larger scenario sets. In summary, enlarging scenario numbers will modify both  
535 expected profit and emission of the power producer, but it may seriously lead  
536 to a computational explosion. The results of the computation time for diverse

537 analyses have been depicted in Fig. 14. It can be seen from this figure that  
538 increasing the number of scenarios will considerably raise the solution time, e-  
539 specially in the bi-objective bidding approach. In this regard, by changing the  
540 attitude of the WTPV system from the second analysis to the third one in the  
541 case study 2, a 1% increase in the expected profit results in a 462% increment  
542 in the solution time. It has to be noticed that the scale of the vertical axis in  
543 Fig. 14 is logarithmic.

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546

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Figures 12, 13 and 14 are placed here

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#### 547 *4.3. Discussion*

548 In the current paper, a comprehensive bidding model for the participation  
549 of wind, thermal, and photovoltaic units has been proposed. In summary, by  
550 examining the presented results in two case studies using the suggested approach  
551 in subsection 2.4, we can conclude that the proposed trading strategies will  
552 increase the expected profit and reduce the expected emission of the power  
553 producer. In order to assess the effectiveness of the second and third trading  
554 strategies in comparison with the first trading strategy, Fig. 15 and Fig. 16 are  
555 provided. According to these figures, it can be concluded that:

- 556 1. In both case studies, the third trading strategy has the highest profit  
557 increment, which these values are 1.36% and 0.68% for the first and second  
558 case studies, respectively.
- 559 2. In both case studies of the second and third trading strategies, the emission  
560 of thermal units decreases compared to the first trading strategy, which is  
561 more striking in the first case study.
- 562 3. Trading strategy 3 has the highest imbalance reduction, especially in the  
563 bi-objective bidding approach.

- 564 4. Reducing the expected production bids in the energy market has led to a  
565 decrease in the cost of imbalances and, consequently, an increase in the  
566 producer's profit.
- 567 5. In the bi-objective bidding approach, the trading strategy of power pro-  
568 ducer will not affect the participation level of thermal units in the spinning  
569 reserve market.

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571 Figures 15 and 16 are placed here

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573 Nevertheless, the following directions are suggested for further research:

- 574 1. Considering a risk measuring index in the bi-objective bidding strategy of  
575 WTPV system as an additional parameter.
- 576 2. Proposing a bi-level bidding model for the WTPV system while it behaves  
577 as a price-maker producer in one of the target electricity markets.

## 578 5. Conclusion

579 In this paper, a new framework for multi-objective bidding strategy of an  
580 integrated wind-thermal-photovoltaic system alongside two different decision-  
581 making schemes was proposed to attain the introduced contributions. In order  
582 to assess the effectiveness of the suggested bidding structure, three different trad-  
583 ing strategies, including coordinated and uncoordinated operation of generation  
584 units, along with their relevant formulation were comprehensively presented,  
585 and subsequently, an efficient technique was applied to solve the bi-objective  
586 problem.

587 The key findings of the suggested model are listed as follows:

- 588 1. The coordinated operation of all energy resources was led to the high-  
589 est expected profit in both single-objective and multi-objective bidding  
590 strategies. In fact, in the bi-objective model, the aim was to evaluate the

591           profitability of the coordinated bidding strategy of all available sources in  
592           the presence of an additional objective function, which in this occasion,  
593           the proposed bidding strategy was also able to gain the total expected  
594           profit of the system.

595       2. The reduction in the output power of thermal units in the bi-objective  
596           approach will lead to considerable imbalance reduction in comparison with  
597           the single-objective one. This imbalance reduction was accompanied by a  
598           decrease in the participation of the system in the energy market.

599       3. The variation in the trading approach of the system in the bi-objective  
600           model did not affect the bidding decisions in the spinning reserve market.

601       4. The emission trading mechanism can be used as a beneficial pattern by  
602           the power producers to increase their profitability as the presented model  
603           in this paper results in higher values of expected profit for all emission  
604           prices lower than 1 €/lbs.

605       5. The greater scenario sets result in higher values of expected profit and its  
606           standard deviation while the expected emission and its standard deviation  
607           are reduced. In this regard, a slight variation in the fundamental output  
608           variables of the problem, i.e., expected profit and expected emission, by  
609           increasing the total number of scenarios will lead to a computational ex-  
610           plosion.

## 611 **References**

612       [1] De Andrade Guerra, J.B.S.O., Dutra, L., Schwinden, N.B.C., Andrade,  
613           S.F. De, 2015. Future scenarios and trends in energy generation in  
614           Brazil: Supply and demand and mitigation forecasts. *J. Clean. Prod.* <http://doi.org/10.1016/j.jclepro.2014.09.082>  
615

616       [2] Ram, M., Child, M., Aghahosseini, A., Bogdanov, D., Lohrmann, A., Breyer,  
617           C., 2018. A comparative analysis of electricity generation costs from

- 618 renewable, fossil fuel and nuclear sources in G20 countries for the period  
619 2015-2030. *J. Clean. Prod.* 199, 687–704.
- 620 [3] Wesseh, P.K., Lin, B., 2017. Options for mitigating the adverse ef-  
621 fects of fossil fuel subsidies removal in Ghana. *J. Clean. Prod.* <https://doi.org/10.1016/j.jclepro.2016.09.214>  
622
- 623 [4] Zafar, M.W., Shahbaz, M., Hou, F., Sinha, A., 2019. From nonrenewable  
624 to renewable energy and its impact on economic growth: The role of re-  
625 search & development expenditures in Asia-Pacific Economic Cooperation  
626 countries. *J. Clean. Prod.* <https://doi.org/10.1016/j.jclepro.2018.12.081>
- 627 [5] Yin, G., Zhou, L., Duan, M., He, W., Zhang, P., 2018. Impacts of carbon  
628 pricing and renewable electricity subsidy on direct cost of electricity gen-  
629 eration: A case study of China’s provincial power sector. *J. Clean. Prod.*  
630 <https://doi.org/10.1016/j.jclepro.2018.09.108>
- 631 [6] Nie, P. yan, Chen, Y. hua, Yang, Y. cong, Wang, X.H., 2016. Subsidies  
632 in carbon finance for promoting renewable energy development. *J. Clean.*  
633 *Prod.* <https://doi.org/10.1016/j.jclepro.2016.08.083>
- 634 [7] Shi, X., Dini, A., Shao, Z., Jabarullah, N.H., 2019. Impacts of photovolta-  
635 ic/wind turbine/microgrid turbine and energy storage system for bidding  
636 model in power system. *J. Clean. Prod.*
- 637 [8] Abedinia, O., Zareinejad, M., Doranehgard, M.H., Fathi, G., Ghadimi, N.,  
638 2019. Optimal offering and bidding strategies of renewable energy based  
639 large consumer using a novel hybrid robust-stochastic approach. *J. Clean.*  
640 *Prod.* 215, 878–889.
- 641 [9] Aliasghari, P., Mohammadi-Ivatloo, B., Alipour, M., Abapour, M., Zare,  
642 K., 2018. Optimal scheduling of plug-in electric vehicles and renewable  
643 micro-grid in energy and reserve markets considering demand response pro-  
644 gram. *J. Clean. Prod.* <https://doi.org/10.1016/j.jclepro.2018.03.058>

