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# Principle and Design of a Single-phase Inverter Based Grounding System for Neutral-to-ground Voltage Compensation in Distribution Networks

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**Abstract**—Neutral-to-ground overvoltage may occur in non-effectively grounded power systems because of the distributed parameters asymmetry and resonance between Petersen coil and distributed capacitances. Thus, the constraint of neutral-to-ground voltage is critical for the safety of distribution networks. In this paper, an active grounding system based on single-phase inverter and its control parameter design method is proposed to achieve this objective. Relationship between its output current and neutral-to-ground voltage is derived to explain the principle of neutral-to-ground voltage compensation. Then, a practical current detection method is proposed to specify the reference of compensated current. A current control method consisting of proportional resonant (PR) and proportional integral (PI) with capacitive current feedback is then proposed to guarantee sufficient output current accuracy and stability margin subjecting to large range of load change. The PI method is taken as the comparative method and the performances of both control methods are presented in detail. Experimental results prove the effectiveness and novelty of the proposed grounding system and control method.

**Index Terms**—Current control, distribution networks, flexible grounding method, neutral voltage compensation.

## I. INTRODUCTION

**E**ITHER in theory or practice, the major objective of grounding system in distribution networks is to constrain the ground current to extinguish the arcs caused by the single-line-to-ground (SLG) fault. However, the other purpose of grounding system is commonly disregarded, i.e., to control the neutral-to-ground voltage within certain limit [1]. This is critical for the safety of the power system especially when the

inherent asymmetry is high.

Inherent asymmetry directly determines the neutral-to-ground voltage in ungrounded system or high resistance grounded (HRG) system [2]. It is caused by the asymmetry of the distributed parameters, i.e., phase-to-ground capacitances and leakage resistances. Several reasons may cause the asymmetry, including inappropriate transposition in overhead lines, single- or two- phase open-circuit, medium voltage (MV) single phase load [3], etc. Moreover, the neutral-to-ground voltage closely relates to the grounding method. Obviously, it is limited to a small value in an effectively grounded system. Whereas, in resonant grounded (RG) system, it may even exceed the line-to-neutral voltage as resonance happens between Peterson coil and distributed capacitances [4]. For the purpose of maintaining power supply reliability and extinguishing fault arcs, most MV distribution networks adopt HRG or RG method, which makes the problem of high neutral-to-ground voltage unavoidable.

Several measures are taken to limit the neutral-to-ground voltage in non-effectively grounded systems [3]. Transposition enhancement is a common method for overhead lines to decrease the asymmetrical voltage. However, this method needs huge amount of work and is complicated to implement. Three phase coupling capacitances are used to balance the distributed capacitances. Nevertheless, it is not flexible enough to adapt the change of operation modes in power system. Improvement of detuning and damping ratio in RG systems can decrease the neutral-to-ground voltage caused by the aforementioned resonance [4]. However, this method is not able to eliminate the neutral-to-ground voltage caused by the asymmetry of distributed parameters.

For the purpose of eliminating the neutral-to-ground overvoltage, an active grounding system is needed with the

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characteristics of injecting certain currents to the neutral point and make it seem like short-circuited to the ground. Obviously, this system cannot be realized by passive components like resistor, reactor or capacitor. Thus, a single-phase inverter based grounding system is adopted in this paper.

The current detection and control methods are essential to the control system of an inverter. These two aspects are great challenges for the design and implementation of the active grounding system. Regarding to current detection methods, literatures [5]-[10] have introduced several charging current detection methods. In [5], the distributed capacitances are detected by twice changing the Petersen coil inductance and measuring the corresponding neutral-to-ground voltage and Petersen coil current. The charging current can be easily calculated then with the measured parameters and the line-to-neutral voltage. However, this method relies on the existence of Petersen coil, thus cannot be adopted in the active grounding system. Literature [7] has introduced a charging current detection method by the phase voltage of the faulty feeder and the variation of three-phase currents. This method can be easily implemented by feeder terminal units. However, the method employs too many sensors, thus the accuracy is hard to be guaranteed. Bolted connection of one phase to the ground with a fixed resistor and a contactor is introduced in [10] to detect the charging current. This method can easily guarantee the current accuracy. However, it still needs a grounding resistor and the detection procedure is too complicated for the control of active grounding system. Additionally, these methods cannot be used directly to compensate the neutral-to-ground voltage as the current for voltage compensation is not identical to the charging current.

The distribution transformer is always in delta/wye connection, thus the three-phase load of the feeder line has no influence on the zero sequence impedance. As the neutral-to-ground voltage only depends on the zero sequence circuit, the real load of the grounding system is thus the distributed impedance. Obviously, the load is mainly capacitive and is likely to be resonant with the LC filter of the grounding system at around fundamental frequency. This may bring about steady state error and undermine stability margin of the control system. These features complicate the topology and parameter design of the active grounding system controller. Several literatures have addressed the load effect and resonance phenomena, and many effective measures have been proposed [11]-[14]. Literature [11] has proposed a mixed controller of proportional integral differential (PID) and Resonant plus load current feedback, to reduce the steady state error and improve the dynamic response while dealing with different load types. However, the design of the controller parameters are not discussed in detail. Literature [12] has discussed the inherent instability of LCL filter in active power filter and introduced the active damping method of capacitive current feedback (CCF) to improve the stability margin. Degradation method can simplify the design of control system for LCL filter [14]. However, as the load types of the grounding system are different from that of the LCL filter, these methods cannot be adopted without modification.

In this paper, a new grounding system based on single-phase inverter is proposed to flexibly control the neutral-to-ground voltage. The relationship between injected current of the grounding system and the neutral-to-ground voltage is firstly derived. Then, a practical current detection method for compensating the neutral-to-ground voltage is introduced by analyzing that relationship. Furthermore, the load effect and resonance phenomena are addressed in detail, followed by a current control strategy. The controller design method is then presented to fulfill the requirements of the control system. Experimental results for validation of the proposed control topology and design method are subsequently provided.

