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Golestan, Saeed; Matas, Jose; Abusorrah, Abdullah M.; Guerrero, Josep M.

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More-stable EPLL

Saeed Golestan, Senior Member, IEEE, Jose Matas, Abdullah M. Abusorrah, Senior Member, IEEE, and Josep M. Guerrero, Fellow IEEE

Abstract—The enhanced PLL (EPLL) is one of the most famous PLLs in single-phase applications and a versatile tool for different signal processing applications, especially for the grid synchronization of power converters. Recently, it has been proved that the EPLL has a quite narrow stable zone (compared to its unstable zone) in the positive parameter space from a small-signal point of view. This zone will be even more narrow if maintaining a minimum stability margin is required. This paper aims to modify the EPLL structure to improve its stability margin and, at the same time, make it unconditionally stable in the positive parameter space from a small-signal point of view.

Index Terms—Enhanced phase-locked loop (EPLL), singlephase systems, synchronization.

I. INTRODUCTION

The EPLL is one of the most famous PLLs in single-phase applications. The block diagram representation of this PLL can be observed in Fig. 1 [1], in which v is the single-phase input signal, \hat{V}_1 , $\hat{\theta}_1$ and $\hat{\omega}$ are estimates of the amplitude, phase angle, and angular frequency of this signal, respectively, and k_p , k_i , and k_v are the control gains.¹ From the structural point of view, the EPLL looks a bit different from a typical single-phase PLL, which is often based on a synchronous reference frame PLL (SRF-PLL) and a fictitious (β -axis) signal generator [2]. However, mathematically speaking, it is equivalent to a single-phase SRF-PLL that generates its β axis input signal directly using the estimated phase angle and amplitude [3].

The EPLL has received considerable research attention over the past two decades. A part of these research activities has focused on applying the EPLL and its extended versions to different signal processing applications. For instance, in addition to the synchronization of power converters in both single-phase and three-phase applications, the EPLL and its extended versions have been widely employed for the detection and separation of fundamental and disturbance (dc,

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S. Golestan and J. M. Guerrero are with the Department of Energy Technology, Aalborg University, Aalborg DK-9220, Denmark (e-mail: sgd@et.aau.dk; joz@et.aau.dk).

J. Matas is with the Department of Electronic Engineering, Technical University of Catalonia, Vilanova i la Geltru 08800, Spain (e-mail: jose.matas@upc.edu).

A. M. Abusorrah is with the Department of Electrical and Computer Engineering, Faculty of Engineering, and Center of Research Excellence in Renewable Energy and Power Systems, King Abdulaziz University, Jeddah, Saudi Arabia (e-mail: aabusorrah@kau.edu.sa).

¹Throughout this paper, $k_p = k_v$ is assumed. This selection is often considered as an optimal choice in the literature [1].

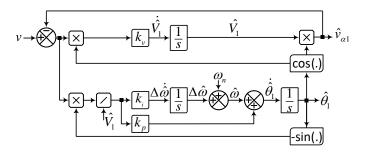


Fig. 1. Conventional EPLL.

harmonics, and interharmonic) components of power signals [4], [5], computation of synchrophasors [6]–[8], fault analysis [9], estimation of parameters of electromagnetic oscillations [10], and implementations of robust resonant controllers [11], among other applications.

Improving the EPLL filtering capability and/or dynamic performance in the grid synchronization applications has also been a main focus of research in the past years. In [12], for instance, an adaptive method to improve the start-up and phase jump tracking ability of the EPLL without affecting its filtering capability is proposed. In [13] and [14], including inloop filters and window functions into the EPLL control loops to provide a more smooth estimation of the grid voltage parameters under noisy conditions is introduced. In [5], adding a dc offset estimation/rejection loop to the EPLL to provide an estimation of the input dc component and, at the same time, make the EPLL immune to the disturbing effect of the dc offset is proposed. In [15], including a single nonadaptive band-pass filter before the EPLL input and a compensator in its output is proposed. The band-pass filter rejects the dc offset and attenuates the input harmonics, and the compensator corrects errors caused by the band-pass filter under off-nominal frequencies. In [16], including an adaptive filter before the EPLL input is proposed. This filter, which is based on delayed signal cancellation operators, improve the EPLL filtering capability without considerably affecting its dynamic response.