- 645 [10] Tan, M., Chen, Y., Su, Y. xin, Li, S. hu, Li, H., 2019. Integrat-  
646 ed optimization model for industrial self-generation and load schedul-  
647 ing with tradable carbon emission permits. *J. Clean. Prod.* <https://doi.org/10.1016/j.jclepro.2018.11.005>  
648
- 649 [11] Khaloie, H., Abdollahi, A., Rashidinejad, M., Siano, P., 2019. Risk-  
650 based probabilistic-possibilistic self-scheduling considering high-impact  
651 low-probability events uncertainty. *Int. J. Electr. Power Energy Syst.* 110,  
652 598–612. <https://doi.org/10.1016/j.ijepes.2019.03.021>
- 653 [12] Perković, L., Mikulčić, H., Duić, N., 2018. Multi-objective optimization of  
654 a simplified factory model acting as a prosumer on the electricity market.  
655 *J. Clean. Prod.* <https://doi.org/10.1016/j.jclepro.2016.12.078>
- 656 [13] Hooshmand, R.A., Nosratabadi, S.M., Gholipour, E., 2018. Event-based  
657 scheduling of industrial technical virtual power plant considering wind and  
658 market prices stochastic behaviors - A case study in Iran. *J. Clean. Prod.*  
659 <https://doi.org/10.1016/j.jclepro.2017.12.017>
- 660 [14] Varkani, A.K., Daraeepour, A., Monsef, H., 2011. A new self-  
661 scheduling strategy for integrated operation of wind and pumped-storage  
662 power plants in power markets. *Appl. Energy* 88, 5002–5012. <https://doi.org/10.1016/j.apenergy.2011.06.043>  
663
- 664 [15] Esmaeily, A., Ahmadi, A., Raeisi, F., Ahmadi, M.R., Esmaeel Nezhad,  
665 A., Janghorbani, M., 2017. Evaluating the effectiveness of mixed-integer  
666 linear programming for day-ahead hydro-thermal self-scheduling consider-  
667 ing price uncertainty and forced outage rate. *Energy* 122, 182–193. <https://doi.org/10.1016/j.energy.2017.01.089>  
668
- 669 [16] Al-Awami, A.T., El-Sharkawi, M.A., 2011. Coordinated trading of wind  
670 and thermal energy. *IEEE Trans. Sustain. Energy* 2, 277–287. <https://doi.org/10.1109/TSTE.2011.2111467>  
671

- 672 [17] Lakshmi, K., Vasantharathna, S., 2014. Gencos wind–thermal scheduling  
673 problem using Artificial Immune System algorithm. *Int. J. Electr. Power*  
674 *Energy Syst.* 54, 112–122. <https://doi.org/10.1016/j.ijepes.2013.06.036>
- 675 [18] Laia, R., Pousinho, H.M.I., Melíco, R., Mendes, V.M.F., 2016. Bidding  
676 strategy of wind-thermal energy producers. *Renew. Energy* 99, 673–681.  
677 <https://doi.org/10.1016/j.renene.2016.07.049>
- 678 [19] Al-Swaiti, M.S., Al-Awami, A.T., Khalid, M.W., 2017. Co-optimized trad-  
679 ing of wind-thermal-pumped storage system in energy and regulation mar-  
680 kets. *Energy* 138, 991–1005. <https://doi.org/10.1016/j.energy.2017.07.10>
- 681 [20] Aghaei, J., Alizadeh, M.I., 2013. Multi-objective self-scheduling of CHP  
682 (combined heat and power)-based microgrids considering demand response  
683 programs and ESSs (energy storage systems). *Energy* 55, 1044–1054. [http-  
684 s://doi.org/10.1016/j.energy.2013.04.048](https://doi.org/10.1016/j.energy.2013.04.048)
- 685 [21] Ahmadi, A., Aghaei, J., Shayanfar, H.A., Rabiee, A., 2012. Mixed integer  
686 programming of multiobjective hydro-thermal self scheduling. *Appl. Soft*  
687 *Comput. J.* 12, 2137–2146. <https://doi.org/10.1016/j.asoc.2012.03.020>
- 688 [22] Simab, M., Javadi, M.S., Nezhad, A.E., 2018. Multi-objective pro-  
689 gramming of pumped-hydro-thermal scheduling problem using nor-  
690 mal boundary intersection and VIKOR. *Energy* 143, 854–866. [http-  
691 s://doi.org/10.1016/j.energy.2017.09.144](https://doi.org/10.1016/j.energy.2017.09.144)
- 692 [23] Soltani, S., Rashidinejad, M., Abdollahi, A., 2017. Stochastic Multiobjec-  
693 tive Distribution Systems Phase Balancing Considering Distributed Energy  
694 Resources. *IEEE Syst. J.* <https://doi.org/10.1109/JSYST.2017.2715199>
- 695 [24] Jannati, J., Nazarpour, D., 2019. Optimal performance of electric ve-  
696 hicles parking lot considering environmental issue. *J. Clean. Prod.* 206,  
697 1073–1088.

- 698 [25] Zakariazadeh, A., Jadid, S., Siano, P., 2014. Stochastic multi-objective  
699 operational planning of smart distribution systems considering demand re-  
700 sponse programs. *Electr. Power Syst. Res.* 111, 156–168.
- 701 [26] Zhong H, Hu Z, Yip TL. Carbon emissions reduction in China’s contain-  
702 er terminals: Optimal strategy formulation and the influence of carbon  
703 emissions trading. *J Clean Prod* 2019;219:518–30.
- 704 [27] Zhao, S., Shi, Y., Xu, J., 2018. Carbon emissions quota allocation based  
705 equilibrium strategy toward carbon reduction and economic benefits in Chi-  
706 na’s building materials industry. *J. Clean. Prod.* 189, 307–325.
- 707 [28] Weather history+ - meteoblue [WWW Document], n.d. URL [http-](https://www.meteoblue.com/en/historyplus)  
708 [s://www.meteoblue.com/en/historyplus](https://www.meteoblue.com/en/historyplus) (accessed 4.22.19).
- 709 [29] Khaloie, H., Abdollahi, A., Rashidineiad, M., 2018. Risk-Constrained Self-  
710 Scheduling and Forward Contracting Under Probabilistic-Possibilistic Un-  
711 certainties, in: *Electrical Engineering (ICEE), Iranian Conference On.*  
712 *IEEE*, pp. 1138–1143. <https://doi.org/10.1109/ICEE.2018.8472668>.
- 713 [30] Bienvenido — ESIOS electricidad · datos · transparencia [WWW Docu-  
714 ment], n.d. URL <https://www.esios.ree.es/es> (accessed 3.14.19).



