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# Effects of Virtual Resistance on Transient Stability of Virtual Synchronous Generators under Grid Voltage Sag

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ABSTRACT-The virtual synchronous generator (VSG) control of a grid-connected converter is an attractive interfacing solution for high-penetration renewable generation systems. Unfortunately, the synchronous resonance (SR) can appear due to the power control loops, which are usually damped by adopting a virtual resistance (VR). However, the effects of VR on the transient stability of the VSG are rarely studied. A virtual point of common coupling and a virtual power angle concept is proposed in this paper to represent the mathematical model of the VSG with VR damping. Based on the model, the transient stability is further analyzed using the phase portrait and the attraction regions of the nonlinear system. It reveals that the VR has a negative and different impact on transient stability, compared with the real grid resistor. In order to keep the VSG with VR to work normally during the grid voltage sag, an enhanced transient stability method, by reducing the active power commands when the grid fault is detected, is introduced. A design-oriented analysis and the parameter design with different VRs are also presented. Finally, the theoretical analysis is verified by experimental results.

*Index Terms*—Virtual synchronous generators (VSGs), transient stability, virtual resistance, synchronous frequency resonance.

#### I. INTRODUCTION

Over the past decades, more and more distributed renewable energy sources are connected to the conventional power grid, using voltage source converters (VSCs) as the interface [1]-[5]. The majority of the grid-connected VSCs are designed to operate in parallel with the conventional grid, which transfers their collected power to the grid under the constraint of grid codes. Grid-following converters can effectively control the current injected into the grid and ride through most grid faults. However, they can not operate in the standalone mode and may have stability problems when connected to a weak grid since

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Chao Wu and Frede Blaabjerg are with the Department of Energy Technology, Aalborg University, Aalborg 9220, Denmark (e-mail: cwu@et.aau.dk and fbl@et.aau.dk). their control is dependent on the voltage synchronization based on a phase-locked loop [2], [3]. Therefore, to avoid the shortcomings of the grid-following converters, grid-forming converters, inspired from the operation of synchronous generators (SGs), have been developed quickly and gained more and more attention [4], [5]. The grid-forming converters can generally provide voltage support, and they can operate in both grid-connected and standalone modes with minor changes in control.

Since the penetration of converter-based renewable energy resources is continuously growing, the existing power grid becomes weaker, i.e., the short circuit ratio (SCR) is becoming lower. As the ratio of SGs based generation decreases, the inertia of the power grid is reduced [6], which will jeopardize the frequency stability during the grid transients [7]. In order to provide inertia support for the grid, like the SGs, the concept of the virtual synchronous generators (with various names such as VSG, virtual synchronous machine, synchronverter, etc.) has been reported in [8]-[12]. In this paper, for the sake of convenience, all these similar control methods are referred to as VSG, which intends to mimic the swing equation of an SG in a converter and emulate the kinetic energy of a rotating mass by adding a short term energy storage. As one of the grid-forming control strategies, VSG controlled converter can support both voltage and frequency simultaneously.

In addition to frequency and voltage support, the VSG can also improve the small-signal stability of the multi-converter system under a weak grid [13], [14]. However, the integration of VSGs will inevitably influence the low-frequency oscillations (LFOs) in power grids, which are usually caused by the interactions among different VSGs. In order to mitigate the LFOs, a parameter alternating VSG controller is proposed by changing the inertia and droop coefficients flexibility [15]. In [16], a positive damping torque method is presented for damping the LFOs. Besides the LFOs caused by the integration of VSGs, there may also be subsynchronous resonance (SSR) when VSG is connected to a series-compensated grid. The virtual impedance method is introduced for suppressing the SSR in [17], [18]. Despite the LFOs and SSR, several investigations have shown that synchronous resonance (SR) is another typical instability of the grid-connected VSG, which inherently exists in the power control loop [19]-[23]. By adding a real resistor to the output of the converter, the grid resistance

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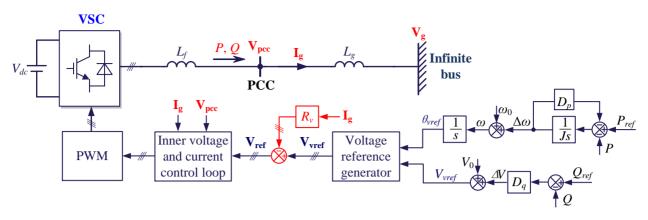


Fig. 1. General topology and control scheme of a three-phase grid-connected VSG using the virtual resistance damping.

can be equivalently increased, which is able to dampen the SR. Still, it causes extra loss and reduces system efficiency. Especially in the high-voltage power grid, the inductive line impedance is typically much higher than the resistive one, where the resistance can be neglected without making any significant error [24]. Thus, the virtual resistance (VR) is inevitably employed in the control loop and inserted into line impedance so that the SR can be suppressed without introducing any power loss. However, most of the research is only focused on the small-signal analysis of the VSG. For the VR properties, and the illustration, selection recommendation have been studied in detail from a small-signal stability perspective over the years [20]-[23]. Yet, the effects of VR on large-signal transient stability are rarely studied.

In contrast to the small-signal stability analysis, only a few studies on transient stability of the VSG, i.e., the ability of the VSG to maintain synchronization with the grid when subjected to a large disturbance [25]-[29], have been reported. In [25], it has been found there is a conflict between the frequency response and the transient stability, indicating large inertia may drive the VSG to lose stability during a large disturbance. A transient damping control method is proposed in [26] based on Lyapunov's direct method. The transient stability can be enhanced, but the design method for the additional damping coefficient is absent. A mode-switching control method is further reported in [27] for riding through the grid voltage sag by changing the VSG mode during the grid faults. However, the mode detection block uses a differentiation element, which may cause a lot of noise and unexpected system instability. Thus, it is challenging to be implemented in practice. Meanwhile, there will be oscillation within a hysteresis boundary when the VSG didn't have an equilibrium point after the grid voltage sag by using the mode-switching control method. The transient stability of a single-loop voltagemagnitude (SLVM) controlled VSG is analyzed in [28]. It was found that the voltage reference of the point of common coupling (PCC) is not ideally tracked in such a control scheme. The output filter  $L_f$  must be considered in SLVM control, which will reduce the power transfer capability, indicating a negative impact on transient stability. Moreover, the overcurrent limitation can not be embedded as there is no inner current loop.