Despite the fact that the EPLL is structurally robust under extreme scenarios such as low sampling frequencies and fixedpoint implementations with a limited number of bits [10], [11], recently it has been proved that it has a quite narrow stable zone (compared to its unstable zone) in the positive parameter space from a small-signal point of view [17]. This stable zone becomes even more narrow if maintaining a minimum stability margin is required.

To deal with the above-mentioned problem, a More-stable EPLL (MsEPLL), which is simply realized by adding some nonlinear terms to the traditional EPLL, is presented in this

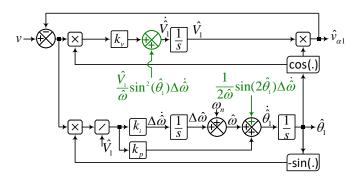


Fig. 2. More-stable EPLL (MsEPLL).

paper. An analytic linear time-periodic (LTP) model for the MsEPLL is then obtained, and its stability is investigated. It will be shown that the MsEPLL has a more decent stability margin compared to the EPLL. It will also be demonstrated that the MsEPLL, contrary to the EPLL, is unconditionally stable in the positive parameter space from a small-signal point of view.

II. MSEPLL

Assume that the single-phase input signal of the EPLL is as (1), where V_1 and θ_1 are the amplitude and phase angle of this signal.

$$v(t) = V_1 \cos(\theta_1) \tag{1}$$

In this case, the governing nonlinear differential equations (GNDEs) of the EPLL can be simply obtained from Fig. 1 as

$$\dot{\hat{\omega}} = \Delta \dot{\hat{\omega}} = \frac{k_i}{2\hat{V}_1} [V_1 \sin(\theta_1 - \hat{\theta}_1) + \hat{V}_1 \sin(2\hat{\theta}_1) - V_1 \sin(\theta_1 + \hat{\theta}_1)] \quad (2)$$

$$\dot{\hat{\theta}}_1 = \hat{\omega} + \frac{\kappa_p}{k_i} \Delta \dot{\hat{\omega}}$$
(3)

$$\dot{\hat{V}}_{1} = \frac{k_{v}}{2} [V_{1} \cos(\theta_{1} - \hat{\theta}_{1}) - \hat{V}_{1} + V_{1} \cos(\theta_{1} + \hat{\theta}_{1}) - \hat{V}_{1} \cos(2\hat{\theta}_{1})].$$
(4)

The highlighted terms in (2) and (4) are some doublefrequency terms, which are equal to zero in the steady state, i.e., when $V_1 = \hat{V}_1$ and $\theta_1 = \hat{\theta}_1$. However, the dynamics of these terms adversely affect the EPLL small-signal stability [17]. This fact suggests that the EPLL small-signal stability may be improved by mitigating the adverse effects of these terms. To this end, as shown in Fig. 2, adding some double-frequency terms to the EPLL structure is suggested. This modification has been inspired from the adaptive notch filter structure [18]. Note that the signal $\Delta \dot{\omega}$ and, therefore, the highlighted doublefrequency terms in the MsEPLL structure, are equal to zero in the steady state.² Note also that the double-frequency term $\frac{1}{2}\sin(2\hat{\theta}_1)$ in Fig. 2 is equal to $\sin(\hat{\theta}_1)\cos(\hat{\theta}_1)$. Therefore, implementing the MsEPLL does not involve the calculation of additional trigonometric functions.

A. LTP Modeling

Considering (1) as the input signal of the MsEPLL in Fig. 2, its GNDEs can be obtained as

$$\Delta \dot{\hat{\omega}} = \frac{k_i}{2\hat{V}_1} \Big[V_1 \sin(\theta_1 - \hat{\theta}_1) + \hat{V}_1 \sin(2\hat{\theta}_1) - V_1 \sin(\theta_1 + \hat{\theta}_1) \Big]$$
(5)

$$\hat{\theta}_1 = \hat{\omega} + \frac{\kappa_p}{k_i} \Delta \dot{\hat{\omega}} + \frac{1}{2\hat{\omega}} \sin\left(2\hat{\theta}_1\right) \Delta \dot{\hat{\omega}}$$
(6)

$$\dot{Y}_{1} = \frac{\kappa_{v}}{2} [V_{1} \cos(\theta_{1} - \hat{\theta}_{1}) - \hat{V}_{1} + V_{1} \cos(\theta_{1} + \hat{\theta}_{1}) - \hat{V}_{1} \cos(2\hat{\theta}_{1})] + \frac{\hat{V}_{1}}{\hat{\omega}} \sin^{2}(\hat{\theta}_{1}) \Delta \dot{\hat{\omega}}.$$
(7)

