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# A DC Hybrid Active Power Filter and Its Nonlinear Unified Controller Using Feedback Linearization

Gaoxiang Li, An Luo, *Senior Member, IEEE*, Zhixing He, *Member, IEEE*, Fujun Ma, *Member, IEEE*, Yandong Chen, *Senior Member, IEEE*, Wenhua Wu, Zhen Zhu, and Josep M. Guerrero, *Fellow, IEEE*

**Abstract**—In current power system, the conversion between DC and AC is widely existing and dc side harmonic problem is prominent. To suppress the second-harmonic current (SHC) at the dc side of single-stage single-phase inverter, a dc hybrid active power filter (DC-HAPF) structure is presented, which composes of bidirectional dc-dc circuit based active power filter and CL passive filter. Here, the CL passive filter is used to mitigate the high frequency harmonics and the active power filter is applied to compensate the low frequency harmonic current. Meanwhile, the influence of filter parameters on harmonic suppression is analyzed based on the average switching model. In addition, for the control of the DC-HAPF, a nonlinear unified controller via feedback linearization is proposed, where the voltage and current dual-loop control is converted to a single-loop control of energy. By analyzing the control system stability and DC-HAPF's performance, appropriate control parameters are selected. To verify the feasibility of the proposed topology and control strategy, a 500W single-stage single-phase inverter with the DC-HAPF is built and a good performance of dc side harmonic suppression has been achieved.

**Index Terms**—Second harmonic current, hybrid active power filter, feedback linearization, single-stage single-phase inverter.

## I. INTRODUCTION

HARMONIC elimination is great significance for improving power quality, reducing power loss and enhancing grid reliability. Power electronic based inverters are widely used in current power systems. According to the topology, the inverters can be classified into the single-phase inverters and the three-phase inverters. Compared with the three-phase inverters, the single-phase inverters are mainly used in systems that with low power range (<10kW) [1]. As for the low-voltage small-power micro-grids, such as home micro-grids generally adopt single-phase power supply structure, and it is easily vulnerable to external devices. So the improvement of power quality for single-phase power supply is important. According to the

instantaneous power theory, there is power ripple at twice the fundamental frequency ( $2f_o$ ) for the output power of the single-phase inverter, which results in the second-harmonic current (SHC) at the dc-side of the single-phase inverter [2]. The SHC will cause additional power loss and higher current stress. Moreover, for the dc voltage sources, such as batteries, photovoltaic cells and fuel cells, the SHC will shorten their lifetime and reduce energy conversion efficiency. A large capacitor is usually used to suppress the dc-side harmonics of single-phase inverter, but it has the disadvantages of large size and poor performance. Therefore, it is necessary to further study the dc-side harmonic suppression for the single-phase inverters.

Moreover, according to the structure, the single-phase inverters can be categorized into the single-stage inverters and the two-stage inverters. [1] and [2] offered an overview of the low frequency power decoupling of single-phase inverters and the dc-side harmonic suppression methods. For the two-stage single-phase inverters, the SHC is mainly mitigated by improving control methods [3]-[14]. In [3], a SHC reduction method is proposed for the dc-dc converters, which regulates the dc-bus voltage. A virtual series impedance, which has high impedance at  $2f_o$  while low impedance at other frequencies, is presented for increasing the impedance of the boost-diode branch or the boost-inductor branch at  $2f_o$  [4]. Various control schemes have been presented for mitigating the SHC in the buck-derived front-end dc-dc converter [5]-[10] and the SHC is suppressed in the control link of dc-dc converter. In [11]-[14], different control strategies are presented for mitigating the low frequency current ripples, where a boost-type differential inverter made up of two bidirectional boost converters is adopted. For the single-stage single-phase inverters, the SHC can be suppressed by adding filter [15]-[21]. In [15], a ripple power port is designed to manage energy storage and decouple capacitor ripple from power ripple. In [16], a bidirectional buck-boost converter is used as the ripple energy storage circuit, which can effectively reduce the energy storage capacitance. A current pulsation smoothing parallel active filter (CPS-PAF) is used for the advantage that it requires a small film capacitor [17]. In [18], an integrator is added into the control loop to inject the ripple current into the dc-link and restrain the dc component of the current reference. In [19], a rectifier is designed for the mitigation of power ripple at twice the line frequency and the dc power is in series with an inductor. A new power decoupling circuit applied to the single-phase current source converter (SCSC) is proposed [20]. An active buffer without a large inductor and capacitor in the dc-link part is designed [21]. In all, to deal with the SHC, different ways are proposed based on the different structures.

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However, the cooperative working mechanism and control performance between the dc active power filter and the passive filter for suppressing the dc-side harmonics are rarely studied.

Feedback linearization is an advanced nonlinear control method without neglecting the higher order terms in the linearization process. This technique has been successfully applied to the areas of power electronic converters [22-24]. By applying exact feedback linearization theory, a nonlinear control strategy is presented for single-phase active power filter [25]. A new feedback linearization approach is proposed, which yields a decoupled linear induction motor (IM) model with two state variables: torque and stator flux magnitude [26]. In [27], a simplified feedback linearization of single-phase active power filter using sliding mode control is proposed. An innovative simplified feedback linearization (SFL) control strategy is designed for the PV inverter with the LCL filter [28]. For achieving excellent performance under various operating conditions, a controller based on the partial feedback linearization is proposed [29]. A controller is designed based on the partial feedback linearization to regulate the line voltage by providing reactive power compensation [30]. In [31], a nonlinear damping controller is designed based on partial feedback linearization for mitigating sub-synchronous oscillation. Compared with traditional controller, the controllers based on feedback linearization have a good dynamic and steady performance. However, owing to the different circuit structures and control targets, the feedback linearization-based controllers also are different. Therefore, it is usually necessary to design the appropriate controller based on the specific application scenarios.

In this paper, for distinguishing the traditional ac hybrid active power filter (HAPF), the concept of dc hybrid active power filter (DC-HAPF) is presented. In addition, to suppress the SHC and high frequency harmonics at the dc side of single-stage single-phase inverters, a DC-HAPF topology composed of bidirectional dc-dc circuit based active power filter and CL filter, is proposed. For the control of DC-HAPF, a nonlinear unified controller using feedback linearization is proposed. The rest of this paper is organized as follows. The single-stage single-phase inverter with the proposed DC-HAPF is introduced in Section II. In addition, the characteristics of the DC-HAPF are analyzed based on the average switching model. After that, Section III introduces the nonlinear unified controller via feedback linearization and the design method of control parameters. Experimental results are presented in Section IV.