The authors in [29] overview the grid-synchronization stability of the converter-based resources, including the VSG control. However, all of these studies overlooked the effects of VR on transient stability.

This paper is going to fill this gap, and the main contributions can be summarized as

1. A virtual PCC and a virtual power angle are proposed to derive the mathematical model of the VSG with VR damping. Differing from the grid resistance, VR is implemented in control and equivalently appears before the PCC, rather than after the PCC. Consequently, the effects of the VR are different from the grid resistance, which is modeled based on the virtual PCC and virtual power angle.

2. The transient stability is analyzed using the phase portrait and the attraction regions of the VSG with VR damping. It reveals that the impacts of VR on transient stability are opposite from the grid resistance, which narrowed the VSG's stability region, resulting in reducing the active power transfer capability.

3. In order to keep the VSG work normally during the grid voltage sag, an improved method, by reducing the active power reference commands when the grid fault is detected, is introduced to enhance the transient stability. A design-oriented analysis and the parameter design with different VRs are also presented based on the phase portrait of the VSG.

This paper is organized as follows. The VSG configuration and SR phenomena are presented in Section II. The virtual PCC and virtual power angle are proposed in Section III. The effects of the VR on transient stability are studied and revealed by the phase portrait analysis and the attraction region of the nonlinear system. Section IV introduces a transient stability enhancement method by reducing the active power reference during the grid voltage sag to avoid the negative impacts. Detailed parameter design guidelines of the coefficient parameters are also presented. The theoretical analysis is verified in Section V by experimental results, and the conclusion is drawn in Section VI.

## II.A GLIMPSE OF THE VSG SYSTEM AND SR PHENOMENA

## A. The VSG System Description

Fig. 1 shows the general topology and control scheme of a grid-connected VSG, including the VR for active damping. A three-phase converter is connected to the traditional power grid

at the PCC through an inductor filter  $L_f$ . The grid is modeled as an infinite bus connected in series with an impedance [19], [21], i.e., an inductance  $L_g$  and a resistor  $R_g$ .  $\mathbf{V_g} = V_g e^{j\omega_g t}$  is the space vector of the grid voltage, where  $\omega_g$  usually is equal to the synchronous angular frequency  $\omega_0$ .  $\mathbf{V_{pcc}} = V_{pcc} e^{j\theta_{pcc}}$  and  $\mathbf{I_g}$ represents the voltage and current space vectors of the PCC voltage and current, respectively, where  $\theta_{pcc}$  is the PCC voltage phase. *P* and *Q* represent the active and reactive power injected into the grid from the PCC. Generally, a large capacitor is used on the dc side, or energy storage is employed to make an inertia contribution, where the dc voltage is taken over by the frontend converter [19] or by the energy storage converter [30]. Hence, constant dc-link voltage is adopted in this paper when studying the transient stability of the VSG as in [25], [27]-[29].

As shown in Fig. 1,  $P_{ref}$  and  $Q_{ref}$  are the active and reactive power references, respectively. The power control is implemented with VSG control to generate the PCC voltage reference, i.e.,  $V_{vref} = V_{vref} e^{i\theta_{vref}}$ .  $R_v$  is the VR for active damping, which is used to suppress the synchronous resonance of VSG [19]-[23]. The PCC voltage reference is changed to Vref, given as  $V_{ref} = V_{vref} - R_{v}I_{g}$ . Usually, inner voltage and current control loops are employed to force  $V_{pcc}$  to track the reference and provide overcurrent protection with limiting the current reference. It should be noted that the outer power control loop mainly determines the transient stability because the bandwidth of the inner loop is usually designed much higher than that of the outer power control loops [2]. Thus, the inner control loop can be regarded as one during the transient stability analysis. Due to the decoupled timescales, an ideal voltage reference tracking is assumed, i.e.,  $V_{pcc} = V_{ref}$ . If a severe grid fault occurs, resulting in the overcurrent protection is triggered, the control scheme should be changed to grid-following control. Under this condition, the transient stability problems are mainly caused by PLL, which has been studied and explained in [31]. Thus, this paper only focuses on the VSG's transient stability under a light grid voltage sag, which won't trigger the overcurrent protection.

To implement the VSG control scheme, the active power control loop is used to adjust the phase of the PCC voltage reference, i.e.,  $\theta_{vref}$ , by emulating the swing equation of the SG, as shown in Fig. 1.  $\omega$  is the angular frequency of the VSG, and  $\omega = \omega_0 + \Delta \omega$ , which can be derived from Fig. 1, given in the complex frequency domain with Laplace transformation as

$$\omega(s) = \omega_0(s) + \frac{1}{Js + D_p} \cdot \left(P_{ref}(s) - P(s)\right) \tag{1}$$

where J and  $D_p$  are the virtual inertia and droop gain of frequency governor.  $\omega(s)$ ,  $\omega_0(s)$ ,  $P_{ref}(s)$  and P(s) are the Laplace transformed variables of  $\omega$ ,  $\omega_0$ ,  $P_{ref}$  and P, respectively.

The reactive power-voltage (Q-V) droop control is adopted for the reactive power control, which is used to regulate  $V_{vref}$ , where the control law of which in the complex frequency domain is given by

$$V_{vref}\left(s\right) = V_0\left(s\right) + D_q\left(Q_{ref}\left(s\right) - Q(s)\right) \tag{2}$$

where  $V_0$  is the normal magnitude of the grid phase voltage, and  $D_q$  is the droop coefficient of the *Q*-*V* droop control.  $V_{vref}(s)$ ,  $V_0(s)$ ,  $Q_{ref}(s)$  and Q(s) are the Laplace transformed variables of  $V_{vref}$ ,  $V_0$ ,  $Q_{ref}$  and Q, respectively.

