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A Zeno-Free Event-Triggered Secondary Control for AC Microgrids

Babak Abdolmaleki, Qobad Shafiee, Senior Member, IEEE, Ali Reza Seifi, Mohammad Mehdi Arefi, Senior Member, IEEE, and Frede Blaabjerg, Fellow, IEEE

Abstract—This paper proposes a secondary voltage, frequency, and active power sharing control for autonomous inverter-based microgrids with event-triggered communications. A proportional-integral consensus-based control scheme is introduced which benefits from need-based (event-triggered) data exchange among distributed generators. The employed event-triggering condition i) ensures the system stability, ii) ensures that the system is Zeno-free and there exists a controllable minimal inter-event time, iii) removes the redundant communications during both transient and steady-state stages, iv) accounts for directed communication network architectures, and v) is fully distributed from both design and implementation standpoints. Effectiveness of the proposed controller for various case studies is verified via MATLAB/Simulink-based simulations. Comparison between different cases and conventional strategies are also included.

Index Terms—Consensus algorithm, event-triggered control, frequency control, microgrid, power sharing, secondary control, voltage control, Zeno behavior.

Nomenclature

ith distributed generator's (DG's) phase angle.
i th DG's measured active & reactive powers.
i th DG's actual active & reactive powers.
i th DG's rated active & reactive powers.
i th DG's output frequency & voltage.
Rated frequency & voltage.
Reference frequency & voltage.
Power measurement filter's cutoff frequency.
Droop coefficients.
Frequency & voltage correction terms.
Conductance & susceptance among DGs $i \& j$.
<i>i</i> th DG's shunt conductance & susceptance.
Maximum frequency & voltage deviations.
Nonnegative proportional gains.
Nonnegative integral gains.
Logical indicators.
Communication weighting from j^{th} DG to i^{th} DG.

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a_i, a_i°	i" DG's in-degree & out-degree in the CN.
$\mathcal{A}, \mathcal{D}, \mathcal{L}$	CN's matrices. Refer to Section II-A.
$t_{k_i}^i$	k_i^{th} triggering instant associated with i^{th} DG.
t_i, t_0^i	i th DG's local clock and activation instant.
$\tilde{\Omega}_i, \tilde{V}_i$	The latest sampled signals of Ω_i , V_i at $t_{k_i}^i$.
au	Minimal inter-event (inter-communication) time.
σ	Positive parameter governing the state-dependent
	part of the triggering conditions in (8).
$\gamma_{\Omega}, \gamma_{V}$	Positive parameters governing the constant parts
	of the triggering conditions in (8).
$1_n,0_n$	Vectors of ones and zeros in \mathbb{R}^n .
\mathcal{I}_n	Identity matrix in $\mathbb{R}^{n \times n}$.

ith DC's in dogree & out dogree in the CN

I. Introduction

SECONDARY CONTROL of islanded microgrids (MGs) compensates for voltage and frequency deviations caused by droop control as well as provides proper power sharing between distributed generators (DGs) [1]. This control level is realized by using a communication network (CN). Therefore, distributed control architectures using sparse CNs, are preferred to the centralzied ones with complex CNs [2].

Most of the previous works in the context of secondary control are conducted based on the continuous CNs (e.g. see [3]-[14]), while the realistic data exchange infrastructures are sample-based and have limited bandwidths [15], [16]. Thus, from a system scaling standpoint, efficient usage of communication medium is mandatory. In networked control systems, a solution to avoid probable network congestions and reduce the communication burden is to use event-triggered (ET) control strategies eliminating redundant communications [17], [18]. Generally, ET control is a strategy under which the desired state is sampled and broadcasted, and the control rule is updated (i.e., an event is triggered), only if some condition(s) is(are) satisfied. Any ET condition must satisfy two system requirements: Stability and Zeno-freeness. Zeno behavior is a phenomenon under which excessive redundant events are triggered over a finite time interval. Because of limited communication and computational capabilities, no control system can be implemented on a digital platform, if the behavior exists [17], [18].

Triggered control of MGs has been introduced in the literature [19]–[28]. Reference [19], proposes a self-triggered coordinated power control scheme for ac MGs where the next event time is determined at any current event time. Thus, the controller cannot respond quickly to the disturbances. A distributed ET load sharing control is proposed in [20]. In this work, an average-consensus algorithm is used to control the inter-DG active power

sharing by controlling their output currents. A distributed ET reactive power sharing control is proposed in [21]. Similarly, a current sharing controller for dc MGs is proposed in [22]. In both of these works, consensus algorithms with nonlinear state feedback are presented, providing proper reactive power sharing and proper current sharing respectively. To address the voltage regulation in converter-based dc MGs, the work in [22] is extended in [23]. In [24], an event-based consensus control is introduced to achieve proper active power sharing among a cluster of ac and dc MGs. In this work, each interlinking converter is considered as an agent which utilizes this event-based controller to share the active powers properly between the MGs. ET secondary control of dc MGs is investigated in [25]. In this work, a full-state feedback ET controller is designed which also uses full-state observation to detect the event times. None of the above works accounts for ET secondary voltage and frequency control of MGs. These problems have been addressed in [26]-[28]. A distributed ET secondary voltage and frequency control is proposed in [26]. The proposed ET conditions in this work, however, do not reduce the communication burden significantly and even may result in Zeno behavior, though the theoretical Zeno exclusion analysis is provided (see [17, Sec. III-A] for more info). In [27], [28], some secondary controllers with ET communications are proposed where the working frequency of the digital communication platform (infrastructure) is not considered. In fact, therein it is assumed that the inter-event time intervals can get any positive value and there is no specific lower bound restriction on the intervals. Moreover, the work in [26], similar to [3]–[11], is based on leader-following consensus algorithm [29] of frequency, i.e., the frequency is treated as a communication data. However, in power systems, frequency is a global entity and hence a frequency-consensus control seems to be redundant. Furthermore, the secondary compensation terms are usually generated by using a pure integrator which leads to a poor transient response, e.g., see [3]-[11], [26]-[28].

Motivated by the above statements and literature, this paper deals with event-triggering of communications, in secondary voltage and frequency control of MGs. Salient features of the proposed control scheme are as follows.

C1: A proportional-integral-based (PI-based) secondary control is proposed based on consensus algorithm. Unlike [19]–[25], [27], the voltage, frequency, and active power sharing control tasks are considered simultaneously. Moreover, different from [3]–[11], [26] the only communication data in frequency-power control are frequency correction terms.

C2: A triggering condition is proposed which *i*) ensures that the system is Zeno-free with inter-event time intervals greater than a *desired time constant*, *ii*) is fully distributed from both design and implementation standpoints providing scalablity and plug-and-play capability, *iii*) benefits from a constant threshold, reducing the communications more effectively, especially in steady state, and *iv*) accounts for directed CNs.

C3: A systematic stability analysis with ultimate uniform boundedness approach is provided. The impacts of design parameters on system's performance and communication pattern are studied as well. Moreover, the results are compared with those under some other existing strategies.

The rest of this paper is structured as follows. Section II pro-

vides the MG's modeling. The proposed controller is designed in Section III. Simulation results for different cases are included in Section IV. Finally, Section V concludes the paper.

II. SYSTEM MODELING

A. Communication Network (CN) Layer

The CN of a MG can be regarded as a directed graph with the DGs and the communication links playing the roles of its nodes and edges, respectively. Consider the graph $\mathcal{G}\subseteq (\mathcal{N},\mathcal{E},\mathcal{A})$, where, $\mathcal{N}=\{1,...,n\},\ \mathcal{E}\subseteq \mathcal{N}\times \mathcal{N},\$ and $\mathcal{A}=[a_{ij}]\in \mathbb{R}^{n\times n}$ are its node set, edge set, and adjacency matrix, respectively. If node i obtains data from node j, then node j is an in-neighbor of node i, node i is an out-neighbor of node j, $(j,i)\in \mathcal{E},\$ and $a_{ij}=1;$ otherwise, nodes j and i are not neighbors, $(j,i)\notin \mathcal{E},\$ and $a_{ij}=0.$ Let $N_i=\{j\mid (j,i)\in \mathcal{E}\},\ N_i^o=\{j\mid (i,j)\in \mathcal{E}\},\ d_i=\sum_{j\in N_i}a_{ij},\$ and $d_i^o=\sum_{j\in N_i^o}a_{ji}$ be the in-neighbor set, out-neighbor set, in-degree, and out-degree of node i, respectively. Laplacian matrix of \mathcal{G} is $\mathcal{L}=\mathcal{D}-\mathcal{A},\$ where, $\mathcal{D}=diag\{d_i\}$ (proper diagonal matrix). A path from node j to node j is a sequence of pairs, belong to $\mathcal{E},\$ expressed as $\{(j,n_1),...,(n_m,i)\}.$ A graph has a spanning tree, if there exists a node (called root node) from which there exists a path to any other node within the graph [29], [30].