## II. DC HYBRID ACTIVE POWER FILTER AND ITS FILTERING CHARACTERISTICS

Fig.1 shows the configuration of single-stage single-phase inverter with the designed DC-HAPF. The CL filter composes of  $C_1$  and  $L_1$ , where  $C_1$  is also the dc-bus capacitor for the single-stage inverter. The dc active power filter is based on the bidirectional dc-dc converter, which composes with  $L_2$ ,  $C_2$ ,  $S_5$  and  $S_6$ . The current  $i_{inv}$  contains a lot of harmonic components, especially the SHC and high frequency harmonics associated with the switching frequency. The CL filter can suppress the high frequency harmonic currents effectively, but it has a poor effect on the SHC. After CL filtering, the harmonic current in  $i_{L1}$  is mainly low-frequency harmonic current, which can be compensated by the APF.

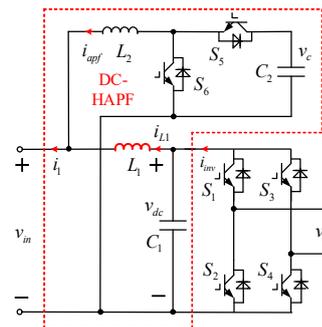


Fig.1. Configuration of single-stage single-phase inverter with DC-HAPF.

According to Fig. 1, by using state-space average method, the mathematical model of APF can be expressed as,

$$\begin{cases} L_2 \frac{di_{apf}}{dt} = v_{in} D_k + (v_{in} - v_c) D_k' \\ C_2 \frac{dv_c}{dt} = i_{apf} D_k' \end{cases} \quad (1)$$

where  $i_{apf}$  is the output current of APF;  $v_{in}$  is the input voltage for APF;  $v_c$  is the voltage of  $C_2$ ;  $D_k$  is the duty-cycle of  $S_6$  in the switching period  $k$ , and  $D_k' + D_k = 1$ , expressed as,

$$D_k = 1 - \frac{v_{in}}{v_c} \quad (2)$$

Applying the Laplace Transformation, (1) can be rewritten as,

$$\begin{cases} i_{apf} = [v_{in} D_k + (v_{in} - v_c) D_k'] / (sL_2) \\ v_c = i_{apf} D_k' / (sC_2) \end{cases} \quad (3)$$

According to two-port network theory, the bidirectional dc-dc circuit based APF at the dc side of single-phase inverter can be equivalent to an impedance. According to (3), the equivalent impedance of the APF can be obtained as,

$$Z_{apf}(s) = \frac{v_{in}}{i_{apf}} = \frac{L_2 C_2 s^2 + D_k^2}{s C_2} \quad (4)$$

By setting  $L_2=1\text{mH}$ ,  $C_2=2\text{mF}$  and  $D_k=0.1$ , the Bode diagram for  $Z_{apf}(s)$  is depicted, as shown in Fig.2.

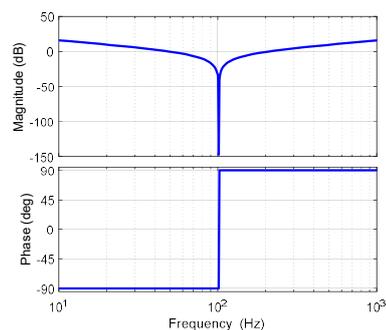


Fig.2. Bode diagram of  $Z_{apf}(s)$ .

Seen from Fig.2, the magnitude of  $Z_{apf}(s)$  is very low at  $2f_0$ , which likes a notch filter. This implies that the equivalent impedance of the APF is very small at  $2f_0$ . At other frequencies, the magnitude of  $Z_{apf}(s)$  is much bigger than that of  $Z_{apf}(s)$  at  $2f_0$ . It means that the APF can provide a channel for SHC and hinder the passing of dc current.

According to (4), the characteristics of  $Z_{apf}(s)$  are determined by three parameters  $L_2$ ,  $C_2$  and  $D_k$ . Because  $C_2$  not only is a filter

capacitor, but also the dc-bus capacitor for the single-stage inverter. So,  $C_2$  is designed based on the dc voltage fluctuation requirement. In order to better design the parameters  $L_2$  and  $D_k$ , the amplitude-frequency characteristics of  $Z_{apf}(s)$  under different  $L_2$  and  $D_k$  are showed in Fig.3.

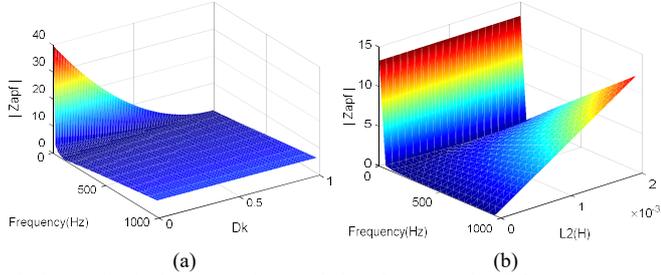


Fig.3. Amplitude-frequency characteristics of  $Z_{apf}(s)$  under different parameters. (a) Under different  $D_k$ . (b) Under different  $L_2$ .

According to Fig.3(a), the amplitude of  $Z_{apf}(s)$  increases significantly with the decrease of  $D_k$  in the low-frequency part (lower than  $2f_0$ ). Similarly, according to Fig.3(b), the amplitude of  $Z_{apf}(s)$  raises rapidly with the increase of  $L_2$  in the high-frequency part (higher than  $2f_0$ ). No matter the increase of  $D_k$  or  $L_2$ , the amplitude ratio of  $Z_{apf}(s)$  is always low at the frequency  $2f_0$ . Hence, the impedance characteristics of  $Z_{apf}(s)$  can be improved by designing the value of  $D_k$  and  $L_2$ .

Replacing the APF with the equivalent impedance  $Z_{apf}(s)$ , the simplified circuit topology of Fig.1 can be depicted in Fig.4, where  $V_{in}$  is the dc voltage source and  $R_0$  is its internal resistance.

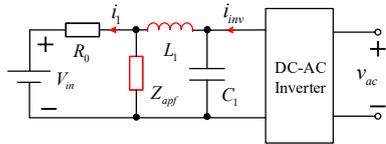


Fig.4. The simplified circuit topology of single-stage single-phase inverter with DC-HAPF.

It is well known that the downstream single-phase inverter can be equivalent to a dc current source  $I_{dc}$  in parallel with an SHC source  $I_{SHC}$  if neglecting the switching harmonics. The circuit topology of the single-stage single-phase inverter with different filters can be further simplified, as shown in Fig.5.