## B. Synchronous Resonance Analysis

In a rotating reference frame with the *d* axis aligned with  $V_g$ ,  $V_{gdq}$  and  $v_{pdq}$  are defined as the voltage vectors of  $V_g$  and  $V_{pcc}$  in *dq*-frame, which are thus expressed as

$$\mathbf{V}_{\mathbf{gdq}} = V_g \quad \mathbf{v}_{\mathbf{pdq}} = V e^{j\delta} \tag{3}$$

where  $\delta$  is defined as the power angle, representing the phase difference between **V**<sub>pcc</sub> and **V**<sub>g</sub>, i.e.,  $\delta = \theta_{pcc} - \theta_g$ . Then, the dynamics of the main circuit can be described in *dq*-frame as

$$L_{g} \frac{d\mathbf{\hat{i}}_{gdq}}{dt} = \mathbf{v}_{pdq} - V_{g} - R_{g} \mathbf{\hat{i}}_{gdq} - jX_{g} \mathbf{\hat{i}}_{gdq}$$
(4)

Denoting the steady operating point in (3) and (4) with subscript "e", and the small-signal deviation added on the steady-state with a cap " $^{n}$ ". Then linearizing (4) around the operating point, it is found that

$$\mathbf{V}_{\mathbf{pdqe}} = V_e e^{j\delta_e} \quad \hat{\mathbf{v}}_{\mathbf{pdq}} = e^{j\delta_e} \left( \hat{v} + jV_e \hat{\delta} \right) \tag{5}$$

$$\mathbf{I}_{gdqe} = \frac{V_e e^{j\delta_e} - V_g}{R_g + jX_g} \tag{6}$$

$$L_{g} \frac{d\mathbf{\hat{i}}_{gdq}}{dt} = \hat{\mathbf{v}}_{pdq} - R_{g} \hat{\mathbf{\hat{i}}}_{gdq} - jX_{g} \hat{\mathbf{\hat{i}}}_{gdq}$$
(7)

By applying a Laplace transform to (7), yields

$$\hat{\mathbf{I}}_{gdq}\left(s\right) = \frac{\hat{\mathbf{V}}_{pdq}\left(s\right)}{sL_{g} + R_{g} + jX_{g}}$$
(8)

The complex power deviation can be expressed as

$$\hat{S} = 1.5 \left( \mathbf{V}_{\mathbf{pdqe}} \hat{\mathbf{i}}_{\mathbf{gdq}}^* + \mathbf{I}_{\mathbf{gdqe}}^* \hat{\mathbf{v}}_{\mathbf{pdq}} \right) = \hat{P} + j\hat{Q}$$
(9)

where the superscript asterisk \* denotes conjugation operator.

As in a high-voltage network, the inductance of the line impedance is much higher than the resistance. Thus the power coupling can be ignored, i.e.,  $\hat{P}$  is mainly determined by  $\hat{\delta}$ and  $\hat{v}$  affects  $\hat{Q}$  a lot. Substituting (5), (6), and (8) into (9), the transfer functions from  $\hat{P}(s)$  to  $\hat{\delta}(s)$  and from  $\hat{Q}(s)$ to  $\hat{v}(s)$  can be derived as

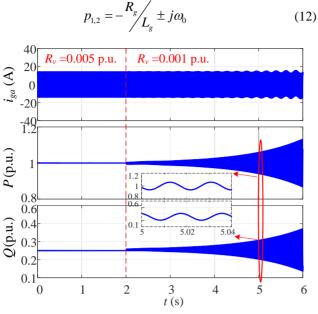
$$G_{\delta p}(s) = \frac{\hat{P}(s)}{\hat{\delta}(s)} = \frac{-Q_e(sL_g + R_g)^2 - Q_eX_g^2 + 1.5V_e^2X_g}{(sL_g + R_g)^2 + X_g^2}$$
(10)

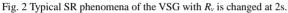
$$G_{vq}(s) = \frac{\hat{Q}(s)}{\hat{v}(s)} = \frac{\frac{Q_e}{V_e} (sL_g + R_g)^2 + \frac{Q_e}{V_e} X_g^2 + 1.5V_e X_g}{(sL_g + R_g)^2 + X_g^2}$$
(11)

From (10) and (11), it can be seen that  $G_{\delta p}(s)$  and  $G_{\nu q}(s)$ 

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contain a pair of conjugate poles, which are deduced as





Thus, when  $R_g/X_g$  is very low, the poles will move closer to the imaginary axis. Consequently, the oscillation near the synchronous frequency  $\omega_0$  can be potentially triggered, which is the root cause of SR. Therefore,  $R_v$  is usually used to suppress the SR when  $R_g/X_g$  is very small. Fig. 2 shows the typical phenomena of the SR, which is triggered by decreasing  $R_v$  from 0.005 p.u. to 0.001 p.u. at 2s.

Based on the above analysis, it can be seen that  $R_{\nu}$  is inevitably adopted to damp the SR from a small-signal stability perspective. However, the effects of  $R_{\nu}$  on transient stability are still unknown, which should be further investigated.

### III. TRANSIENT STABILITY ANALYSIS WHEN CONSIDERING VIRTUAL RESISTANCE

Generally, The dynamic performance of  $\delta$  determines the transient stability of the VSG during the grid voltage sag studied in this paper. The transient stability is guaranteed if  $\delta$  can be attracted to a stable steady-state value after the grid voltage sag. Otherwise, the system will lose stability if  $\delta$  diverges to infinite.