Considering the definitions made in (8), in which each parameter is defined as a nominal value (indicated by the subscript n) plus a small perturbation (indicated by Δ), (5) can be linearized as shown in (9) at the bottom of the page.

$$V_1 = V_n + \Delta V_1, \quad \theta_1 = \theta_n + \Delta \theta_1, \quad \omega = \omega_n + \Delta \omega$$

$$\hat{V}_1 = V_n + \Delta \hat{V}_1, \quad \hat{\theta}_1 = \theta_n + \Delta \hat{\theta}_1, \quad \hat{\omega} = \omega_n + \Delta \hat{\omega}$$
(8)

Note that $\theta_n = \int \omega_n dt = \omega_n t + \varphi_n$. Without loss of generality, $\varphi_n = 0$ is assumed in this paper.

In a similar manner, one can obtain (10) and (11) by substituting (8) into (6) and (7) and linearizing them.

$$\Delta \dot{\hat{\theta}}_{1} \approx \Delta \hat{\omega} + \frac{k_{p}}{k_{i}} \Delta \dot{\hat{\omega}} + \frac{1}{2\omega_{n}} \sin(2\theta_{n}) \Delta \dot{\hat{\omega}}$$
(10)
$$\Delta \dot{\hat{V}}_{1} \approx \frac{k_{v}}{2} \left[\left\{ 1 + \cos(2\theta_{n}) \right\} \Delta V_{e} - V_{n} \sin(2\theta_{n}) \Delta \theta_{e} \right]$$
$$+ \frac{V_{n}}{\omega_{n}} \frac{1 - \cos(2\theta_{n})}{2} \Delta \dot{\hat{\omega}}$$
(11)

Using (9)-(11), which are a set of LTP differential equations in the time domain, the LTP model of the MsEPLL can be obtained as depicted in Fig. 3(a). Note that the only difference

²A hidden assumption here is that the single-phase input signal is without harmonics. Note that in the presence of harmonics, the signal $\Delta \hat{\omega}$ may contain some oscillatory ripples depending on the EPLL bandwidth.

$$\Delta \dot{\omega} = \underbrace{\frac{k_i}{2V_n} \left(1 - \frac{\Delta \hat{V}_1}{V_n}\right)}{2(V_n + \Delta \hat{V}_1)}}_{\approx \frac{k_i}{2(V_n + \Delta \hat{V}_1)}} \left[\underbrace{(V_n + \Delta V_1) \sin(\Delta \theta_1 - \Delta \hat{\theta}_1)}_{\approx \frac{\Delta \theta_e}{2}} + \underbrace{(V_n + \Delta \hat{V}_1) \sin(2\theta_n + \Delta \hat{\theta}_1) - (V_n + \Delta V_1) \sin(2\theta_n + \Delta \theta_1 + \Delta \hat{\theta}_1)}_{\approx \frac{k_i}{2}}\right] \\ \approx \frac{k_i}{2} \left[(1 - \cos(2\theta_n)) \underbrace{(\Delta \theta_1 - \Delta \hat{\theta}_1) - \sin(2\theta_n)}_{(\Delta \theta_1 - \Delta \hat{\theta}_1)} + \underbrace{(V_n + \Delta \hat{V}_1) \sin(2\theta_n + \Delta \theta_1 + \Delta \hat{\theta}_1)}_{(\Delta V_1 - \Delta \hat{V}_1)/V_n}\right]$$
(9)

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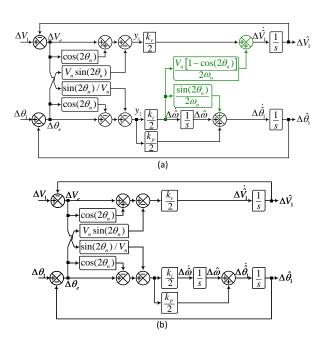


Fig. 3. (a) LTP model of the MsEPLL. (b) LTP model of the EPLL.

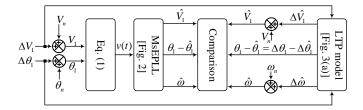


Fig. 4. Model verification procedure.

of this model compared to the EPLL LTP model, which is shown in Fig. 3(b) [17], lies in the parts marked with green color. These parts are the result of linearizing the double-frequency terms (green-color terms) in Fig. 2.