## II. PRINCIPLE OF ACTIVE GROUNDING SYSTEM

### A. Principle of Neutral-to-ground voltage compensation

A typical 10kV non-effectively grounded distribution network [15] with one feeder is studied in this paper. Fig. 1 shows the topology of the distribution network with the proposed active grounding system. Since the 10kV busbar is supplied from the 110kV system via a wye/delta transformer  $T_d$ , there is no actual neutral point. Thus, a zigzag/wye transformer  $T_z$  is applied to virtualize one, and the grounding system is connected between the point and the ground. Fig. 2 shows the simplified distribution network, where  $E_A, E_B, E_C$  are three phase voltages. The distributed capacitance and resistance of phase  $X$  ( $X=A, B$  or  $C$ ) are  $C_X$  and  $R_X$ , respectively. The grounding system is composed of a single-phase full-bridge inverter, a LC-type output filter and a coupling transformer  $T_i$ . The DC bus of the inverter is supplied by a three phase uncontrolled rectifier which connects to the secondary windings of  $T_z$ . The output current of the system is controlled by the PWM pulses of IGBT to execute compensated current reference detection and neutral-to-ground voltage compensation. The transformer is used to regulate the inverter output voltage and isolate the inverter from the distribution network.

Assume that the inverter output current is totally under control, then the grounding system can be treated as an ideal

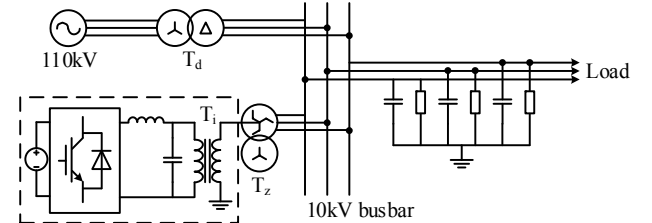


Fig. 1. Topology of distribution network and active grounding system (in dashed box).

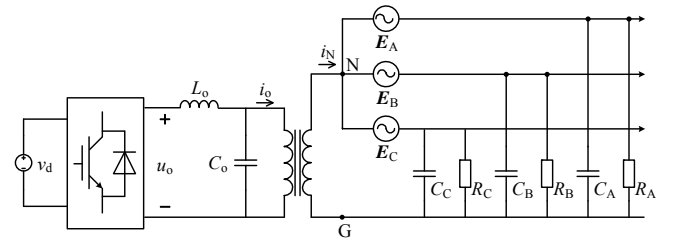


Fig. 2. Simplified distribution network.

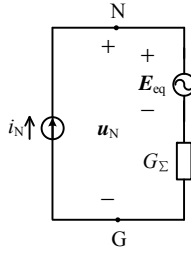


Fig. 3. Simplified circuit of the distribution network.

current source. According to electric circuit theories, the partition of distribution network can be simplified to a voltage source in series with an impedance. Therefore, the circuit of the whole system can be simplified to Fig. 3, where  $E_{eq}$  and  $G_{\Sigma}$  denote the equivalent voltage source and impedance of the distribution network, respectively. They are shown in (1) and (2), where  $Y_X$  is the phase-to-ground admittance, i.e.,  $Y_X = j\omega_0 C_X + 1/R_X$ , and  $\omega_0$  denotes the fundamental angular frequency.

$$E_{eq} = -G_{\Sigma}(E_A Y_A + E_B Y_B + E_C Y_C) \quad (1)$$

$$G_{\Sigma} = \frac{1}{Y_{\Sigma}} = \frac{1}{Y_A + Y_B + Y_C} \quad (2)$$

Therefore, the relationship between the output current of the grounding system  $i_N$  and the neutral-to-ground voltage  $u_N$  is

$$u_N = i_N G_{\Sigma} + E_{eq} = G_{\Sigma}(i_N - E_A Y_A - E_B Y_B - E_C Y_C). \quad (3)$$

Obviously, if  $i_N$  can be controlled to the value in (4), the neutral-to-ground voltage will be zero, which means the asymmetry of distribution network is fully compensated.

$$i_0 = E_A Y_A + E_B Y_B + E_C Y_C \quad (4)$$

It can be further concluded that the compensated current reference also meets (4) while an inductor or resistor is parallel connected to the grounding system. This indicates the grounding system is suitable for distribution network with both HRG and RG grounding. However, as the distributed parameters of the distribution network are complicated to be precisely detected, direct calculation of  $i_0$  is not practical.

As the line-to-neutral voltages are balanced and positive-sequenced,  $E_B$  and  $E_C$  can be substituted by expressions of  $E_A$ . Take the initial phase angle of  $E_A$  as the zero phase base, i.e.,  $E_A = E_A \angle 0^\circ$ , then (3) can be rewritten to

$$u_N = G_{\Sigma}(i_N e^{j\theta} - i_0 e^{j\theta_0}). \quad (5)$$

In (5),  $\theta$  and  $\theta_0$  denote the phase angle of  $i_N$  and  $i_0$ , respectively. Therefore, the magnitude of neutral-to-ground voltage can be obtained.

$$u_N(i_N, \theta) = |G_{\Sigma}| \sqrt{i_N^2 + i_0^2 - 2i_N i_0 \cos(\theta - \theta_0)} \quad (6)$$

Take the first-order partial derivative operation of  $u_N$ , then the change rate of  $u_N$  with the magnitude and phase angle of  $i_N$  can be observed.