Without the VR damping control,  $V_{pcc} = V_{vref}$  and  $\theta_{pcc} = \theta_{vref}$ . Thus, *P* and *Q*, can be easily derived using  $V_{vref}$  and  $\theta_{vref}$ . Combining with (2),  $V_{pcc}$  can be solved as a function of  $\delta$ , and the relationship *P*- $\delta$  can be derived. However, when  $R_v$  is used,  $\mathbf{V}_{pcc} = \mathbf{V}_{ref} = \mathbf{V}_{vref} - R_v \mathbf{I}_g$ , which can be expressed with  $\delta$  as follows

$$V_{pcc}e^{j\delta} = V_{vref}e^{j\theta_{vref}} - R_v \cdot \frac{V_{pcc}e^{j\delta} - V_g}{j\omega_0 L_g}$$
(13)

On the other hand, substituting Q into (2),  $V_{vref}$  can be deduced as the function of  $V_{pcc}$  and  $\delta$ , i.e.,  $V_{vref}$  ( $V_{pcc}$ ,  $\delta$ ). Combining with (13), the intermediate variables  $V_{vref}$  and  $\theta_{vref}$ should be eliminated to derive the relationship between  $V_{pcc}$  and  $\delta$ , finally getting the P- $\delta$  relationship for transient stability analysis. But, due to the nonlinear trigonometric functions in (13), the explicit analytical expressions for  $V_{pcc}(\delta)$  can not be solved. Thus, the P- $\delta$  relationship can not be obtained with an explicit mathematical analysis expression when  $R_v$  is adopted. To solve this problem, a virtual PCC is proposed in this paper for analyzing the effects of  $R_v$  on transient stability.

## A. A Virtual PCC Proposed for Analyzing the Transient Response with $R_{\nu}$

The virtual PCC, which is equivalently derived from the control diagram, is before the real PCC, as shown in Fig. 3. The space vector of the virtual PCC voltage is denoted as  $\mathbf{V}_{vref}$ . The virtual power angle  $\delta_{vir}$  is thus defined as  $\delta_{vir} = \theta_{vref} - \theta_g$ . The active and reactive power transmitted from the virtual PCC to the grid, denoted as  $P_{vir}$  and  $Q_{vir}$ , can be easily obtained. Then, the power injected into the grid from the real PCC, i.e., P and Q, can be derived by using  $P_{vir}$ ,  $Q_{vir}$ , based on (14) and (15). Substituting (15) into (2), the relationship between  $V_{vref}$  and  $\delta_{vir}$  can be derived, which is shown in (16). Note that (14), (15), and (16) are shown at the bottom of this page, where  $R_{eq} = R_g + R_v$ ,  $K_X$  and  $K_R$  are

$$K_{X} = \frac{X_{g}}{R_{eq}^{2} + X_{g}^{2}}, \quad K_{R} = \frac{R_{eq}}{R_{eq}^{2} + X_{g}^{2}}$$
(17)

It should be noted that the power loss on  $R_v$  is not real, which is implemented in the control diagram and equivalently changes the power transmission.

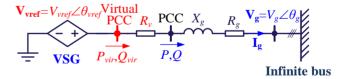


Fig. 3. Equivalent circuit of the VSG using virtual resistance damping.

$$P = P_{vir} - \frac{2}{3} \cdot \frac{\left(P_{vir}^{2} + Q_{vir}^{2}\right)R_{v}}{V_{vref}^{2}} = \frac{3}{2} \cdot \frac{R_{v}\left(V_{vref}V_{g}\cos\delta_{vir} - V_{g}^{2}\right) + X_{g}V_{vref}V_{g}\sin\delta_{vir} + R_{g}\left(V_{vref}^{2} - V_{vref}V_{g}\cos\delta_{vir}\right)}{R_{eq}^{2} + X_{g}^{2}}$$
(14)

$$Q = Q_{vir} = \frac{3}{2} \cdot \frac{X_g \left( V_{vref}^2 - V_{vref} V_g \cos \delta_{vir} \right) - R_{eq} V_{vref} V_g \sin \delta_{vir}}{R_{eq}^2 + X_g^2}$$
(15)

$$V_{vref} = \frac{1.5K_x D_q V_g \cos \delta_{vir} + 1.5K_R D_q V_g \sin \delta_{vir} - 1 + \sqrt{\left(1.5K_x D_q V_g \cos \delta_{vir} + 1.5K_R D_q V_g \sin \delta_{vir} - 1\right)^2 + 6K_x D_q (V_0 + D_q Q_{ref})}}{3K_x D_q}$$
(16)

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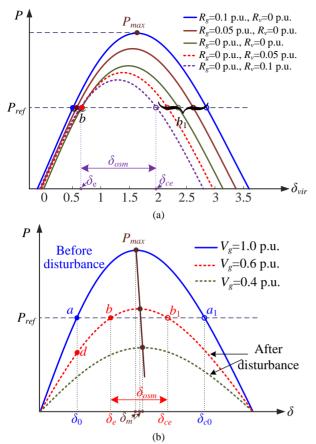


Fig. 4. P- $\delta_{vir}$  curves for (a) with different  $R_g$  and different  $R_v$  when  $V_g = 1.0$  p.u., and (b)  $R_g = 0$ ,  $R_v = 0$  when the grid voltage drops. The other parameters are the same as given in Table I in Section V.

Substituting (16) to (14), the instantaneous relationship between *P* and the virtual power angle  $\delta_{vir}$  can be obtained. The corresponding *P*- $\delta_{vir}$  curves with different VR and different grid resistors are plotted in Fig. 4(a). From there, it can be found that considering the impacts of the reactive power control loop, the effects of  $R_v$  and  $R_g$  on the active power transmission capability of the PCC are very different. The maximum power  $P_{max}$  that can be transmitted becomes higher with a larger  $R_g$ . However,  $P_{max}$  is reduced with a larger  $R_v$ .