B. Physical and Control Layers

From Fig. 1, each DG comprises a voltage sourced inverter, a LC filter, inner current and voltage controllers, power measurement filters, and a droop-control unit. Details on the design of these parts are provided in [31], [32]. The inner controllers are normally designed such that the subsystem comprising them, the inverter, and LC filter has a high bandwidth but the average power measurement filters are very slow. Therefore, neglecting the dynamics of the mentioned subsystem, one can consider each DG as a droop-controlled voltage source which is connected to the rest of the MG through a connector. The state model of *i*th DG can then be expressed as [33]

$$\dot{\delta}_i = 2\pi f_i,\tag{1a}$$

$$\dot{P}_i = 2\pi f_c(\hat{P}_i - P_i),\tag{1b}$$

$$\dot{Q}_i = 2\pi f_c(\hat{Q}_i - Q_i),\tag{1c}$$

$$f_i = f_{nom} + \Omega_i - m_i P_i, \tag{1d}$$

$$V_i = V_{nom} + \Gamma_i - n_i Q_i. \tag{1e}$$

In a Kron-reduced electric network model [33], \hat{P}_i & \hat{Q}_i are as

$$\hat{P}_i = G_i V_i^2 + \sum_j V_i V_j G_{ij} \cos(\delta_i - \delta_j) + \sum_j V_i V_j B_{ij} \sin(\delta_i - \delta_j),$$
(2a)

$$\hat{Q}_i = -B_i V_i^2 - \sum_j V_i V_j B_{ij} \cos(\delta_i - \delta_j) + \sum_j V_i V_j G_{ij} \sin(\delta_i - \delta_j),$$
(2b)

where,
$$G_i = G_{ii} + \sum_j G_{ij}$$
, $B_i = B_{ii} + \sum_j B_{ij}$.

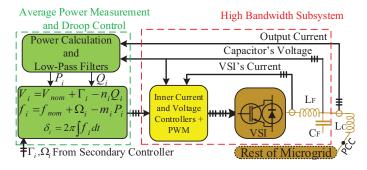


Fig. 1. Physical and control layers of i^{th} distributed generation unit (DG).

III. SECONDARY CONTROL DESIGN

The aim is to shift the droop characteristics along the voltage and frequency axes, so that in steady state one has

$$[V_i, f_i, m_i P_i]^T \to [V_{ref}, f_{ref}, m_j P_j]^T, \quad \forall i, j. \tag{3}$$

This aim ensures proportional active power sharing between the DGs, if one selects $m_i = \overline{\Delta f}/P_i^*$ and $n_i = \overline{\Delta V}/Q_i^*$ [32].

Remark 1: Because of line impedance effect, accurate voltage regulation leads to poor reactive power sharing and vice versa [13]. Therefore, following the research line composed of the works in [3]–[11], [26], this paper focuses on the voltage regulation task, and reactive power responses are omitted for brevity. In addition, the ET reactive power controller provided in [21] can be modified slightly, to cover the directed CNs.

A. Event-Triggered PI-based Secondary Control

Once the DGs talk to each other via the CN described in Section II-A, the aim in (3) can be achieved by using a consensus-based secondary control [4]–[11], [29]. In this way, the following proportional-integral-based (PI-based) correction terms are proposed for $i^{\rm th}$ DG.

$$\Omega_{i} = K_{i}^{f} (b_{i}^{f} \Delta f_{i} + b_{i}^{\Omega} \tilde{z}_{i}^{\Omega}) + I_{i}^{f} \int (b_{i}^{f} \Delta f_{i} + b_{i}^{\Omega} \tilde{z}_{i}^{\Omega}) dt, (4a)$$

$$\Gamma_{i} = n_{i} \int \dot{Q}_{i} dt + K_{i}^{V} \left(b_{i}^{V} \Delta V_{i} + (1 - b_{i}^{V}) \tilde{z}_{i}^{V} \right)$$

$$+ I_{i}^{V} \int \left(b_{i}^{V} \Delta V_{i} + (1 - b_{i}^{V}) \tilde{z}_{i}^{V} \right) dt, (4b)$$

$$\Delta f_i = f_{ref} - f_i, \ \ \tilde{z}_i^{\Omega} = \left(\frac{1}{d_i} \sum\nolimits_j a_{ij} \tilde{\Omega}_j \right) - \tilde{\Omega}_i, \eqno(5a)$$

$$\Delta V_i = V_{ref} - V_i, \ \tilde{z}_i^V = \left(\frac{1}{d_i} \sum_{j} a_{ij} \tilde{V}_j\right) - \tilde{V}_i,$$
 (5b)

where, if the DG has direct access to f_{ref} (resp. V_{ref}), then $b_i^f=1$ (resp. $b_i^V=1$), otherwise $b_i^f=0$ (resp. $b_i^V=0$); if the DG cooperates with its in-neighbors $b_i^\Omega=1$, otherwise $b_i^\Omega=0$. The local parts in (4) employ the continuous local signals f_i , V_i , and \dot{Q}_i , while the neighborhood errors $\tilde{z}_i^f, \tilde{z}_i^V$ use the latest sampled communication data as follows.

$$\begin{cases} \tilde{\Omega}_i(t) = \Omega_i(t_{k_i}^i), \\ \tilde{V}_i(t) = V_i(t_{k_i}^i), \end{cases} \quad t \in [t_{k_i}^i, t_{k_i+1}^i), \ k_i = 0, 1, \cdots.$$
 (6)

The triggering instant $t_{k_i}^i$ is when the signals V_i and Ω_i are sampled and transmitted to the out-neighbors. Please, note that

over $[t_{k_i}^i, t_{k_i+1}^i)$ the signals $\tilde{\Omega}_i$ and \tilde{V}_i remain constant, while the neighbors' latest received data, i.e., $\tilde{\Omega}_j$ and \tilde{V}_j , $\forall j$ may vary.

Remark 2: The data exchange among the DGs is normally realized by using a wireless/wired CN with time-triggered signal transmission strategy. In this strategy, a high frequency periodic data sampling and communication should be adopted to implement the controller in (4) such that the time interval between any two consecutive triggering instants are equal to a sampling time τ_s , i.e., $t_{k_i+1}^i - t_{k_i}^i = \tau_s, \forall i, k$.

Although the periodic transmission strategy provides a good performance, it leads to many redundant data exchanges, especially in steady state, when the control goal is achieved and not so many communications are required. Thus, an ET control under which every DG decides on its own to sample and transmit data to CN *only when it is needed* seems effective.

Question: Now, the question is that, when are the right triggering instants $t_{k_i}^i$, $k_i = 0, 1, \cdots$ —the instants when, each DG decides on its own to sample its local data Ω_i and V_i , and to broadcast these samples—?

Answer: The appropriate triggering instants should be designed such that, i) performance of the system undergoes a little degradation while using $\tilde{\Omega}_i$ & \tilde{V}_i instead of Ω_i & V_i in (5), and ii) the intervals between consecutive triggering instants have a lower bound τ which is the digital communication platform's (infrastructure's) capability (working frequency).

One way is to control the deviations of the continuous signals Ω_i, V_i from their latest sampled quantities $\tilde{\Omega}_i, \tilde{V}_i$, i.e., $e_i^\Omega = \tilde{\Omega}_i - \Omega_i$ and $e_i^V = \tilde{V}_i - V_i$. To this end, one should compare $|e_i^\Omega|$ and $|e_i^V|$ with some thresholds, every τ seconds. The employed thresholds should comprise a state-dependent part and a constant part [17]. The state-dependent part governs the triggering pattern over transients and usually converges to zero in steady state. Hence, to avoid trigger chattering in steady state, the constant part is included [17]. Accordingly, the following triggering instant is proposed for i^{th} DG.

$$t_{k_i+1}^i = \inf\{t_i > t_{k_i}^i + \tau : (8a) \text{ or } (8b)\},$$
 (7)

where,
$$|e_i^{\Omega}| > \sigma b_i^{\Omega} |\tilde{z}_i^{\Omega}| + \gamma_{\Omega},$$
 (8a)

$$|e_i^V| > \sigma(1 - b_i^V)|\tilde{z}_i^V| + \gamma_V, \tag{8b}$$

where, $\tilde{z}_i^{\Omega} = \frac{1}{d_i} \sum a_{ij} (\tilde{\Omega}_j - \tilde{\Omega}_i)$, $\tilde{z}_i^V = \frac{1}{d_i} \sum a_{ij} (\tilde{V}_j - \tilde{V}_i)$ are the local neighborhood errors; inf denotes the infimum sign. The proposed ET controller is explained in Algorithm 1.

Remark 3: In (7), the triggering conditions in (8) are checked every τ seconds (not continuously); therefore, in addition to the communication burden, the computational burden is accordingly reduced. Moreover, if τ be selected greater than or equal to the communication medium's working sampling time, one can ensure that Zeno phenomenon (sampling chattering) is canceled out. Note that b_i^{Ω} and b_i^{V} indicate whether i^{th} DG cooperates with its in-neighbors or not. Therefore, they are included to make (8a) and (8b) adaptive to this issue.

B. Design Guidelines and Requirements

In what follows, based on the upcoming theoretical analyses in Appendix A, the readers are provided with some design hints.

