Wide Area Protection Scheme Preventing Cascading Events Caused by Load Flow Transferring

Zhou Liu, Zhe Chen

Department of Energy Technology
Aalborg University
Aalborg, Denmark
zli@et.aau.dk, zch@et.aau.dk

Haishun Sun

Huazhong University of Science and
Technology
Wuhan, China
haishunsun@hust.edu.cn

Yanting Hu

School of Engineering Education
Glyndwr University
Wrexham, UK
y.hu@glyndwr.ac.uk

Abstract—Load flow transferring after an initial contingency is regarded as one of the main reasons of causing unexpected cascading trips. A multi agent system (MAS) based wide area protection strategy is proposed in this paper to predict the load flow transferring from the point of view of impedance relays, and prevent the unexpected relay operations accordingly. The variations of node injections during the post fault transient period will be also considered in the prediction algorithm. The power system of Eastern Denmark modeled in real time digital simulator (RTDS) will be used to demonstrate the proposed strategy. The simulation results indicate this strategy can successfully predict and prevent the unexpected relay operation caused by load flow transferring.

Index Terms—Cascading trips, load flow transferring, multi agent system, wide area protection

I. INTRODUCTION

Nowadays, power system blackouts are regarded as the most severe disasters which could result in devastating effects on human society and industry. Especially with the modern development, power system is operated nearer to operation margin and with less redundancy [1], which is already in a high risk of overloading operation situation. Also, recent large scale blackouts in USA and Europe [2] [3] give an alarm on the vulnerability of prevailing power systems.

When N-1 (or N-k) contingency occurs in a heavily loaded power system, a large amount of load flow will be re distributed and transferred to the remained transmission network, which may cause those critical transmission lines overloaded. Then the related backup relays may mistakenly take the overload situation as a remote fault to trip the some transmission lines unexpectedly, which will overload the rest system further. Consequently, cascading trips and network splitting may happen inevitably. However, if the load flow transferring can be identified timely and the trip of the critical overload lines is delayed/blocked quickly, the overload situation might be mitigated by timely emergent protection and control schemes.

So far, many research efforts have been taken to prevent cascading events. One emergent prediction control algorithm is based on dc load flow sensitivities, including line outage

distribution factor (LODF) and generator shift factor (GSF). The method predicts the component outage caused by load flow transferring and distinguishes the overload situation [4] [5]. Moreover, the variation of system state variables during transient period after an outage has also been studied over the whole system [6] or by local measured information [7]. However, those dc load flow based predicting methods only consider the flow of active power and assume bus voltages and reactive power flow being constant, which is not the case in real situation, especially in the cascading events.

In this paper, with the aim of preventing the unexpected relay operation caused by load flow transferring in the post fault stage, a sensitivity method based on impedance principle is presented to predict and identify the possible overloaded line caused by load flow transferring in the point of view of relays, the variations of both active power and reactive power are considered. Furthermore, in order to eliminate the unexpected relay operation which will normally have a negative effect on system stability, MAS will be applied for wide area information exchanging and sharing. The power system of eastern demark will be used as test system and modeled in RTDS to demonstrate the proposed prediction algorithm and protection strategy. The rest of paper is organized as follows: a brief introduction of the sensitivity based prediction and identification algorithm is presented in Section II; multi agent system based control strategy is described in Section III; then in Section IV, the strategy is demonstrated on the power system modeled in RTDS; and finally, the conclusion is made in Section V.

II. PREDICTION AND IDENTIFICATION ALGORITHM

A. Relay operation characteristics

In this paper, the impedance relay is used as an example and the zone 3 relay will be the studied objective. The classic characteristics of impedance relay on the line ij are shown in Figure 1. $V_i \angle \theta_i, V_j \angle \theta_j$ represent the bus voltages of the line ij ends respectively. $Z_{ij} \angle \varphi_{lineij}$ is the impedance of line ij . Z_{Tset}, Z_{Tsetij} are the zone 3 set values at the impedance angle φ_{lineij} and power factor angle φ_{ij} respectively. $Z_{aij} \angle \varphi_{ij}$ is the measured impedance by the relay. At current power factor angle φ_{ij} , the relay operation margin can be expressed as:

$$M_{Tij} = Z_{aij} - Z_{Tsetij} \quad (1)$$

where

$$Z_{aij} = \frac{Z_{ij}V_i}{\sqrt{(V_i - V_j \cos \theta_{ij})^2 + (V_j \sin \theta_{ij})^2}} \quad (2)$$

$$Z_{Tsetij} = Z_{Tset} \cos(\Delta \varphi) \quad (3)$$

$$\Delta \varphi = \varphi_{lineij} - \varphi_{ij} \quad (4)$$

The set value of zone 3 relay is defined according to NERC proposed relay loadability limit [8], which is given by:

$$Z_{Tset} = \frac{V_{min}^2}{S_{max} \cos(\varphi_{line} - \varphi_{max})} \quad (5)$$

where S_{max} , V_{min} , φ_{line} , φ_{max} represent the load capacity limit of the line, low voltage limit of the bus, impedance angle of the line and maximum load flow angle respectively.

(a) Transmission line with impedance relays

(b) Characteristics of three zone impedance relay

Figure 1. Traditional impedance relay on transmission line

Normally, the measured impedance Z'_{aij} should be located outside the zone 3 circle area and the relay operation margin is positive as expressed by M'_{Tij} in Fig. 1. When Z_{aij} enters the zone 3 area, the backup relay will be initiated to trip the line within a preset delay. At this situation, the sign of M_{Tij} is changed to be negative. If this negative margin is caused by the post fault load flow transferring, this trip will be regarded as unexpected one because it is not functioned to clear a fault in its backup relay zone, and would induce overloaded on other lines and might further result in cascaded events.

B. Impedance sensitivity to system operation variables

With the aim of finding the influence factors between relay measured impedance and load flow transferring, the linearization method can be applied here. The impedance seen by Relay 1 in Fig. 1 can be rewritten with (6) (7) (8).

$$\overline{Z_{aij}} = R_{aij} + jX_{aij} \quad (6)$$

$$R_{aij} = \frac{V_i(G_{ij}V_j \cos \theta_{ij} + B_{ij}V_j \sin \theta_{ij} - G_{ij}V_i)}{(B_{ij}^2 + G_{ij}^2)(V_i^2 + V_j^2 - 2V_iV_j \cos \theta_{ij})} \quad (7)$$

$$X_{aij} = \frac{V_i(B_{ij}V_i + G_{ij}V_j \sin \theta_{ij} - B_{ij}V_j \cos \theta_{ij})}{(B_{ij}^2 + G_{ij}^2)(V_i^2 + V_j^2 - 2V_iV_j \cos \theta_{ij})} \quad (8)$$

where $\overline{Y_{ij}} = \overline{Z_{ij}}^{-1} = G_{ij} + jB_{ij}$, then the linearized form of (7) (8) is given by (9) (10).

$$\Delta R_{aij} = C_{R\theta i} \Delta \theta_i + C_{R\theta j} \Delta \theta_j + C_{Rv i} \Delta V_i + C_{Rv j} \Delta V_j \quad (9)$$

$$\Delta X_{aij} = C_{X\theta i} \Delta \theta_i + C_{X\theta j} \Delta \theta_j + C_{Xv i} \Delta V_i + C_{Xv j} \Delta V_j \quad (10)$$

where C_{ij} is the sensitivity matrix including the sensitivities of impedance (R_{aij}, X_{aij}) to related bus voltages ($\theta_i, \theta_j, V_i, V_j$), C_{Rij} and C_{Xij} are submatrices of C_{ij} .

$$C_{ij} = \begin{bmatrix} C_{Rij} \\ C_{Xij} \end{bmatrix} = \begin{bmatrix} C_{R\theta i} & C_{R\theta j} & C_{Rv i} & C_{Rv j} \\ C_{X\theta i} & C_{X\theta j} & C_{Xv i} & C_{Xv j} \end{bmatrix} = \begin{bmatrix} \frac{\partial R_{aij}}{\partial \theta_i} & \frac{\partial R_{aij}}{\partial \theta_j} & \frac{\partial R_{aij}}{\partial V_i} & \frac{\partial R_{aij}}{\partial V_j} \\ \frac{\partial X_{aij}}{\partial \theta_i} & \frac{\partial X_{aij}}{\partial \theta_j} & \frac{\partial X_{aij}}{\partial V_i} & \frac{\partial X_{aij}}{\partial V_j} \end{bmatrix} \quad (11)$$