To demonstrate the principle of transient instability, Fig. 4(b) illustrates the conceptual P- $\delta$  curves of the VSG with different grid voltage sags, where  $\omega_g = \omega_0$  is assumed as the steady-state angular frequency after a disturbance for illustration convenience. There are two types of transient problems with different depths of grid voltage sag, i.e., the equilibrium point exists or not. According to IEEE Standards 1547-2018 [32], the VSG should continue to supply power at least for 10 s when the grid voltage drops to 0.5-0.8 p.u., indicating that the VSG should keep working normally during the fault for a long time. Therefore, this paper aims to promote the VSG to have equilibrium points and ride through the grid fault, as shown with the dashed red line in Fig. 4(b). There are two equilibrium points, i.e., b and  $b_1$ , representing the stable equilibrium point (SEP) and the unstable equilibrium point (UEP). The corresponding power angles are denoted as  $\delta_e$  and  $\delta_{ce}$ . During the transient period, the system should not go across  $b_1$ .

Otherwise, it will lose synchronization with the grid, and  $\delta$  will go beyond  $\delta_{ce}$  and then go to infinite.

Therefore,  $\delta_{osm} = \delta_{ce} - \delta_e$  is the maximum allowed power angle overshoot. If  $\delta$  does not go beyond  $\delta_{ce}$  during the transient period, the system can finally operate stably at point *b*.

From Fig. 4(a), it can be found that not only the effects of  $R_{e}$ and  $R_{\nu}$  on the active power transmission capability are different, but also on the variation range of the virtual power angle  $\delta_{vir}$ .  $\delta_{osm}$  is much larger with a larger  $R_g$ . However, the impacts of  $R_v$ are the opposite. The variation range of  $\delta_{vir}$  is narrowed with a larger  $R_{\nu}$ . Although increasing  $R_{\rho}$  and  $R_{\nu}$  can both suppress the synchronous resonance, the influences on transient stability will be completely different. In practice, the performance of  $\delta$ determines the VSG transient instability. Here,  $\delta$  is replaced by the response of the virtual power angle  $\delta_{vir}$ . From Fig. 4, it can also be found that although the power transmission capability varies with different  $R_g$  and  $R_v$ , all the *P*- $\delta_{vir}$  curves have a similar sinusoidal trend as the *P*- $\delta$  relationship without  $R_{e}$  and  $R_v$  in Fig. 4(b). P goes up first monotonously to  $P_{max}$  with the increase of  $\delta_{vir}$ , and then monotonously declines to zero. The grid resistor  $R_g$  can benefit the transient performance due to that  $P_{max}$  is higher, and the maximum allowed power angle overshoot  $\delta_{osm}$  is wider with  $R_g$ . Yet, increasing  $R_g$  will increase the power loss and reduce system efficiency. In order to suppress the synchronous resonance and avoid additional power loss, virtual resistance  $R_{y}$  is usually adopted. However, from Fig. 4, it can be concluded that adding  $R_{\nu}$  makes the transient performance worse. Since  $P_{max}$  is lower and  $\delta_{osm}$  is narrowed with a larger  $R_{\nu}$ , it will jeopardize the transient power angle stability.

Remarks: it should be noted that the maximum power  $P_{max}$  in Fig. 4(a) is not the static power transfer limit which ignores the dynamic states and control strategy [33]. The power transfer capability in this paper is calculated according to the specific control strategy, which affects the modulation index, leading to different  $P-\delta_{vir}$  curves obtained by using different virtual resistances.

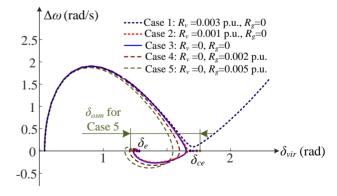


Fig. 5. The nonlinear system's phase portrait with different  $R_g$  and  $R_v$  when the grid voltage drops from 1 p.u. to 0.6 p.u.

#### B. The Transient Behaviors Based on the Phase Portrait

To figure out how the performances and responses are affected by using VR, the dynamic model needs to be established first. According to the previous analysis, it can be

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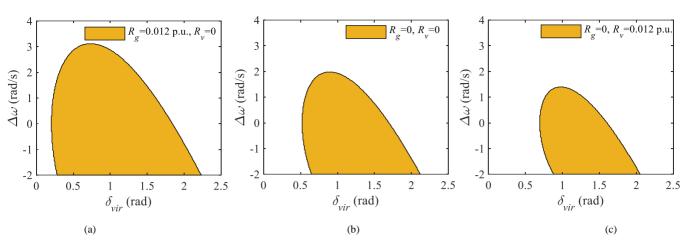


Fig. 6. Attraction region of the VSG with different  $R_g$  and  $R_v$  when the grid voltage drops to 0.6 p.u., (a)  $R_g = 0.012$  p.u.,  $R_v = 0$ ; (b)  $R_g = 0$ ,  $R_v = 0$ ; (c)  $R_g = 0$ ,  $R_v = 0$ ,  $R_v = 0.012$  p.u.

known that the system is a second-order nonlinear system. The dynamic response of the virtual power angle can be represented in the standard form as

$$\begin{bmatrix} \dot{\delta}_{vir} \\ \Delta \dot{\omega} \end{bmatrix} = \begin{bmatrix} \Delta \omega + \omega_0 - \omega_g \\ -\frac{D_p}{J} \Delta \omega - \frac{P(\delta_{vir})}{J} + \frac{P_{ref}}{J} \end{bmatrix}$$
(18)

where dot (·) denotes time derivative, and  $P(\delta_{vir})$  is shown in (14).

By setting all the differential items, i.e., the left terms in (18), to zero, the equilibrium point  $\mathbf{x}_e = [\delta_{vire}, \Delta \omega_e]^T$  can be derived. This implies  $\Delta \omega_e = \omega_g - \omega_0$ , and  $\delta_{vire}$  should satisfy that

$$P(\delta_{vire}) = P_{ref} - D_p \left( \omega_g - \omega_0 \right)$$
(19)

The influence of  $R_g$  and  $R_v$  on the transient behavior is illustrated in Fig. 5 based on the phase portrait of the system in (18). It can clearly be observed that increasing  $R_v$  narrows the allowable range for the overshoot of  $\delta_{vir}$ . As a result, the peak power angle during the transient period is more closed to the UEP or even goes beyond it and causes instability. Such as a larger  $R_v$ , i.e.,  $R_v = 0.003$  p.u., can cause the loss of synchronization with the grid, even when the equilibrium points exist. In contrast, a larger  $R_g$  can broaden the allowable range for the overshoot of  $\delta_{vir}$ , leading to a peak power angle much smaller than the UEP during the transient period, enhancing the transient stability of the system.