$$\frac{\partial u_N(i_N, \theta)}{\partial i_N} = |G_{\Sigma}| \frac{i_N - i_0 \cos(\theta - \theta_0)}{\sqrt{i_N^2 + i_0^2 - 2i_N i_0 \cos(\theta - \theta_0)}} \quad (7)$$

$$\frac{\partial u_N(i_N, \theta)}{\partial \theta} = |G_{\Sigma}| \frac{i_N i_0 \sin(\theta - \theta_0)}{\sqrt{i_N^2 + i_0^2 - 2i_N i_0 \cos(\theta - \theta_0)}} \quad (8)$$

It can be seen from (4) that  $i_0$  and  $\theta_0$  are fixed in a specific

distribution network. From (7), when we set  $\theta$  to certain value  $\theta^*$ ,  $u_N$  has an inflection point in

$$i_N = i_0 \cos(\theta^* - \theta_0). \quad (9)$$

The trend of  $u_N$  needs to be discussed under several conditions. If  $-\pi/2 \leq \theta^* - \theta_0 < \pi/2$ ,  $u_N$  will first decrease then increase when  $i_N$  increases from 0 to infinite. The break point is determined by (9). This means  $u_N$  has a minimal value at the point. If  $\pi/2 \leq \theta^* - \theta_0 < 3\pi/2$ ,  $u_N$  will be monotonically increasing. Therefore,  $u_N$  has a minimal value at the point determined by (9) as well. From (8), when we set  $i_N$  to certain value of  $i^*$ ,  $u_N$  has another inflection point in

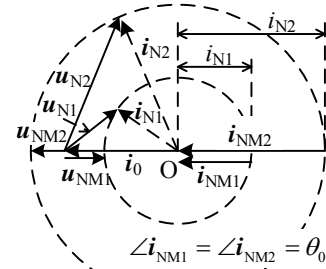
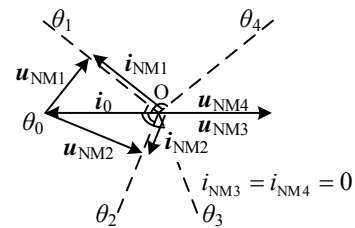
$$\theta = \theta_0. \quad (10)$$

### B. Compensation Current Detection Method

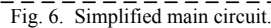
Comparing (9) with (10), interesting conclusions can be found. Firstly, the inflection point determined by (9) is related to  $\theta^*$ , which means it changes with the set value of  $\theta$ . However, the inflection point determined by (10) is independent to  $i_N$ . That is to say, whatever value  $i_N$  is chosen, the inflection point will not vary. Secondly,  $\theta$  must be chosen to  $\theta_0$  to make the inflection point in (9) equal to the magnitude of  $i_0$ , which is the compensated current reference; whereas, the inflection point in (10) is right the phase angle of  $i_0$ . These features can be used to quickly locate the magnitude and phase of  $i_0$ .

From the analysis above, it can be seen that if sinusoidal currents with any fixed magnitude and changing phases are injected to the neutral, the phase of  $i_0$  can be located just by detecting the minimal  $u_N$ . Comparatively, only when the phase of the injected current is set to  $\theta_0$  could the magnitude of  $i_0$  be located in the same way, which is almost impossible as  $i_0$  is unknown. This can be seen more directly from the vector diagrams in Fig. 4 and Fig. 5. In these figures, the magnitude of  $u_N$  is divided by the magnitude of  $G_{\Sigma}$  to simplify the analysis.

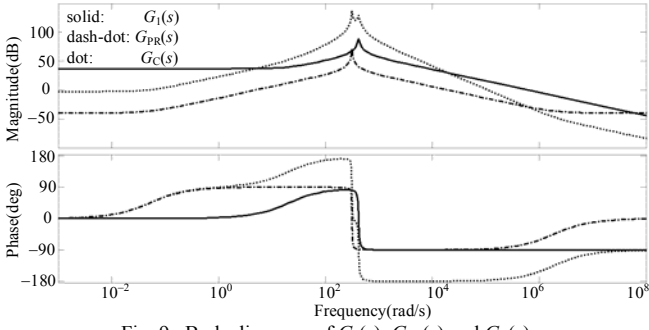
Fig. 4 shows the variation of  $u_N$  when different magnitudes of  $i_N$  are chosen. Two typical values are chosen, that is,  $i_{N1}$  and  $i_{N2}$ . The first one is smaller than  $i_0$ , and the second is larger. Assuming the two groups of  $i_N$  with fixed magnitudes are

Fig. 4. Vector diagram of  $u_N$  when  $i_N$  varies.Fig. 5. Vector diagram of  $u_N$  when  $\theta$  varies.

Firstly, preset the magnitude of  $i_N$  to certain value; search the minimal magnitude of  $u_N$  by changing the angles of  $i_N$  and injecting them to the neutral; the phase angle corresponding to minimal  $u_N$  is namely  $\theta_r$ . Then, fix the angle of  $i_N$  to  $\theta_r$ ; search the minimal magnitude of  $u_N$  again by changing the magnitudes of  $i_N$  and injecting them to the neutral; the corresponding magnitude is namely  $i_r$ . Finally, the current reference for compensating the distribution network asymmetry is with the magnitude of  $i_r$  and the angle of  $\theta_r$ .