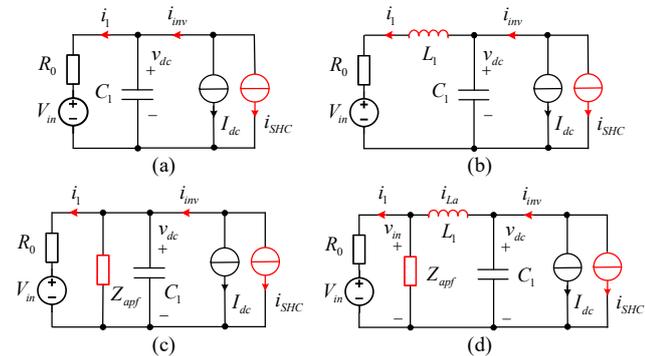


Fig.5. The simplified circuit of the single-stage single-phase inverter with different filters. (a) With filter C. (b) With filter CL. (c) With filter C+APF. (d) With filter CL+APF.

According to Fig.5, the equivalent control diagrams of single-stage single-phase inverter with different filter can be depicted in Fig.6.

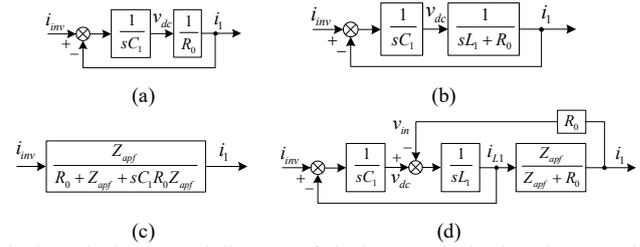


Fig.6. Equivalent control diagrams of single-stage single-phase inverter with different filters. (a) With filter C. (b) With filter CL. (c) With filter C+APF, (d) With filter CL+APF.

According to Fig.6(a), the transfer function from  $i_{inv}$  to  $i_1$  can be expressed as,

$$i_1 = \frac{1}{sC_1R_0 + 1} i_{inv} \quad (5)$$

Similarly, from Fig.6(b), the transfer function from  $i_{inv}$  to  $i_1$  can be expressed as,

$$i_1 = \frac{1}{sC_1(sL_1 + R_0) + 1} i_{inv} \quad (6)$$

Similarly, from Fig.6(c), the transfer function from  $i_{inv}$  to  $i_1$  can be expressed as,

$$i_1 = \frac{Z_{apf}}{R_0 + Z_{apf} + sC_1R_0Z_{apf}} i_{inv} \quad (7)$$

Similarly, from Fig.6(d), the transfer function from  $i_{inv}$  to  $i_1$  can be expressed as,

$$i_1 = \frac{Z_{apf}}{(s^2L_1C_1 + 1)(Z_{apf} + R_0) + sC_1R_0Z_{apf}} i_{inv} \quad (8)$$

By setting  $L_1 = 0.1\text{mH}$ ,  $C_1 = 1.5\text{mF}$ ,  $L_2 = 1\text{mH}$ ,  $C_2 = 2\text{mF}$ ,  $R_0 = 0.01\text{ohm}$ , and  $D_k = 0.1$ , the Bode plots for (5), (6), (7) and (8) are depicted in Fig.7.

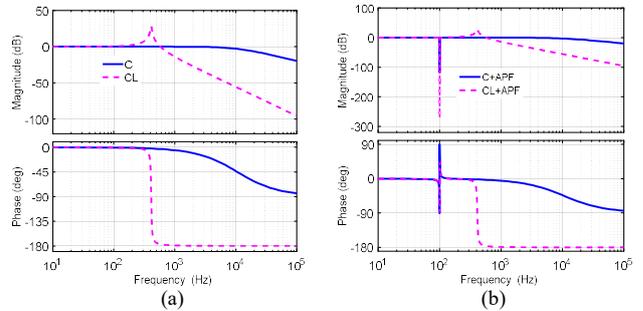


Fig.7. Bode diagrams of the transfer functions from  $i_{inv}$  to  $i_1$ . (a) Bode diagrams of (5) and (6). (b) Bode diagrams of (7) and (8).

As seen from Fig.7(a), the magnitude of (5) is higher than that of (6) in the high frequency part. It shows that CL filter has a good effect on suppressing the high-frequency harmonic current. Seen from Fig.7(b), the magnitude of (7) and (8) are very low at the frequency  $2f_0$  and it shows that the APF can suppress SHC effectively. In addition, the magnitude of (7) is higher than that of (8) in the high-frequency part, and it shows that CL+APF has a better control effect than C+APF for high frequency harmonics. Therefore, the proposed DC-HAPF integrates the merits of both active power filter and passive filter.

Seen from (8), the internal resistance  $R_0$  can affect the filtering effect. Similarly, the values of  $D_k$  and  $L_1$  also have a great influence on the performance of DC-HAPF. To better analyze

the influence of the  $D_k$ ,  $L_1$  and  $R_0$  on the filtering effect, the amplitude-frequency characteristics of (8) under different  $D_k$ ,  $L_1$  and  $R_0$  can be depicted in Fig.8.

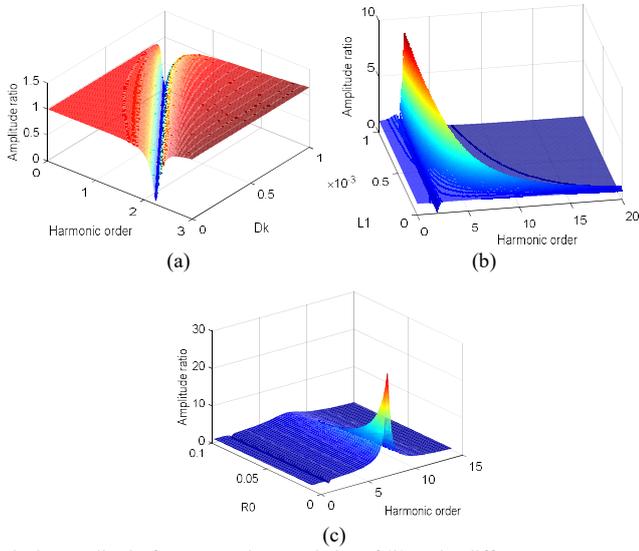


Fig.8. Amplitude-frequency characteristics of (8) under different parameters. (a) Under different  $D_k$ , (b) Under different  $L_1$ , (c) Under different  $R_0$ .

Seen from Fig.8(a), the trap frequency of (8) gradually increases with the decrease of  $D_k$  in the low frequency part. Similarly, according to Fig.8(b), the amplitude of (8) significantly decreases with the increase of  $L_1$  in the high-frequency part but rapidly increases in the low frequency part. No matter the  $L_1$  increases or not, the amplitude of (8) stays the same at the frequency  $2f_0$ . Hence, the SHC can be improved by designing the values of  $D_k$  and  $L_1$ . In addition, as shown in Fig.8(c), the amplitude of (8) decreases with the increase of impedance  $R_0$ . It shows that the increase of the resistance  $R_0$  can suppress the harmonic current. However, the resistance  $R_0$  is determined by the characteristics of the dc voltage source  $V_{in}$ , and artificially increasing the resistance  $R_0$  will increase the additional power loss.