To evaluate the accuracy of the obtained LTP model, a timedomain comparison between the MsEPLL and its LTP model as shown in Fig. 4 is carried out. The comparison is conducted in the Matlab/Simulink. The control parameters of the MsEPLL and its LTP model are considered as $k_p = k_v = 444$ and $k_i = 49348$ [17]. A small voltage sag test and a small phase jump test are considered for the comparison here. The results of these tests can be observed in Fig. 5. As shown, the predictions of the LTP model are closely matched to the actual results. Note that changing the type of the test (for example, considering a frequency jump instead of the voltage sag or phase jump) does not considerably affect the accuracy of the LTP model. However, the magnitude of the disturbance may have a considerable impact on accuracy. For example, if a 0.5p.u. voltage sag instead of the 0.1-p.u. voltage sag is applied, the model demonstrates a reduced accuracy. The reason is that obtaining the LTP model of the MsEPLL (or, generally, any nonlinear system) involves assuming small-signal perturbations around its working points/trajectories. Applying a largesignal disturbance contradicts this assumption and, therefore, causes some inaccuracies.

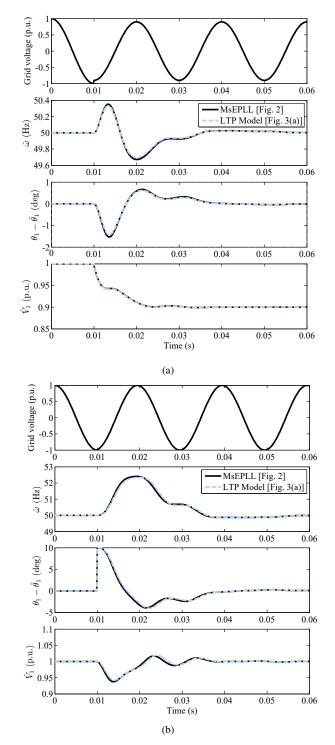


Fig. 5. Accuracy assessment of the LTP model of the MsEPLL. (a) 0.1-p.u. voltage sag test. (b) 10° phase jump test.

B. Open-Loop Harmonic Transfer Function (HTF)

To facilitate the understanding of the procedure for obtaining the open-loop HTF of the MsEPLL, consider the signal y_1 in Fig. 3(a). In the time domain, this signal is equal to

$$y_1(t) = (1 + \cos(2\theta_n))\Delta V_e(t) - V_n \sin(2\theta_n)\Delta \theta_e(t).$$
(12)

Replacing the trigonometric functions in (12) by their equivalent expressions in terms of exponential, i.e., $\cos(2\theta_n) =$

 $0.5(e^{j\omega_p t} + e^{-j\omega_p t})$ and $\sin(2\theta_n) = -j0.5(e^{j\omega_p t} - e^{-j\omega_p t})$, where $\omega_p = 2\omega_n$, and applying the Laplace transform results in

$$y_1(s) = \Delta V_e(s) + \frac{1}{2} \Delta V_e(s - j\omega_p) + \frac{1}{2} \Delta V_e(s + j\omega_p) - V_n \left[\frac{j}{2} \Delta \theta_e(s + j\omega_p) - \frac{j}{2} \Delta \theta_e(s - j\omega_p) \right].$$
(13)

Substituting *s* by $s+jm\omega_p$ ($m \in \mathbb{Z}$) in (13) and arranging the resulting equations in a matrix form gives (14) at the bottom of the page. This matrix equation, which is of infinite dimension, is the HTF of (12). Considering the above way of formulation, one can easily obtain the open-loop HTF of the MsEPLL as (15). Note that some terms of (15) have been already described in (14). The remaining terms are described in (16).

Following a similar procedure as above, the open-loop HTF of the EPLL may also be obtained from its LTP model (Fig. 3(b)) as shown in (17).

III. COMPARISON OF EPLL AND MSEPLL

A. Stability Region

Transfer function $G_{ol,MSEPLL}^{htf}(s) = (k_p/2) L_{ol,MSEPLL}^{htf}(s)$ in (15), as mentioned before, is the open-loop HTF of the MSE-PLL. According to the Generalized LTP Nyqusit stability criterion, the small-signal stability of the MSEPLL can be assessed by obtaining the open-loop eigenloci of $L_{ol,MSEPLL}^{htf}(s)$ for s belonging to a strip defined by $-j\omega_p/2 < \text{Im}(s) < j\omega_p/2$ and counting the number of encirclement of the point $-1/K + j0.^3$

 ${}^{3}L^{\text{htf}}_{ol,\text{MsEPLL}}(s)$ is of infinite dimension. Therefore, a truncated version of it should be considered for the stability analysis.