Algorithm 1 The proposed event-triggering algorithm. initialization: 1: Sample $\tilde{\Omega}_i \leftarrow \Omega_i$, $\tilde{V}_i \leftarrow V_i$, and $\tilde{t}_i \leftarrow t_i$ 2: Store the samples in the Data Store Unit (DSU) 3: Send Ω_i and V_i to out-neighbors 4: Compute Ω_i and Γ_i in (4a) and (4b) while secondary control is active do Compute $e_i^{\tilde{\Omega}} = \tilde{\Omega}_i - \Omega_i$, $e_i^V = \tilde{V}_i - V_i$, and $t_i - \tilde{t}_i$ 6: Alert the data receiver 7: if $\{t_i - \tilde{t}_i > \tau\}$ &{(8a) or (8b) holds} then \triangleright Trigger 8: 9: Do lines 1 to 3 of the algorithm 10: end if for all $j \in N_i$ do 11: if new data received then 12: Data receive Update and store Ω_i and V_i 13: 14: end if

** t_i (resp. \tilde{t}_i) is local clock (resp. latest triggering instant) of i^{th} DG.

Compute Ω_i and Γ_i in (4a) and (4b)

end for

17: end while

15:

16:

Stability: For stable operation, i) the matrix \mathbf{A} in (11) must be Hurwitz; ii) each DG must have more in-neighbors than outneighbors, i.e., $d_i > d_i^o$, $\forall i$ (cf. Section II-A); iii) $\sigma < 0.5$, and $\tau < \min(\tau_0^\Omega, \tau_0^V)$ (cf. (22)).

Desired equilibrium: To achieve the aim in (3) the inter-DG CN must has a spanning tree rooted at a DG with $b_i^f, b_i^V \neq 0$. **Control gains:** One should choose the non-negative gains such that the stability requirements are satisfied.

Event-triggering parameters: The triggering conditions contain the 4 parameters τ , γ_{Ω} , γ_{V} , and σ_{Ω} . According to (22), τ can get a wide range of values for stable operation of system. However, the stability may not be enough solely; hence, one should choose τ according to the first part of Appendix A-E. From (26) and (27) one can see that γ_{Ω} and γ_{V} determine steady-state frequency and voltage errors, respectively. Therefore, considering $2\gamma_{\Omega}$ and $2\gamma_{V}$ as the maximum neighborhood errors one should choose proper gammas. Finally, looking at second part of Appendix A-E one should select σ as large as possible, for instance $\sigma=0.49$.

IV. CASE STUDIES

To verify the effectiveness of the proposed controller, an islanded 220-V, 50-Hz three-phase 5-bus MG with four DGs is simulated in MATLAB/Simulink environment. Each DG has the dynamics in (1) which feeds its local bus through the connector Z_C . Each feeder line is modeled with a lumped series RL impedance Z_L . The loads are modeled by constant impedance loads. Single-line diagram of the test MG is depicted in Fig. 2 where the electrical and control requirements of different parts are also given. Note that $\overline{\Delta f} = 0.25\text{-Hz}$ and $\overline{\Delta V} = 11\text{-V}$.

A. Performance Assessment: Activation and Load Changes

In this case, the directed CN depicted in Fig. 2, is used for inter-DG communications. The parameters in (8)-(12) are as follows: $\tau^{-1} = 25$ -Hz, $K_i^V = K_i^f = 5$, $I_i^V = I_i^f = 10$,

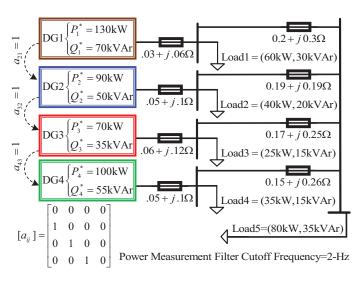


Fig. 2. Test microgrid system; specifications of different parts are also given.

 $\mathbf{b}_f = \mathbf{b}_V = [1, 0, 0, 0]^T, \ \mathbf{b}_{\Omega} = [0, 1, 1, 1]^T, \ \sigma = 0.49,$ $\gamma_{\Omega} = 0.001/2$, and $\gamma_{V} = 0.05/2$. Fig. 3 indicates the performance of the controller over different stages. Prior to the proposed controller's activation at t = 4s, the MG is controlled by droop control. At t = 8s, load 5 increases by 33% of total load. Load 5 decreases to its initial value, at t = 12s. Fig. 3(a)-(c) indicate that for t < 3s the DGs' voltages and frequencies are deviated from the nominal values, and the active powers are shared properly. Activation of the secondary controller at t = 4s restores the voltages and frequencies to the reference values of 220-V and 50-Hz while guarantees proportional active power sharing between the DGs. It is shown that after load changes at t = 8s and t = 12s, the voltages and frequencies are restored back to the reference values, and proportional active power sharing still remains. Fig. 3(d) depicts the triggering (communication) instants for all the DGs. It is indicated that i) the communication burden is highly reduced, ii most of the communications are triggered during the transient stages, and iii) the inter-event time intervals are always greater than τ , i.e., Zeno behavior does not appear.

B. Impacts of Communication Delay and Feedback Gains

Fig. 4 shows the controller performance for the case in Section IV-A, but with $K_i^V = K_i^f = 10$, $I_i^V = I_i^f = 20$ and communication delays of 0 and 160 milliseconds. Comparing Fig. 3(a)-(c) and Fig. 4(a)-(c), it is obvious that, the more feedback gain, the more synchronization speed, and the better transient response. Comparing Fig. 4(a)-(c) and Fig. 4(d)-(f), one can see that the communication delay slows down the synchronization speed and results in some transient oscillations. However, the desired control aim can be reached properly, for a practical range of delays (in the order of tens of milliseconds).

C. Plug-and-Play Capability and Link Failure Investigation

In this case, all the parameters defined in the preamble of Section IV-A are employed again. To preserve connectivity of the CN in Fig. 2, a link is established from DG 1 to DG 4.

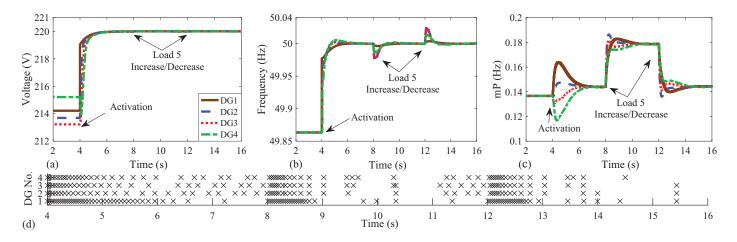


Fig. 3. Performance of the proposed controller; (a) voltages, (b) frequencies, (c) $m_i P_i s$, and (d) communication (triggering) instants.

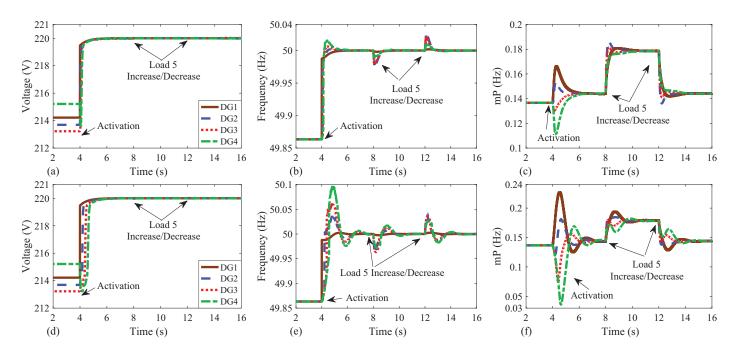


Fig. 4. Performance of the controller with doubled gains under delay of (a)-(c) 0s and (d)-(f) 0.16s; (a)&(d) voltages, (b)&(e) frequencies, and (c)&(f) $m_i P_i s$.

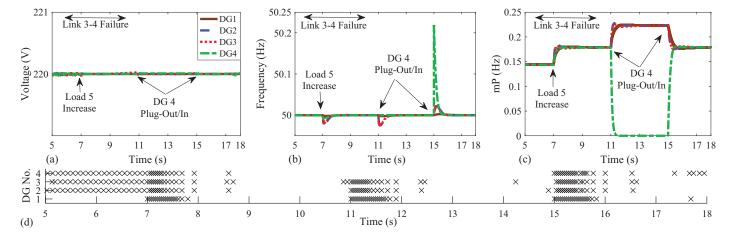


Fig. 5. Link 3-4 failure and plug-and-play capability with 4th DG; (a) voltages, (b) frequencies, and (c) $m_i P_i s$.

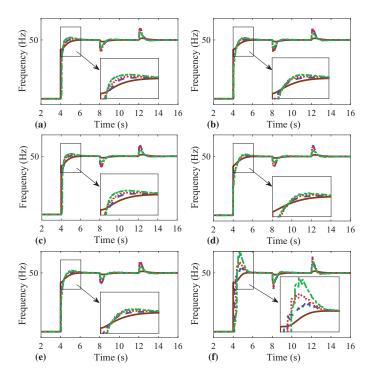


Fig. 6. Impact of different parameters on the frequency responses. (a) $\sigma=0,$ $\tau=1/25,$ $\gamma_V,$ $\gamma_\Omega=0,$ (b) $\sigma=0.49,$ $\tau=1/25,$ $\gamma_V,$ $\gamma_\Omega=0,$ (c) $\sigma=0,$ $\tau=1/25,$ $\gamma_V,$ $\gamma_\Omega\neq0,$ (d) $\sigma=0.49,$ $\tau=0,$ $\gamma_V,$ $\gamma_\Omega\neq0,$ (e) $\sigma=0.49,$ $\tau=1/25,$ $\gamma_V,$ $\gamma_\Omega\neq0,$ and (f) $\sigma=0.49,$ $\tau=1/8,$ $\gamma_V,$ $\gamma_\Omega\neq0.$

From t=6s to t=10s the link between DGs 3 and 4 is interrupted. The circuit breaker CB is intentionally opened at t=11s, and $4^{\rm th}$ DG becomes disconnected (its communication links are also interrupted) until t=15s when the DG joins the secondary controlled MG again. Note that prior to t=15s a synchronization process is started, CB is closed, and the communication links associated with $4^{\rm th}$ DG are all recovered. Fig. 5 depicts the performance of the proposed controller for this scenario. Fig. 5(a)-(c) indicate that i) the controller is resilient to the link failure, ii) once $4^{\rm th}$ DG leaves the MG, other DGs increase their supplied active powers proportional to their ratings and regulate their voltages and frequencies, and iii) as soon as $4^{\rm th}$ DG connects back to the MG, immediately participates in proportional active power sharing, as well as, voltage and frequency regulation.

