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PLL with MAF-Based Prefiltering Stage: Small-Signal Modeling and Performance Enhancement

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Abstract—In three-phase applications, the synchronous-reference frame phase-locked loop (SRF-PLL) is a standard PLL, which benefits from a simple structure and satisfactory performance under symmetrical and undistorted grid conditions. Under unbalanced and harmonically distorted conditions, however, it suffers from a very poor performance in the detection of grid voltage parameters. To deal with this challenge, incorporating different filters inside its control loop or before its input has been proposed. Recently, using the moving average filter (MAF) as the SRF-PLL prefiltering stage has been suggested in several works. The MAF is a linear-phase filter that can behave like an ideal low-pass filter under certain conditions. The main aim of this letter is to derive the small-signal model of the SRF-PLL with MAF-based prefiltering stage (briefly called the PMAF-PLL), which has not been presented before. This model enables the designer to simply analyze the stability condition and dynamic behavior of the PMAF-PLL. After developing the model, a simple modification to enhance the PMAF-PLL performance under frequency varying environments is presented. Finally, the equivalence of PMAF-PLL and the space-vector Fourier Transform based PLL (SVFT-PLL), which is a well-known PLL in three-phase applications, is proved. This equivalence implies that the small-signal model of the PMAF-PLL and the method presented to enhance its performance are valid for the SVFT-PLL.

Index Terms—Moving average filter (MAF), phase-locked loop (PLL), synchronization.

I. INTRODUCTION

Besides the problem of grid voltage imbalance, which may be due to asymmetrical voltage sags, single-phase loading and grid impedance imbalance, the synchronization of grid-connected power electronics based equipment is facing more serious challenges: presence of dc offset and large harmonic components in the grid voltage; while the former may be caused by grid faults, A/D conversion, measurement devices, etc. [1], the latter is commonly due to the proliferation of power electronics based nonlinear loads [2]. To deal with these

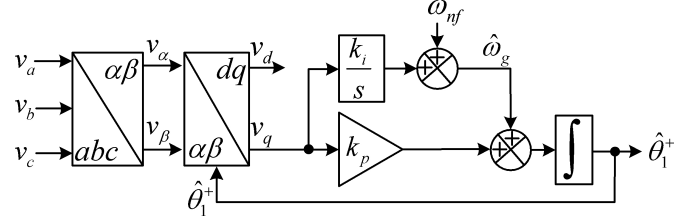


Fig. 1. Schematic diagram of the SRF-PLL.

challenges, many advanced synchronization techniques have been developed in recent years. Most of these techniques are based on phase-locked loops (PLLs) [3].

Fig. 1 shows the schematic diagram of the standard synchronous-reference frame PLL (SRF-PLL), which is a standard PLL in three-phase applications. In the SRF-PLL, the three-phase voltages are transformed into the dq reference frame by applying the Clarke's transformation and then the Park's transformation. The signal v_q (or v_d , depending on the Park's transformation), which contains the phase error information, is then fed to a proportional-integral (PI) controller to ensure a zero average phase error under both phase-angle jumps and frequency drifts. The SRF-PLL has a limited disturbance (dc offset, harmonic, and imbalance) rejection capability. To deal with this issue, including additional filter(s) either inside the SRF-PLL control loop or before its input has been proposed. The conventional infinite impulse response low-pass filters [4], the moving average filter (MAF) [5]–[7], the notch filter [8], the dq -frame delayed signal cancellation operator [9]–[11] and the repetitive regulator [12] are well-known in-loop filtering techniques, and the complex coefficient filters [13], [14], the recursive discrete Fourier transform [15], the $\alpha\beta$ -frame delayed signal cancellation operator [10]–[11], [16]–[17], and the dual second-order generalized integrators [18] are popular prefiltering techniques.

Recently, using the MAF as the SRF-PLL prefiltering stage has been proposed in several works [19]–[21]. The schematic diagram of the SRF-PLL with MAF-based prefiltering stage (hereafter, briefly called the PMAF-PLL) can be observed in Fig. 2. In the PMAF-PLL, the SRF-PLL and MAF-based prefiltering stage are both working in the synchronous-reference frame, but with different rotating angles. This rotating angle difference has made the small-signal modeling and, consequently, the stability and dynamic behavior analysis of the