Taking all the concerned relays into consideration, the sensitivity of impedances can be expressed in the matrix form as (12); also based on load flow Jacobin J defined by (15), the sensitivity H of impedance to node powers can be derived from (13), where $C_{R\theta}$, C_{RV} , $C_{X\theta}$ and C_{XV} are submatrices of C ; H_{RP} , H_{RQ} , H_{XP} and H_{XQ} are submatrices of H .

$$\begin{bmatrix} \Delta R_a \\ \Delta X_a \end{bmatrix} = C \begin{bmatrix} \Delta \theta \\ \Delta V \end{bmatrix} = \begin{bmatrix} C_{R\theta} & C_{RV} \\ C_{X\theta} & C_{XV} \end{bmatrix} \begin{bmatrix} \Delta \theta \\ \Delta V \end{bmatrix} \quad (12)$$

$$\begin{bmatrix} \Delta R_a \\ \Delta X_a \end{bmatrix} = H \begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix} = \begin{bmatrix} H_{RP} & H_{RQ} \\ H_{XP} & H_{XQ} \end{bmatrix} \begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix} \quad (13)$$

where

$$H = CJ^{-1} \quad (14)$$

$$\begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix} = J \begin{bmatrix} \Delta \theta \\ \Delta V \end{bmatrix} = \begin{bmatrix} J_{P\theta} & J_{PV} \\ J_{Q\theta} & J_{QV} \end{bmatrix} \begin{bmatrix} \Delta \theta \\ \Delta V \end{bmatrix} = \begin{bmatrix} \frac{\partial \Delta P}{\partial \theta} & \frac{\partial \Delta P}{\partial V} \\ \frac{\partial \Delta Q}{\partial \theta} & \frac{\partial \Delta Q}{\partial V} \end{bmatrix} \begin{bmatrix} \Delta \theta \\ \Delta V \end{bmatrix} \quad (15)$$

C. Flow transferring prediction and identification

In order to predict the post fault load flow transferring based on pre fault system data, the simulation method of line outage is shown in Figure 2. Figure 2 (a) is a network operated in normal situation without line outage. Suppose line l from bus m to bus n were opened by circuit breakers due to some kind of faults, as shown in Figure 2 (b). A line outage may be modeled by adding two virtual power injections ($\Delta P_m, \Delta Q_m, \Delta P_n, \Delta Q_n$) to the network, one at each end of the line to be dropped [9], which is shown in Figure 2 (c). At this situation of Figure 2 (c), the line is still kept in the network, and the effects of its being dropped are modeled by the virtual injections.

(a) Network before line l outage

(b) Network after line l outage (c) Modeling the outage by injections

Figure 2. Line outage simulation in power network

With the aim of making these two situations have the equal effect, the necessary requirements should be satisfied as:

$$P'_{mn} = P_{mn} + \Delta P_{mn} = \Delta P_m = -\Delta P_n \quad (16)$$

$$Q'_{mn} = Q_{mn} + \Delta Q_{mn} = \Delta Q_m + \frac{b}{2} V_m'^2 \\ = -\Delta Q_n + \frac{P_{mn}'^2 + Q_{mn}'^2}{V_m'^2} X_{mn} - \frac{b}{2} V_n'^2 \quad (17)$$

where

$$V_m' = V_m + \Delta V_m \quad (18)$$

$$V_n' = V_n + \Delta V_n \quad (19)$$

P_{mn}, Q_{mn}, V_m, V_n represent the line flows and node voltages in the pre fault state; $P'_{mn}, Q'_{mn}, V_m', V_n'$ represent these variables in the post fault state; $\Delta P_{mn}, \Delta Q_{mn}, \Delta V_m$ and ΔV_n represent the variations of these variables when the virtual injections have been applied, b is the susceptance of line l to ground.