D. Impacts of Different Parameters

In order to illustrate how different parameters affect the controller performance and the communication burden, the frequency responses and the number of communications for the scenario in Section IV-A ($t \in [4s,16s]$) are recorded and the results for different cases are given in Fig. 6 and Fig. 7. Note that the cases are defined in the caption of Fig. 6. Comparing the cases (a), (b), (c), and (e) one can see that σ and $\gamma_{\Omega}, \gamma_{V}$ dramatically reduces the communication burden, while some similar satisfactory performances and frequency responses can be achieved; however, γ_{Ω} and γ_{V} are more effective than σ . Comparing the cases (d), (e), and (f) one can see that τ reduces the number of communications more effectively while

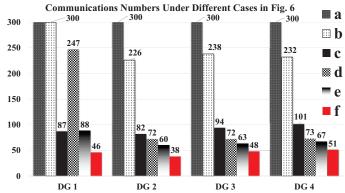


Fig. 7. The number of communications associated with the cases in Fig. 6.

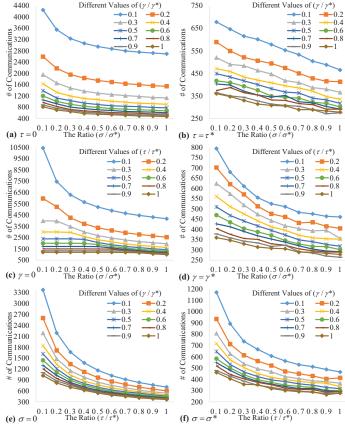


Fig. 8. Parametric graph for total number of communications versus different parameters where $\sigma^*=0.49,\, \tau^*=0.04,\, \gamma_\Omega^*=0.001/2,\, {\rm and}\,\, \gamma_V^*=0.05/2.$

it ensures that the inter-event times are controllable lower-bounded. In addition, from Fig. 6, i) the system performance and frequency response under different parameters is reasonable, and ii) τ affects the system response similar to a communication delay, inducing transient overshoot and oscillations. To further investigate the parameters' impacts on the communications, the scenario in Section IV-A is re-simulated 600 times for different parameters, and the DGs' total number of communications is figured in Fig. 8. Note that i) the parameters are varied with steps of 0.1 of the star-signed values in Fig. 8's caption, and ii) the parameters γ_{Ω} , γ_{V} are changed together and are simply represented by γ . Generally speaking, all the parameters

TABLE I
COMPARISON OF THIS PAPER WITH PREVIOUS WORKS

	ET Condition Thresholds			Control Settings	
Ref.	State-	Commetant	Time-	PI-	Frequency
	Dependent	Constant	Dependent	Based	Consensus
[26]	✓	×	×	×	✓
[27]	✓	✓	×	×	×
[28]	✓	✓	×	×	×
This Paper	✓	✓	✓	✓	x

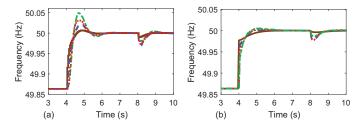


Fig. 9. Freuency responses under (a) the integrator-based frequency-consnesus controller, and (b) the PI-based frequency-consensus-less controller in this paper.

contribute to communication reduction, however, there are some interesting impacts that should be pointed out. According to Fig. 8(a)-(b), increase of γ_{Ω} and γ_{V} alleviates the impact of σ on the communication frequency which validates the analyses in the second part of Appendix A-E. Similarly, the increase of τ alleviates the impact of σ . Because, according to the first part of Appendix A-E, in the presence of larger τ the measurement errors grow more, such that after τ seconds they violate the thresholds in (8) more likely; hence, for small values of σ and large values of τ the communications are governed by τ , predominantly. Under periodic time-triggered communications, the number of communications is proportional to the frequency $\frac{1}{\tau}$. However, by incorporating γ_{Ω} and γ_{V} into the triggering condition, the communications become aperiodic and behave different from the function $\frac{1}{\tau}$. This issue is shown in Fig. 8(e)-(f), where the $\frac{1}{\tau}$ behavior is alleviated as $\frac{\gamma}{\gamma^*}$ increases.

E. Comparison with the Existing Methods

In Table I, the proposed methodology in this paper is compared with the ET controllers in [26]–[28] in terms of triggering

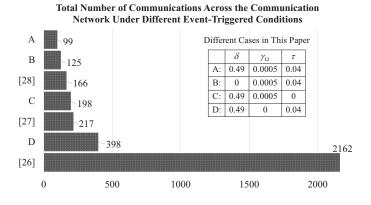


Fig. 10. Comparison between different ET conditions in terms of communication burden across the communication network over $t \in [8s, 16s]$.

conditions and control settings. The controller in this paper compared to those in [26]–[28] is PI-based; in addition, it does not employ frequency leader-following consensus which seems to be redundant in power systems where the frequency reaches agreement per se. Therefore, different from [26] (and also the works in [3]–[11]) and similar to [27], [28], only *one* data does flow between the DGs in frequency-active power control task. Moreover, the employed thresholds in ET condition (7) have state-dependent, constant, and time-dependent parts *at the same time*, resulting in *i*) less communications in both transient and steady-state stages, and *ii*) controllable desired lower bound for inter-event times.

In order to highlight the superior performance of the PI-based frequency-consensus-free controller, the frequency response associated with the scenario in Section IV-A (activation and first load change) under the proposed controller is compared with that under the integrator-based leader-following-based controllers. Fig. 9, indicates that the proposed controller demonstrates better transient response.

On the other hand, to compare the mentioned works in terms of communication burden and ET conditions efficiency, the case study in Section IV-A is re-simulated for each one, and the total number of all the DGs' communications over $t \in [8s, 16s]$ is figured in Fig. 10. It should be noted that to make a fair comparison it is assumed that i) all the DGs can access the frequency reference directly, i.e., $b_i^f=1, \forall i, \ \emph{ii})$ since some references do not consider voltage control, the DGs voltages are engaged with the V-Q droop control, i.e., $\Gamma_i=0, \forall i$, and iii) an undirected ring-structured version of the CN in Fig. 2 is established among the DGs, i.e., $b_i^{\Omega} = 1, a_{ij} = a_{ji}, \forall i, j$. From Fig. 10, one can see how the proposed ET condition with all the state-dpendent, constant, and time-dependent parts, i.e., case A, needs effectively lower data exchange than those needed by the other methods and cases. Moreover, according to the results of the cases A and B, one can see that the success of the proposed triggering instant in reducing the communication burden, owes to the use of τ and γ . It is also shown that even without the constant part, i.e., case D, the proposed condition is more effective than the one in [26]. The reason is that unlike the proposed condition in (7)-(8), the condition in [26] is checked continuously, resulting in a huge number of communications. Under the case C, the ET condition is also checked continuously; however, similar to [27], [28] the condition has a constant part threshold and hence the results in this case are settled in between the results of [27], [28].

V. CONCLUSION

In this paper, the amount of inter-DG communications in secondary control of ac MGs, is highly reduced. Herein, some proportional-integral-based correction terms are introduced wich utilizes an ET data exchange strategy. In this method, some triggering conditions, reducing the communications in both transient and steady-state stages, are employed for directed CNs which ensures that the inter-event time intervals are controllable, lower bounded. Stability and mathematical analyses are also provided. PnP capability of the DGs and the effects of design parameters are clarified, by mathematical analysis and

simulation results. In addition, the results are compared with those of the conventional methods.

APPENDIX A MATHEMATICAL ANALYSES

Lemma: Let \mathcal{L} be a graph's Laplacian matrix $d_i \geq d_i^o$, one then has $\mathcal{L}\mathbf{1}_n = \mathbf{0}_n$ and $\mathbf{x}^T \mathcal{L}\mathbf{x} \geq \frac{1}{2} \sum_i \sum_{j \in N_i} a_{ij} (x_i - x_j)^2$, where $\mathbf{x} = [x_1, \dots, x_n]^T \in \mathbb{R}^n$.

