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Paper

# Stability Analysis and Active Damping for *LLCL*-Filter-Based Grid-Connected Inverters

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A higher-order passive power filter (*LLCL* filter) for a grid-connected inverter is becoming attractive for the industrial applications owing to the possibility of reducing the cost of copper and the magnetic material. To avoid the well-known resonance problems of the *LLCL* filter, it is necessary to use either passive or active damping methods. In this study, the stability of the *LLCL*-filter-based grid-connected inverter is analyzed and a critical resonant frequency for the *LLCL* filter is identified when sampling and transport delays are considered. In the high-resonant-frequency region, active damping is not required; however, active damping is necessary in the low-resonant-frequency region. The basic *LLCL* resonance damping properties of different feedback states based on a notch filter concept are also studied. Then, an active damping method using capacitor current feedback for the *LLCL* filter is introduced. On the basis of this active damping method, a design procedure for the controller is given. Last, both simulation and experimental results are provided to validate the theoretical analysis of this study.

Keywords: LLCL filter, grid-connected converter, active damping, current control, resonant frequency, stability

# 1. Introduction

Recently, due to the energy crisis, Distributed Generation (DG) systems using clean renewable energy such as solar energy, wind energy, etc., have become an important issue in the technical research. The voltage Source Inverter (VSI) has increasingly been used to enable the integration of renewable power generations into the power grid<sup>(1)</sup>. Typically, a simple series inductor *L* is inserted between the voltage source inverter (VSI) and the grid to attenuate the high-frequency Pulse Width Modulation (PWM) harmonics to a desirable limit. But the high values of the *L* filter needs to be adopted to reduce the current harmonics around the switching frequency, which would lead to a poor dynamic response of the system and a high power loss. A low-pass passive power filter, the *LCL* filter, can achieve a high harmonic attenuation performance with less total inductance<sup>(2)</sup>.

In order to further reduce the total inductance, the *LLCL* filter was proposed <sup>(3)</sup>. Compared with the *LCL* filter, the total inductance and volume of the *LLCL* filter can be reduced by  $25\%\sim40\%$ . So, the *LLCL* filter for the grid-connected inverter is becoming attractive for industrial applications <sup>(4)</sup>. The applications of *LLCL* filter for a three-phase three-wire Shunt Active Power Filter (SAPF) <sup>(5)</sup> and a Large-Scale Wave Power Plant <sup>(6)</sup> have been analyzed.

As a high order filter, the LLCL filter has also a resonant

problem. To suppress the possible resonances of an *LCL* filter or an *LLCL* filter, active damping  $^{(7)-(12)}$  or passive damping  $^{(13)-(15)}$  methods may be adopted. Passive damping is realized by adding additional components in the system but it causes a decrease of the overall system efficiency. For a stiff grid application, the passive damping strategy seems to be more attractive. In order to achieve a higher efficiency and flexibility, the active damping method might be preferred, although at the risk of higher cost of sensors and more control complexity. Normally, digital sampling and transport delays caused by controller and modulation, as well as discretization effects are taken into account. The delay will influence the stability of the system and when the resonant frequency varies, damping method is usually required in an *LCL* filter <sup>(9)</sup>.

For *LLCL* filter, when the ratio of the resonant frequency to the control frequency is high the system can be stable without damping but the system robustness is not good if the resonant frequency is around the 1/6 of the control frequency. In this paper, all possible feedback states of currents and voltages of *LLCL* filter capacitors and inductors with different feedback transfer functions are considered. The results show how the various feedback signals need to be fed back based on notch concept in order to achieve resonance damping. Based on the available choices of feedback variables, active damping of the capacitor current control strategy is used for *LLCL* filter. The Proportional-Resonant (PR) controller is also used in this paper. PR can provide larger gain at the fundamental frequency to eliminate the steady state error compared with PI regulator<sup>(16)</sup>.