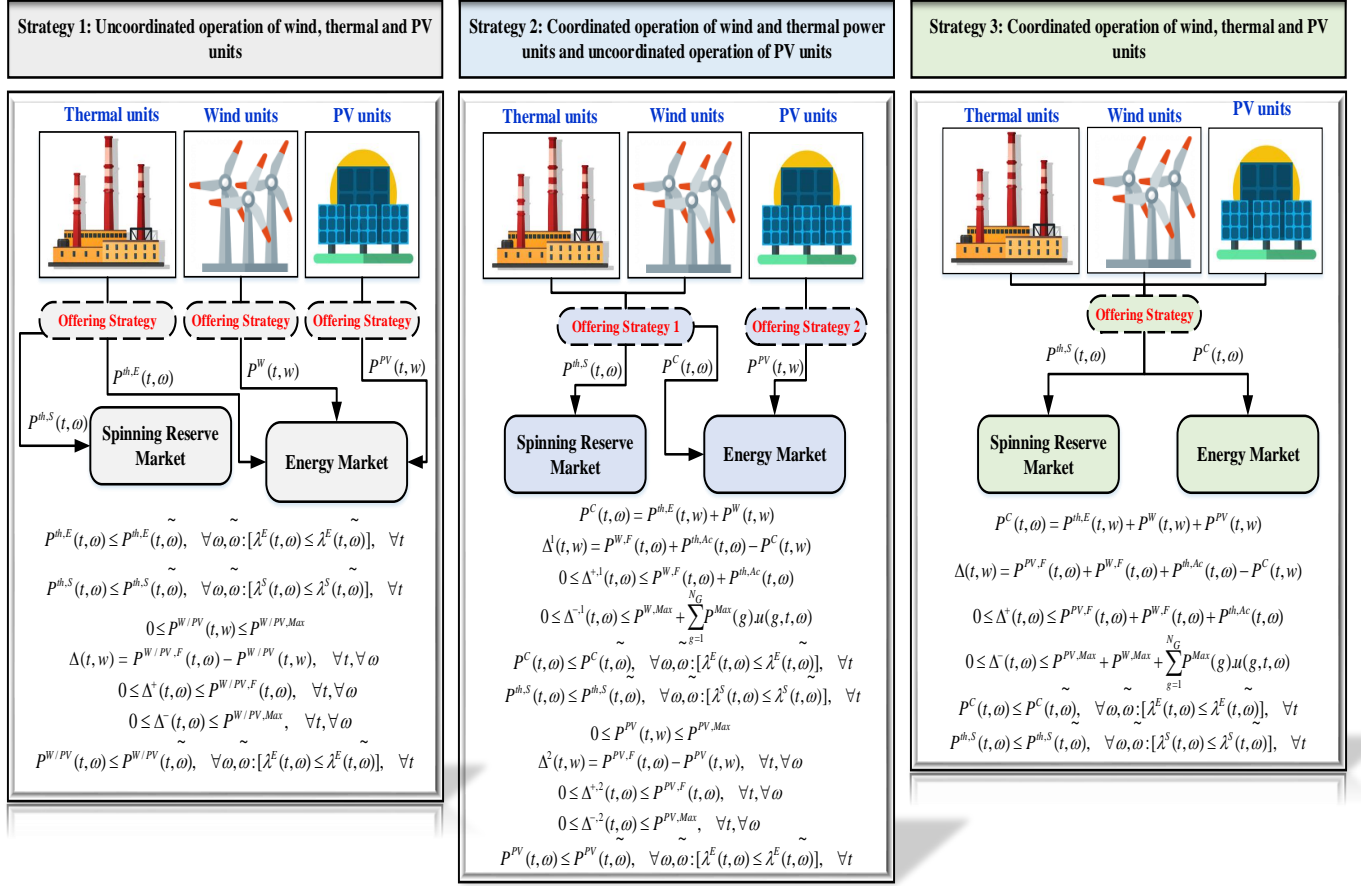


Figure 1: Schematic of different bidding strategies

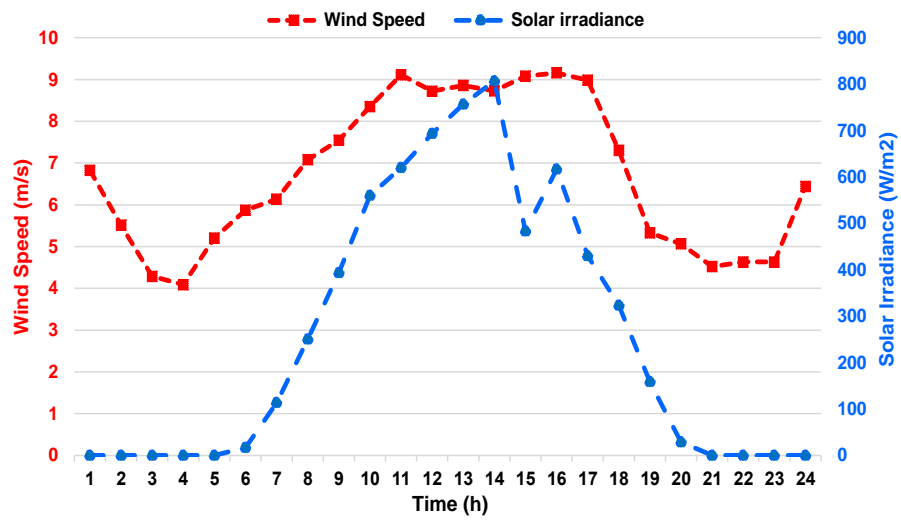
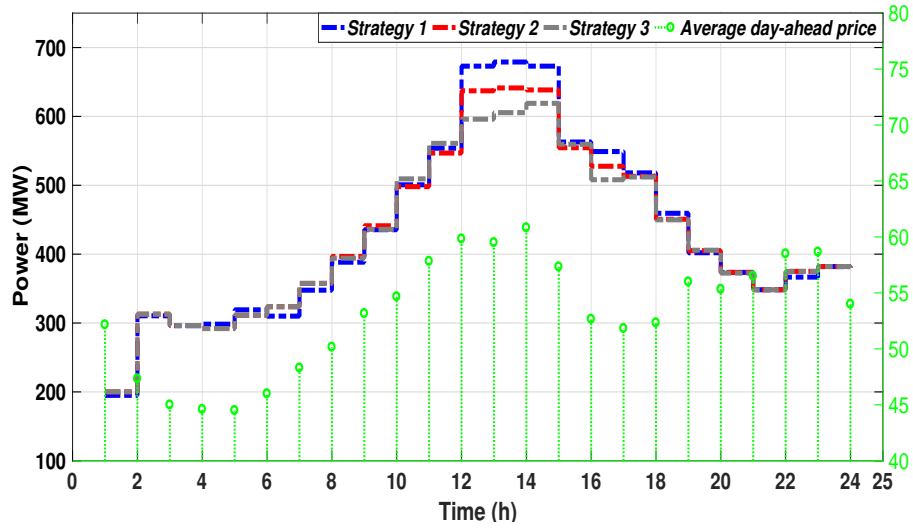
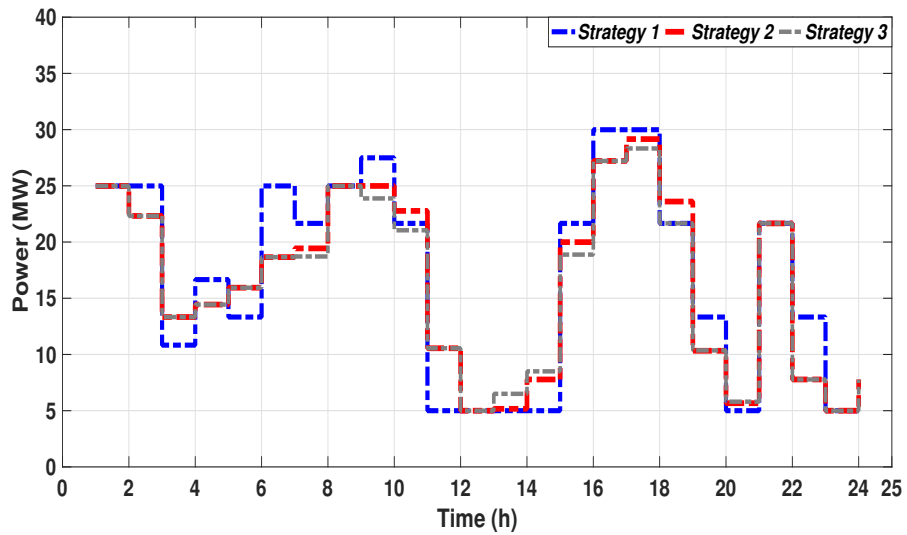


Figure 2: Expected values for hourly wind speed and solar irradiance



(a) Expected participation in the day-ahead energy market in different trading strategies



(b) Expected participation in the spinning reserve market in different trading strategies