In this way, it can be assumed that line l is isolated from the remainder of the network even though the breakers are closed. Compared the situation in Figure 2 (c) with Figure 2 (a), the variations are mainly expressed by those virtual injections. So if the $\Delta P_m, \Delta Q_m$ and $\Delta P_n, \Delta Q_n$ can be obtained, the variation of impedances in the relays of rest lines can be easily deduced by (13) based on pre fault system data.

1) Virtual injection powers calculation

The line flows P_{mn}, Q_{mn} of the line l can be expressed as:

$$P_{mn} = V_m V_n (G_{mn} \cos \theta_{mn} + B_{mn} \sin \theta_{mn}) - G_{mn} V_m^2 \quad (20)$$

$$Q_{mn} = V_m V_n (G_{mn} \sin \theta_{mn} - B_{mn} \cos \theta_{mn}) + B_{mn} V_m^2 \quad (21)$$

Then the linear relationship between line flow and these virtual injection powers can be expressed as:

$$\begin{bmatrix} \Delta P_{mn} \\ \Delta Q_{mn} \end{bmatrix} = D_{mn} \begin{bmatrix} \Delta \theta_m \\ \Delta \theta_n \\ \Delta V_m \\ \Delta V_n \end{bmatrix} = L_{mn} \begin{bmatrix} \Delta P_m \\ \Delta P_n \\ \Delta Q_m \\ \Delta Q_n \end{bmatrix} \quad (22)$$

$$L_{mn} = D_{mn} J_{mnmn}^{-1} \quad (23)$$

where D_{mn} is the sensitivity matrix including the sensitivities of line flow to the bus voltages ($\theta_i, \theta_j, V_i, V_j$), L_{mn} is the sensitivity matrix of line flow to virtual injections. J_{mnmn} is the submatrix of load flow Jacobin J .

According to load flow sensitivities in the pre fault state, ΔV_m and ΔV_n can be also expressed by $\Delta P_m, \Delta Q_m, \Delta P_n, \Delta Q_n$, then based on equations (16)-(23), $\Delta P_m, \Delta Q_m, \Delta P_n, \Delta Q_n$ can be calculated easily.

2) Sensitivity based relay impedance prediction

When the virtual injection variations $\Delta P_m, \Delta Q_m$ and $\Delta P_n, \Delta Q_n$ are obtained, the impedance seen by relays in the post fault state can be previously calculated based on the pre fault sensitivities. Based on equation (13), the predicted impedance variations ($\Delta R_{aij}^{Pl}, \Delta X_{aij}^{Pl}$) on any transmission line ij , after line l is tripped, can be calculated by:

$$\begin{bmatrix} \Delta R_{aij}^{Pl} \\ \Delta X_{aij}^{Pl} \end{bmatrix} = C_{ij} J_{ijmn}^{-1} \begin{bmatrix} \Delta P_m \\ \Delta P_n \\ \Delta Q_m \\ \Delta Q_n \end{bmatrix} = H_{ijmn} \begin{bmatrix} \Delta P_m \\ \Delta P_n \\ \Delta Q_m \\ \Delta Q_n \end{bmatrix} \quad (24)$$

where J_{ijmn} is the submatrix of load flow Jacobin J , and H_{ijmn} is the submatrix of H defined by (14).

3) Flow transferring identification

After the line l is tripped by the related relay to clear the fault, the practical impedance can be real time measured by relays on the key transmission lines, named by Z_{aij}^M ; and the predicted one can be named by Z_{aij}^P . It can be inferred that in those load flow transferring cases, Z_{aij}^P and Z_{aij}^M will be approximately same; while in the cases of internal faults, this condition can not be satisfied. In order to distinguish the load flow transferring from internal faults, the identification criterion can be written as:

$$|Z_{aij}^M - Z_{aij}^P| < \varepsilon |Z_{aij}^P| \quad (25)$$

where

$$Z_{aij}^M = R_{aij}^M + jX_{aij}^M \quad (26)$$

$$Z_{aij}^P = R_{aij}^P + jX_{aij}^P \\ = R_{aij}^0 + \Delta R_{aij}^P + j(X_{aij}^0 + \Delta X_{aij}^P) \quad (27)$$