First, the system and its stability are analyzed in Section 2. In Section 3, a more general analysis of different active

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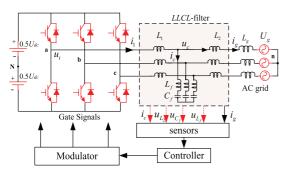


Fig. 1. General structure of three-phase grid-connected inverter with *LLCL* filter

Table 1. Test system parameters

DC link voltage $U_{dc}$	650 V	Grid frequency $f_o$	50 Hz
Grid phase voltage $U_g$	220 V	Sampling frequency $f_d$	10 kHz
Switching frequency $f_s$	10 kHz	Sampling period $T_d$	100 us

resonance damping solutions is carried out. The basic *LLCL* resonance damping properties of different feedback states are studied. In Section 4, design procedures of current controller and capacitor current feedback active damping are described. Last, simulated and experimental results are shown to verify the proposed design method.

# 2. Modeling and Stability of *LLCL*-Filter-Based Grid-Connected Inverter

**2.1 Modeling of** *LLCL***-Filter-Based Grid-Connected Inverter** A three-phase voltage source converter connected to the grid via an *LLCL* filter is studied as shown in Fig. 1.  $U_{dc}$  is the dc input voltage of the inverter. The inverter output voltage and current are represented as  $u_i$  (phase voltage) and  $i_1$ , and the grid voltage and current are represented as  $u_g$  and  $i_g$ .  $i_c$  is the capacitor current,  $u_{Cf}$  is the output voltage of the capacitor,  $u_{Lf}$  is the output voltage of the resonant inductor,  $u_c$  is the voltage of  $L_f$ - $C_f$  circuit and  $L_g$  is the grid impedance. The grid current feedback control will be discussed in this paper. The system parameters are given in Table 1.

Neglecting the influence of the grid impedance and the Equivalent Series Resistances (ESRs) of inductors and capacitors, the transfer function  $i_g(s)/u_i(s)$  of the *LLCL* filter can be derived in (1).

As shown in (2),  $\omega_r$  is the resonant frequency in radians per second),  $f_r$  is the resonant frequency in Hz. If the inductance of  $L_f$  is set to zero, then the transfer functions of the *LCL* filter can also be calculated. For voltage source converters the inverter-side current harmonics are dominated by the switching frequency. According to IEEE 519-1992<sup>(17)</sup>, harmonics higher than the 35th should be less than 0.3% of the rated fundamental current. Figure 2 shows bode plots of

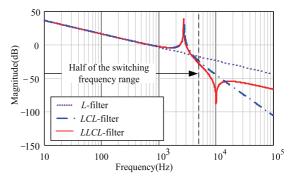


Fig. 2. Bode plots of transfer functions  $i_g(s)/u_i(s)$  for different filters

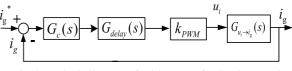


Fig. 3. Block diagram of grid current feedback control

transfer functions  $i_g(s)/u_i(s)$  for different filters. For *L* filter, L = 3.6 mH. For *LCL* filter,  $L_1 = 2.4 \text{ mH}$ ,  $L_2 = 1.2 \text{ mH}$  and  $C_f = 4 \mu\text{F}$ . For *LLCL* filter,  $L_1 = 2.4 \text{ mH}$ ,  $L_2 = 1.2 \text{ mH}$ ,  $L_f = 64 \mu\text{H}$  and  $C_f = 4 \mu\text{F}$ . The characteristics of the three filters at the low frequencies are similar. The dominant harmonics of the grid-side current of the *LLCL* filter will be around the double of the switching frequency since the harmonics around the switching frequency are attenuated by the trap circuit  $L_f$ - $C_f$ . That is the reason *LLCL* filter has smaller inductance or capacitance than *LCL* filter when they meet the same harmonic requirement of the grid-injected current <sup>(18)</sup>.

According to (2), the resonant frequency of the *LLCL* filter can be higher than the resonant frequency of the *LCL* filter due to the smaller size. The ratio of the resonant frequency and the sampling frequency is related to the stability of *LCL* filter due to the delay<sup>(11)</sup>. It means that if an *LCL* filter with high resonant frequency is chosen the design of the active damping gets more difficult and a poorer robustness is obtained<sup>(19)-(22)</sup>.