Proof of lemma: According to the definition of Laplacian matrix (i.e., $d_i = \sum_{j \in N_i} a_{ij}$), \mathcal{L} has a zero eigenvalue, with $\mathbf{1}_n$ being its corresponding right eigenvector; hence, $\mathcal{L}\mathbf{1}_n = \mathbf{0}_n$. Moreover, one can expand $\mathbf{x}^T \mathcal{L}\mathbf{x}$ and its transpose $\mathbf{x}^T \mathcal{L}^T \mathbf{x}$ as

$$\mathbf{x}^T \mathcal{L} \mathbf{x} = \sum_i (d_i x_i^2 - \sum_{j \in N_i} a_{ij} x_i x_j),$$

$$\mathbf{x}^T \mathcal{L}^T \mathbf{x} = \sum_i (d_i x_i^2 - \sum_{j \in N_i} a_{ji} x_i x_j).$$

Now, considering $r_i=d_i-d_i^o$, $d_i=\sum_{j\in N_i}a_{ij}$, and $d_i^o=\sum_{j\in N_i}a_{ji}$, one can rewrite the above equations as

$$\mathbf{x}^T \mathcal{L} \mathbf{x} = \sum_i \sum_{j \in N_i} (a_{ij} x_i^2 - a_{ij} x_i x_j),$$

$$\mathbf{x}^T \mathcal{L}^T \mathbf{x} = \sum_i \sum_{j \in N_i} (a_{ij} x_j^2 - a_{ij} x_i x_j) + \sum_i r_i x_i^2.$$

Therefore, since $\mathbf{x}^T \mathcal{L} \mathbf{x} = \frac{1}{2} (\mathbf{x}^T \mathcal{L} \mathbf{x} + \mathbf{x}^T \mathcal{L}^T \mathbf{x})$, one can write

$$\mathbf{x}^T \mathcal{L}\mathbf{x} = \frac{1}{2} \sum_{i} \sum_{j \in N_i} a_{ij} (x_i - x_j)^2 + \frac{1}{2} \sum_{i} r_i x_i^2.$$

Hence, if $r_i \geq 0$, then $\mathbf{x}^T \mathcal{L} \mathbf{x} \geq \frac{1}{2} \sum_i \sum_{j \in N_i} a_{ij} (x_i - x_j)^2$.

A. Secondary Controlled Microgrid System Model

Let $\mathbf{V} = \operatorname{col}\{V_i\}$, $\tilde{\mathbf{V}} = \operatorname{col}\{\tilde{V}_i\}$, $\boldsymbol{\delta} = \operatorname{col}\{\delta_i\}$, $\boldsymbol{\Omega} = \operatorname{col}\{\Omega_i\}$, $\tilde{\boldsymbol{\Omega}} = \operatorname{col}\{\hat{P}_i\}$, and $\mathbf{P} = \operatorname{col}\{P_i\}$ be the state column vectors. One can then write (1), (4), and (5) as

$$\mathbf{V} = \mathbf{K}_{V} \left(\mathbf{b}_{V} (V_{ref} \mathbf{1}_{n} - \mathbf{V}) - (\mathcal{I}_{n} - \mathbf{b}_{V}) \mathcal{D}^{-1} \mathcal{L} \tilde{\mathbf{V}} \right)$$

$$+ \mathbf{I}_{V} \int \left(\mathbf{b}_{V} (V_{ref} \mathbf{1}_{n} - \mathbf{V}) - (\mathcal{I}_{n} - \mathbf{b}_{V}) \mathcal{D}^{-1} \mathcal{L} \tilde{\mathbf{V}} \right) dt,$$

$$+ \mathbf{n} \int \dot{\mathbf{Q}} dt - \mathbf{n} \mathbf{Q} + V_{nom} \mathbf{1}_{n},$$

$$\mathbf{\Omega} = \mathbf{K}_{f} \left(\mathbf{b}_{f} (\Delta f^{*} \mathbf{1}_{n} + \mathbf{m} \mathbf{P} - \mathbf{\Omega}) - \mathbf{b}_{\Omega} \mathcal{D}^{-1} \mathcal{L} \tilde{\mathbf{\Omega}} \right)$$

$$+ \mathbf{I}_{f} \int \left(\mathbf{b}_{f} (\Delta f^{*} \mathbf{1}_{n} + \mathbf{m} \mathbf{P} - \mathbf{\Omega}) - \mathbf{b}_{\Omega} \mathcal{D}^{-1} \mathcal{L} \tilde{\mathbf{\Omega}} \right) dt,$$

$$\dot{\mathbf{P}} = -2\pi f_{c} \mathbf{P} + 2\pi f_{c} \hat{\mathbf{P}},$$

$$(9c)$$

$$\dot{\delta} = 2\pi f_{nom} \mathbf{1}_n + 2\pi \mathbf{\Omega} - 2\pi \mathbf{mP}, \tag{9d}$$

where, $\mathbf{K}_V = \operatorname{diag}\{K_i^V\}$, $\mathbf{K}_f = \operatorname{diag}\{K_i^f\}$, $\mathbf{I}_V = \operatorname{diag}\{I_i^V\}$, $\mathbf{I}_f = \operatorname{diag}\{I_i^f\}$, $\mathbf{b}_V = \operatorname{diag}\{b_i^V\}$, $\mathbf{b}_f = \operatorname{diag}\{b_i^f\}$, $\mathbf{b}_\Omega = \operatorname{diag}\{b_i^\Omega\}$ are diagonal matrices; $\Delta f^* = f_{ref} - f_{nom}$. From (2a), $\hat{\mathbf{P}} = \hat{\mathbf{P}}(\mathbf{V}, \boldsymbol{\delta})$ is a function of \mathbf{V} , $\boldsymbol{\delta}$ with a Taylor expansion around $\mathbf{x}_b = (V_{ref}\mathbf{1}_n, \mathbf{0}_n)$ as

$$\hat{\mathbf{P}} = \mathbf{G}\mathbf{V} + \mathbf{L}\boldsymbol{\delta} - \hat{\mathbf{P}}(\mathbf{x}_h) + \hat{\mathbf{P}}_{h,o,t},\tag{10}$$

where, $\hat{\mathbf{P}}_{h.o.t}$ stands for high-order terms; \mathbf{L} denotes an electrical Laplacian matrix with the adjacency matrix $[V_{ref}^2 B_{ij}]$; \mathbf{G} is a conductance matrix with $V_{ref}(2G_i + \sum_j G_{ij})$ and $V_{ref}G_{ij}$ being its diagonal and off-diagonal entries, respectively.

Remark 4: According to the proposed triggering instant (7) described in Algorithm 1, after every triggering instant each DG postpones checking (8a) and (8b) for τ seconds which can be regarded as a sampling-induced time delay. Therefore, in addition to the impacts of the conditions in (8) over the interval $[t_{k_i}^i + \tau, t_{k_i+1}^i)$, the effects of this sampling delay should be investigated. Next, each case is discussed separately.

B. Event-Triggering Conditions Analysis

Considering $\mathbf{e}_V = \tilde{\mathbf{V}} - \mathbf{V}$ and $\mathbf{e}_{\Omega} = \tilde{\mathbf{\Omega}} - \mathbf{\Omega}$ and substituting (10) into (9), one can write the system state model as

$$\dot{\mathbf{x}} = \mathbf{A}\mathbf{x} + \mathbf{u}, \text{ where, } \mathbf{u} = \mathbf{C}\mathbf{e} + \mathbf{w}, \tag{11}$$

$$\text{and, } \mathbf{e} = \begin{bmatrix} \mathbf{e}_{V} \\ \mathbf{e}_{\Omega} \end{bmatrix}, \begin{cases} \mathbf{x} = [\mathbf{V}^{T} \boldsymbol{\delta}^{T} \mathbf{\Omega}^{T} \mathbf{P}^{T}]^{T}, \\ \mathbf{w} = [\mathbf{w}_{V}^{T} \mathbf{w}_{\delta}^{T} \mathbf{w}_{\Omega}^{T} \mathbf{w}_{P}^{T}]^{T}, \end{cases}$$

$$\mathbf{A} = \begin{bmatrix} \mathbf{A}_{V} & \mathbf{0}_{n} & \mathbf{0}_{n} & \mathbf{0}_{n} \\ \mathbf{0}_{n} & \mathbf{0}_{n} & \mathbf{A}_{\delta\Omega} & \mathbf{A}_{\delta P} \\ \mathbf{A}_{\Omega V} & \mathbf{A}_{\Omega\delta} & \mathbf{A}_{\Omega} & \mathbf{A}_{\Omega P} \\ \mathbf{A}_{PV} & \mathbf{A}_{P\delta} & \mathbf{0}_{n} & \mathbf{A}_{P} \end{cases}, \mathbf{C} = \begin{bmatrix} \mathbf{C}_{V} & \mathbf{0}_{n} \\ \mathbf{0}_{n} & \mathbf{0}_{n} \\ \mathbf{0}_{n} & \mathbf{C}_{\Omega} \\ \mathbf{0}_{n} & \mathbf{0}_{n} \end{bmatrix};$$

$$\mathbf{M}_{V} = \mathcal{I}_{n} + \mathbf{K}_{V} \mathbf{b}_{V} + \mathbf{K}_{V} (\mathcal{I}_{n} - \mathbf{b}_{V}) \mathcal{D}^{-1} \mathcal{L}$$

$$\mathbf{M}_{\Omega} = \mathcal{I}_{n} + \mathbf{K}_{f} \mathbf{b}_{f} + \mathbf{K}_{f} \mathbf{b}_{\Omega} \mathcal{D}^{-1} \mathcal{L}$$