### III. NONLINEAR UNIFIED CONTROL VIA FEEDBACK LINEARIZATION

In order to improve the control performance of system, the nonlinear unified controller using feedback linearization is designed in Fig.9. Applying feedback linearization theory, the appropriate new state variables are obtained and the inverse function is established. According to the new state variables, the nonlinear system can be converted into the linear system. Then, a linear system controller is designed based on the obtained linear system. Finally, according to the inverse function, the primary control variable can be obtained by the state variables and control variable of the linear system, which can realize the control of the nonlinear system.

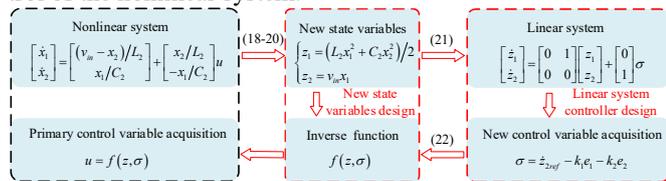


Fig.9. Design of the nonlinear unified controller using feedback linearization.

Replacing the duty-cycle  $D_k$  by the input variable  $u$ , (1) can be rewritten as,

$$\begin{cases} \frac{di_{apf}}{dt} = \frac{v_{in} - v_c}{L_2} + \frac{v_c}{L_2} u \\ \frac{dv_c}{dt} = \frac{i_{apf}}{C_2} - \frac{i_{apf}}{C_2} u \end{cases} \quad (9)$$

According to (9), selecting  $x=[x_1, x_2]=[i_{apf}, v_c]$  as state variables,  $y_x=h(x)=x_1$  as output and  $u=D_k$  as the input, the single-input single-output (SISO) nonlinear system based on differential geometry method can be obtained as,

$$\begin{cases} \dot{x} = f(x) + g(x)u \\ y_x = h(x) = x_1 \end{cases} \quad (10)$$

where

$$f(x) = \begin{bmatrix} \frac{v_{in} - x_2}{L_2} \\ \frac{1}{C_2} x_1 \end{bmatrix} \quad (11)$$

$$g(x) = \begin{bmatrix} \frac{1}{L_2} x_2 \\ -\frac{1}{C_2} x_1 \end{bmatrix} \quad (12)$$

where,  $f(x)$  and  $g(x)$  are controllable matrices. According to (11), (12) and Lie derivatives [28], there is,

$$ad_f g(x) = \frac{\partial g(x)}{\partial x} f(x) - \frac{\partial f(x)}{\partial x} g(x) = \begin{bmatrix} 0 \\ -\frac{v_{in}}{L_2 C_2} \end{bmatrix} \quad (13)$$

Combining (12) and (13), there is,

$$[g(x) \quad ad_f g(x)] = \begin{bmatrix} \frac{x_2}{L_2} & 0 \\ -\frac{x_1}{C_2} & -\frac{v_{in}}{L_2 C_2} \end{bmatrix} \quad (14)$$

Seen from (14), the rank of matrix (14) is 2, and the order of system (10) is also 2. Based on feedback linearization theory and differential geometry method, the system (10) can be precisely linearized. Thus, it can be determined that there is an output function making the relative order of the system be equal to the dimension of the system. The characteristic of system (10) is that it is nonlinear for the state variable  $x$ , but linear for the control variable  $u$ .

Applying Lie derivatives [28], according to (10)-(12), there is,

$$\begin{cases} L_f h(x) = \frac{\partial h(x)}{\partial x} \cdot f(x) = \frac{v_{in} - x_2}{L_2} \\ L_g h(x) = \frac{\partial h(x)}{\partial x} \cdot g(x) = \frac{1}{L_2} x_2 \end{cases} \quad (15)$$

According to (15), the relative order of the system (10) is 1, not equal to the dimension of the system. The original system (10) cannot be precisely linearized owing to the output function. It is necessary to reconstruct a new output function to re-

alize the precise feedback linearization. Supposing the new output function is  $\omega(x)$ , it needs to satisfy the following differential equation,

$$\frac{\partial \omega(x)}{\partial x} g(x) = 0 \quad (16)$$

According to (12) and (16), there is,

$$\frac{\partial \omega(x)}{\partial x} g(x) = \frac{\partial \omega(x)}{\partial x_1} \frac{1}{L_2} x_2 - \frac{\partial \omega(x)}{\partial x_2} \frac{1}{C_2} x_1 = 0 \quad (17)$$

For (17), a solution can be obtained,

$$\omega(x) = \frac{L_2 x_1^2 + C_2 x_2^2}{2} \quad (18)$$

Clearly, the new output function is APF's energy function, which has a clear physical meaning.

According to (11) and (18), there is,

$$L_f \omega(x) = v_{in} x_1 \quad (19)$$

Combing (18) and (19), the coordinate transformation can be derived as,

$$\begin{cases} z_1 = \omega(x) = \frac{L_2 x_1^2 + C_2 x_2^2}{2} \\ z_2 = L_f \omega(x) = v_{in} x_1 \end{cases} \quad (20)$$

By coordinate transformation, (10) can be described as,

$$\begin{cases} \dot{z} = \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix} z + \begin{bmatrix} 0 \\ 1 \end{bmatrix} \sigma \\ y_z = z_1 \end{cases} \quad (21)$$

where  $z_1$  and  $z_2$  are the state variables of the linear system and  $\sigma$  is the new control variable, satisfying,

$$u = \frac{1}{L_g L_f \omega(x)} (-L_f^2 \omega(x) + \sigma) \quad (22)$$

where  $L_f^2 \omega(x)$  and  $L_g L_f \omega(x)$  can be expressed as,

$$L_f^2 \omega(x) = \frac{v_{in}^2 - x_2 v_{in}}{L_2} \quad (23)$$

$$L_g L_f \omega(x) = \frac{v_{in} x_2}{L_2} \quad (24)$$

Since the APF is used to compensate harmonic currents, the current  $i_{apf}$  must follow the reference signal  $i_x$  fast and precisely. Meanwhile, the voltage  $v_c$  should follow the reference value  $v_{ref}$ . Similarly, for the system (21),  $z$  should follow the reference signal  $z_{ref}$  fast and precisely. When the system is stable, according to (20), there is,

$$\begin{cases} \frac{1}{2} L_2 x_1^2 + \frac{1}{2} C_2 x_2^2 = \frac{1}{2} L_2 i_{ref}^2 + \frac{1}{2} C_2 v_{ref}^2 \\ v_{in} x_1 = v_{in} i_{ref} \end{cases} \quad (25)$$

From (25), there is,

$$\begin{cases} x_1 = i_{ref} \\ x_2 = \pm v_{ref} \end{cases} \quad (26)$$

where  $x_2$  have two solutions, but only one is positive. In the practical system,  $x_2$  is the voltage of  $C_2$  and is positive. So, when  $z$  follows  $z_{ref}$ , it can guarantee that  $i_{apf}$  can follow the reference current  $i_x$ , and  $v_c$  can follow the reference voltage  $v_{ref}$ . Finally, the two control goals ( $v_{ref}$  and  $i_x$ ) can be translated into a control target  $z_{ref}$ .