Figure 3: Single objective bidding approach

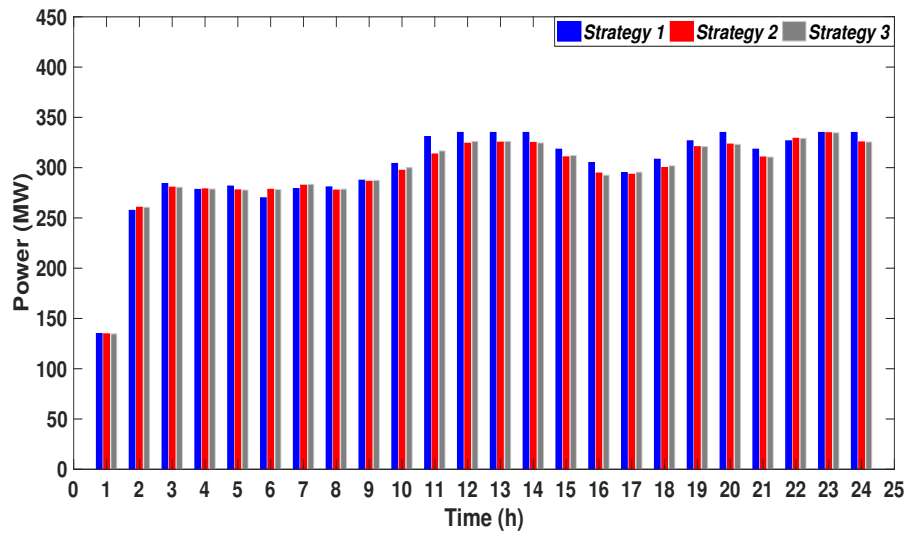
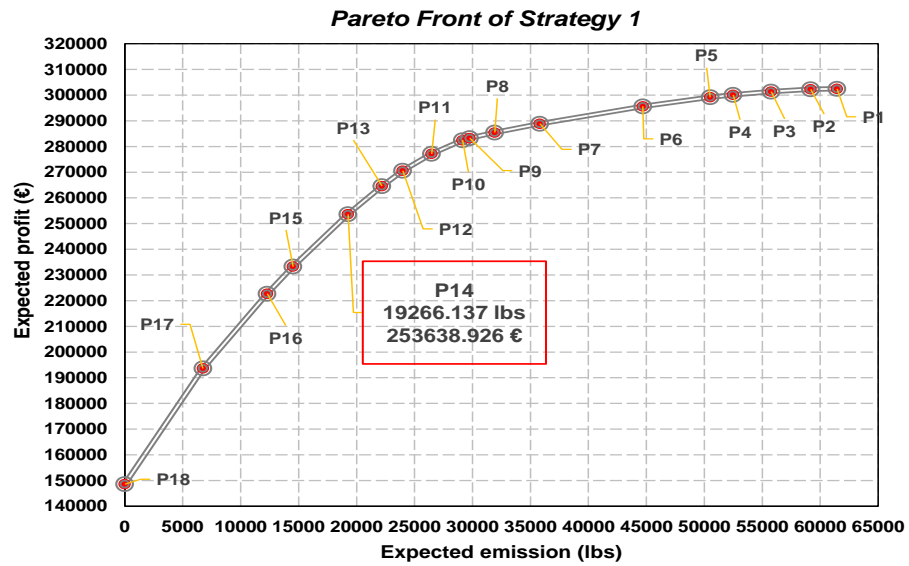
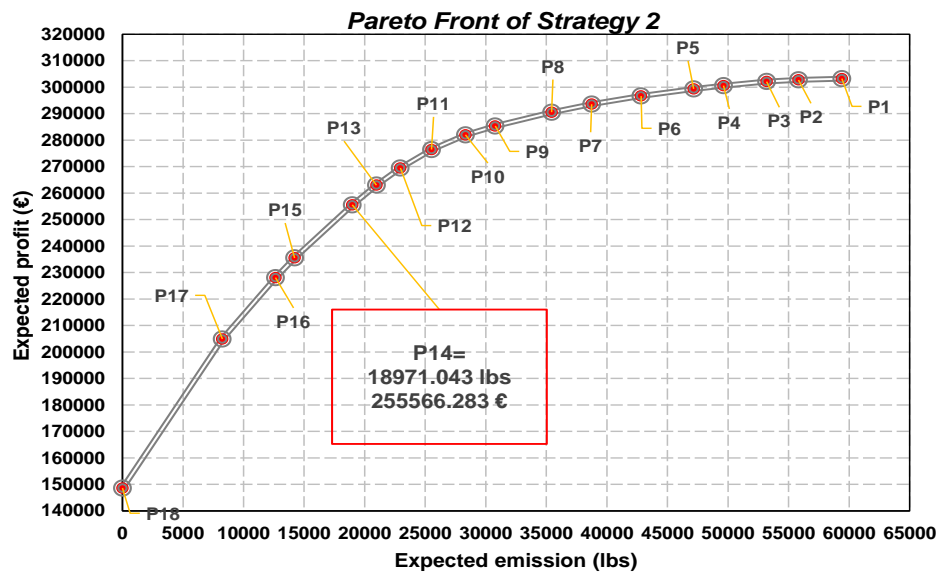


Figure 4: Comparison of expected amount of production bids of thermal units in the day-ahead energy market for all trading strategies (case study 1)



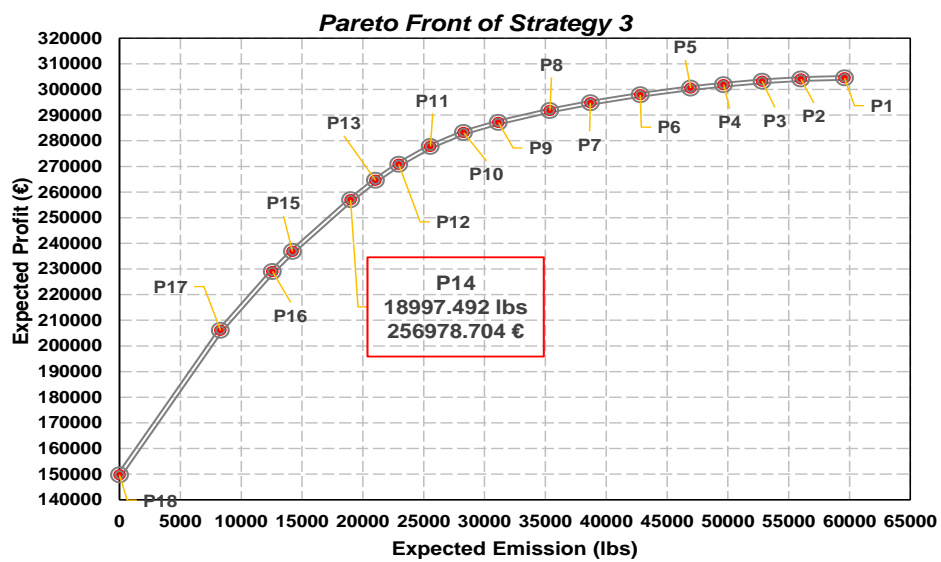
	<b>P1</b>	<b>P2</b>	<b>P3</b>	<b>P4</b>	<b>P5</b>	<b>P6</b>	<b>P7</b>	<b>P8</b>	<b>P9</b>
$F_{1,pu}$	1	0.9990	0.9929	0.9847	0.9787	0.9556	0.9117	0.8896	0.8754
$F_{2,pu}$	0	0.0370	0.0925	0.1459	0.1780	0.2726	0.4173	0.4805	0.5158
	<b>P10</b>	<b>P11</b>	<b>P12</b>	<b>P13</b>	<b>P14</b>	<b>P15</b>	<b>P16</b>	<b>P17</b>	<b>P18</b>
$F_{1,pu}$	0.8700	0.8356	0.7927	0.7541	0.6827	0.5503	0.4818	0.2927	0
$F_{2,pu}$	0.5257	0.5691	0.6097	0.6388	0.6865	0.7638	0.8001	0.8902	1