2.2 Stability of LLCL-Filter-Based Grid-Connected **Inverter with Different Resonant Frequencies** The control block diagram of a single loop controller of the LLCL filter based three-phase grid-connected inverter without any damping methods is shown in Fig. 3.  $T_d$  is the sampling period. The inverter can be modeled as a linear gain  $k_{PWM}$ , expressed as  $k_{PWM} = 0.5 U_{dc}$ .  $G_c(s)$  is a PR controller as shown in (3), where  $k_p$  and  $k_i$  are representing its proportional gain and the integral gain of the fundamental resonant frequency respectively.  $G_{delay}(s)$  is the delay part in series with the forward path. In the s-domain one sample period delay  $e^{-T_d s}$ is included due to computation in a real application. When the PWM reference is held on and compared to the triangular carrier to generate the duty cycle, a Zero-Order-Hold (ZOH) is in series of the open loop and discretization of the system introduces delay, as shown in (4). A PWM delay of half sampling period is introduced. Hence, the total delay in the continuous form is shown in (5).

$$G_c(s) = k_p + \frac{k_i s}{s^2 + (\omega_0)^2}$$
(3)

 Table 2.
 *LLCL*-filter parameters and resonant frequency of three cases under study

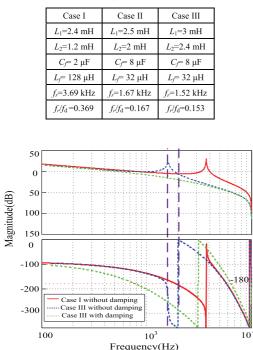


Fig. 4. Bode plot of the forward path transfer function for the grid current feedback control

G(s) is the open transfer function of the grid current feedback control considering the total delay, which can be expressed as:

$$G(s) = G_{delay}(s)k_{PWM}G_c(s)G_{u_i \to i_g}(s) \cdots \cdots \cdots \cdots \cdots (6)$$

Table 2 shows three different cases with different resonant frequencies. Figure 4 shows the bode plot of the forward path transfer function for the grid current feedback control. It can be seen from Fig. 4 that the *LLCL* filter resonance has no influence on system stability when the resonant frequency is high (Case I), because the phase is already well below  $-180^{\circ}$  before the re sonant frequency due to the sampling and transport delay. When the resonant frequency is low (Case III), the phase curve passes through  $-180^{\circ}$  at the resonant frequency and the system is not stable without damping. When active damping is added in Case III, the resonance is damped and the system can be stable.

This analysis identifies that there is also a critical frequency for *LLCL* filter, and above it, active damping can be avoided by adjusting the controller gain.

 $G_c(s)$  can be regarded as  $k_p$  at crossover frequency. When  $\angle G_o(j\omega_k) = -\pi$ , the phase of the single open loop is shown in (7). The root of the function can be calculated as  $\omega_k = \pi/(3T_d)$ . If a phase angle is already below  $-180^\circ$  at this resonant frequency, the system can be stable. It can also be deduced that the critical frequency  $f_k = f_d/6$ .

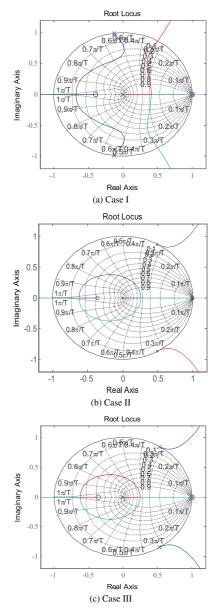
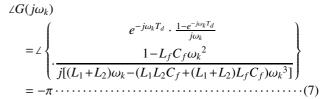


Fig. 5. Root loci of grid current feedback (without damping) of different cases specified in Table 2



Hence, a single loop is sufficient to be stable when the resonant frequency is above the critical frequency and active damping is necessary when the resonant frequency is below the critical frequency. As shown in Table 1,  $f_d$  is 10 kHz. Figure 5 shows the closed loop root loci of the three cases in Table 2 for the single loop grid current feedback in z-domain. A Zero-Order-Hold (ZOH) transform is applied on the transfer function  $i_g(s)/u_i(s)$  of the *LLCL* filter. Figure 5(a) depicts the case when the resonant frequency of the *LLCL* filter is above the critical frequency. The poles initially track inside the unit circle. Figure 5(b) shows the case when the resonant frequency of the *LLCL* filter is at the critical frequency.

and the system is on the edge to be unstable. When the resonant frequency is less than the critical frequency the system will always be unstable regardless of what the proportional gain is without damping, as shown in Fig. 5(c). In this case, a damping method is necessary to be used.