In order to ensure that  $z$  follows the reference signal  $z_{ref}$ , a state error vector is defined as follows,

$$\begin{cases} e_1 = z_1 - z_{1ref} \\ e_2 = z_2 - z_{2ref} \end{cases} \quad (27)$$

where  $z_{1ref}$  is the reference signal of  $z_1$ , and  $z_{2ref}$  is the reference signal of  $z_2$ .

According to (21) and (27), there is,

$$\begin{cases} \dot{e}_1 = e_2 \\ \dot{e}_2 = \sigma - \dot{z}_{2ref} \end{cases} \quad (28)$$

where

$$\dot{z}_{2ref} = v_{in} \left( \frac{v_{in} - v_{ref}}{L_2} + \frac{v_{ref}}{L_2} u \right) \quad (29)$$

Defining the control law,

$$\sigma = \dot{z}_{2ref} - k_1 e_1 - k_2 e_2 \quad (30)$$

According to (28) and (30), there is,

$$\begin{bmatrix} \dot{e}_1 \\ \dot{e}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -k_1 & -k_2 \end{bmatrix} \begin{bmatrix} e_1 \\ e_2 \end{bmatrix} \quad (31)$$

According to (31), the characteristic equation can be obtained as,

$$A(\lambda) = \begin{bmatrix} -\lambda & 1 \\ -k_1 & -k_2 - \lambda \end{bmatrix} = \lambda^2 + k_2 \lambda + k_1 = 0 \quad (32)$$

where  $\lambda$  is the characteristic root.

When  $k_1 > 0$  and  $k_2 > 0$ ,  $\lambda$  possesses negative real part, the system (31) is stable and the proposed nonlinear unified controller via feedback linearization can follow the target accurately. To analyze the effect of parameters  $k_1$  and  $k_2$  on the controller performance, according to (31), the state variables  $e_1$  and  $e_2$  curves can be obtained as follow,

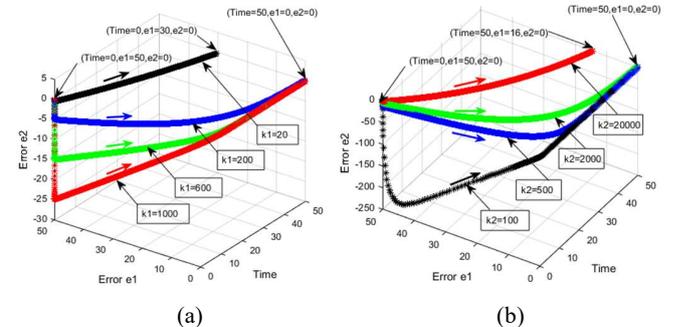


Fig.10. State variables  $e_1$  and  $e_2$  curves under different parameters  $k_1$  and  $k_2$ . (a)  $k_2=2000$ . (b)  $k_1=500$ .

Seen from Fig.10(a), when  $k_2=2000$ , with the increase of  $k_1$ , the convergence rate of error  $e_1$  gradually increases. The error  $e_2$  first increases then decreases and the fluctuation is bigger when  $k_1$  is bigger. From Fig.10(b), when  $k_1=500$ , with the decrease of  $k_2$ , the convergence rate of error  $e_1$  gradually increases. The error  $e_2$  first increases then decreases and the fluctuation is bigger when  $k_2$  is smaller. Seen from Fig.10, the error  $e_1$  gradually decreases from 50 to 0 and the error  $e_2$  gradually converges to 0 after an oscillation. As the error  $e_2$  is the derivative of error  $e_1$  and the error  $e_1=e_2=0$  when the system is stable, under the proposed controller, the system can follow the target accurately and the stability is better. When  $k_1$  is smaller and  $k_2$  is bigger, the convergence rate of error  $e_1$  is smaller. In order to improve

the tracking speed and accuracy of the target,  $k_1$  should be smaller and  $k_2$  should be larger since  $e_2$  is the derivative of error  $e_1$ .

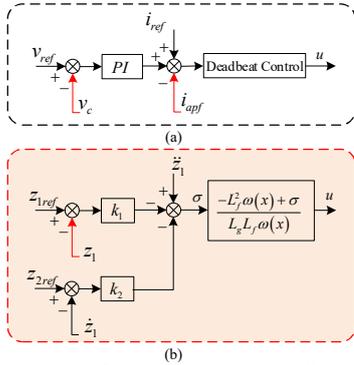


Fig. 11. Controller structure of DC-HAPF. (a) The traditional double loop control. (b) The proposed nonlinear unified control.

Based on the analysis above, the traditional double loop control and the proposed nonlinear unified controller via feedback linearization of DC-APF can be shown in Fig.11. Seen from Fig.11(a), for the traditional dual-loop control, the voltage outer loop is generally controlled by PI controller and current inner loop usually adopts the deadbeat control or other control. From Fig.11(b), the proposed nonlinear unified controller is controlled based on the APF's energy, which can realize the unified control of APF's voltage and current. Compared with the traditional double loop control, the proposed nonlinear unified controller is controlled based on the tracking error and the derivative of error simultaneously, and it has better dynamic and steady performance.

Moreover, to analyze the robustness of the proposed controller to the circuit parameters  $L_2$  and  $C_2$ , a Lyapunov function is defined as follow,

$$V = \frac{1}{2} \tilde{e}_1^2 + \frac{1}{2k_1} \tilde{e}_2^2 \quad (33)$$

where  $\tilde{e}_1$  and  $\tilde{e}_2$  are the real state error, expressed as follows,

$$\begin{cases} \tilde{e}_1 = \tilde{z}_1 - z_{1ref} \\ \tilde{e}_2 = \tilde{z}_2 - z_{2ref} \end{cases} \quad (34)$$

where  $\tilde{z}_1$  and  $\tilde{z}_2$  are the real state variables of  $z_1$  and  $z_2$ , respectively. According to (33), due to  $k_1 > 0$ ,  $\tilde{e}_1^2 \geq 0$  and  $\tilde{e}_2^2 \geq 0$ , there is  $V \geq 0$ .