Figure 5: Pareto front for trading strategy 1



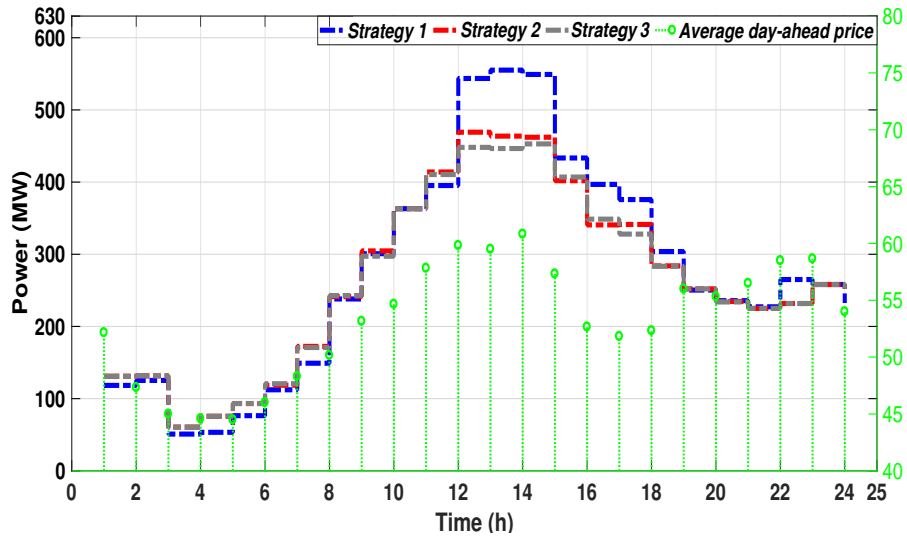
	P1	P2	P3	P4	P5	P6	P7	P8	P9
F <sub>1,pu</sub>	1	0.9968	0.9928	0.9831	0.9750	0.9575	0.9375	0.9180	0.8843
F <sub>2,pu</sub>	0	0.0603	0.1045	0.1645	0.2059	0.2791	0.3478	0.4034	0.4819
	P10	P11	P12	P13	P14	P15	P16	P17	P18
F <sub>1,pu</sub>	0.8626	0.8268	0.7817	0.7397	0.6917	0.5622	0.5139	0.3640	0
F <sub>2,pu</sub>	0.5231	0.5703	0.6138	0.6469	0.6806	0.7606	0.7872	0.8610	1

Figure 6: Pareto for trading strategy 2

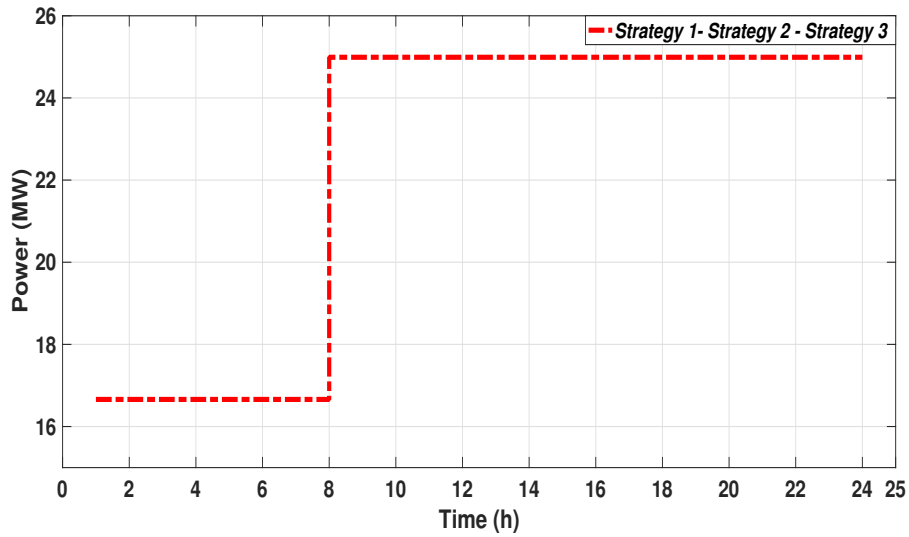


	<b>P1</b>	<b>P2</b>	<b>P3</b>	<b>P4</b>	<b>P5</b>	<b>P6</b>	<b>P7</b>	<b>P8</b>	<b>P9</b>
<b>F<sub>1,pu</sub></b>	1	0.9970	0.9914	0.9828	0.9742	0.9572	0.9372	0.9177	0.8874
<b>F<sub>2,pu</sub></b>	0	0.0600	0.1136	0.1667	0.2122	0.2816	0.3505	0.4063	0.4773
	<b>P10</b>	<b>P11</b>	<b>P12</b>	<b>P13</b>	<b>P14</b>	<b>P15</b>	<b>P16</b>	<b>P17</b>	<b>P18</b>
<b>F<sub>1,pu</sub></b>	0.8621	0.8272	0.7824	0.7418	0.6929	0.5627	0.5121	0.3637	0
<b>F<sub>2,pu</sub></b>	0.5253	0.5713	0.6148	0.6468	0.6811	0.7613	0.7891	0.8606	1

Figure 7: Pareto front for trading strategy 3



(a) Expected participation in the day-ahead energy market in different trading strategies



(b) Expected participation in the spinning reserve market in different trading strategies

Figure 8: Multi-objective bidding approach



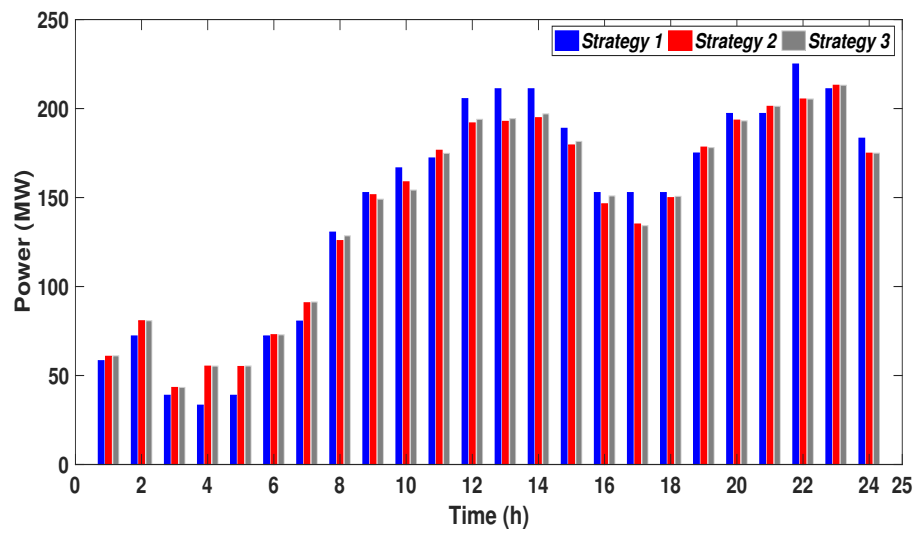
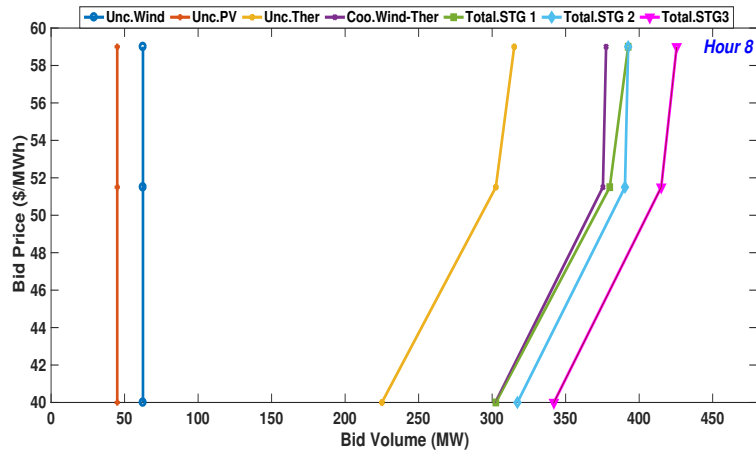
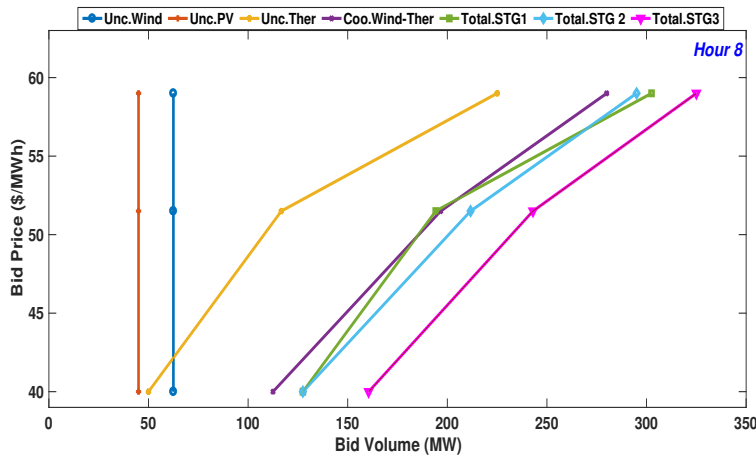