# 3. Active Damping with Different Feedback States

**3.1** Notch Filter Concept Active damping methods can be classified into two main classes: multi-loop and filterbased active damping <sup>(7)</sup>. Traditionally, a notch filter is directly added in the current loop to compensate the resonant peak of the *LCL* filter. In order to provide a good damping the frequency of the Notch filter has to be tuned at the resonance frequency of the *LCL* filter. Notch filter concept can also be implemented by multi-loop control. The control structure of the inner current loop with a notch filter concept <sup>(22)</sup> is shown in Fig. 6.

$$B(s) = \frac{k_{PWM}}{1 + k_{PWM}K(s)N(s)} = \frac{s^2 + \omega_r^2}{s^2 + 2\zeta_2\omega_r s + \omega_r^2}$$
.....(8)

In order to eliminate the resonant peak at the frequency  $\omega_r$ , the notch B(s) should have a negative peak in  $\omega_r$ , so it can be expressed as (8). There are different variables which can be chosen as the control object for *LLCL* filter. K(s) is the feedback coefficient. Table 3 shows the transfer functions of different variables feedback. The structure of N(s) depends on the feedback variables including the filter capacitor voltage  $u_{cf}$ , filter capacitor current  $i_c$ , filter resonant inductor voltage in grid side  $u_{L2}$ , inductor voltage in resonant circuit  $u_{Lf}$ . It can be seen from Table 3, the feedback function of the grid side inductor voltage is a little complex. The sensor location depends on the application situations. For different ratios between the resonant frequency and the control frequency, the selected approaches behave differently<sup>(10)</sup>.

**3.2 Filter Capacitor Current Feedback** For the *LCL* filter, the capacitor current feedback and capacitor voltage feedback are often used<sup>(10)</sup>. When the capacitor current feedback is sensed, K(s) can easily be configured as a proportional coefficient, which is isolated with the system

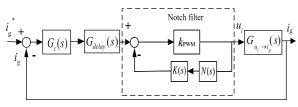


Fig. 6. Active damping based on a notch filter concept

parameters. N(s) can be expressed as:

$$N(s) = G_{u_i \to i_c}(s) = \frac{\omega^2 {}_r L_2 C_f s}{(s^2 + \omega^2 {}_r)(L_1 + L_2)} \cdots \cdots \cdots (9)$$

Then the open loop transfer function of the capacitor current feedback control from  $i_g$  to  $i_g^*$  is shown in (10).

The capacitor current feedback can dampen the resonant peak and make the system stable.

$$G'(s)_{lopen} = \frac{k_{PWM}\omega_{r}^{2}(L_{f}C_{f}s^{2}+1)G_{c}(s)G_{delay}(s)}{(s^{2}+\omega_{r}^{2})(L_{1}+L_{2})+K_{i_{c}}G_{delay}(s)k_{PWM}L_{2}s\omega_{r}^{2}}\frac{1}{s}$$
.....(10)

**3.3 Filter Capacitor Voltage Feedback** When the capacitor voltage is sensed, a derivative filter capacitor voltage feedback can be used for the resonance damping. Some papers have illustrated this method for an *LCL* filter. As shown in Table 3, a differential feedback is necessary but it may cause noise problems in the control, because it will amplify high-frequency signals.