Differentiating (33), there is,

$$\dot{V} = \tilde{e}_1 \dot{\tilde{e}}_1 + \frac{1}{k_1} \tilde{e}_2 \dot{\tilde{e}}_2 \quad (35)$$

According to (28), (30) and (34), there is,

$$\begin{cases} \dot{\tilde{e}}_1 = \tilde{e}_2 \\ \dot{\tilde{e}}_2 = -k_1 \tilde{e}_1 - k_2 \tilde{e}_2 \end{cases} \quad (36)$$

Substituting (36) into (35), there is,

$$\begin{aligned} \dot{V} &= \tilde{e}_1 \tilde{e}_2 + \frac{1}{k_1} \tilde{e}_2 (-k_1 \tilde{e}_1 - k_2 \tilde{e}_2) \\ &= \frac{-k_2}{k_1} \tilde{e}_2^2 \leq 0 \end{aligned} \quad (37)$$

See from (37), only when the  $\tilde{e}_2 = 0$ , there is  $\dot{V} = 0$ . Therefore, according to the Lyapunov theory, the system is stable. When the system is stable, there is,

$$\begin{cases} \tilde{e}_1 = \frac{1}{2} [(L_2 + \Delta L_2) i_{apf}^2 + (C_2 + \Delta C_2) v_c^2 - L_2 i_{ref}^2 - C_2 v_{ref}^2] = 0 \\ \tilde{e}_2 = v_{in} i_{apf} - v_{in} i_{ref} = 0 \end{cases} \quad (38)$$

where  $\Delta L_2$  and  $\Delta C_2$  are the parameter errors of  $L_2$  and  $C_2$ , respectively.

From (38), when  $\tilde{e}_2 = 0$ , there is  $i_{apf} = i_{ref}$ ; when  $\tilde{e}_1 = 0$ , there will be a fixed error for the dc voltage  $v_c$ . Moreover, when the real circuit parameter  $L_2$  or  $C_2$  is bigger, the dc voltage  $v_c$  will be slightly smaller than  $v_{cref}$ , when the real parameter is smaller, the dc voltage  $v_c$  will be slightly bigger than  $v_{cref}$ . Based on the analysis above, the circuit parameter error only affects the control of the dc voltage  $v_c$  and it does not affect the harmonic suppression effect of the DC-HAPF. Therefore, the proposed controller can suppress the harmonic current effectively, and has a strong robustness to circuit parameters  $L_2$  and  $C_2$ .

#### IV. EXPERIMENTS

To validate the feasibility of the proposed DC-HAPF and nonlinear unified controller via feedback linearization, a prototype for single-stage single-phase inverter with DC-HAPF is built in lab for verification, and the proposed control strategy is implemented in TMS320F28335. Fig.12 gives the schematic diagram of this single-stage single-phase inverter with DC-HAPF. The parameters of circuit are shown in Table I and the parameters of controllers are shown in Table II. The experimental results are shown as follows.

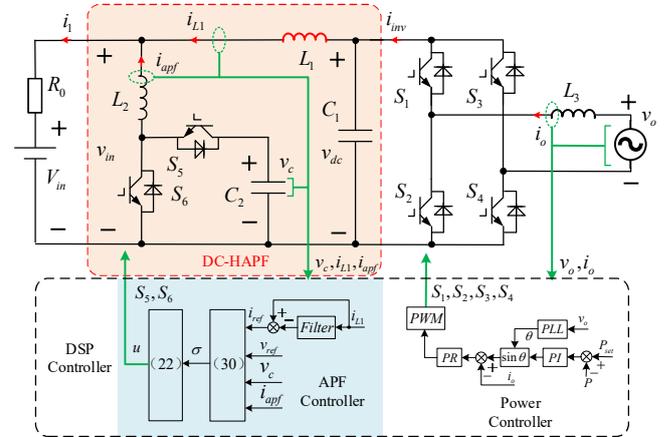


Fig. 12. Schematic diagram of the prototype.

Firstly, the harmonic suppression performances of four different kinds of filters are compared and shown in Fig.13. Compared with Fig.13(a) with filter C, the current  $i_1$  in Fig.13(b) with filter CL mainly has the SHC and less high-frequency harmonic currents. So, the switching harmonic currents can be effectively suppressed by CL filter. Seen from Fig.13(c) with filter C+APF, the SHC is suppressed. As the active power filter is difficult to suppress the high-frequency harmonics, the current  $i_1$  still has lots of high frequency harmonic components. From Fig.13(d) with filter CL+APF, the SHC and switching harmonics in the current  $i_1$  are greatly suppressed and the current  $i_1$  are much better than that of Fig.13 (b) and (c). So, the proposed DC-HAPF can effectively suppress the harmonic currents at the dc-side of single-phase inverter. Note that the current THD with C+APF is lower than that with filter C and higher than that with

filter CL since there are lots of high frequency switching harmonics. However, with the work of filter CL+APF, the THD of dc current  $i_1$  is less than 5% and is the lowest. From Fig. 13, the passive filter CL can effectively suppress the high-frequency harmonics, and it is helpful for the active power filter to compensate the low frequency harmonic currents. Therefore, the DC-HAPF can effectively suppress the lower- and high-frequency harmonic currents at the dc-side of single-phase inverter, which integrates the merits of active power filter and passive power filter.

TABLE I  
PARAMETERS OF CIRCUIT

Parameter	Value
Voltage of DC voltage source $V_{in}/V$	48
Internal resistance of DC power $R_0/\Omega$	0.01
Capacitance of CL filter $C_1/mF$	1.5
Inductance of CL filter $L_1/mH$	0.1
Capacitance of active power filter $C_2/mF$	2
Inductance of active power filter $L_2/mH$	1.5
AC voltage $v_{ac}/V$	50
Inductance $L_3/mH$	2

TABLE II  
PARAMETERS OF CONTROLLERS

Parameter	Value
Rated active power $P_{set}/W$	500
Rated reactive power $Q_{set}/W$	0
PI controller parameter $K_p$	0.001
PI controller parameter $K_I$	1
PR controller parameter $K_{PR}$	0.5
PR controller parameter $K_{PR}$	500
Capacitance voltage $v_{ref}/V$	65
PWM switching frequency $f_{pwm}/kHz$	10
Sampling frequency $f_s/kHz$	10
Controller parameter $k_1$	1
Controller parameter $k_2$	20000