The phase portrait showed the performances of the virtual power angle and frequency changes during the grid voltage sag. However, it is just based on one initial condition, which cannot predict and analyze what will happen with different initial states. Thus, the attraction region with the different initial states is also derived in Fig. 6 to investigate the effects of  $R_g$  and  $R_v$  further. If the initial state belongs to the attraction region, the VSG will be stable after the grid voltage drops to 0.6 p.u.. From Fig. 6, it can clearly be observed that the attraction region can be expanded with the increase of  $R_g$  but reduced by adding  $R_v$ , which verifies that  $R_v$  has negative impacts on the transient stability.

Obviously, there is a conflict by adding  $R_{\nu}$ . When the parasitic  $R_g$  in the circuit is too small, especially in the high-voltage power grid, adding  $R_{\nu}$  is necessary to suppress the synchronous resonance. However,  $R_{\nu}$  is unexpected from a transient stability perspective. Therefore, there is an urgent demand to weaken the effects of  $R_{\nu}$  on transient stability.

## IV. REDUCING THE ACTIVE POWER REFERENCE TO ENHANCE TRANSIENT STABILITY

## A. Effect of Power Reference During the Grid Voltage Sag

From the analysis mentioned above, the main cause for the transient instability is the large virtual power angle overshoot with narrowed allowable range while  $R_{\nu}$  is adopted. Thus, a natural ideal for stability enhancement is to broaden the allowable range of  $\delta_{vir}$ , which can be easily achieved by reducing the active power reference when the grid voltage drops, as shown in Fig. 7. Once grid fault occurs,  $P_{ref}$  is reduced to  $P_{refn}$ , the SEP and UEP are thus changed from b,  $b_1$  to  $b_n$ ,  $b_{1n}$ , respectively. As a consequence, the allowable overshoot range of  $\delta_{vir}$ , i.e.,  $\delta_{osmn}$ , is much wider than the original one  $\delta_{osm}$ , which can effectively enhance the transient stability.

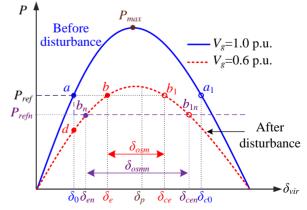


Fig. 7. The diagram of P- $\delta_{vir}$  curves with reduced active power reference when grid voltage drops.

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#### B. Design of Power Reference During Grid Voltage Sag

Although reducing the active power reference during the transient period is effective, detecting the grid fault and how to design  $P_{refn}$ , need to be discussed further.

Since the transient problems are caused by grid voltage sag, which also leads to a voltage drop on  $V_{pcc}$  (so as  $V_{vref}$ ), thus,  $V_{pcc}$ (or  $V_{vref}$ ) can be used to detect whether the grid voltage sag occurs. Fig. 8 shows the normal values of  $V_{vref}$  with different power requirements. From there, it can be seen that  $V_{vref}$  will increase when  $Q_{ref}$  increases, which can help improve the transient behaviors. However, Vvref declines with a larger active power requirement. The worst case is that  $V_{vref}$  decreases to 0.977 p.u. when  $Q_{ref} = 0$ ,  $P_{ref} = 1$  p.u. without  $R_g$  and  $R_v$ . If  $R_g$ and  $R_v$  are considered, the minimum  $V_{vref}$  rises a bit at the normal operation. In order to keep a margin, the threshold voltage level of detecting the grid voltage sag is setting at 0.95 p.u., i.e.,  $V_{vrefth} = 0.95$  p.u.. Once  $V_{vref} \ll V_{vrefth}$  is detected, indicating the grid voltage sag occurs, a power reduction, which is related to the voltage drop, is introduced to the active power reference, as shown in Fig. 9. There is a switch, i.e., k, which is 1 when the grid fault is detected. If  $V_{vref} > V_{vrefth}$ , k = 0, then the additional path does not affect the normal operation. It should be noted that increasing  $Q_{ref}$  can also enhance the transient stability when a voltage sag occurs. However,  $P_{ref}$  should be reduced simultaneously due to the grid-connected converter's limited capacity in reality. There is a rated apparent power for each converter, which cannot be exceeded. Therefore, increasing  $Q_{ref}$  and decreasing  $P_{ref}$  should be combined and optimized together, which is worthy of more in-depth study.

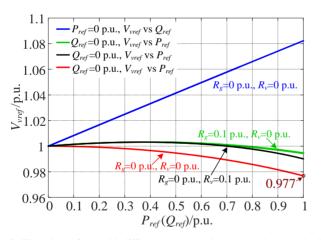


Fig. 8. The values of  $V_{vref}$  with different power requirements under normal grid voltage.

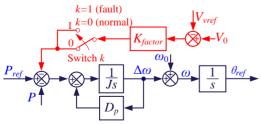


Fig. 9. Block diagram of the active power control loop with  $P_{nef}$  reduction during the grid voltage sag.

From Fig. 9, the dynamic of the second-order nonlinear system is changed differently from (18), which can be derived as

$$\begin{bmatrix} \dot{\delta}_{vir} \\ \Delta \dot{\omega} \end{bmatrix} = \begin{bmatrix} \Delta \omega + \omega_0 - \omega_g \\ -\frac{D_p}{J} \Delta \omega - \frac{P(\delta_{vir})}{J} + \frac{P_{ref}}{J} - \frac{K_{factor} \left( V_0 - V_{vref} \left( \delta_{vir} \right) \right)}{J} \end{bmatrix}$$
(20)

where  $P(\delta_{vir})$  and  $V_{vref}(\delta_{vir})$  are shown in (14) and (16), respectively.