Figure 9: Comparison of expected amount of production bids of thermal units in the day-ahead energy market for all trading strategies (case study 2)

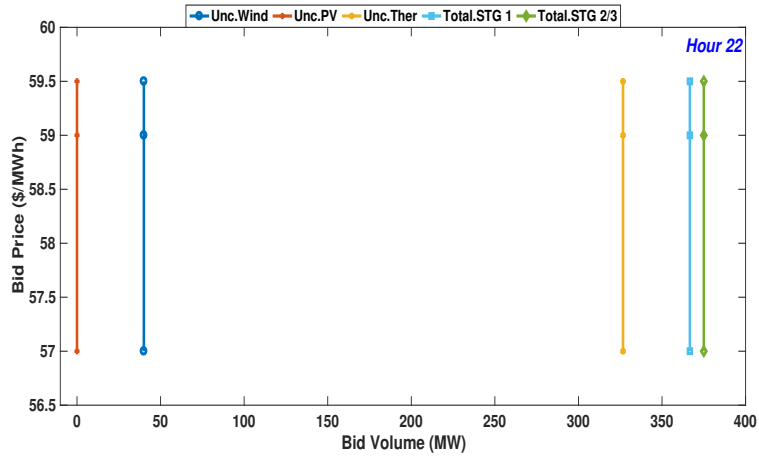


(a) Single objective bidding approach

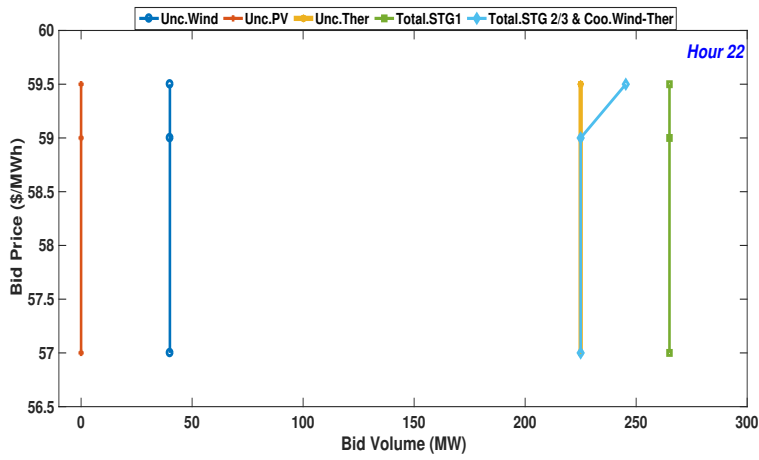


(b) Multi-objective bidding approach

Figure 10: Day-ahead energy market bidding for hour 8



(a) Single objective bidding approach



(b) Multi-objective bidding approach

Figure 11: Day-ahead energy market bidding for hour 22

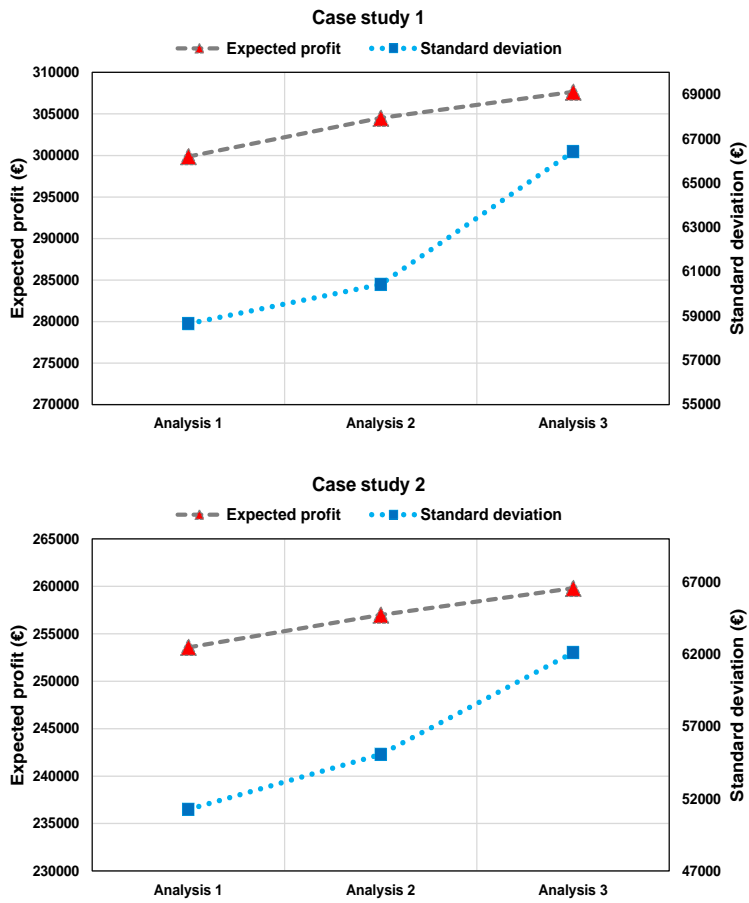


Figure 12: Comparison of expected profit and its standard deviation in various analyses

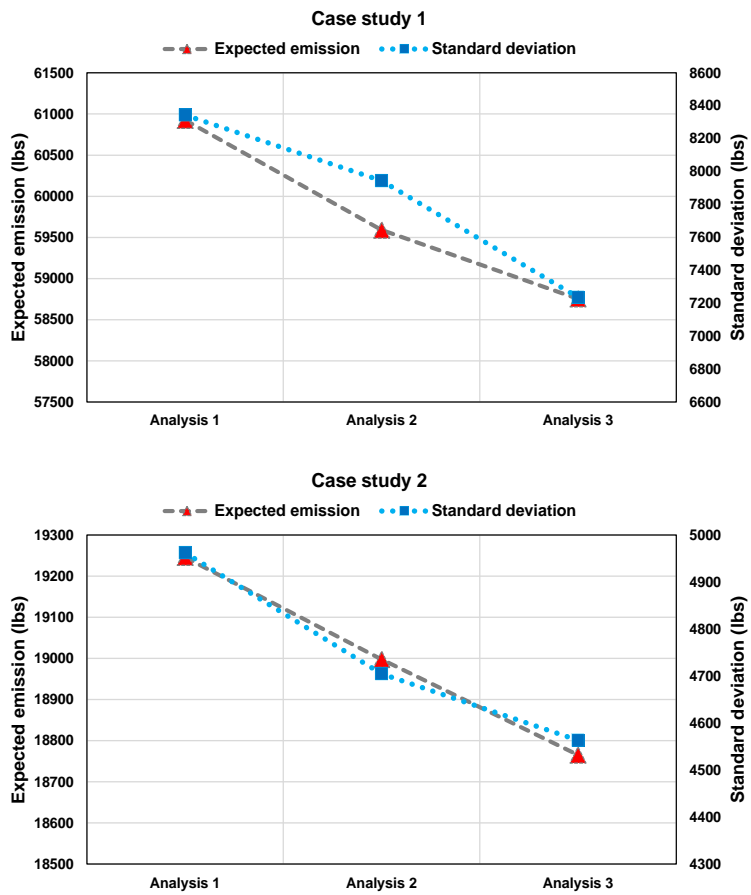


Figure 13: Comparison of expected emission and its standard deviation in various analyses