$$\mathbf{A}_{V} = -\mathbf{M}_{V}^{-1} \mathbf{I}_{V} (\mathbf{b}_{V} + (\mathcal{I}_{n} - \mathbf{b}_{V}) \mathcal{D}^{-1} \mathcal{L}),$$

$$\mathbf{A}_{\Omega} = -\mathbf{M}_{\Omega}^{-1} \mathbf{I}_{f} (\mathbf{b}_{f} + \mathbf{b}_{\Omega} \mathcal{D}^{-1} \mathcal{L}), \quad \mathbf{A}_{P} = -2\pi f_{c} \mathcal{I}_{n},$$

$$\mathbf{A}_{\Omega \delta} = 2\pi f_{c} \mathbf{M}_{\Omega}^{-1} \mathbf{K}_{f} \mathbf{b}_{f} \mathbf{m} \mathbf{L}, \quad \mathbf{A}_{P \delta} = 2\pi f_{c} \mathbf{L}, \quad \mathbf{A}_{\delta \Omega} = 2\pi \mathcal{I}_{n},$$

$$\mathbf{A}_{\Omega V} = 2\pi f_{c} \mathbf{M}_{\Omega}^{-1} \mathbf{K}_{f} \mathbf{b}_{f} \mathbf{m} \mathbf{G}, \quad \mathbf{A}_{P V} = 2\pi f_{c} \mathbf{G},$$

$$\mathbf{A}_{\Omega P} = -\mathbf{M}_{\Omega}^{-1} (2\pi f_{c} \mathbf{K}_{f} \mathbf{b}_{f} - \mathbf{I}_{f} \mathbf{b}_{f}) \mathbf{m}, \quad \mathbf{A}_{\delta P} = -2\pi \mathbf{m},$$

$$\mathbf{C}_{V} = \mathbf{M}_{V}^{-1} \mathbf{I}_{V} (\mathbf{b}_{V} - \mathcal{I}_{n}) \mathcal{D}^{-1} \mathcal{L}, \quad \mathbf{C}_{\Omega} = -\mathbf{M}_{\Omega}^{-1} \mathbf{I}_{f} \mathbf{b}_{\Omega} \mathcal{D}^{-1} \mathcal{L},$$

$$\mathbf{w}_{V} = \mathbf{M}_{V}^{-1} (V_{ref} \mathbf{I}_{V} \mathbf{b}_{V} \mathbf{1}_{n} - \mathbf{K}_{V} (\mathcal{I}_{n} - \mathbf{b}_{V}) \mathcal{D}^{-1} \mathcal{L} \dot{\mathbf{e}}_{V}),$$

$$\mathbf{w}_{\Omega} = \mathbf{M}_{\Omega}^{-1} (\Delta f^{*} \mathbf{I}_{f} \mathbf{b}_{f} \mathbf{1}_{n} + \mathbf{K}_{f} \mathbf{b}_{f} \mathbf{m} \mathbf{w}_{P} - \mathbf{K}_{f} \mathbf{b}_{\Omega} \mathcal{D}^{-1} \mathcal{L} \dot{\mathbf{e}}_{\Omega}),$$

$$\mathbf{w}_{P} = 2\pi f_{c} (\hat{\mathbf{P}}_{h,o,t} - \hat{\mathbf{P}} (\mathbf{x}_{b})), \quad \mathbf{w}_{\delta} = 2\pi f_{nom} \mathbf{1}_{n}, \tag{12}$$

Note that A, x, and w respectively are the state matrix, state vector, and disturbance vector with the components in (12).

Under the conditions in (8) one always has $|e_i^V| < \sigma |\tilde{z}_i^V| + \gamma_V$ and $|e_i^{\Omega}| < \sigma |\tilde{z}_i^{\Omega}| + \gamma_{\Omega}$; therefore

$$|\mathbf{e}_V| \le \sigma |\mathcal{D}^{-1} \mathcal{L}(\mathbf{V} + \mathbf{e}_V)| + \gamma_V \mathbf{1}_n,$$
 (13a)

$$|\mathbf{e}_{\Omega}| \le \sigma |\mathcal{D}^{-1} \mathcal{L}(\mathbf{\Omega} + \mathbf{e}_{\Omega})| + \gamma_{\Omega} \mathbf{1}_{n},$$
 (13b)

where, $|\cdot|$ denotes the entry-wise absolute value matrix/vector i.e., $|\mathfrak{M}| = [|\mathfrak{m}_{ij}|], \forall \mathfrak{M} = [\mathfrak{m}_{ij}]$. By using the widely-known triangle inequality one can bound (13) as

$$|\mathbf{e}_V| \le \sigma |\mathcal{D}^{-1}\mathcal{L}||\mathbf{V}| + \sigma |\mathcal{D}^{-1}\mathcal{L}||\mathbf{e}_V| + \gamma_V \mathbf{1}_n.$$
 (14a)

$$|\mathbf{e}_{\Omega}| \le \sigma |\mathcal{D}^{-1}\mathcal{L}||\mathbf{\Omega}| + \sigma |\mathcal{D}^{-1}\mathcal{L}||\mathbf{e}_{\Omega}| + \gamma_{\Omega}\mathbf{1}_{n},$$
 (14b)

Consider the matrix $\mathcal{M} = \mathbf{I}_n - \sigma | \mathcal{D}^{-1} \mathcal{L} |$. Since $\mathcal{L} = \mathcal{D} - \mathcal{A}$, one has $|\mathcal{D}^{-1} \mathcal{L}| = \mathbf{I}_n + \mathcal{D}^{-1} \mathcal{A}$; thus $\mathcal{M} = (1 - \sigma) \mathbf{I}_n - \sigma \mathcal{D}^{-1} \mathcal{A}$. From the Geršgorian discs theorem [34], if $\sigma < 0.5$, all of the eigenvalues of \mathcal{M} have positive real parts. Therefore, according to [35, Th. 5.1.4], \mathcal{M} is *invertible* and (14) can be written as

$$|\mathbf{e}| \leq \mathbf{C}_{1}|\mathbf{x}| + \mathbf{C}_{2}, \text{ where, } \mathbf{C}_{2} = \begin{bmatrix} \gamma_{V} \mathcal{M}^{-1} \mathbf{1}_{n} \\ \gamma_{\Omega} \mathcal{M}^{-1} \mathbf{1}_{n} \end{bmatrix},$$

$$\mathbf{C}_{1} = \begin{bmatrix} \sigma \mathcal{M}^{-1}|\mathcal{D}^{-1}\mathcal{L}| & \mathbf{0}_{n} & \mathbf{0}_{n} & \mathbf{0}_{n} \\ \mathbf{0}_{n} & \mathbf{0}_{n} & \sigma \mathcal{M}^{-1}|\mathcal{D}^{-1}\mathcal{L}|\mathbf{0}_{n} \end{bmatrix} (15)$$

From (11), (15), and the triangle inequality, if $|\mathbf{w}| < w^* \mathbf{1}_{4n}$, then with $\mathcal{T}_1 = |\mathbf{C}|\mathbf{C}_1$ and $\mathcal{T}_2 = |\mathbf{C}|\mathbf{C}_2 + w^* \mathbf{1}_{4n}$ one has

$$|\mathbf{u}| \le \mathcal{T}_1|\mathbf{x}| + \mathcal{T}_2. \tag{16}$$

The statements (11) and (16)) resemble [36, eq. (28)] and [36, eq. (29)], respectively. Accordingly, if $\bf A$ in (11) is Hurwitz, the stability and boundedness analyses of the system follows the results of [36, Th. 2]. In other words, the solutions of the system (11) are ultimately uniformly bounded (UUB). The interested reader can refer to [36] for more info on the notion of UUBness and the systematic approach for calculating the solutions bounds. According to the foregoing analysis, the system is stable if $\sigma < 0.5$, the matrix $\bf A$ is Hurwitz, and $|\bf w| < w^* {\bf 1}_{4n}$.