From Fig. 9 and (20), we can know that the coefficient  $K_{factor}$ is the key factor for enhancing transient stability. Thus, it is an important issue to design this factor. According to (20), the transient behaviors with the method of reducing  $P_{ref}$  are illustrated in Fig. 10 by using the phase portrait. It can be observed that without the additional power reduction path, instability occurs when the grid voltage drops from 1 p.u. to 0.6 p.u. with  $R_v = 0.015$  p.u.. In the same case, the instability can be avoided by increasing the coefficient factor  $K_{factor}$ , due to the enlarged allowable range of  $\delta_{vir}$ . Otherwise, instability can occur if  $K_{factor}$  is not large enough, i.e.,  $K_{factor} = 0.5$ . Furthermore, as can be seen from the figure, the maximum frequency deviation  $\Delta \omega_{max}$  is decreased a lot for case 5 compared with case 1. This means the proposed control strategy can also reduce the frequency deviations during the grid voltage sags, which benefits the frequency stability during the transient period.

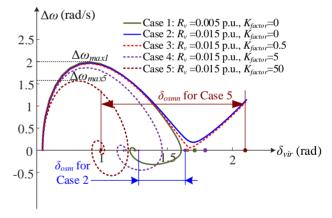


Fig. 10. The influence of parameters  $K_{factor}$  on the phase portrait of the VSG with  $R_g = 0.003$  p.u. when  $V_g = 1 \rightarrow 0.6$  p.u..

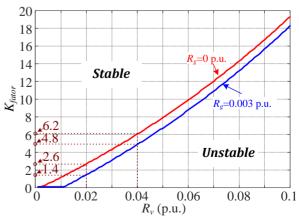


Fig. 11. The required  $K_{factor}$  for specified  $R_g$  and  $R_v$  when  $V_g = 1 \rightarrow 0.6$  p.u.

Although a larger  $K_{factor}$  is beneficial for transient stability, it will also reduce the transferred active power more. According to IEEE Standards 1547-2018 [24], the VSG should keep providing power normally for a long time when the grid voltage drops to 0.5-0.8 p.u. Thus, too large  $K_{factor}$  can not be accepted. How to obtain a critical  $K_{factor}$  for a specified  $R_v$  is urgently needed. Using Matlab command "ode45" to solve the nonlinear state equations in (20) by sweeping  $K_{factor}$  from a large value to a small one with a tiny calculation step, the critical value can be obtained. The procedure was then repeated to find all critical values of  $K_{factor}$  under different  $R_g$  and  $R_v$  settings, as shown in Fig.11, where the stable and unstable regions of operation are located above and below the boundary line, respectively. It can be seen that the minimum required  $K_{factor}$  for the stable operation increases with the increase of  $R_{\nu}$ . Meanwhile, a larger  $R_{g}$  can make the minimum required  $K_{factor}$  decline. For example, if  $R_v = 0.02$  p.u,  $K_{factor} > 1.4$  is required when  $R_g = 0.003$  p.u., but  $K_{factor} > 2.6$  must be adopted for  $R_g = 0$  p.u.

It is worth noting that the analysis methodology for a transient issue and the stability assessment in this paper can be applied to the other types of grid disturbances using a similar procedure. The enhancement method for transient stability is also effective during other types of grid faults, such as a grid impedance change. There is another concern about the power balance when decreasing the active power reference during the grid faults. However, it should be noted that the power balance is not maintained by one converter at the fault side, which is usually achieved by secondary or tertiary control from a systematic view. In this paper, only the primary control of the converter is mainly focused on and studied during the grid faults. Thus, the detailed power balance issue during grid faults is out of the scope of this paper.

## V. EXPERIMENTAL VERIFICATION

To verify the theoretical analysis for the effects of the VR on transient stability, meanwhile, to validate the improved method of reducing the active power reference, experiments are carried out with a three-phase grid-connected converter. The experimental setup is shown in Fig. 12. A constant dc voltage supply provides the input dc voltage, and a Chroma grid simulator is employed to emulate the infinite bus. The dSPACE DS1007 platform is used to implement the control strategies, where the needed voltage and current are measured by the dSPACE DS2004 A/D board. The calculated active power and the power angle are transmitted to the oscilloscope through the DS2102 D/A board. For example, the phase angles of  $V_{pcc}$  and Vg are measured by two PLLs in the dSPACE DS1007 platform, denoting as  $\theta_{pcc}$  and  $\theta_{g}$ . Then, the power angle is  $\delta = \theta_{pcc} - \theta_{g}$  is calculated, which is further transmitted to the oscilloscope through the DS2102 D/A board.

The main parameters of the VSG are presented in Table I, where a low voltage and power level were intentionally chosen for the convenience of establishing an experimental setup. SCR is set at 2 to emulate a weak grid. Thus, the grid inductance is calculated as 12 mH.  $D_p$  and  $D_q$  are the droop coefficients selected according to the grid codes, like in [25]. A large virtual inertia J is designed to satisfy the allowed RoCoF requirement [7], [25]. Firstly, the transient behaviors of the VSG under the grid voltage drops from 1 p.u. to 0.6 p.u. are tested in Fig. 13 and Fig. 14. From top to bottom in each picture, the corresponding experimental waveforms are the grid linevoltage, i.e.,  $V_{gab}$ , the active power P, power angle  $\delta$ , and the line current of phase a,  $I_{ga}$ , respectively.

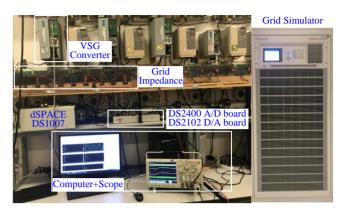


Fig.12. The hardware platform used in the experiments to validate the theoretical analysis.