#### 3.4 Filter Resonant Inductor Voltage Feedback

When the resonant inductor voltage is sensed, the integral feedback can be expected to keep the system stable. Normally, the filter capacitor current or voltage is sensed for the *LCL* filter. This is a new active damping method for *LLCL* filter which can reduce the cost of sensors <sup>(23)</sup>. The feedback coefficient is integral and the structure of N(s) is the transfer function from  $u_i$  to  $u_{Lf}$ .

The next section will only analyze the design of capacitor current feedback as an active damping method, as this is the most promising method.

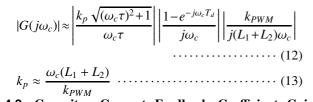
# 4. Design of Current Regulator and Capacitor Current Feedback Coefficient

**4.1 PR Controller Gain Design** The maximum possible controller gains for the system can now be analytically determined using the concepts developed in (24)–(26). The proportional gain is then set to achieve unity gain at the desired crossover frequency  $f_c/\omega_c$ . The choice of  $k_p$  can be decided by the system bandwidth satisfying the desired phase margin  $\Phi_m^{(9)}$ . For a single loop control, the phase angle at the crossover frequency can be described in (11). As shown in Fig. 2, the *LLCL* filter is approximate to an *L* filter in the low frequency. In addition, the cross-over frequency  $\omega_c$  can be determined.

The system open-loop gain achieves unity at  $\omega_c$ . Then the maximum gain can be calculated as:

Variable	$u_{c_f}$	$i_c$	$u_{\scriptscriptstyle L_f}$	$u_{L_2}$
N(s)	$\frac{\omega_r^2 L_2}{(s^2 + \omega_r^2)(L_1 + L_2)}$	$\frac{\omega_r^2 L_2 C_f s}{(s^2 + \omega_r^2)(L_1 + L_2)}$	$\frac{\omega_{r}^{2}L_{2}C_{f}s^{2}}{(s^{2}+\omega_{r}^{2})(L_{1}+L_{2})}$	$\frac{\omega_r^2 L_2 (L_f C_f s^2 + 1)}{(s^2 + \omega_r^2)(L_1 + L_2)}$
K(s)	$sK_{u_{C_f}}$	$K_{i_c}$	$K_{u_{L_f}}/s$	$K_{u_{L2}}\frac{C_f s}{L_f C_f s^2 + 1}$

Table 3. Transfer functions of different variables as feedback



4.2 Capacitor Current Feedback Coefficient Gain

The denominator of the closed loop transfer function of the *LLCL* filter is shown in (14) based on (10). The minimum value of  $K_{ic}$  can be found from (13) using the limiting ratio of the proportional gain  $k_p$  to dampen as shown in (14). According to the Routh's Stability Criterion, the range of  $K_{ic}$ can be obtained to be like given in (15).

$$D(s) = [L_1 L_2 C_f + (L_1 + L_2) L_f C_f] s^4 + K_{i_c} k_{PWM} L_f L_2 C_f s^3 + (L_1 + L_2) s^2 + k_p k_{PWM} s + k_p k_i k_{PWM} \cdots \cdots (14)$$

$$K_{i_c} \ge \frac{k_p}{(L_1 + L_2)L_2} [L_1 L_2 + (L_1 + L_2)L_f] \cdots \cdots \cdots (15)$$

 $GM_1$  and  $GM_2$  are defined by the gain margins of (10) at  $f_r$ and  $f_d/6$  respectively<sup>(9)</sup>. Then the limitation of  $K_{ic}$  can be obtained from (16) and (17).  $GM_1 > 0$  means the gain is lower than 0 dB at the corresponding frequency. When  $f_r < f_d/6$ ,  $GM_1 > 0$ . When  $f_r > f_d/6$ ,  $GM_1 < 0$  and  $GM_2 > 0$  to make sure the magnitude of the loop gain at  $f_d/6$  must be lower than 0 dB and at  $f_r$  must be larger than 0 dB. (17) is the lower limitation and (16) is the upper limitation.  $K_{ic}$  should satisfy this region.