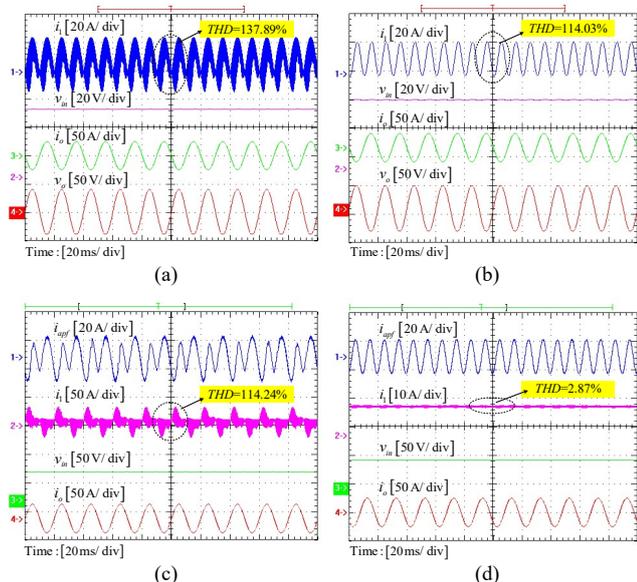


Fig. 13. Experimental waveforms with different filters. (a) With filter C. (b) With filter CL. (c) With filter C+APF. (d) With filter CL+APF.

Fig. 14 shows the experimental waveforms when the DC-HAPF is controlled by different control methods. Seen from Fig. 14(a), adopting the traditional deadbeat control, the current  $i_1$  has two oscillation processes when the power changes suddenly. When the power doubles suddenly, there will be a big input error and

a longer response time since the voltage outer loop is controlled by PI controller. Fig. 14(b) shows the experimental waveforms under the sliding mode control, where the current inner loop is controlled by sliding mode controller and the voltage outer loop is controlled by PI controller. As seen from Fig. 14(b), although the sliding mode control has good dynamic performance, the current  $i_1$  also has an oscillation process because of the current reference is affected by the voltage PI controller. From Fig. 14(c), adopting the nonlinear unified controller, since the voltage and current dual-loop control is converted to a single-loop control of energy, the current  $i_1$  basically has no oscillation process when the power changes suddenly. In addition, as the proposed controller is designed based on the tracking error and the derivative of error, the DC-HAPF can attenuate the tracking error fast, and the THD of dc current  $i_1$  is 2.87% and the lowest. Based on the analysis above, the steady and dynamic performances of the proposed nonlinear unified control are better than the ones of traditional deadbeat control and sliding mode control.

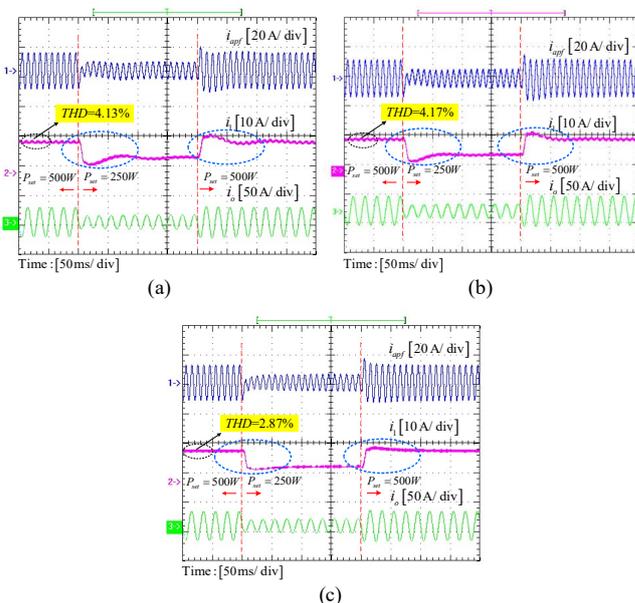


Fig. 14. Experimental waveforms under different control methods. (a) Deadbeat control. (b) Sliding mode control. (c) Proposed nonlinear unified control.

Fig. 15(a) shows the experimental waveforms under the different parameter  $k_1$ . When  $k_1$  increases from 1 to 20000 suddenly, the THD of waveform of dc current  $i_1$  decreases from 4.92% to 3.49%. Fig. 15(b) shows the experimental waveforms under the different parameter  $k_2$ . When  $k_2$  increases from 2000 to 20000 suddenly, the THD of waveform of dc current  $i_1$  decreases from 4.94% to 2.87% and the waveform is smoother. No matter increase  $k_1$  or  $k_2$ , the THD of dc current  $i_1$  will decrease. Since the parameter  $k_2$  is the coefficient of  $e_2$  in the controller and  $e_2$  is the derivative of  $e_1$ , the target tracking error  $e_1$  reduces faster and the steady state error is smaller when  $k_2$  is bigger. Therefore, the THD of dc current  $i_1$  is smaller when  $k_1=1$  and  $k_2=20000$ . In addition, to analyze the influence of the parameter  $D_k$  on filtering performance, as the duty ratio of converter is directly proportional to  $v_{ref}$ , here it will change  $v_{ref}$  to show the influence on the operation performance of DC-HAPF. Seen from Fig. 15(c), when  $v_{ref}$  is decreased from 100V to 60V, the high-frequency harmonic current in  $i_{app}$  decreases gradually

and the waveform of dc current  $i_1$  becomes better gradually. When the system is stable, the capacitor voltage  $v_c$  will be equal to  $v_{ref}$ . With the decrease of voltage  $v_c$ , the change value of current  $i_{apf}$  will decrease in the same switching cycle, and then the distortion of current  $i_{apf}$  will be narrow. Therefore, the waveform of dc current  $i_1$  is better when  $v_{ref}=60V$ .

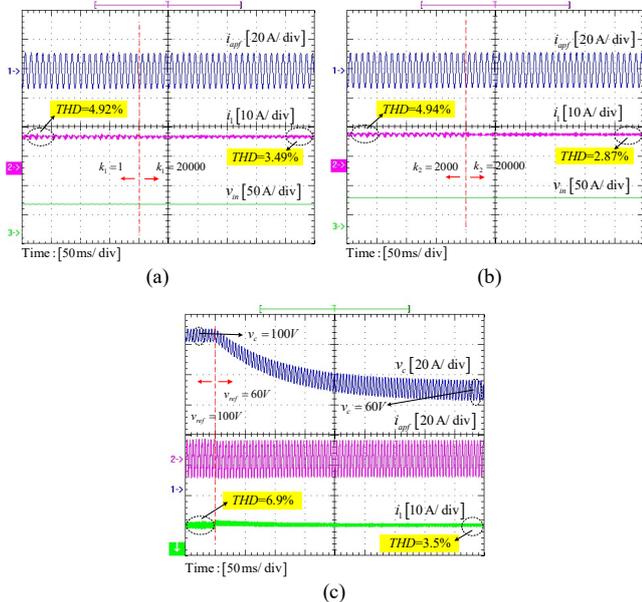


Fig. 15. Experimental waveforms under different control parameters. (a) Under different  $k_1$  when  $k_2=2000$ . (b) Under different  $k_2$  when  $k_1=1$ . (c) Under different  $v_{ref}$ .