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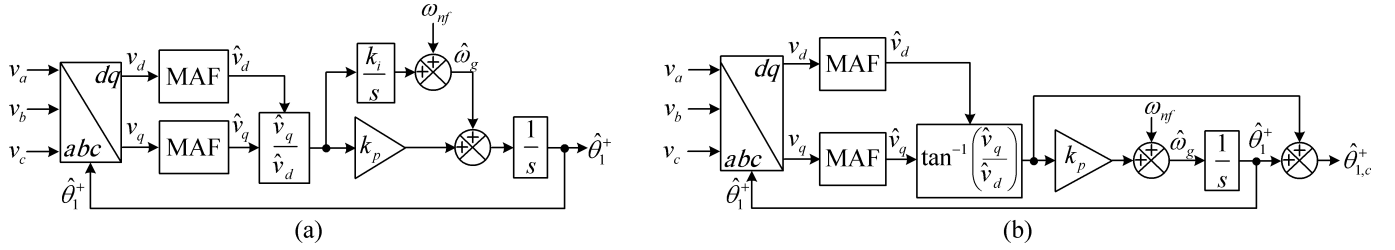


Fig. 10. Schematic of (a) the MAF-PLL and (b) the QT1-PLL.

 TABLE I
CONTROL PARAMETERS

	Enhanced PMAF-PLL	Standard MAF-PLL	QT1-PLL
Proportional gain, k_p	804	41.42	49.8
Integral gain, k_i	40426	710.68	—
MAF window length, T_w	0.02 s	0.02 s	0.02 s

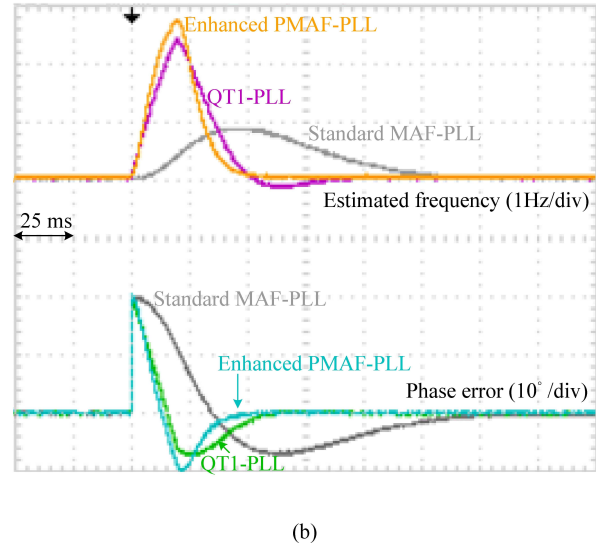
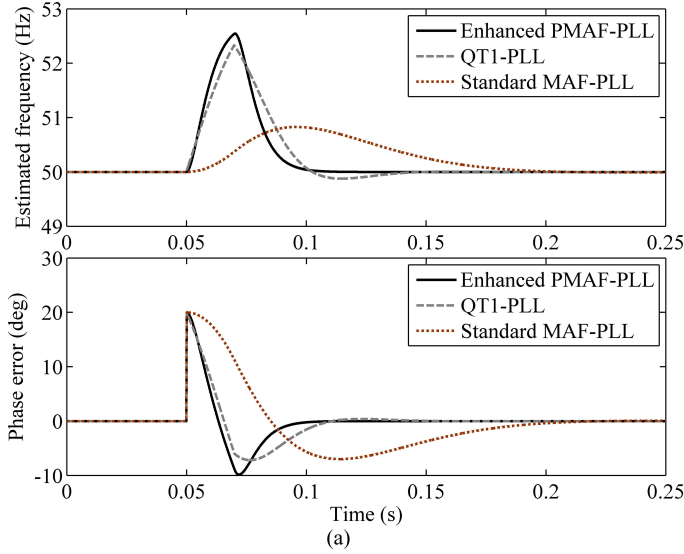


Fig. 11. (a) Simulation and (b) experimental results under the test case 1.

Notice that the SVFT and discrete Fourier Transform (DFT) have the same z -transforms, because the SVFT corresponds to the application of the DFT to a complex signal.

In the space-vector notation, the input-output relation of the MAF-based prefiling stage in Fig. 2 can be described as

$$\vec{v}_{\alpha\beta,1}^+(t) = e^{j\theta_{nf}} [G_{MAF}(t) * (e^{-j\theta_{nf}} v_{\alpha\beta}(t))] \quad (19)$$

where $\vec{v}_{\alpha\beta,1}^+(t) = \hat{v}_{\alpha,1}^+(t) + j\hat{v}_{\beta,1}^+(t)$, $\vec{v}_{\alpha\beta}(t) = v_{\alpha}(t) + jv_{\beta}(t)$, and $*$ denotes the convolution product. Taking the Laplace transform of both sides of (19) yields

$$\frac{\vec{v}_{\alpha\beta,1}^+(s)}{v_{\alpha\beta}(s)} = G_{MAF}(s - j\omega_{nf}) \quad (20)$$

which corresponds in the z -domain to

$$\frac{\vec{v}_{\alpha\beta,1}^+(z)}{v_{\alpha\beta}(z)} = G_{MAF}(ze^{-j\omega_{nf}T_s}) = \frac{1}{N} \sum_{n=0}^{N-1} e^{j\frac{2\pi n}{N}} z^{-n}. \quad (21)$$