R_{aij}^0 and X_{aij}^0 are measured impedance in the pre fault state; ΔR_{aij}^P and ΔX_{aij}^P are predicted variation of the impedance in the post fault state; ε represents the threshold of error caused by linearization and neglecting transient characteristics of components. If the criterion holds, this relay will define this trigger caused by flow transferring. It should be blocked or extend the delay settings until this line reached its thermal limit, and the emergent countermeasures should be taken to eliminate the overload situation. Otherwise, if the criterion cannot hold, the relay will define this situation as an internal fault and trip the line according to traditional functions.

D. Transient period consideration

So far, the network structure and all other node injections have been assumed unchanged. However, during transient period in the post fault stage, node injection powers are not constant, especially the reactive powers of generators, which is the main reason of error production. Assuming the load model in this paper applies static constant power load, the variation of generator node injection should be considered in the impedance prediction algorithm. Consequently, according to superposition principle, the final predicted relay impedance variation ($\Delta R_{aij}^P, \Delta X_{aij}^P$) on line ij , after line l is tripped, can be expressed as:

$$\begin{bmatrix} \Delta R_{aij}^P \\ \Delta X_{aij}^P \end{bmatrix} = \begin{bmatrix} \Delta R_{aij}^{Pl} \\ \Delta X_{aij}^{Pl} \end{bmatrix} + \begin{bmatrix} \Delta R_{aij}^{Pg} \\ \Delta X_{aij}^{Pg} \end{bmatrix} \quad (28)$$

where

$$\begin{bmatrix} \Delta R_{aij}^{Pg} \\ \Delta X_{aij}^{Pg} \end{bmatrix} = C_{ij} J_{ijg}^{-1} \begin{bmatrix} \Delta P_{g1} \\ \vdots \\ \Delta P_{gn} \\ \Delta Q_{g1} \\ \vdots \\ \Delta Q_{gn} \end{bmatrix} = H_{ijg} \begin{bmatrix} \Delta P_{g1} \\ \vdots \\ \Delta P_{gn} \\ \Delta Q_{g1} \\ \vdots \\ \Delta Q_{gn} \end{bmatrix} \quad (29)$$

J_{ijg} and H_{ijg} are the submatrices of J and H respectively, which represent the relationship of node voltages and relay impedances to generator node injections. $\Delta P_{g1}, \Delta Q_{g1} \dots \Delta P_{gn}, \Delta Q_{gn}$ represent the variations of n generator node injections.

Actually, the sensitivity matrix H is a high order matrix and the values of most elements in each line are quite small,

When the proposed protection strategy is taken into effect, the virtual injections and the sensitivities based on pre fault system data can be obtained, as shown in Table I.

TABLE I. VIRTUAL INJECTIONS AND RELATED SENSITIVITY

For Line T3 Outage between Bus 9 and Bus 8					Virtual Injections (p.u.)	
Sensitivity matrix D_{89}					$\begin{bmatrix} \Delta P_8 \\ \Delta P_9 \\ \Delta Q_8 \\ \Delta Q_9 \end{bmatrix} = \begin{bmatrix} 11.8 \\ -11.8 \\ -0.0035 \\ 1.87 \end{bmatrix}$	
53.3641	-53.3641	15.9851	-5.7506	-5.6143		
5.6143	54.8958	-54.6597				
Sensitivity matrix L_{89}						
0.0090	-0.5486	0.0141	-0.0148			
0.0071	0.0058	0.1168	-0.2042			

Then based on the impedance sensitivity method described in Section II, the related sensitivities and the predicted impedance variation can be obtained, as shown in Table II.