Parameters		Values
Distribution Network	Damping ratio $d$	0.08
	Phase-to-ground capacitance $C_A, C_B$	8.76 $\mu\text{F}$
	Phase-to-ground capacitance $C_C$	14 $\mu\text{F}$
	Fundamental frequency $f_0$	50 Hz
	Phase-to-neutral voltage $E_X$	10.5/ $\sqrt{3}$ kV
Grounding system	Transformer ratio	10.5/ $\sqrt{3}$ :0.32
	Output inductance $L_o$	0.5 mH
	Output capacitance $C_o$	50 $\mu\text{F}$
	Inverter gain $K_{\text{pwm}}$	300
	DC voltage	600 V

Fig. 9. Bode diagrams of  $G_1(s)$ ,  $G_{PR}(s)$  and  $G_C(s)$ .

the steady state error might increase. Fig. 8 also shows Bode diagrams as  $C_s$  varies in nominal, 60%, and 30% of nominal. Magnitude in fundamental angular frequency decreases from 67.7 dB to 47.1 dB as  $C_s$  decreases, which means significant increase of steady state error at fundamental frequency. Moreover, if the resonant frequency locates in the medium band, the phase margin of the control system might decrease. In order to guarantee minimal steady state error in fundamental frequency, the proportional resonance controller is usually adopted [16]. However, the controller also brings about  $-180^\circ$  phase shift, as the Bode diagrams in Fig. 9 show. Since the crossover frequency  $\omega_c$  is always in the medium band, which is probably larger than  $\omega_r$  and  $\omega_0$ , the phase margin of the whole control system  $G_C(s) = G_{PR}(s)G_1(s)$  approaches zero, which makes the system easily unstable.

### B. Capacitive current feedback

From the analysis above, the resonance should be carefully damped to meet control performance requirements [17]–[19]. This paper presents an active damping method that flexibly damps the resonance without any loss as illustrated in Fig. 10. In this method, the current of  $C_o$  is feedback to the control loop with a ratio of  $H_i$ . Therefore, the transfer function from current regulator output  $v_r$  to output current  $i_o$  is

$$G_2(s) = \frac{i_o(s)}{v_r(s)} = \frac{K_{pwm}(sR_sC_s + 1)}{s^2R_sL_o(C_o + C_s) + s(L_o + K_{pwm}H_iR_sC_o) + R_s}. \quad (13)$$

Obviously, the capacitive current feedback (CCF) introduces a ratio of  $K_{pwm}H_iR_sC_o$  to the  $s$  term of the denominator. As a result, the magnitude of  $G_2$  decrease significantly at the original resonant frequency  $\omega_r$ , which effectively damps the control system. Fig. 11 shows both Bode diagrams of the original system and damped system. It is clear that CCF damps the magnitude at the resonant frequency and enhances the phase margin of the system. The damping degree rises as the feedback ratio  $H_i$  increases, which means smaller magnitude in resonant frequency and larger phase margin. Meanwhile, the CCF also brings smaller magnitude at fundamental frequency, which

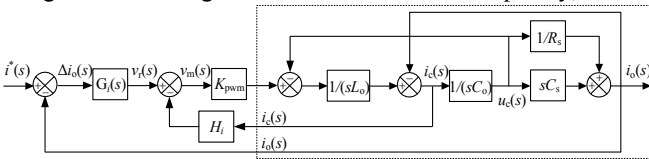


Fig. 10. Control diagram with proposed CCF.

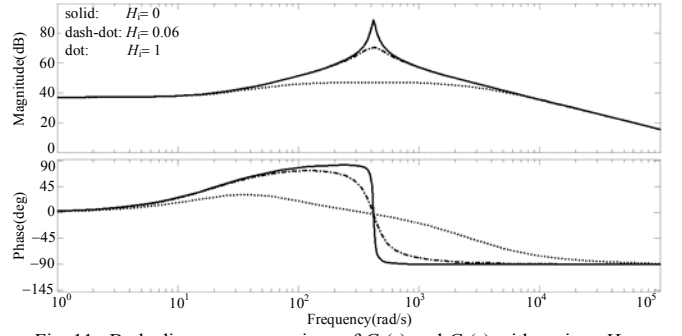


Fig. 11. Bode diagrams comparison of  $G_1(s)$  and  $G_2(s)$  with various  $H_i$ . undermines the steady state performance. Therefore, the current regulator must have significant magnitude at fundamental frequency to achieve minimal steady state error.

### C. Current Regulator

PR controller with damped form is used in current regulator to enhance the steady state performance and adapt to the power system frequency variation.

$$G_{PR}(s) = k_{p\_PR} + \frac{2k_i\omega_i s}{s^2 + 2\omega_i s + \omega_0^2} \quad (14)$$

The magnitude of PR controller in both low and high frequency band is determined only by the proportional ratio  $k_{p\_PR}$ . To avoid the high order harmonic interference, the crossover frequency of the whole control system is always set in the medium band, typically 1/10 of the switching frequency [20]. In order to fulfill this requirement,  $k_{p\_PR}$  should not be too large. However, the limited  $k_{p\_PR}$  may not ensure the system stability as shown later. Therefore, PR controller can hardly meet both the requirements of anti-interference and control system stability. Thus, an additional PI controller is introduced.

$$G_{PI}(s) = k_{p\_PI} + \frac{k_i}{s} \quad (15)$$

The compound controller has the advantage of infinite gain at zero frequency and fixed gain in high frequency. Thus, it is easy to enlarge the system gain in low band and avoid its influence to the crossover frequency. The integral ratio  $k_i$  should also be carefully chosen to prevent the  $-90^\circ$  phase shift in low frequency from undermining phase margin. Consequently, the current regulator and the open-loop transfer function of the whole system can be described as follows.

$$G_i(s) = G_{PR}(s)G_{PI}(s) \quad (16)$$

$$G_t(s) = G_{PR}(s)G_{PI}(s)G_2(s) \quad (17)$$

## IV. CONTROL PARAMETER DESIGN

### A. PWM constraint

The PWM constraint is firstly described so that the conclusion can be used in the following analysis. For a realizable pulse width modulation, the modulation waveform should only cross the carrier waveform once in a switching period. That is to say, the maximum frequency of modulation waveform should not exceed the switching frequency [21]. Therefore, the following expression stands.