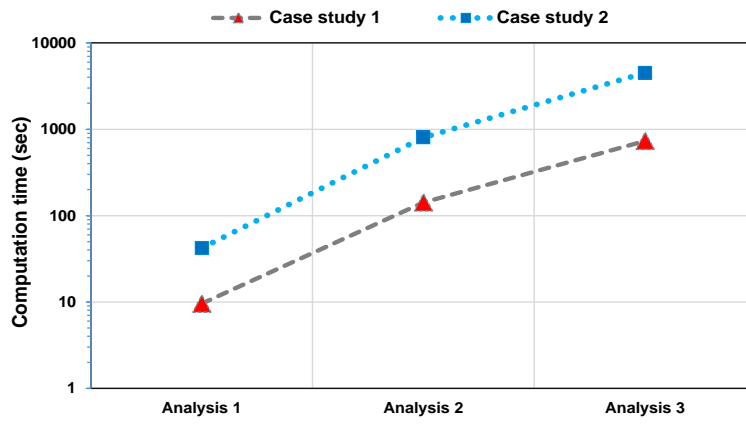
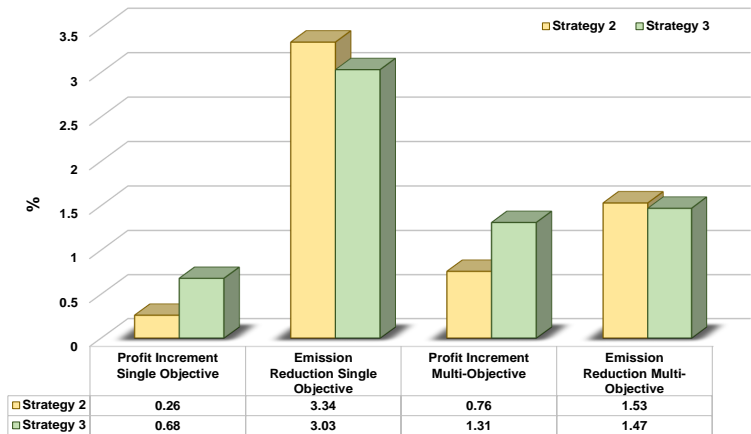
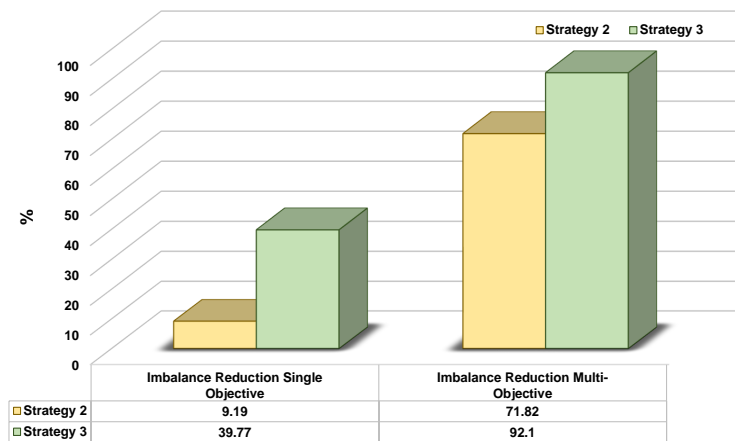


Figure 14: Comparison of computation time in various analyses

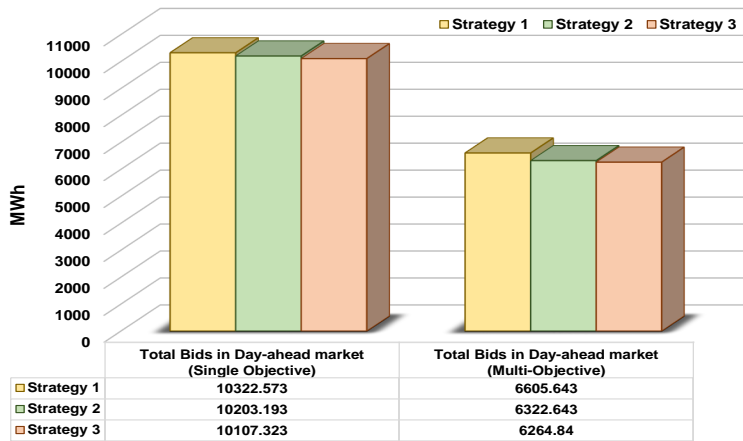


(a) Profit increment and emission reduction in both case studies

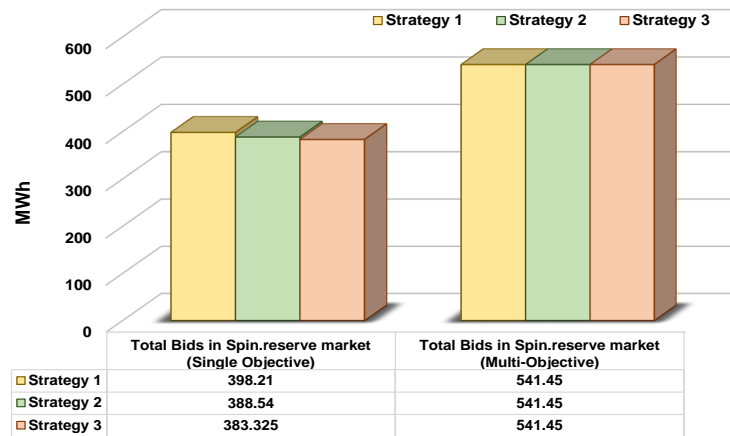


(b) Imbalance reduction in both case studies

Figure 15: Comparison of profit increment, emission and imbalance reductions in the second and third trading strategies



(a) Expected total bids in the day-ahead energy market for both case studies



(b) Expected total bids in the spinning reserve market for both case studies

Figure 16: Comparison of expected total day-ahead energy and spinning reserve bids in different trading strategies