TABLE II. IMPEDANCE PREDICTION ON T4

For Line T4 between Bus 10 and Bus 9						
Sensitivity matrix C_{109}				Predicted impedance (ohm)		
-1.1346	1.1346	-0.0312	0.0318	$\begin{bmatrix} R_{a109}^0 \\ X_{a109}^0 \end{bmatrix} = \begin{bmatrix} 37.45 \\ 1.25 \end{bmatrix}$		
-0.0310	0.0310	1.1422	-1.1621			
Sensitivity matrix H_{10989}				$\begin{bmatrix} \Delta R_{a109}^{pl} \\ \Delta X_{a109}^{pl} \end{bmatrix} = \begin{bmatrix} -13.3589 \\ 0.0365 \end{bmatrix}$		
0.0001	0.0064	0.0006	0.0005			
-0.000	-0.0009	-0.0007	-0.0057			

With consideration of node injection variation, if the delay communication takes 5 circles, the predicting calculation can be started after 10 circles, namely 0.2s after the fault. Here the nodes of generator G01, G11, G21 and G22 will be chosen to be monitored. Then the injection variation and predicted curves can be shown in Figure 6.

Figure 6. Generator injection variation and predicted impedance locus

From Figure 6 (e), the biggest error about 3Ω between predicted impedance (blue locus) and measured impedance (black locus) appeared just after the fault was cleared. But in about 500ms, the error decreased into 2Ω . So the threshold of identification criterion (25) can be set as 2Ω , and ε applies 0.08. Then this load flow transferring induced relay operation can be prevented by the proposed protection strategy in Section III.

V. CONCLUSION

In this paper, a multi agent system based protection strategy is proposed to prevent the post fault load flow transferring induced unexpected relay operation. Impedance sensitivity based prediction algorithm is used to predict the impedance locus in the post fault state, based on the pre fault system data. The injection variations of generator nodes during the post fault state, including both active and reactive powers, have been considered to correct the prediction algorithm. The RTDS based case study has demonstrated the proposed strategy can successfully predict the impedance reviewed by relay on key transmission lines and prevent the unexpected relay trips due to flow transferring in the post fault state.

REFERENCES

- [1] P. Kundur, *Power System Stability and Control*, McGraw-Hill Press, 1993
- [2] T. Cutsem and C. Vournas, *Voltage stability of Electric Power System*, Springer, 2008.
- [3] J. McCalley, O. Oluwaseyi, V. Krishnam, R. Dai, C. Singh, K. Jiang, "System Protection Schemes: Limitations, Risks, and Management," Final Report from PSERC, 2010.
- [4] L. Cheng, B. Zhang, Z. Hao, J. Shu, Z. Bo, "Feasibility Study on Active Power Security Protection of Transmission Section", *Power and Energy Engineering Conference, 2009, APPEEC*, 2009.
- [5] K. Yunus, G. Pinares, L. Tuan, L. Bertling, "A combined zone-3 relay blocking and sensitivity-based load shedding for voltage collapse prevention", *Innovative Smart Grid Technologies Conference Europe (ISGT Europe)*, 2010.
- [6] T. Bi, H. Xu, S. Huang, Q. Yang, "Flow transferring identification algorithm with consideration of transient period", *Power & Energy Society General Meeting*, 2009.
- [7] X. Dong, L. Ding, K. Liu, S. Shi, B. Wang, L. Cui, Z. Bo, "Smart system protection based on local information", *10th IET International Conference on Developments in Power System Protection (DPSP 2010)*, pp. 1-4, 2010.
- [8] NERC, Aug. 2005, "Relay loadability exceptions: determination and application of practical relaying loadability ratings," [Online]. Available: <http://www.nerc.com/~filez/spctf.html>.
- [9] J. Zhu, *Optimization of Power System Operation*, John Wiley & Sons, Inc., Hoboken, New Jersey, 2009.
- [10] Z. Liu, Z. Chen, H. Sun, C. Liu, "Control and Protection Cooperation Strategy for Voltage Instability", *47th International Universities' Power Engineering Conference (UPEC)*, 2012.
- [11] V. Akhmatov, "Analysis of dynamic behaviour of electric power systems with large amount of wind power", Ph.D. dissertation, Dept. Electric Power. Eng., Technical Univ. Denmark, Kgs. Lyngby, 2003.