$$H_i \leq \frac{4f_{sw}L_o}{K_{pwm}} \quad (18)$$

### B. PI controller

As the PI controller has  $-90^\circ$  phase shift in low frequency band, which might decrease the phase margin of the control system, the corner frequency of the controller should be much smaller than the crossover frequency. That is

$$\frac{k_i}{k_{p\_PI}} \ll \omega_c. \quad (19)$$

The proportional ratio  $k_{p\_PI}$  can be adjusted to slightly modify the performance of the whole system. In order to simplify parameter design,  $k_{p\_PI}$  is set to one, so that in the medium frequency band and above, the effect of PI controller is negligible. Therefore, the following expression of integral ratio stands.

$$k_i \ll \omega_c \quad (20)$$

### C. Crossover frequency

To prevent phase shift of PR controller from decreasing the phase margin, the crossover frequency  $\omega_c$  is always set to be in the medium band far away from the fundamental frequency. Thus, the PR controller can be simplified to a pure amplifier loop at crossover frequency determined by the proportional ratio. As analyzed above, the PI controller at the crossover frequency can be treated as a proportional loop with the gain of  $k_{p\_PI}$ . Thus, the gain of current controller at the crossover frequency is

$$|G_i(j\omega_c)| = |G_{PR}(j\omega_c)G_{PI}(j\omega_c)| = k_{p\_PR}. \quad (21)$$

As the magnitude of open-loop gain at the crossover frequency is unity, the relationship of  $\omega_c$ ,  $k_{p\_PR}$  and  $H_i$  can be obtained by the following equation.

$$|G_i(j\omega_c)| = 1 \quad (22)$$

Using (13) to (21), following equation can be drawn.

$$\left| \frac{k_{p\_PR}K_{pwm}(1+j\omega_cR_sC_s)}{R_s[1-\omega_c^2L_o(C_o+C_s)]+j\omega_c(L_o+K_{pwm}H_iR_sC_o)} \right| = 1 \quad (23)$$

Notice that the distribution network damping ratio  $d=1/(\omega_oR_sC_s)$  has typical values of 0.03 to 0.08. It is reasonably negligible comparing to one. The capacitance of LC filter  $C_o$  is always set to be much smaller than the distributed capacitance  $C_s$ . Thus, (23) can be rewritten to

$$\left| \frac{k_{p\_PR}(1-jd\frac{\omega_o}{\omega_c})}{\frac{d\omega_oL_o}{K_{pwm}}+H_i\frac{C_o}{C_s}-j\frac{1}{K_{pwm}}(\frac{1}{\omega_cC_s}-\omega_cL_o)} \right| = 1. \quad (24)$$

Considering the reactance of  $C_s$  at the crossover frequency is far less than that of  $L_o$ , thus, (24) can be further simplified to

$$k_{p\_PR}^2 - H_i^2(\frac{C_o}{C_s})^2 = (\frac{\omega_cL_o}{K_{pwm}})^2. \quad (25)$$

It can be observed from (18) that  $H_i$  is limited to a small value. Furthermore,  $C_o$  is much smaller than  $C_s$ , thus the following expression stands.

$$k_{p\_PR} = \frac{\omega_cL_o}{K_{pwm}} \quad (26)$$

As the zero-frequency gain of  $G_2(s)$  is  $K_{pwm}/R_s$  from (13), if single PR controller with certain proportional ratio of (26) is used, the whole system gain at zero-frequency will be

$$\frac{\omega_cL_o}{K_{pwm}} \frac{K_{pwm}}{R_s} = \frac{\omega_cL_o}{R_s}. \quad (27)$$

With the typical values listed in TABLE I, it can be seen that  $\omega_cL_o/R_s$  is less than one. Thus, the gain of the control system with single PR controller in zero frequency is below 0 dB line, which means the whole control system is marginally unstable as shown in Fig. 12. It also shows the stabilized control system after adding PI controller.

### D. Steady state error and stability margin constraint

The magnitude of output current error at fundamental frequency is used to describe the steady state error.

$$E_i = \left| \frac{i^*(j\omega_o) - i_o(j\omega_o)}{i^*(j\omega_o)} \right| \quad (28)$$

Assuming that unity feedback of output current is applied, the equation above can be described by open-loop transfer function

$$E_i = \left| 1 - \frac{G_i(j\omega_o)}{1+G_i(j\omega_o)} \right| = \left| \frac{1}{1+G_i(j\omega_o)} \right|. \quad (29)$$

As the magnitude of PR controller is  $k_{p\_PR} + k_r$  at the fundamental frequency, using expressions from (13) to (17), (29) can be transformed to

$$\frac{1}{E_i} = \left| 1 + \frac{(k_{p\_PR} + k_r)K_{pwm}}{d\omega_oL_o + K_{pwm}H_iC_o/C_s - j(1/\omega_oC_s - \omega_oL_o)} \right|. \quad (30)$$

At fundamental frequency, the reactance of  $L_o$  is negligible. Also,  $H_iC_o/C_s$  is negligible comparing to  $k_{p\_PR} + k_r$ . The reactance of  $C_s$  at fundamental frequency is also neglected to simplify the analysis. As a result, the steady state error constraint can be described as

$$\frac{k_{p\_PR} + k_r}{H_i} \approx \frac{C_o}{C_s E_i}. \quad (31)$$

Obviously, the gain of current controller at fundamental frequency is inversely proportional to the steady state error. Increasing the gain can obtain better steady state performance. However, the CCF ratio  $H_i$  is proportional to the error, which

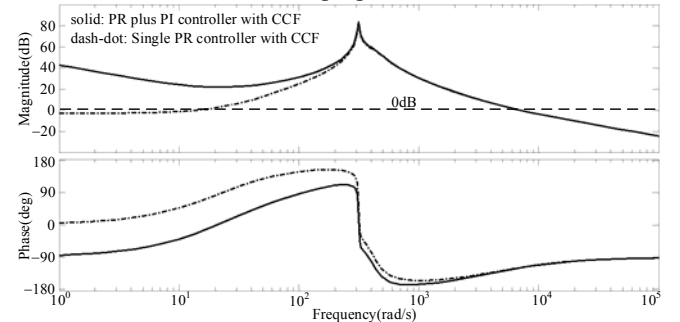


Fig. 12. Bode diagrams of open-loop transfer function with single PR controller and PR plus PI controller.



means better damping of load resonance brings larger steady state error.