Fig. 6 shows the eigenloci of the transfer matrix $L_{ol,MsEPLL}^{hff}(s)$ for different value of γ , which is the only control parameter in this transfer matrix. It is observed that by increasing the value of γ , an eigenvalue curve of $L_{ol,MsEPLL}^{hff}(s)$ gets closer to the negative real axis. However, regardless of the value of γ , it does not intersect the negative real axis and, therefore, cannot encircle the point -1/K+j0 for positive K. Considering that $L_{ol,MsEPLL}^{hff}(s)$ has no unstable pole, it can be concluded that the MsEPLL is stable for positive $K = k_p/2$ and, therefore, positive k_p . The same observation and stability conclusion can be made for any other value of γ . It means that the MsEPLL is stable in the positive parameter space, i.e., $k_p > 0$ and $k_i > 0$, from a small-signal point of view.

For the case of the EPLL, however, the situation is different [17]. This fact can be better visualized in Fig. 7, which shows the eigenloci of the transfer matrix $L_{ol, \text{EPLL}}^{\text{hff}}(s)$ for different value of γ . For instance, in Fig. 7(a), which corresponds to $\gamma = 50$, an eigenvalue curve of $L_{ol, \text{EPLL}}^{\text{hff}}(s)$ intersects the negative real axis at -5.08e - 4. According to the Generalized LTP Nyqusit stability criterion, it means that the EPLL, which its open-loop HTF is $G_{ol, \text{EPLL}}^{\text{hff}}(s) = KL_{ol, \text{EPLL}}^{\text{hff}}(s)$, remains stable if $K = \frac{k_p}{2} < \frac{1}{5.08e - 4} = 1968.5$ or, equivalently, $k_p < 3937$. Similarly, according to Fig. 7(b) and (c), which are corresponding to $\gamma = 500$ and $\gamma = 1000$, respectively, it can be concluded that the EPLL remains stable if $K = \frac{k_p}{2} < \frac{1}{0.0148} = 67.6$ or, equivalently, $k_p < 304.9$ and $k_p < 135.1$. It is clear that by increasing the value of γ , the stable range of k_p is decreased. Fig. 8, which shows the stability region of the EPLL when $\gamma = k_i/k_p$ changes in the range of 50 to 1000, helps to better visualize this fact.

$$\begin{bmatrix}
\begin{aligned}
y_{1}\left(s-j\omega_{p}\right) \\
y_{1}\left(s\right) \\
y_{1$$

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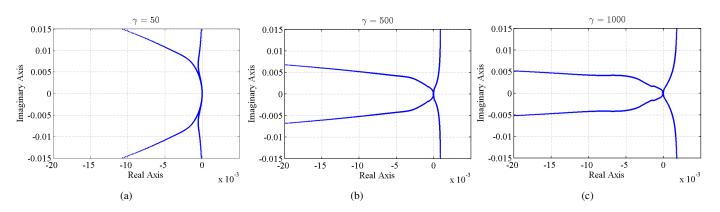


Fig. 6. Eigenloci of the transfer matrix $L_{ol.MsEPLL}^{htf}(s)$ for different value of γ . (a) $\gamma = 50$. (b) $\gamma = 500$. (c) $\gamma = 1000$.

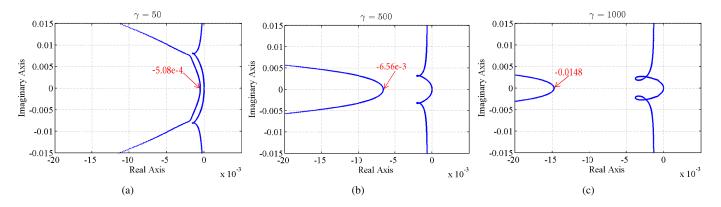


Fig. 7. Eigenloci of the transfer matrix $L_{ol,EPLL}^{hff}(s)$ for different value of γ . (a) $\gamma = 50$. (b) $\gamma = 500$. (c) $\gamma = 1000$.