C. Sampling Delay Effects Analysis

In this part, the focus is on the cybernetic aspect of the system and the underlying physical and control layers i.e., (9b) and (10) are neglected. According to Remark 4, if *over the \tau seconds after triggering instants* the measurement errors do not violate the thresholds, the system is the ET control system investigated previously. Otherwise, the time-dependent threshold in (7) introduces a delay of τ to the system and hence one can write $\tilde{\mathbf{V}} = \tilde{\mathbf{V}}(t) = \mathbf{V}(t-\tau)$ & $\tilde{\mathbf{\Omega}} = \tilde{\mathbf{\Omega}}(t) = \mathbf{\Omega}(t-\tau)$. By replacing them in (9) and taking Laplace transform—where s stands for the Laplace operator—one has

$$(s\mathbf{M}' - \mathbf{A}')\mathbf{y} = \mathbf{y}_{0} + \frac{1}{s}\mathbf{y}^{*} + \mathbf{D}'\hat{\mathbf{P}}(s), \text{ where,}$$
(17)
$$\mathbf{M}' = \begin{bmatrix} \mathbf{M}'_{V} & \mathbf{0}_{n} & \mathbf{0}_{n} \\ \mathbf{0}_{n} & \mathbf{M}'_{\Omega} & \mathbf{0}_{n} \\ \mathbf{0}_{n} & \mathbf{0}_{n} & \mathcal{I}_{n} \end{bmatrix}, \mathbf{A}' = \begin{bmatrix} \mathbf{A}'_{V} & \mathbf{0}_{n} & \mathbf{0}_{n} \\ \mathbf{0}_{n} & \mathbf{A}'_{\Omega} & \mathbf{A}'_{\Omega P} \\ \mathbf{0}_{n} & \mathbf{0}_{n} & \mathbf{A}'_{P} \end{bmatrix},$$

$$\mathbf{y} = \begin{bmatrix} \mathbf{V}(s) \\ \mathbf{\Omega}(s) \\ \mathbf{P}(s) \end{bmatrix}, \mathbf{y}^{*} = \begin{bmatrix} V_{ref}\mathbf{I}_{V}\mathbf{b}_{V}\mathbf{1}_{n} \\ \Delta f^{*}\mathbf{I}_{f}\mathbf{b}_{f}\mathbf{1}_{n} \\ \mathbf{0}_{n} \end{bmatrix}, \mathbf{D}' = \begin{bmatrix} \mathbf{0}_{n} \\ \mathbf{D}'_{\Omega} \\ \mathbf{D}'_{P} \end{bmatrix},$$

$$\mathbf{y}_{0} = \begin{bmatrix} (\mathcal{I}_{n} + \mathbf{K}_{V}\mathbf{b}_{V})\mathbf{V}_{0} + \mathbf{K}_{V}(\mathcal{I}_{n} - \mathbf{b}_{V})\mathcal{D}^{-1}\mathcal{L}\tilde{\mathbf{V}}\tilde{\mathbf{0}}_{0} \\ (\mathcal{I}_{n} + \mathbf{K}_{f}\mathbf{b}_{f})\mathbf{\Omega}_{0} + \mathbf{K}_{f}\mathbf{b}_{\Omega}\mathcal{D}^{-1}\mathcal{L}\tilde{\mathbf{0}}_{0} \end{bmatrix};$$

$$\mathbf{y}_{0} = \begin{bmatrix} (\mathcal{I}_{n} + \mathbf{K}_{V}\mathbf{b}_{V})\mathbf{V}_{0} + \mathbf{K}_{V}(\mathcal{I}_{n} - \mathbf{b}_{V})\mathcal{D}^{-1}\mathcal{L}\tilde{\mathbf{0}}_{0} \\ (\mathcal{I}_{n} + \mathbf{K}_{f}\mathbf{b}_{f})\mathbf{\Omega}_{0} + \mathbf{K}_{f}\mathbf{b}_{\Omega}\mathcal{D}^{-1}\mathcal{L}\tilde{\mathbf{0}}_{0} \end{bmatrix};$$

$$\mathbf{p}_{0} = \begin{bmatrix} (\mathcal{I}_{n} + \mathbf{K}_{V}\mathbf{b}_{V} + \mathbf{K}_{V}(\mathcal{I}_{n} - \mathbf{b}_{V})\mathcal{D}^{-1}\mathcal{L}\tilde{\mathbf{0}}_{0} \\ (\mathcal{I}_{n} + \mathbf{K}_{f}\mathbf{b}_{f} + \mathbf{K}_{f}\mathbf{b}_{\Omega}\mathcal{D}^{-1}\mathcal{L}e^{-\tau s}, \\ \mathbf{A}'_{V} = \mathcal{I}_{N} + \mathbf{K}_{f}\mathbf{b}_{f} + \mathbf{K}_{f}\mathbf{b}_{\Omega}\mathcal{D}^{-1}\mathcal{L}e^{-\tau s}, \\ \mathbf{A}'_{\Omega} = -\mathbf{I}_{f}\mathbf{b}_{f} - \mathbf{I}_{f}\mathbf{b}_{\Omega}\mathcal{D}^{-1}\mathcal{L}e^{-\tau s}, \\ \mathbf{A}'_{\Omega P} = -(2\pi f_{c}\mathbf{K}_{f}\mathbf{b}_{f} - \mathbf{I}_{f}\mathbf{b}_{f})\mathbf{m}, \mathbf{A}'_{P} = -2\pi f_{c}\mathcal{I}_{n}, \\ \mathbf{D}'_{O} = 2\pi f_{c}\mathbf{K}_{f}\mathbf{b}_{f}\mathbf{m}, \mathbf{D}'_{P} = 2\pi f_{c}\mathcal{I}_{n}. \end{cases}$$
(18)

Note that y is the vector of states' Laplace transforms; the zerosub-scripted quantities in y_0 are initial values' vectors; $\hat{\mathbf{P}}(s)$ is the Laplace transform of the non-filtered power vector $\hat{\mathbf{P}}$.

Let us derive sufficient conditions for stability of the system (17) with the characteristic polynomial $\det(s\mathbf{M}'-\mathbf{A}')=0$. Since \mathbf{A}' , \mathbf{M}' are partitioned triangle matrices, one can write $\det(s\mathbf{M}'-\mathbf{A}')=\det(s\mathbf{M}'_V-\mathbf{A}'_V)\det(s\mathbf{M}'_\Omega-\mathbf{A}'_\Omega)\det(s\mathcal{I}_n-\mathbf{A}'_P)$ and therefore it suffices to analyze the roots of the polynomials $\det(s\mathbf{M}'_V-\mathbf{A}'_V)=0$, $\det(s\mathbf{M}'_\Omega-\mathbf{A}'_\Omega)=0$, $\det(s\mathcal{I}_n-\mathbf{A}'_P)=0$. As the above determinants are zero, the matrices $s\mathbf{M}'_V-\mathbf{A}'_V$, $s\mathbf{M}'_\Omega-\mathbf{A}'_\Omega$, $s\mathcal{I}_n-\mathbf{A}'_P$ are singular; hence, the preceding polynomials have solution if and only if

one has $x^T(s\mathbf{M}_V'-\mathbf{A}_V')x=0$, $x^T(s\mathbf{M}_\Omega'-\mathbf{A}_\Omega')x=0$, and $x^T(s\mathcal{I}_n-\mathbf{A}_P')x=0$ for some real unit-norm vector x [13]. These are simply scalar polynomials with coefficients in the form of quadratic functions. Therefore, one can extract sufficient conditions of having their roots with negative real parts which is equivalent to the stability of the system. According to (18), $x^T(s\mathcal{I}_n-\mathbf{A}_P')x=0$ have roots with negative real parts and hence the stability of the system is boiled down to checking the location of the roots of $x^T(s\mathbf{M}_V'-\mathbf{A}_V')x=0$ and $x^T(s\mathbf{M}_\Omega'-\mathbf{A}_\Omega')x=0$ that, from (18), one can check the roots of the polynomials below, instead.

$$a_1^V s + a_0^V + (a_2^V s + a_\tau^V)e^{-\tau s} = 0,$$
 (19a)

$$a_1^{\Omega}s + a_0^V + (a_2^{\Omega}s + a_{\tau}^{\Omega})e^{-\tau s} = 0,$$
 (19b)

where, $a_{\tau}^V = x^T \mathbf{I}_V (\mathcal{I}_n - \mathbf{b}_V) \mathcal{D}^{-1} \mathcal{L}x$, $a_{\tau}^V = x^T \mathbf{I}_f \mathbf{b}_{\Omega} \mathcal{D}^{-1} \mathcal{L}x$, $a_0^V = x^T \mathbf{I}_f \mathbf{b}_f x$, $a_1^V = x^T (\mathcal{I}_n + \mathbf{K}_V \mathbf{b}_V) x$, $a_1^\Omega = x^T (\mathcal{I}_n + \mathbf{K}_f \mathbf{b}_f) x$, $a_2^V = x^T \mathbf{K}_V (\mathcal{I}_n - \mathbf{b}_V) \mathcal{D}^{-1} \mathcal{L}x$, and $a_2^\Omega = x^T \mathbf{K}_f \mathbf{b}_{\Omega} \mathcal{D}^{-1} \mathcal{L}x$. Equations (19a) and (19b) correspond to [37, Eq. (2.46)]. From the Lemma, if $d_i \geq d_i^o$, $\forall i$, then a_{τ}^V , a_{τ}^Ω , a_2^V , a_2^Ω are positive and hence the system is stable at $\tau = 0$. The roots of (19a) and (19b) are continuous as a function of positive τ . In this way, according to the direct method provided in [37, Chap. 2.3.2], if at some τ roots of (19) cross the imaginary axis, one has $e^{j\omega\tau} = -a_{\tau}^V/(j\omega e^{j\omega\tau} a_2^V + j\omega a_1^V + a_0^V)$ and $e^{j\omega\tau} = -a_{\tau}^\Omega/(j\omega e^{j\omega\tau} a_2^\Omega + j\omega a_1^\Omega + a_0^\Omega)$, resulting in (20a) and (20b), respectively (see [37, Eqs. (2.47)-(2.48)]).