**4.3 Design Example** Taken Case III as an example, the basic design procedures can be addressed as:

- 1) Determine the specifications of the loop gain. According to Case III, the resonant frequency is smaller than  $f_d/6$ , so  $GM_1$  should be larger than 0. The desired phase margin  $\Phi_m$  should be larger than 40° in order to get a good dynamic response and stability margin.
- 2) Obtain the value of  $k_p$  and  $f_c$  to satisfy all the requirements according to (11), (13) and (14),  $f_c = 1$  kHz is chosen to obtain fast dynamic response. Then  $k_p$  is calculated as 0.06 according to (13).
- 3) Figure 7 shows the closed loop root locus branch of the system with the capacitor current coefficient increasing when  $k_p$  is set to 0.06. There is a stable range of  $K_{ic}$  which can be obtained as shown in Fig. 7. The calculated gain should follow the region. For Case III, the limitation region is from 0.024–0.032.
- 4) Taking  $f_c = 1 \text{ kHz}$  and the calculated feedback gain in (15), (16) and (17) to check whether they satisfy the function and  $GM_1$  is larger than 0.

### 5. Simulation and Experimental Results

**5.1 Simulation Results** In order to illustrate the stability and verify the active damping method of the *LLCL* filter based grid-connected inverter, a three-phase inverter with 6kW rated power is simulated using PLECS Blockset and

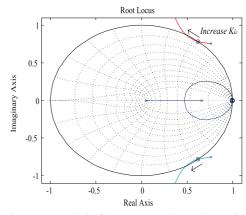


Fig. 7. Root loci of the system with  $K_{ic}$  increasing

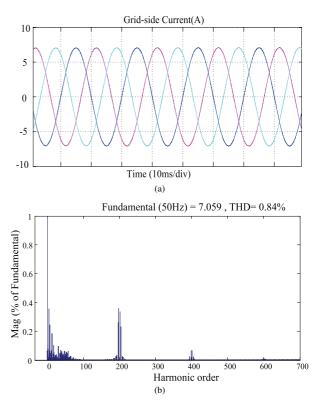


Fig. 8. Grid-side currents of *LCL* filter based inverter (a) Current waveforms and (b) The current spectrum

MATLAB. This paper uses PR controller and SPWM modulation. The detailed system parameters are listed in Table 1.

As discussed above, the *LLCL* filter can get the same harmonic attenuation as the *LCL* filter with a smaller inductance or capacitor which means *LLCL* filter has some superiority. A comparison is done by the simulations. Fig. 8 and Fig. 9 show the grid-side currents of *LCL* filter based inverter and *LLCL* filter based inverter respectively. For the *LCL* filter,  $L_1 = 2.4$  mH,  $L_2 = 1.2$  mH and  $C_f = 4 \mu$ F; For *LLCL* filter,  $L_1 = 2.4$  mH,  $L_2 = 1.2$  mH,  $L_f = 64 \mu$ H and  $C_f = 4 \mu$ F. The grid-current THD of *LCL* filter based inverter is 0.84% and harmonics around switching frequency are higher than 0.3% of the fundamental current. The grid-current THD of *LLCL* filter based inverter is 0.61% and dominant harmonics are around the double of the switching frequency. It shows the *LLCL* filter.

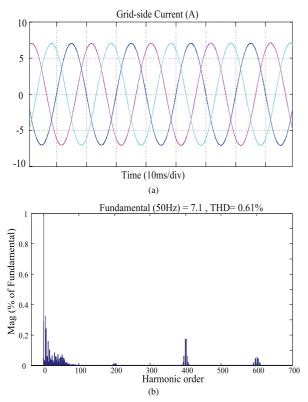


Fig. 9. Grid-side currents of the *LLCL* filter based inverter (a) Current waveforms and (b) The current spectrum

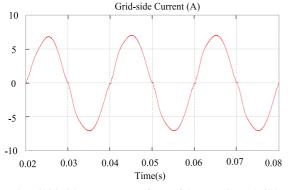


Fig. 10. Grid-side current waveform of Case I ( $f_{res} = 3.69 \text{ kHz}$ )

Then, in order to investigate the stability of the system without damping in different resonant frequencies, the *LLCL* filter is analyzed into three cases as shown in Table 2, with different parameters: one with a high resonant frequency, one with a critical resonant frequency and the other with a low resonant frequency. According to (11), the controller gain is  $k_p = 0.06$  and  $k_i = 20$ .