It can be observed that (18) and (21) are identical, which proves the equivalence of SVFT and MAF-based prefiling

stages. Thanks to this equivalence, it can be concluded that the PMAF-PLL and SVFT-PLL are mathematically equivalent, and therefore, the same small-signal model and properties as those of the PMAF-PLL can be considered for the SVFT-PLL.

VII. SIMULATION AND EXPERIMENTAL RESULTS

In this section, the performance of the enhanced PMAF-PLL is evaluated using simulation and experimental studies. In obtaining all results, the sampling frequency is fixed at 10 kHz. To provide a base for comparison, the standard MAF-PLL [5] and the quasi-type-1 PLL (QT1-PLL) [26] are also implemented and their results are compared with those of the enhanced PMAF-PLL. The schematic of these two PLLs can be observed in Fig. 10. Designing the control parameters of the standard MAF-PLL is carried out using the symmetrical optimum method, as explained in [5]. For the case of the QT1-PLL, the parameter design procedure is more straightforward as the PI controller is replaced with a simple gain. This gain is selected so that the minimum 2% settling time in response to

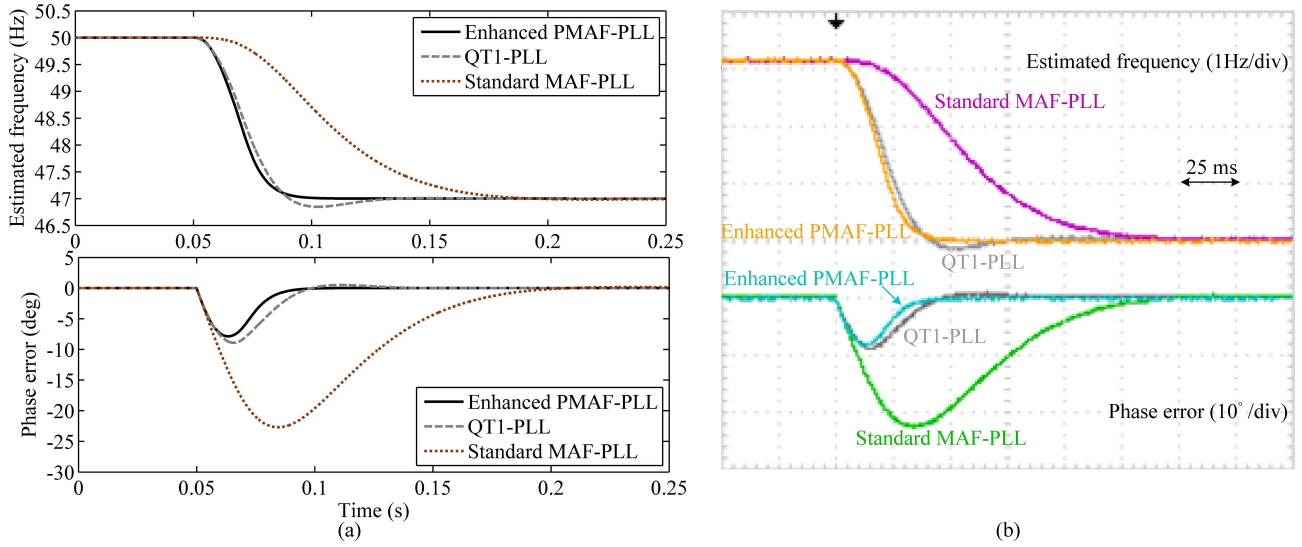


Fig. 12. (a) Simulation and (b) experimental results under the test case 2.