In DC-HAPF, the inductance  $L_1$  is very important for the high frequency harmonic current suppression. The experimental waveforms with different  $L_1$  can be obtained, as shown in Fig.16.

As seen from Fig.16(a), when the value of  $L_1$  is changed from 0.1mH to 1mH, the waveforms of  $i_{apf}$  and  $i_1$  both occur oscillation. According to Fig16(b), when the value of  $L_1$  is changed from 0.1mH to 0.01mH, the current  $i_1$  also becomes worse and it has large amount of high frequency harmonic current. When the value of  $L_1$  is bigger,  $L_1$  will hinder the transmission of electrical energy. When the value of  $L_1$  is smaller,  $L_1$  cannot effectively filter out the high frequency harmonic current. So, no matter the value of inductance  $L_1$  is too big or too small, the quality of current  $i_1$  will be deteriorated. When the value of  $L_1$  changes, the current  $i_{L1}$  changes and it will affect the harmonic control effect of active filters. To better suppress harmonics, an appropriate inductance  $L_1$  is important.

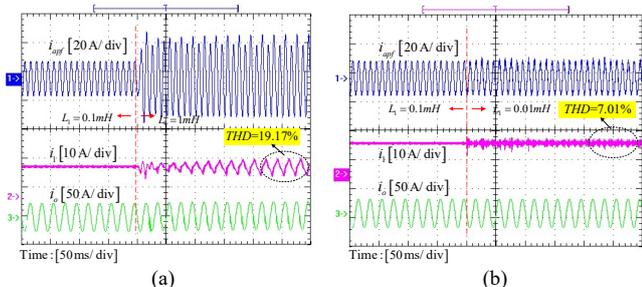


Fig. 16. Experimental waveforms under different  $L_1$ . (a) Increase  $L_1$  from 0.1mH to 1mH. (b) Decrease  $L_1$  from 0.1mH to 0.01mH.

Fig.17 shows the experimental waveforms under the disturbance of parameter  $L_2$  or  $C_2$ . Seen from Fig.17(a), when  $L_2$  is increased by 20% suddenly, the changed value of current  $i_{apf}$  will decrease at the same switching cycle, and then the output harmonic current will slightly decrease. Therefore, the harmonic suppression effect of DC-HAPF becomes better and the THD of dc current  $i_1$  becomes lower. Seen from Fig.17(b), when  $L_2$  is decreased suddenly, the changed value of current  $i_{apf}$  will increase at the same switching cycle, and then the output harmonic current will slightly rise. Therefore, the harmonic suppression effect of DC-HAPF becomes worse and the THD of dc current  $i_1$  becomes higher. From Fig.17(a) and Fig.17(b), no matter parameter  $L_2$  is bigger or smaller than normal value, the harmonic currents can be effectively suppressed by DC-HAPF and the system is stable. As seen from Fig.17(c), when  $C_2$  is increased by 20%, the fluctuations of dc voltage  $v_c$  will decrease, and then the harmonic suppression effect of DC-HAPF will be slightly better. Meanwhile, the dc voltage  $v_c$  becomes slightly smaller, which is consistent with the robustness analysis in Section III. Seen from Fig.17(d), when  $C_2$  is decreased by 20%, the fluctuations of dc voltage  $v_c$  will increase, and then the harmonic suppression effect of DC-HAPF will be slightly worse. Meanwhile, the dc voltage  $v_c$  slightly becomes bigger, which is also consistent with the robustness analysis in Section III. From Fig.17(c) and Fig.17(d), no matter parameter  $C_2$  is bigger or smaller than normal value, the harmonic currents can be effectively suppressed by DC-HAPF. Compared with the parameter  $C_2$ , the parameter  $L_2$  has a greater impact on the performance of the controller. Therefore, the DC-HAPF with non-linear unified controller via feedback linearization has a strong robustness since the proposed controller is regulated based on the tracking error and the derivative of error.

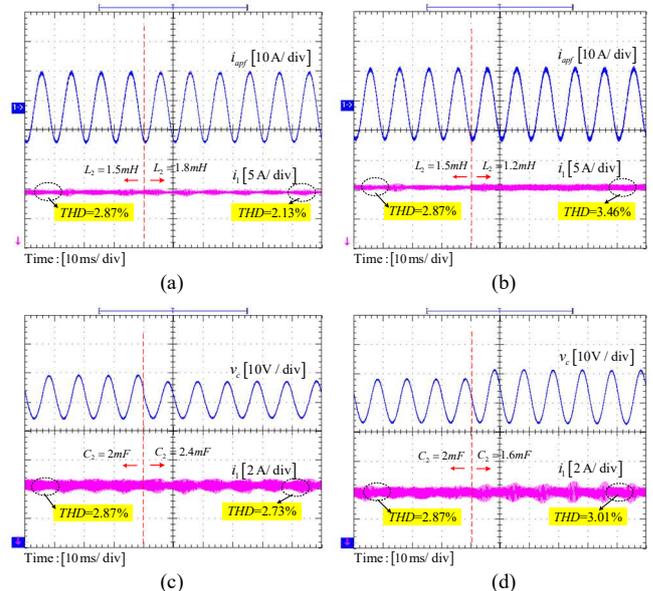


Fig. 17. Experimental waveforms under different  $L_2$  or  $C_2$ . (a) +20% change of  $L_2$ . (b) -20% change of  $L_2$ . (c) +20% change of  $C_2$ . (d) -20% change of  $C_2$ .

## V. CONCLUSION

In order to solve the dc side harmonic problem and distinguish traditional ac hybrid active filter, this paper proposed the concept of DC-HAPF. For suppressing the harmonic current at

the dc side of the single-stage single-phase inverter, a dc hybrid active power filter structure is presented, which integrates the merits of active power filter and passive power filter. Moreover, a nonlinear unified controller is proposed by applying feedback linearization theory, where the voltage and current dual-loop control is converted to a single-loop control of energy. Since the proposed controller is controlled based on the tracking error and the derivative of error, the DC-HAPF can attenuate the tracking error fast, and the robustness of the proposed controller is good. The proposed energy-based controller also has potential application value in other scenarios, which can improve the controller's performance by converting the typical voltage and current dual-loop control into a single-loop control of energy.

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