(1) Case I: high frequency  $f_{res} = 3.69 \text{ kHz}$ 

In the Case I, the resonant frequency is high (3.69 kHz) and the crossover frequency is set to 1 kHz in order to get a fast response and to meet a phase margin limitation. It can be seen from Fig. 10 the system is stable.

(2) Case II: critical frequency  $f_{res} = 1.67 \text{ kHz}$ 

As it mentioned before, there is a critical frequency for the *LLCL* filter. It is calculated as  $f_d/6$  based on the function (7). It can be seen from Fig. 11, the system is almost unstable at the critical frequency. When the grid impedance  $i_g$  is increased, the resonant frequency will be deduced more.

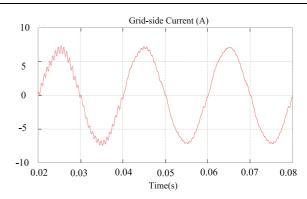


Fig. 11. Grid-side current waveform of Case II ( $f_{res} = 1.67 \text{ kHz}$ )

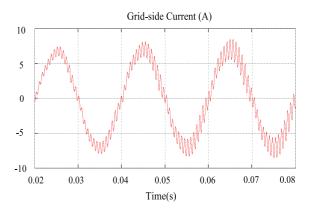


Fig. 12. Grid-side current waveform of Case II when  $L_2 + L_g = 2.4 \text{ mH} (f_{res} = 1.60 \text{ kHz})$ 

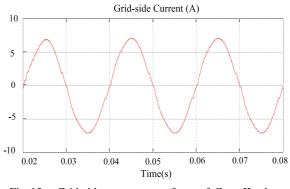


Fig. 13. Grid-side current waveform of Case II when  $L_2 + L_g = 1.2 \text{ mH} (f_{res} = 1.95 \text{ kHz})$ 

As shown in Fig. 12, when the grid impedance  $L_g$  is set to 0.4 mH, the resonant frequency is reduced to 1.6 kHz, which is under the critical frequency and the system is unstable.

As shown in Fig. 13, when the grid-side inductance  $L_2$  is changed to 1.2 mH, the resonant frequency is increased to 1.95 kHz and the system is changed from critical state to stable state.

(3) Case III: Low frequency  $f_{res} = 1.52 \text{ kHz}$ 

In Case III, the resonant frequency is low (1.52 kHz). It can be seen from Fig. 14 that the system is unstable without damping.

So, when designing the parameters it is better to make the resonant frequency higher in order to get a better stability and robustness. When the resonant frequency is lower or nearby the critical frequency, the active damping method is necessary to be used. In this paper, take Case III as an example,

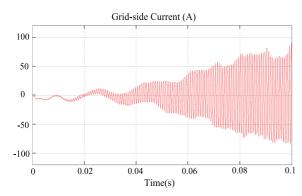


Fig. 14. Grid-side current waveform of Case III ( $f_{res} = 152 \text{ kHz}$ )

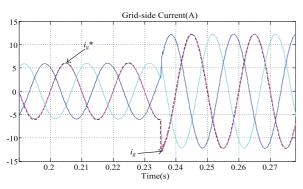


Fig. 15. Grid-side current waveforms of Case I (high resonant frequency) without active damping

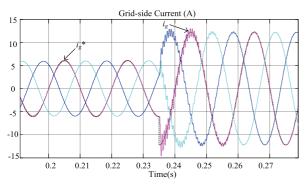


Fig. 16. Grid-side currents waveforms of Case III (low resonant frequency) with active damping

the active damping with capacitor current feedback is used. Applying the parameters described in Table 1 and Table 2, the crossover frequency is set to 1 kHz in order to get a high response and meet the phase margin limitation.