TABLE I
Main parameters of the VSG system used in experiments

Parameters	Description	Value	p.u.
$P_{ref}$	Rated active power	2 kW	1.0
$Q_{ref}$	Rated reactive power	0	0
$V_0$	Rated voltage	100 V	1.0
$V_{g}$	Normal grid voltage	100 V	1.0
$\omega_0$	Grid angular frequency	314 rad/s	1.0
$L_g$	Grid inductance	12 mH	0.5
$R_{g}$	Equivalent grid resistance	$22.5 \text{ m}\Omega$	0.003
$D_p$	<i>P-f</i> droop gain	$25 P_{ m max}/\omega_0$	25
J	Virtual inertia	$10 P_{\rm max}/\omega_0$	10
$D_q$	Q-V droop gain	$0.1V_0/Q_{ m max}$	0.1

In Fig.13, when  $R_v = 0.005$  p.u. is adopted, the system can return to the stable steady-state when  $V_g$  drops from 1 p.u. to 0.6 p.u.. However, if  $R_v$  is increased to 0.015 p.u., the system becomes unstable, and a low-frequency oscillation is observed when the fault is triggered. This implies that instability is caused by the narrowed allowable overshoot range of  $\delta$ . The results validate the theoretical analysis for the effects of  $R_v$  on the transient stability in Fig. 4.

In Fig.14, a reduction of the active power reference during the grid voltage sag is performed to enhance the transient stability with different coefficient parameters settings. From Fig. 14(a), it can be found that the method of reducing  $P_{ref}$  with a large coefficient  $K_{factor}$  can stabilize the VSG when the grid voltage drops. However, if  $K_{factor}$  is not large enough, i.e.,  $K_{factor} = 0.2$ , the transient instability still exists. The results agree with the theoretical analysis of the improved method of reducing the active power reference shown in Fig. 10 and Fig. 11, respectively.

To further validate the improved method for transient stability, Fig. 15 shows the transient waveforms for the grid voltage drops from 1 p.u. to 0.4 p.u.. If  $P_{ref}$  keeps constant like that before the fault or  $K_{factor}$  is too small, there will be no equilibrium point. The system definitely loses its stability,

which can not be removed even if the fault was cleared, as shown in Fig. 15(a). Nevertheless, if  $K_{factor}$  is sufficiently large, i.e.,  $K_{factor} = 50$  in Fig. 15(b), the system can operate stably during the fault. Moreover, the system can return to the original

state when the fault was cleared as long as it is stable during the fault. These experimental results further validate the effectiveness of the enhanced method for the transient stability.

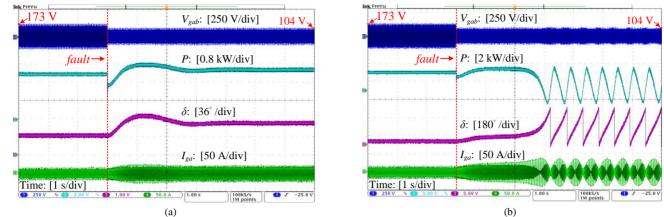
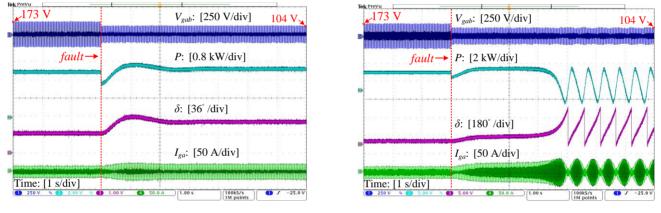


Fig. 13. Experimental transient responses of the VSG with different  $R_v$  when  $V_g$  drops from 1 p.u. to 0.6 p.u. (a)  $R_v = 0.005$  p.u. and (b)  $R_v = 0.015$  p.u.



(a)

(b) Fig. 14. Experimental transient responses of the VSG with  $R_v = 0.015$  p.u. when  $V_e$  dips from 1 p.u. to 0.6 p.u. The improved method of reducing active power reference are added with different coefficients, (a)  $K_{factor} = 5$ , (b)  $K_{factor} = 0.2$ .

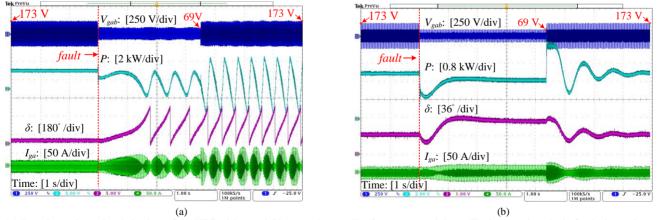


Fig. 15. Experimental transient behaviors of the VSG with  $R_v = 0.015$  p.u. when  $V_g$  dips from 1 p.u. to 0.4 p.u. The improved method of reducing active power reference is added with different coefficients, (a)  $K_{factor} = 20$ , (b)  $K_{factor} = 50$ .

## VI. CONCLUSION

The effects of VR on transient stability are first studied in this paper. A virtual PCC and a virtual power angle are proposed to represent the mathematical model of the VSG with VR damping. Based on that, transient stability is analyzed using the phase portrait and the attraction regions of the system. It reveals that the impacts of VR on transient stability are opposite from the grid resistance, which narrowed the stability region of the VSG, resulting from reducing the active power transfer capability. In This article has been accepted for publication in a future issue of this journal, but has not been fully edited. Content may change prior to final publication. Citation information: DOI 10.1109/TIE.2021.3082055, IEEE Transactions on Industrial Electronics

order to keep the VSG with VR work normally during the grid voltage sag, an enhanced transient stability method, by reducing the active power reference as the grid fault is detected, is introduced. A design-oriented analysis and the parameter design with different VRs are also presented, indicating that a more considerable reduction on active power reference is required with a larger VR during the grid fault. Finally, experimental results have verified the effectiveness of the theoretical analysis and the enhanced method for transient stability.

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