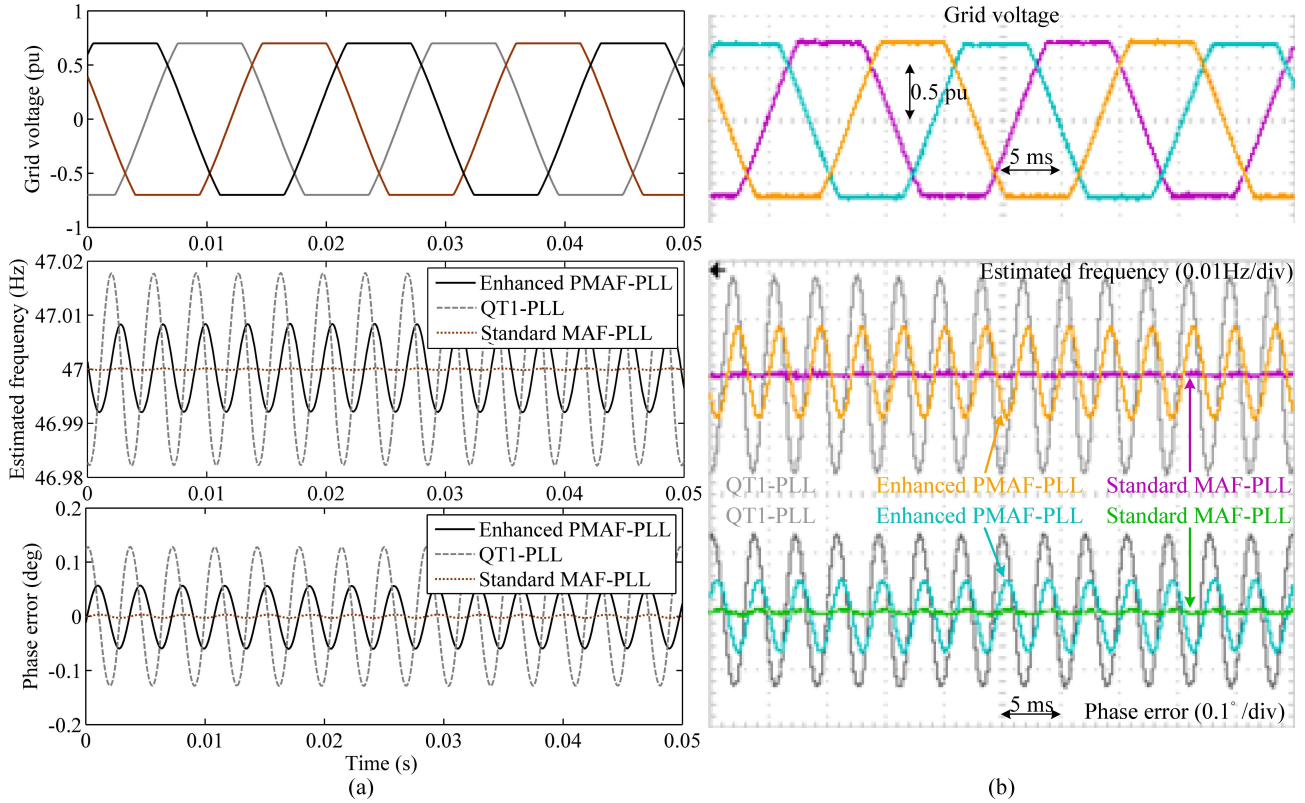


Fig. 13. (a) Simulation and (b) experimental results under the test case 3.

phase angle jumps is achieved. Table I summarizes the control parameters of all PLLs under analysis.

The following three test cases are designed.

- 1) Test case 1: The grid voltage experiences a phase-angle jump of $+20^\circ$. The grid frequency is at its nominal value during this test.
- 2) Test case 2: The grid frequency undergoes a -3 Hz step change.
- 3) Test case 3: All three phases of the grid voltage are

clamped at 0.7 pu. The total harmonic distortion of the grid voltage is 13.76%. During this test, the grid frequency is fixed at 47 Hz to take into account the effect of grid frequency variation on the filtering capability of the PLLs.

Figs. 11 and 12 show the simulation and experimental results under the test cases 1 and 2, respectively. It can be observed that the enhanced PMAF-PLL has the fastest dynamic response among all PLLs.

Fig. 13 evaluates the PLLs performance under the test case 3. The standard MAF-PLL, as shown, has the highest filtering capability, and the enhanced PMAF-PLL has the second best performance in this test.

VIII. CONCLUSION

In this letter, the small-signal modeling of the SRF-PLL with MAF-based prefiltering stage (briefly called, the PMAF-PLL) was presented. This model significantly simplifies the stability analysis and dynamic performance studies. A simple yet effective method to compensate for the phase and amplitude errors of the PMAF-PLL in the presence of frequency drifts was then proposed and its effectiveness was confirmed through a performance comparison with the state-of-the-art PLLs. The equivalence of the PMAF-PLL and SVFT-PLL was also proved, which implies that the small-signal model of the PMAF-PLL and the method presented to enhance its performance are also valid for the SVFT-PLL.

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