In order to get enough phase margins in Case III, the crossover frequency should be set below the resonant frequency. According to (13), the PR controller gain should be  $k_p = 0.06$ . Figure 15 and Fig. 16 show the dynamic performance of Case I and Case III respectively when the reference current changes from 6.5 A to 12.9 A at time 0.235 s to test the dynamic performance. The black dash line is the single phase of the reference grid current  $i_g^*$ . It can be seen from Fig. 15, there is no oscillations during the transient in the high resonant frequency without damping methods. The tracking performance between  $i_g$  and  $i_g^*$  is good.

Figure 16 shows the dynamic performance in the low resonant frequency of the *LLCL* filter when the capacitor current feedback active damping method is used.  $K_{ic}$  in Case III is

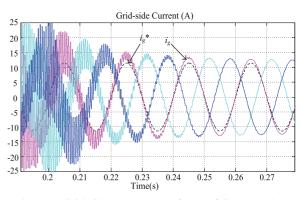


Fig. 17. Grid-side currents waveforms of Case III when active damping is enabled at time 021 s

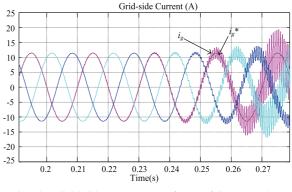


Fig. 18. Grid-side currents waveforms of Case III when  $K_{ic}$  is increased at time 0235 s

chosen to be 0.028 according to the design method. It can be seen from Fig. 16 that there is an oscillation when the reference current steps. But it becomes stable after half a period.

Figure 17 shows that the system is unstable at the beginning in the low resonant frequency case, but it turns out to be stable when active damping is enabled at 0.21s in Case III. After three period circles the grid current tracks the reference current. Fig.18 shows that the system becomes unstable when the value of the capacitor feedback coefficient is increased to 0.05. There is a limited stable region for the feedback coefficient, which verifies the analysis in Fig. 7.

**5.2 Experimental Results** The experimental setup consists of a 2.2 kVA Danfoss three-phase converter connected to the grid through an isolating transformer and the DC-link supplied by Delta Elektronika power sources. The control algorithm is implemented on a dSPACE DS1103 board. Due to the limitation of the setup, the power in the experiment is lower than in the simulation. The system parameters are listed in Table 1 and Table 2.

Figure 19 shows the dynamic transition of the grid-side currents and  $L_f$ - $C_f$  circuit voltage in the high resonant frequency case (Case I) when the power is increased without active damping. The reference current steps from 2.4 A–4.8 A and the system can be stable without damping, when the ratio of the resonant frequency to the control frequency is higher than 1/6. Figure 20 shows the grid-side currents and  $L_f$ - $C_f$  circuit voltage when the active damping is enabled in the low resonant frequency case (Case III). The capacitor current proportional feedback active damping is used. The system cannot be stable without damping, when the ratio of the resonant

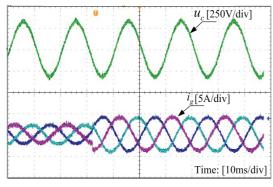


Fig. 19. Experimental results in high resonant frequency case I without active damping

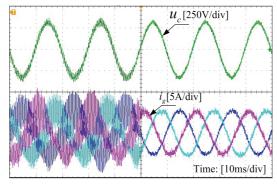


Fig. 20. Experimental results in low resonant frequency case III when active damping is enabled

frequency to the control frequency is lower than 1/6.

# 6. Conclusion

Compared with the *LCL* filter, the resonant frequency of *LLCL*-filter is higher and it is easier to be stable. The work presented in this paper shows when damping method is not required for an *LLCL* filter considering different sampling and transport delays. The critical frequency is determined by the delay time and sample frequency.

In the low resonant frequency case, or critical case, the resonant frequency is easy to be changed due to the parameter variation and the grid impedance variation. Then, the damping methods are necessary to be used. Based on the analysis of possible feedback variables, the capacitor current feedback active damping control strategy is chosen for the *LLCL* filter. Simulation and experimental results prove the influence of the resonant frequency and the design of capacitor current proportional feedback. The control of the *LCL* filter and *LLCL* filter are similar and the additional inductor of *LLCL* filter brings no extra control difficulties.

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