$$\begin{cases} \omega^2 = [(a_{\tau}^V)^2 - (a_0^V)^2]/[(a_1^V)^2 - (a_2^V)^2], \\ \omega\tau = \arg(-\frac{j\omega a_2^V + a_{\tau}^V}{j\omega a_1^V + a_0^V}) + 2\pi k, k = 0, 1, \cdots, \end{cases}$$
 (20a)

$$\begin{cases} \omega^{2} = [(a_{\tau}^{\Omega})^{2} - (a_{0}^{\Omega})^{2}]/[(a_{1}^{\Omega})^{2} - (a_{2}^{\Omega})^{2}], \\ \omega\tau = \arg(-\frac{j\omega a_{2}^{\Omega} + a_{\tau}^{\Omega}}{j\omega a_{1}^{\Omega} + a_{0}^{\Omega}}) + 2\pi k, k = 0, 1, \cdots, \end{cases}$$
(20b)

where, $\arg(\cdot)$ denotes the argument operator. From [37, Prop. 2.1], if (19) with $\tau=0$ is stable and the first lines of (20a) and (20b) do not have solutions, then the polynomials in (19) are delay-independent stable (independent of τ). Otherwise, the first-line equations in (20a) and (20b) yield the positive crossing frequencies $\omega_c^V = \sqrt{(a_\tau^V)^2 - (a_0^V)^2}/\sqrt{(a_1^V)^2 - (a_2^V)^2}$ and $\omega_c^\Omega = \sqrt{(a_\tau^\Omega)^2 - (a_0^\Omega)^2}/\sqrt{(a_1^\Omega)^2 - (a_2^\Omega)^2}$, respectively. Substituting these crossing frequencies for ω in the argument equations in (20a) and (20b), respectively, one can obtain the respective crossing delays as

$$\tau_k^V \omega_c^V = \pi + \arctan(\frac{a_2^V \omega_c}{a_\tau^V}) - \arctan(\frac{a_1^V \omega_c}{a_0^V}) + 2\pi k, (21a)$$

$$\tau_k^{\Omega}\omega_c^{\Omega} = \pi + \arctan(\frac{a_2^{\Omega}\omega_c}{a_1^{\Omega}}) - \arctan(\frac{a_1^{\Omega}\omega_c}{a_0^{\Omega}}) + 2\pi k, (21b)$$

where, $k = 0, 1, \cdots$. Correspondingly,

$$\tau_0^V = \left(\pi + \arctan\left(\frac{a_2^V \omega_c^V}{a_\tau^V}\right) - \arctan\left(\frac{a_1^V \omega_c^V}{a_0^V}\right)\right) / \omega_c^V, \tag{22a}$$

$$\tau_0^{\Omega} = \left(\pi + \arctan(\frac{a_2^{\Omega}\omega_c^{\Omega}}{a_2^{\Omega}}) - \arctan(\frac{a_1^{\Omega}\omega_c^{\Omega}}{a_2^{\Omega}})\right)/\omega_c^{\Omega}; \quad (22b)$$

which implies the stability for
$$\tau < \min(\tau_0^V, \tau_0^{\Omega})$$
.

D. Equilibrium Analysis

According to (4a), in steady state one has

$$b_i^f(f_{ref} - f_{com}) + \frac{b_i^{\Omega}}{d_i} \sum_{j \in N_i} a_{ij} (\tilde{\Omega}_j - \tilde{\Omega}_i) = 0, \quad (23)$$

where, f_{com} is common frequency. Eq. (23) can be written as

$$\mathbf{b}_f(f_{com} - f_{ref})\mathbf{1}_n + \mathbf{b}_{\Omega}\mathcal{D}^{-1}\mathcal{L}\tilde{\mathbf{\Omega}} = \mathbf{0}_n, \tag{24}$$

corresponding to [14, eq.(8)]. Therefore, if the CN among the DGs has a rooted spanning tree and $b_i \neq 0$ for at least one root node, then the results of [14, Th. 2] hold, i.e., in steady state one has $f_i = f_{ref}$, $\tilde{\Omega}_i = \tilde{\Omega}_j$, $\forall i,j$. One can bound the neighborhood error of Ω_i as

$$\left|\frac{1}{d_i}\sum a_{ij}(\Omega_j - \Omega_i)\right| \le |\tilde{z}_i^{\Omega}| + \frac{1}{d_i}\sum a_{ij}(|e_j| + |e_i|).$$
 (25)

From (1d), (8a), & (25), in steady state when $\tilde{z}_i^{\Omega} = 0$, one has

$$m_i P_i = \Omega_i \Rightarrow \left| \frac{1}{d_i} \sum a_{ij} (m_j P_j - m_i P_i) \right| \le 2\gamma_{\Omega}.$$
 (26)

The last inequality implies that in steady state, the active powers are shared properly but with the maximum neighborhood error of $2\gamma_{\Omega}$ Hertz. According to (1d), this error can be translated into (regarded as) steady-state frequency error.

From (4b), if $b_i^V=1$, i.e., the DG voltage is not affected by its neighbors, then in steady state one has $V_i=V_{ref}$. Otherwise, its steady-state voltage is influenced by their in-neighbors. Let $z_i^V=\frac{1}{d_i}\sum_j a_{ij}(V_j-V_i), \forall d_i\neq 0$ be the neighborhood voltage error. Then, one has $z_i^V=\tilde{z}_i^V-\frac{1}{d_i}\sum_j a_{ij}(e_j^V-e_i^V)$. From (9a), one has $(b_i^V-1)\tilde{z}_i^V=b_i^V\Delta V_i$ in steady state. By using these equations, (8b), and the triangle inequality one has

$$|z_i^V| \le 2\gamma_V, \quad \forall i | b_i^V = 0. \tag{27}$$

Hence, the maximum neighborhood voltage error is $2\gamma_V$.

E. Inter-Event Time Analysis

Transient effects of τ : Consider the functions $y_i^\Omega = |e_i^\Omega|$ and $y_i^V = |e_i^V|$ over $[t_{k_i}^i, t_{k_i+1}^i)$. According to the event-triggering condition in (7), the inter-event time intervals are always greater than τ . In what follows the growth of the functions y_i^Ω and y_i^V over the first τ seconds after triggering instant $t_{k_i}^i$ is investigated. Differentiating them by using (4) yields $\dot{y}_i^\Omega \leq |\dot{\Omega}_i| \leq \alpha_{k_i}^\Omega$ and $\dot{y}_i^V \leq |\dot{V}_i| \leq \alpha_{k_i}^V$; where, $\alpha_{k_i}^\Omega$ and $\alpha_{k_i}^V$ are the corresponding maximum values over $[t_{k_i}^i, t_{k_{i+1}}^i)$. Considering $y_i^\Omega(t_{k_i}^i) = y_i^V(t_{k_i}^i) = 0$ and integrating these inequalities, one can write $y_i^\Omega(t_{k_i}^i + \tau) \leq \alpha_{k_i}^\Omega \tau$ and $y_i^V(t_{k_i}^i + \tau) \leq \alpha_{k_i}^V \tau$, which demonstrate the maximum possible growth of measurement errors over the first τ seconds and can be used for proper selection of τ .

Inter-event times: According to (7), if $y_i^\Omega(t_{k_i}^i+\tau)>\sigma b_i^\Omega|\tilde{z}_i^\Omega|+\gamma_\Omega$ or $y_i^V(t_{k_i}^i+\tau)>\sigma(1-b_i^V)|\tilde{z}_i^V|+\gamma_V$, then $t_{k_i+1}^i-t_{k_i}^i=\tau$, otherwise $t_{k_i+1}^i-t_{k_i}^i>\tau$. For the second case, considering $y_i^\Omega(t_{k_i}^i)=y_i^V(t_{k_i}^i)=0$ and integrating $\dot{y}_i^\Omega\leq\alpha_{k_i}^\Omega$, $\dot{y}_i^V\leq\alpha_{k_i}^V$ one has $y_i^\Omega\leq\alpha_{k_i}^\Omega(t-t_{k_i}^i)$ and $y_i^V\leq\alpha_{k_i}^V(t-t_{k_i}^i)$. From (8), the next event time $t_{k_i+1}^i$ is when $y_i^\Omega>\sigma b_i^\Omega|\tilde{z}_i^\Omega|+\gamma_\Omega$ or $y_i^V>\sigma(1-b_i^V)|\tilde{z}_i^V|+\gamma_V$. Hence, if $t_{k_i+1}^i-t_{k_i}^i>\tau$, then

$$t_{k_i+1}^i - t_{k_i}^i > \min(\tau_{k_i}^{\Omega}, \tau_{k_i}^V) = \tau_{k_i}$$
 (28)

where $\alpha_{k_i}^\Omega \tau_{k_i}^\Omega = \sigma b_i^\Omega |\tilde{z}_i^\Omega| + \gamma_\Omega$ and $\alpha_{k_i}^V \tau_{k_i}^V = \sigma (1 - b_i^V) |\tilde{z}_i^V| + \gamma_V$. The bound in (28) is a function of $\sigma \in [0, 0.5)$, γ_Ω , and γ_V . Accordingly, if $\gamma_i^\Omega = \gamma_i^V = 0$ then τ_i^Ω and τ_i^V are proportional to σ , i.e., the more σ , the less τ_i^Ω , τ_i^V , and the

more communications. In fact, the parameters γ_i^{Ω} , γ_i^{V} alleviate the impact of σ on the communication and inter-event time.

All in all, if τ is small then the inter-event times are highly affected by σ , γ_{Ω} , and γ_{V} such that the more σ , γ_{Ω} , and γ_{V} , the more inter-event times, and the less communications. But then, for large values of τ the inter-event times are mainly affected by τ and the other parameters have less effects.

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