It can be seen from Fig. 12 that, with careful selection of controller parameters, the phase of the open-loop transfer function will not exceed the  $-180^\circ$  line. These selection tips include that the corner frequency of PI controller should be far away from the crossover frequency, and the resonant cutoff frequency of PR controller should be as small as possible. Consequently, infinite gain margin can be achieved.

While dealing with phase margin constraint, it is necessary to consider the effect of resonant ratio to phase shift. Consider the PR controller at crossover frequency,

$$G_{PR}(j\omega_c) = k_{p\_PR} + 2k_r\omega_i / s. \quad (32)$$

As is analyzed above, the PI controller can be treated as a pure amplifier loop at the crossover frequency. Therefore, phase margin ( $PM$ ) can be expressed as follows.

$$PM = 180^\circ + \angle G_{PR}(j\omega_c) + \angle G_2(j\omega_c) \quad (33)$$

Using (13) and (32), considering that the reactance of  $C_s$  at crossover frequency is negligible, the constraint of phase margin is derived in the Appendix and is expressed as follows.

$$\frac{k_r}{k_{p\_PR}} \geq \frac{\omega_c(\omega_c L_o C_s + K_{pwm} C_o H_i \tan PM)}{2\omega_i(\omega_c L_o C_s \tan PM - K_{pwm} C_o H_i)} \quad (34)$$

## V. PARAMETER DESIGN AND EXPERIMENTAL RESULTS

In order to validate the theoretical analysis, comparative investigations are carried out on two control methods of PI and PR plus PI (compound controller) with or without CCF. As stability margin is not easy to be observed in experimental results, Bode diagrams are used to illustrate it. Experiment analysis focuses on the dynamic and steady state performance.

### A. Parameter design

According to the theoretical analysis, the parameters of PI and PR controller are constraint by expressions (20), (26), (31) and (34). Thus, the crossover frequency, steady state error and phase margin need to be set forward.

As the switching frequency is fixed to 10 kHz, the crossover frequency is set to 1 kHz. The steady state error is set to 0.5% to guarantee good steady state performance. The phase margin is set to  $60^\circ$  to ensure sufficient stability margin. The corner frequency of PI controller is set to 30 Hz to avoid interference of steady state accuracy and stability margin. Therefore, the parameters of the two controllers can be obtained in TABLE II. The Bode diagram of the regulated open-loop transfer function is shown in Fig. 13. It can be seen that the crossover frequency of the control system is  $7.13 \times 10^3$  rad/s, slightly over the set value. The gain at fundamental frequency is 83.3 dB, which means a steady state error of  $6.45 \times 10^{-5}$ , a far smaller

TABLE II

CONTROL PARAMETERS		
	Parameters	Values
PI controller	Proportional ratio $k_{p\_PI}$	1
	Integral ratio $k_i$	189
PR controller	Proportional ratio $k_{p\_PR}$	0.01
	Resonant ratio $k_r$	6.4
	Damping ratio $\omega_i$	3.14
CCF	Feedback ratio $H_i$	0.06

value than the set value. This is because the resonant ratio  $k_r$  is not only determined by the steady state error constraint expression (31), but also  $PM$  constraint expression (34). The larger  $k_r$  is chosen here to meet both requirements. The phase of open-loop function does not exceed the  $-180^\circ$  line, validating that the gain margin is infinite. Additionally, the phase margin is  $61.3^\circ$ , which is close to the set value.

Comparative Bode diagrams of PI and compound controller are also shown in Fig. 13, both without CCF. Obviously, the former has greater crossover frequency and phase margin, indicating quicker response and better stability than the proposed one. However, it is not able to effectively suppress the harmonics of the output currents. The compound controller without CCF suffers from the  $-180^\circ$  phase shift of load resonance thus is not stable because of negative gain margin.

The voltage and current ratings of the proposed grounding system also need to be discussed. From the system topology, the voltage rating relates to the neutral-to-ground voltage illustrated in (1) and (2). The compensated current of the grounding system is determined by the asymmetry of the distributed parameters, which is illustrated in (4). From these expressions, it can be observed that the worst case occurs in two-phase open-circuit condition. In this condition, the neutral voltage rises to line-to-neutral voltage and the compensated current reference reaches 1/3 of the system charging current. Therefore, the nominal voltage is identical to the line-to-neutral voltage and the nominal current is set to 1/3 of the system charging current. Please note that it is not the objective of the proposed grounding system to compensate the ground current in SLG fault. Actually, parallel connected Petersen Coil is needed to provide large reactive power to compensate the ground current which is mainly capacitive.