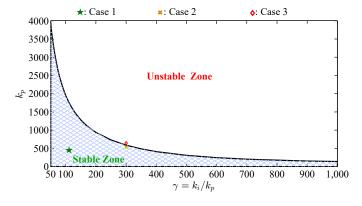


Fig. 8. Small-signal stability region of the EPLL.

In summary, the MsEPLL is unconditionally stable in the positive parameter space from a small-signal point of view. The EPLL, however, has a considerable unstable zone.

B. Stability Margin

The main aim of this section is to conduct a comparison between the EPLL and MsEPLL from the stability margin point of view. Three case studies, which are corresponding to three sets of control parameters, are considered.

1) Case 1: In this case, the control parameters of the EPLL and MsEPLL are considered as $k_p = k_v = 444$ and $\gamma = k_i/k_p = 111.14$ [17]. This set of parameters, which is marked with a

green star in Fig. 8, is in the stable zone of the EPLL and away from its stability border.

Fig. 9(a) shows the open-loop LTP Nyquist plots of the EPLL and MsEPLL for Case 1. Note that the open-loop eigenloci of both the EPLL and MsEPLL intersect the lower half of the unit circle and also the real axis at two points. It means that they have two eigenvalue phase margins (PMs) and two eigenvalue gain margins (GMs). The eigenvalue PMs and GMs of the EPLL and MsEPLL, which indicate how close their open-loop eigenloci are to the critical point -1 + j0, can be observed above Fig. 9(a). It is observed that the MsEPLL has a rather more decent stability margin than the EPLL.

To verify the above observation, a comparison between the EPLL and MsEPLL in response to a phase jump test is carried out. The results of this test can be seen in Fig. 10. It can be observed that the MsEPLL has a lower overshoot in estimating the phase, frequency, and amplitude and, therefore, has a more damped dynamic response. For instance, the overshoot of the MsEPLL in estimating the phase angle is 38%, while it is around 50% for the case of the EPLL. Note that the PM of a control system and its overshoot in response to a step input are closely related to each other; A lower PM always results in a larger overshoot [19].

2) Case 2: In this case, the control parameters of the EPLL and MsEPLL are considered $k_p = k_v = 550$ and $\gamma = k_i/k_p =$ 300. This set of parameters, which is marked with a × character in Fig. 8, is in the stable zone of the EPLL, but close to the

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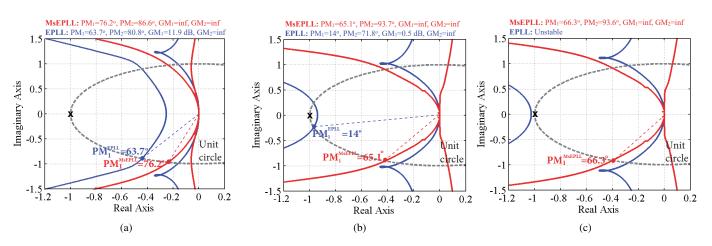


Fig. 9. Open-loop LTP Nyquist plots of the EPLL and MsEPLL for different sets of control parameters. (a) Case 1. (b) Case 2. (c) Case 3. In all cases, to avoid confusion, only one eigenvalue PM of the EPLL and MsEPLL is highlighted.

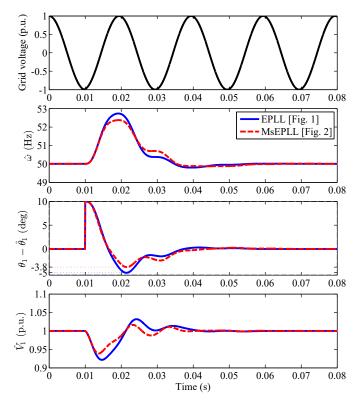


Fig. 10. A comparison between the EPLL and MsEPLL under Case 1 ($k_p = k_v = 444$ and $\gamma = k_i/k_p = 111.14$) and in response to 10° phase jump test.

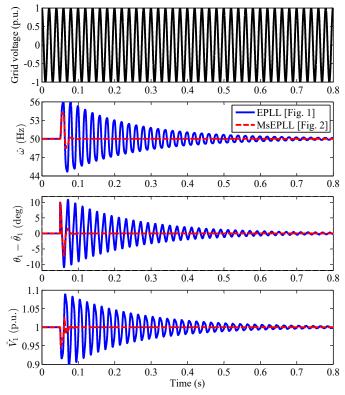


Fig. 11. A comparison between the EPLL and MsEPLL in response to 10° phase jump test under Case 2 ($k_p = k_v = 550$ and $\gamma = k_i/k_p = 300$).

stability border.