Table 1: Taxonomy of the reviewed papers

Ref.	Combination of Various Energy Sources	Problem Type	Uncertain Parameters					Uncertainty Modeling	Objective Functions	Solution Methodology of MOP
			EM	SPRM	BM	REP	OS			
[7]	Large consumer	BS	✓	—	—	✓	—	✓	CSM	—
[8]	Large consumer	BS	✓	—	—	✓	—	✓	CSM	—
[9]	Microgrid	SS	✓	✓	—	✓	—	SP	CSM	—
[10]	Industrial Plant	SS	—	—	—	—	—	—	CSM	—
[11]	Thermal	SS	✓	✓	—	✓	—	PP	PFM	—
[12]	Large consumer	SS	—	—	—	—	—	—	CSM+ICM	WSM
[13]	VPP	SS	✓	✓	—	✓	—	SP	PFM	—
[14]	Wind-PSP	SS	—	—	—	✓	—	SP	PFM	—
[15]	Hydro-thermal	SS	✓	✓	—	—	—	SP	PFM	—
[16]	Wind-thermal	BS	✓	—	—	✓	—	SP	PFM	—
[17]	Wind-thermal	SS	—	—	✓	—	—	—	PFM	—
[18]	Wind-thermal	BS	✓	—	—	✓	—	SP	PFM	—
[19]	Wind-thermal-PSP	BS	✓	—	✓	✓	—	SP	PFM	—
[20]	Microgrid	SS	—	—	✓	—	—	—	CSM+EMM	EPM
[21]	Hydro-thermal	SS	—	—	—	—	—	—	PFM+EMM	EPM
[22]	Hydro-thermal-PSP	EED	—	—	—	—	—	SP	CSM+EM	NBIM
<b>This paper</b>	<b>Wind-thermal-PV</b>	<b>BS</b>	✓	✓	✓	✓	—	<b>SP</b>	<b>PFM+EMM</b>	<b>WSM+FSA</b>

Note : EM-Energy market; SPRM-Spinning reserve market; BM-Balancing market; REP-Renewable production; OS-Other sources;

MOP-Multi-objective programming; PSP-Pumped storage Plant; VPP-Virtual Power Plant;

MG-Microgrid; PV-Photovoltaic; BS-Bidding strategy; SS-Self-Scheduling; EED-Economic emission dispatch; SP-Stochastic programming;

RO-Robust optimization; PP-Probabilistic possibilistic; PFM-Profit maximization; CSM-Cost minimization;

EMM-Emission minimization; ICM-Investment cost minimization;WSM-Weighted sum method;

WSM+FSA-Weighted sum method+Fuzzy satisfying approach; EPM-Epsilon Constraint method; NBIM-Normal boundary intersection method

Table 2: Thermal units information

Thermal Units	Cost coefficients of generator			$P_{min}$ (MW)	$P_{max}$ (MW)
	$a_g(\text{€}/\text{MW}^2\text{h})$	$b_g(\text{€}/\text{MWh})$	$c_g(\text{€}/\text{h})$		
G1	0.0144	31.400	40.260	0	50
G2	0.0339	43.022	85.509	5	45
G3	0.0339	42.022	82.342	5	45
G4	0.0330	28.090	42.760	25	100
G5	0.0248	26.504	49.140	25	100

Table 3: Technical specification of thermal units

Thermal units	RDR(g) (MW/hr)	RUR(g) (MW/hr)	STDRL(g) (MW/hr)	STURL(g) (MW/hr)	STUC(g) (€)
G1	50	50	30	20	0
G2	15	15	20	15	88
G3	15	15	20	15	88
G4	50	50	60	50	110
G5	50	50	60	50	110

Table 4: Emission coefficients of thermal units

Thermal units	Coefficient of SO <sub>2</sub> emission function			Coefficient of NO <sub>x</sub> emission function		
	$\alpha_g$ (lbs/MW <sup>2</sup> )	$\beta_g$ (lbs/MW)	$\gamma_g$ (lbs)	$\alpha_g$ (lbs/MW <sup>2</sup> )	$\beta_g$ (lbs/MW)	$\gamma_g$ (lbs)
G1	0.0249	3.554	1.866	0.0087	1.345	3.716
G2	0.0167	12.259	4.470	0.0073	5.945	5.298
G3	0.0167	11.259	4.470	0.0073	5.945	5.298
G4	0.0157	2.762	2.262	0.0095	0.820	4.653
G5	0.0157	2.762	2.262	0.0095	0.820	4.653

Table 5: Information on wind turbines and PV site

Parameter	Value	unit	Parameter	Value	unit
$v_{ci}$	3	m/s	$\eta^{PV}$	15	%
$v_r$	15	m/s	$S^{PV}$	$10^6$	$m^2$
$v_{co}$	25	m/s	$P_{rated}^{PV}$	150	MW
$P_{rated}^W$	250	MW	-	-	-

Table 6: Results of single objective bidding strategy in various trading strategies

Trading strategy	Expected profit (€)	Expected emission (lbs)	Imbalance cost (€)
Wind uncoordinated	94868.919	—	16995.914
PV uncoordinated	53734.278	—	8373.622
Thermal uncoordinated	153831.439	61455.848	—
Sum uncoordinated wind and thermal	248700.358	61455.848	16955.914
Coordinated wind and thermal	249486.914	59401.666	14663.655
Sum uncoordinated wind, PV and thermal (Strategy 1)	302434.636	61455.848	25369.536
Sum uncoordinated PV and coordinated wind-thermal (Strategy 2)	303221.192	59401.666	23037.277
Coordinated wind, PV and Thermal (Strategy 3)	304509.778	59590.001	15278.357

Table 7: Results of Multi-objective bidding strategy in various trading strategies

Trading strategy	Expected profit (€)	Expected emission (lbs)	Imbalance cost (€)
Wind uncoordinated	94868.919	—	16995.914
PV uncoordinated	53734.278	—	8373.622
Thermal uncoordinated	105035.729	19266.137	—
Sum uncoordinated wind and thermal	199904.648	19266.137	16955.914
Coordinated wind and thermal	201832.005	18971.043	-1225.947
Sum uncoordinated wind, PV and thermal (Strategy 1)	253638.926	19266.137	25369.536
Sum uncoordinated PV and coordinated wind-thermal (Strategy 2)	255566.283	18971.043	7147.675
Coordinated wind, PV and Thermal (Strategy 3)	256978.704	18997.492	2003.541

Table 8: Results of emission quota arbitraging for Pareto optimal solutions of strategy 3

Total Emission (lbs)	Profit without emission trade (€)	Emission trades (lbs)	Net profits (€)			
			$\lambda^{EM}=0.1$ (€/lbs)	$\lambda^{EM}=0.3$ (€/lbs)	$\lambda^{EM}=0.5$ (€/lbs)	$\lambda^{EM}=1$ (€/lbs)
59590.001	304509.778	-39590.001	<b>300550.778</b>	292632.778	284714.778	264919.777
56009.132	304058.522	-36009.132	300457.608	293255.782	286053.956	268049.390
52814.999	303192.137	-32814.990	299910.637	<b>293347.637</b>	286784.638	270377.147
49652.657	301854.928	-29652.657	298889.662	292959.131	287028.600	272202.271
46939.804	300526.825	-26939.804	297832.845	292444.884	<b>287056.923</b>	273587.021
42807.933	297896.198	-22807.933	295615.405	291053.818	286492.232	275088.265
38700.833	294798.142	-18700.833	292928.059	289187.892	285447.726	276097.309
35374.524	291777.572	-15374.524	290240.120	287165.215	284090.310	<b>276403.048</b>
31145.031	287088.975	-11145.031	285974.472	283745.466	281516.460	275943.944
28286.335	283176.988	-8286.335	282348.355	280691.088	279033.821	274890.653
25544.215	277774.429	-5544.215	277220.008	276111.165	275002.322	272230.214
22952.056	270843.444	-2952.056	270548.238	269957.827	269367.416	267891.388
21044.007	264561.387	-1044.007	264456.986	264248.185	264039.384	263517.380
18997.492	256978.704	1002.508	257078.955	257279.456	257479.958	257981.212
14221.486	236828.236	5778.514	237406.087	238561.790	239717.493	242757.218
12567.015	229008.445	7432.985	229751.744	231238.341	232724.938	236441.430
8303.996	206041.240	11696.004	207210.840	209550.041	211889.242	217737.244
0	149735.991	20000.000	151735.991	155735.991	159735.991	169735.991