### B. Experimental results

To verify the proposed active grounding system practically, a 100kVA prototype is built in laboratory, based on the topology in Fig. 1 and parameters in TABLE I. Slight change has been made to the topology that a step-up transformer is used to convert a 380V power supply to 10kV, substituting the 110kV supply and transformer  $T_d$ . The inverter of the grounding system mainly consists of two parallel connected single-phase IPM modules FF450R12ME4 from Infineon. The capacity of coupling transformer  $T_i$  is 100kVA. The inherent phase-to-ground capacitance and resistance is realized by two groups of capacitors and resistors corresponding to nominal

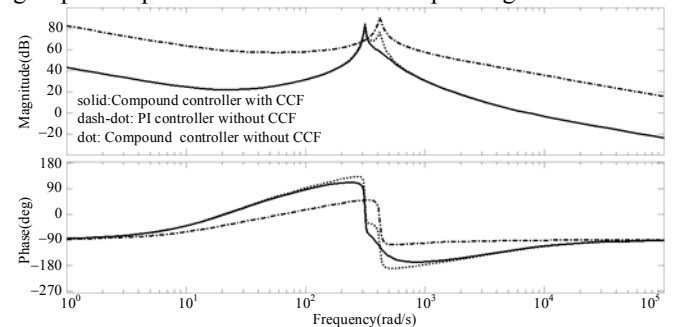


Fig. 13. Bode diagrams of open-loop transfer function with compound controller and CCF.

value in TABLE I and 30% of them to represent two different load levels. The control methods discussed above are executed in a digital signal processor TMS320F28335 development platform with carrier waveform frequency of 10 kHz. In the experimental process, a step-up of load from 0 to 30% nominal load is firstly carried out, followed by another step-up from 30% nominal load to 100%. The controller of PI without CCF is taken as the comparative controller to the proposed compound controller with CCF. The reference values of output current are detected by the compensation current detection method proposed in Section II. Dynamic waveforms subjecting to the two step-ups with different controllers are shown in Fig. 14 to Fig. 17. The error of the output current  $\Delta i_o$  (see Fig. 7) is shown for explicit observation of the control performance.

From the dynamic waveforms of output currents, it can be seen that both methods can reach stable system output. The adjusting time of PI controller is slightly smaller than the proposed method because of larger bandwidth of PI control system as shown in Fig. 13. However, Fig. 14 and Fig. 15 indicate that PI method suffers from larger overshoot than the proposed method with almost twice the value of output current and neutral-to-ground voltage, which is harmful for the safety of power supply apparatus. It can be seen from Fig. 16 that with PI method the percentage error of output current is smaller subjecting to 100% nominal load than 30% of nominal load, which can be explained by the load effect in section III.

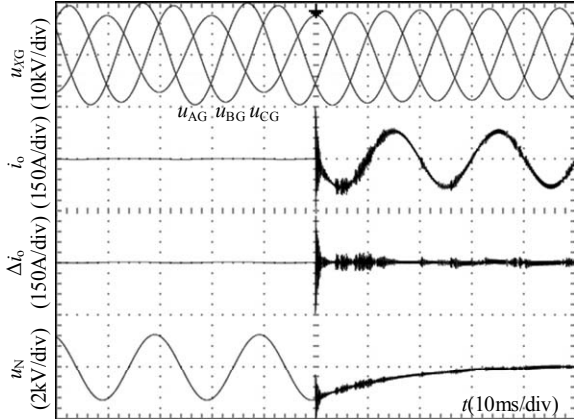


Fig. 14. Dynamic waveforms subjecting to load step-up from 0 to 30% nominal load with PI controller.

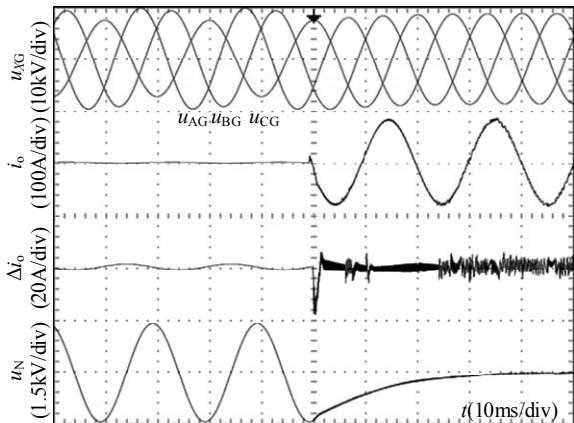


Fig. 15. Dynamic waveforms subjecting to load step-up from 0 to 30% nominal load with proposed method.

Comparatively, as shown in Fig. 17, with the proposed controller, the percentage errors of output current before and after load change are relatively closer than that of PI method, which indicates the proposed controller is more suitable for load change than PI controller. It should be noticed that the dynamic process of neutral-to-ground voltage after load change are longer than that of output current, due to the large time constant of the load.

Fig. 18 and Fig. 19 show steady state waveforms of the two control methods subjecting to 100% nominal load. Greater error in the fundamental components of output current error and neutral-to-ground voltage can be observed with PI controller than the proposed method. Spectrum analysis indicates that the neutral-to-ground voltage subjecting to the proposed method mainly contain harmonics with integrally multiple orders of the switching frequency. The neutral-to-ground voltage waveform in Fig. 18 shows a reduced voltage of around 42V subjecting to PI method. Spectrum analysis indicates the total harmonic distortion (THD) of the output current as 5.1%. From the output current and current error waveform in Fig. 19, it can be seen that the steady state error of the proposed method reaches 3%. The neutral-to-ground voltage is reduced by the grounding system with the proposed method to around 21V, better than PI method. The THD of the output current with the proposed method reaches 3.0%, also better than that of PI method. Both

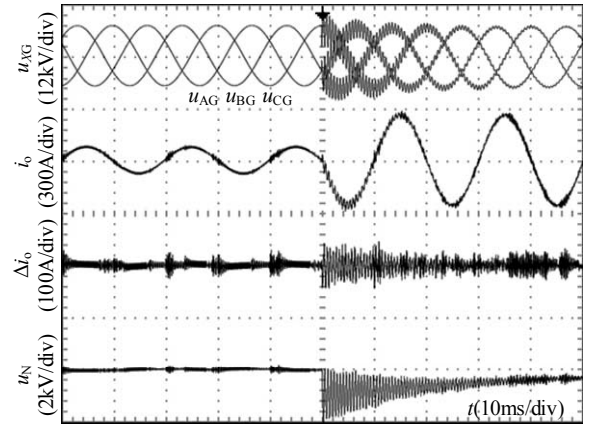


Fig. 16. Dynamic waveforms subjecting to load step-up from 30% nominal load to 100% with PI controller.