Fig. 9(b) shows the open-loop LTP Nyquist plots of the EPLL and MsEPLL and highlights their eigenvalue PMs and GMs. It is observed that an open-lop eigenvalue curve of the EPLL is very close to the critical point -1+j0 and, therefore, causes a low PM and GM. Such a low PM is expected to cause a highly oscillatory dynamic response for the EPLL. The MsEPLL, however, has a quite decent stability margin.

To verify the above observation, the comparison of the EPLL and MsEPLL in response to 10° phase jump test is repeated. As expected, the transient response of the EPLL is

highly oscillatory. The MsEPLL, however, has a much more damped dynamic response and reaches the steady state in a short while after the phase jump.

3) Case 3: In this case, $k_p = k_v = 600$ and $\gamma = k_i/k_p = 300$ are selected. This set of parameters, which is marked with a red diamond in Fig. 8, is in the unstable zone of the EPLL, but close to the stability border.

Fig. 9(c) shows the open-loop LTP Nyquist plots of the EPLL and MsEPLL. As shown, an eigenvalue curve of the EPLL encircles the critical point -1 + j0, which makes it unstable. The MsEPLL, however, has a decent stability margin.

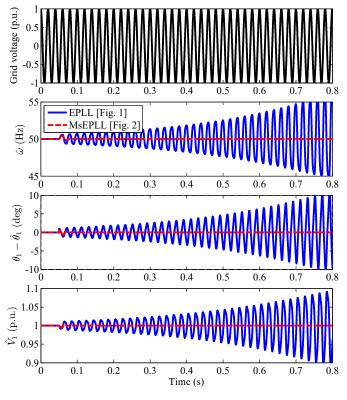


Fig. 12. A comparison between the EPLL and MsEPLL in response to 1° phase jump. Before the phase jump, the control parameters are set to the values selected in Section III-B2. At the same moment with the phase jump, the control parameters are changed to the values selected in Section III-B3.

To verify the above observations, the control parameters of the EPLL and MsEPLL are initially set to the values selected in Section III-B2 (Case 2). Suddenly, the control parameters are changed to the values selected in this section (Case 3). At the same time, an extremely small phase jump (1° phase jump) is also applied. The result of this test can be observed 12. As expected the EPLL becomes unstable. The MsEPLL, however, remains stable.

By obtaining its open-loop eigenloci or using time-domain simulation results, it can be shown that the MsEPLL is stable at any point in the unstable zone of the EPLL in Fig. 8. For instance, Fig. 13, which shows the time-domain simulation results of the MsEPLL in response to a large-signal test (60° phase jump), supports this fact. Note that the selected control parameters, i.e., $k_p = k_v = 4000$ and $\gamma = k_i/k_p = 1000$, are corresponding to the upper right-hand corner of the positive parameter space in Fig. 8. Note also that the results of the EPLL are not shown as it is unstable.

C. Further Investigations

In this section, further comparative investigations between the EPLL and MsEPLL are conducted. Throughout these studies, the control parameters of the EPLL and MsEPLL are set to the same values selected in Section III-B1.

First, it can be interesting to see whether the enhanced stability margin of the MsEPLL compared to the EPLL causes a negative effect on its filtering capability. To this end, a com-

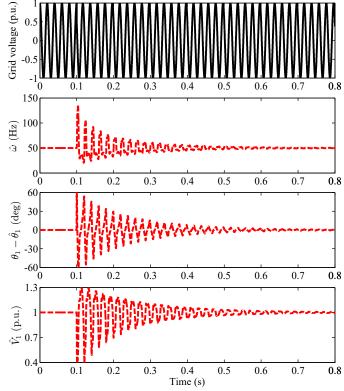


Fig. 13. Performance of the MsEPLL in response to a 60° phase jump. The selected control parameters are $k_p = k_v = 4000$ and $\gamma = k_i/k_p = 1000$. Note that the results of the EPLL is not shows as it is unstable in this case.

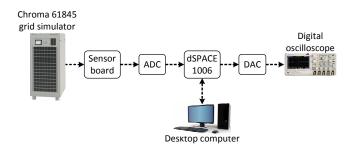
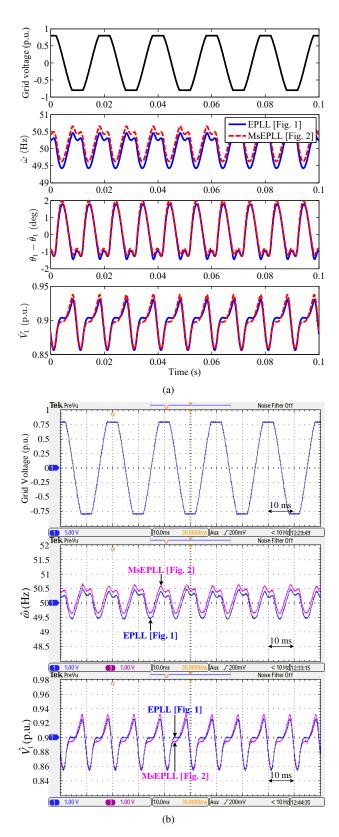


Fig. 14. Experimental setup.

parison between the EPLL and MsEPLL under a harmonicallydistorted grid condition is carried out. The grid voltage signal is considered as a sinusoid that has been clipped to 0.8 p.u. at both the top and bottom. Note that such a signal is corresponding to a total harmonic distortion (THD) approximately equal to 9%. Both the simulation and experimental results of this test are presented. The experimental setup can be observed in Fig. 14. It can be observed in the obtained results (see Fig. 15) that the EPLL and MsEPLL have a comparable filtering capability. It means that the enhanced stability margin of the MsEPLL compared to the EPLL does not negatively affect its filtering ability.

Considering that voltage sags are a common disturbance in power systems, and \hat{V}_1 (which is an estimation of the grid voltage amplitude) is a key component in realizing the MsEPLL (see highlighted terms in Fig. 2), a comparison between the EPLL and MsEPLL under a voltage sag scenario

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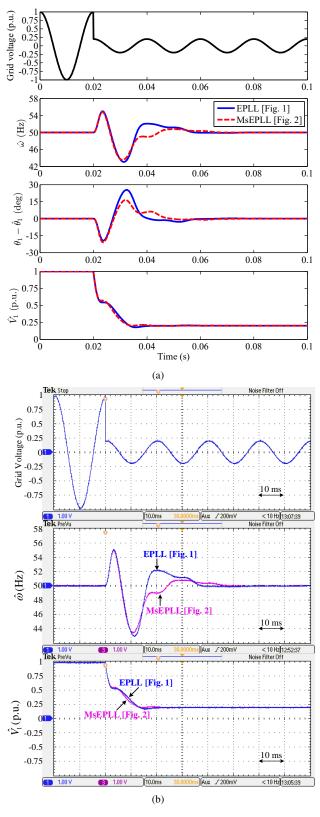


Fig. 15. A comparison between the EPLL and MsEPLL under a harmonicrich grid condition. (a) Simulation results. (b) Experimental results. Note that the phase error signal in the experimental results cannot be shown as the actual phase angle is unknown.

Fig. 16. A comparison between the EPLL and MsEPLL under a 0.8-p.u. voltage sag. (a) Simulation results. (b) Experimental results. Note that the phase error signal in the experimental results cannot be shown as the actual phase angle is unknown.

can be interesting. To this end and, at the same time, to highly excite their nonlinearities, a severe voltage sag (0.8 p.u.) is

considered. The simulation and experimental results of this test can be observed in Fig. 16. As shown, no very large difference between the transient behavior of the EPLL and MsEPLL is observed.

IV. CONCLUSIONS

Improving the stability properties of the EPLL, which is a versatile signal processing tool in different engineering applications, was the main motivation of this paper. To this end, a so-called MsEPLL was presented. By deriving an LTP model for the MsEPLL and obtaining its open-loop HTF, it was demonstrated that the MsEPLL (contrary to the conventional EPLL) is unconditionally stable in the positive parameter space from a small-signal point of view. It was also demonstrated that the MsEPLL always has a more decent stability margin compared to the conventional EPLL. All these observations were verified using some numerical tests.

In addition to improving the EPLL stability properties, this paper may contribute towards improving the stability properties of other single-phase synchronization systems. The reason is that the EPLL, as shown in [3], has a close relationship with a large number of single-phase synchronization systems. Therefore, a similar approach as that presented in this paper may be used for improving the stability properties of these single-phase synchronization systems.

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