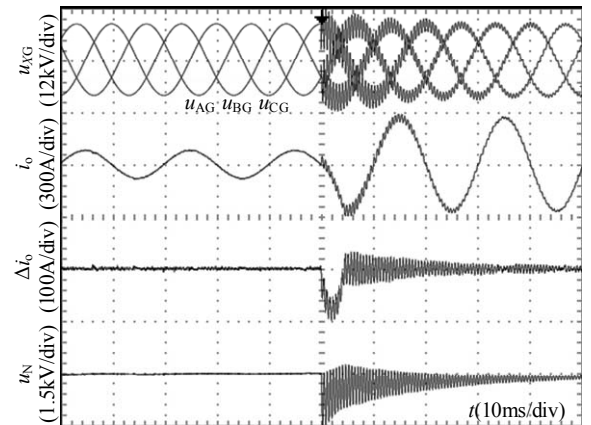


Fig. 17. Dynamic waveforms subjecting to load step-up from 30% nominal load to 100% with proposed method.

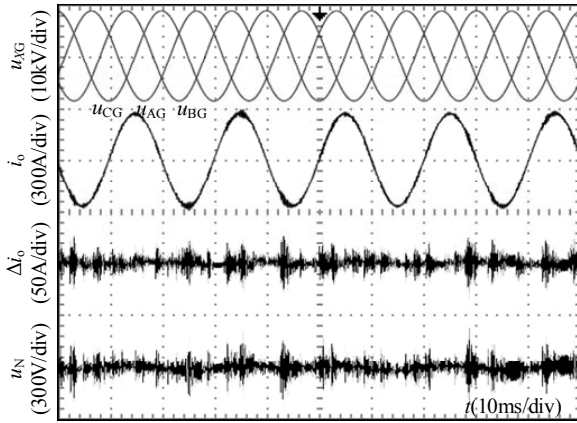


Fig. 18. Steady state waveforms subjected to 100% nominal load with PI controller.

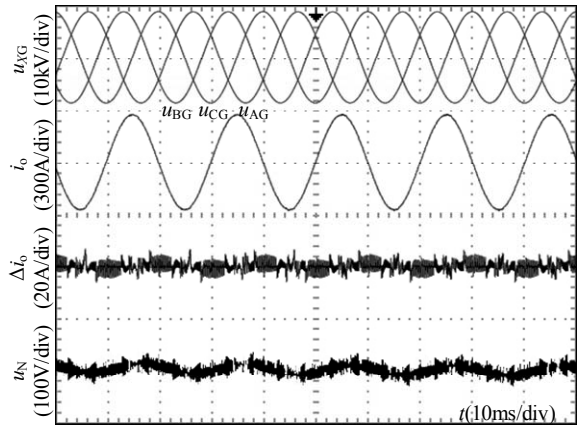


Fig. 19. Steady state waveforms subjected to 100% nominal load with proposed method.

of the neutral-to-ground voltage and output current THD indicate a better steady state performance of the proposed method than PI method.

## VI. CONCLUSION

The proposed active grounding system is able to effectively constrain the neutral-to-ground voltage to avoid possible overvoltage caused by asymmetrical distributed parameters or resonance between Petersen coil and phase-to-ground capacitance. A practical compensation current detection method is proposed which firstly specifies the phase angle, and then the magnitude of the current reference. Current control method is also presented which consists of a PR plus PI controller and capacitive current feedback. The proposed control method is suitable for large range of load change and is immune to possible resonance between load capacitance and output LC filter inductance. Experimental results show that the proposed control method has better performance in dynamic and steady state than PI method.

## APPENDIX

The limit of  $k_r/k_{p\_PR}$  constraint by phase margin ( $PM$ ) is derived here. The expression of  $G_2(j\omega_c)$  can be easily obtained from (13). Dividing both the nominator and denominator by  $j\omega_c R_s C_s$ , and considering that  $C_0 \ll C_s$  and substituting  $d$  for

$1/(\omega_0 R_s C_s)$ , it yields

$$G_2(j\omega_c) = \frac{K_{pwm}(1 - jd\frac{\omega_0}{\omega_c})}{\frac{L_o + K_{pwm}H_i R_s C_o}{R_s C_s} + j(\omega_c L_o - \frac{1}{\omega_c C_s})}. \quad (A.1)$$

As the reactance of  $C_s$  at crossover frequency is much smaller than that of  $L_o$  and  $d\omega_0/\omega_c \ll 1$ , (A.1) can be rewritten as

$$\angle G_2(j\omega_c) = -\arctan \frac{\omega_c L_o R_s C_s}{L_o + K_{pwm}H_i R_s C_o}. \quad (A.2)$$

Using (A.2) and (32), (33) can be rewritten as

$$PM = 180^\circ - \arctan \frac{2k_r \omega_i}{k_{p\_PR} \omega_c} - \arctan \frac{\omega_c L_o R_s C_s}{L_o + K_{pwm}H_i R_s C_o}. \quad (A.3)$$

Equation (A.3) can be rewritten by an inequality as

$$\arctan \frac{2k_r \omega_i}{k_{p\_PR} \omega_c} + \arctan \frac{\omega_c L_o R_s C_s}{K_{pwm}H_i R_s C_o} > 180^\circ - PM. \quad (A.4)$$

Applying the tangent function operation to both sides of (A.4), following expression can be obtained.

$$\frac{k_r}{k_{p\_PR}} \geq \frac{\omega_c (\omega_c L_o C_s + K_{pwm} C_o H_i \tan PM)}{2\omega_i (\omega_c L_o C_s \tan PM - K_{pwm} C_o H_i)} \quad (A.5)$$

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