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Article

Influence of Battery Parametric Uncertainties on the State-of-Charge Estimation of Lithium Titanate Oxide-Based Batteries

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Abstract: State of charge (SOC) is one of the most important parameters in battery management systems, as it indicates the available battery capacity at every moment. There are numerous battery model-based methods used for SOC estimation, the accuracy of which depends on the accuracy of the model considered to describe the battery dynamics. The SOC estimation method proposed in this paper is based on an Extended Kalman Filter (EKF) and nonlinear battery model which was parameterized using extended laboratory tests performed on several 13 Ah lithium titanate oxide (LTO)-based lithium-ion batteries. The developed SOC estimation algorithm was successfully verified for a step discharge profile at five different temperatures and considering various initial SOC initialization values, showing a maximum SOC estimation error of 1.16% and a maximum voltage estimation error of 44 mV. Furthermore, by carrying out a sensitivity analysis it was showed that the SOC and voltage estimation error are only slightly dependent on the variation of the battery model parameters with the SOC.

Keywords: lithium-ion batteries; lithium titanate oxide (LTO) batteries; hybrid pulse power characterization test; model parameterization; equivalent electrical circuit; state of charge (SOC); extended Kalman filter

1. Introduction

Lithium-ion (Li-ion) batteries have developed as the key energy storage technology for automotive applications and are also evaluated in different stationary renewable energy storage applications [1–5]. This is mainly because Li-ion batteries are characterized by superior performance in terms of power capability, efficiency, lifetime than other storage technologies [2,6]. Moreover, in the past years, the price of Li-ion batteries has been decreasing faster than expected. However, Li-ion batteries are sensitive to overcharging and overdischarging. Thus, an accurate estimation of the battery state-of-charge (SOC), which will avoid the overcharging and overdischarging operation, is a very important feature of the battery management systems (BMS) [7]. In the case of a wrong SOC estimation, significant damage in the battery may occur and ultimately the lifetime of the battery can be dramatically reduced [7–9].

Because the SOC cannot be directly measured, it is imperative to use an algorithm that can accurately estimate it, based on certain battery physical quantities (e.g., battery voltage and current). The Coulomb counting method [7,10] and the open circuit voltage method [7,11,12] are the two most used methods for SOC estimation. Coulomb counting method makes full use of the current measurement since the SOC is defined as the integration of current over the time, divided by the battery capacity. The accuracy of this method is related to the current measurement error, and to

the battery capacity and the Coulombic efficiency. Moreover, the initial SOC should be known in order to estimate the actual SOC of the battery. All these factors heavily affect the SOC estimation result in the Coulomb counting method and are hard to be ignored. Since the open circuit voltage (OCV) is monotonically decreasing while the battery is discharging, an OCV-SOC lookup table is able to predict the battery SOC. Nevertheless, for an accurate OCV measurement, the battery has to be rested for hours in order to reach its electrochemical equilibrium. Consequently, the applicability of this method for SOC estimation in real-life applications is questionable. Wei et al. [13] estimate SOC online by identifying the OCV through a multi-timescale estimator, which is efficient in the calculation. The estimated SOC relies heavily on the look-up table, but the OCV-SOC relationship is dependent on the temperature and changes while the battery is aging. Data-driven methods based on neural networks and regression models are also applied to estimate the SOC [14,15]. The accuracy of data-driven methods relies on the features of the training samples. It means that accurate SOC estimation is guaranteed only if the test data are similar to the training samples. In order to meet the requirement of various applications, SOC estimation methods must be both accurate and robust. Therefore, model-based methods are proposed for SOC estimation. For these methods, the difference between the measured battery terminal voltage and the model estimated voltage is utilized to correct the SOC. Furthermore, model-based methods are insensitive to the initial SOC and measurement noise. Kalman filter [16–18], H infinity filter [19,20], PI-observer [21], Particle filter [22], RTLS-based observer [23], FBCRLS-based observer [24] etc. are applied to calculate the correcting gain in the SOC estimation structure. Among the aforementioned approaches, Extended Kalman filters (EKF) offer a good tradeoff between estimation accuracy and computing burden for real applications.

According to the accuracy and suitability for different applications, different types of battery performance models have been developed, such as electrochemical models, statistically-based models, and electrical models. Electrochemical models are conventional models that use the equations governing the electrochemical phenomena (chemical reactions) that occur in a battery cell [25,26]. The implementation of these models requires extended knowledge about the battery chemical, mechanical and electrical properties and thus they are more appropriate for battery design optimization process than for battery SOC estimation. Recently, there have also been some efforts on using reduced order electrochemical for SOC estimation [27].

Statistically-based models rely on machine learning methods, such as, neural network, support vector machines; however, large numbers of training samples are needed for guaranteeing its accuracy and robustness, which limits its usage in real applications. Electrical models have a simple and concise structure, using simple circuit components (e.g., resistors, capacitors etc.) for estimating the battery voltage [28–30]. Furthermore, it is more effective for implementing the battery characteristics to a BMS by electrical model. The parameters of the electrical model are changing under different conditions of SOC, C-rate, temperature, as presented in [28]. Consequently, in order to parameterize a battery electrical model, which is able to accurately estimate the battery SOC and voltage for a wide range of operating conditions, the dependence of the battery parameters on the aforementioned states should be considered during the parametrization stage. Nevertheless, such an extended battery parameterization requires extensive laboratory tests, which are extremely time-consuming and cost-demanding and sometimes are not reflected in the model accuracy improvement. The sensitivity analysis of Li-ion battery model on battery parameters was studied in [31]; in this work, a simple Thévenin battery model was used and only the variation of the model's parameters with the SOC was considered. Similarly, in [32] the authors have evaluated the sensitivity of the estimated battery voltage to the changes with the SOC of the parameters' values of a second order RC-equivalent circuit. In none of the aforementioned papers, a thorough investigation on the influence of the Li-ion battery parameters' variation (with SOC and temperature) on the accuracy of the estimated battery SOC and voltage estimation was carried out. Therefore, in this paper a sensitivity analysis was performed, in order to observe the influence of the battery model parameters variation with SOC and temperature, on the

accuracy of the proposed equivalent electrical circuit model and subsequently on the accuracy of the SOC estimation. The aging dependency is not considered in this work.

The remainder of this paper is organized as follows: the battery model is introduced in Section 2. The identification of the parameters of the battery equivalent electrical circuit (EEC), which was carried out based on laboratory measurements is described in Section 3. The following section presents the EKF methodology, which was used for estimating the battery SOC. The SOC and voltage estimation accuracy of the EKF method is evaluated in Section 5. The last section evaluates the sensitivity of the battery SOC and voltage estimation on the changes of EEC parameters.

2. Battery Model Based on EEC Parameterization

The equivalent electric circuit (EEC) models are an effective approach to represent the dynamic behavior of Li-ion batteries. Depending on the application and the required accuracy, different types of battery EEC models have been developed. The Rint model, the first order RC-model, and the second order RC-model, as well as the model based on impedance spectroscopy, have been proposed for predicting the battery voltage [28,33]. In this work, the dynamic behavior of the LTO-based battery was modeled using the second-order RC-equivalent circuit that is presented in Figure 1.

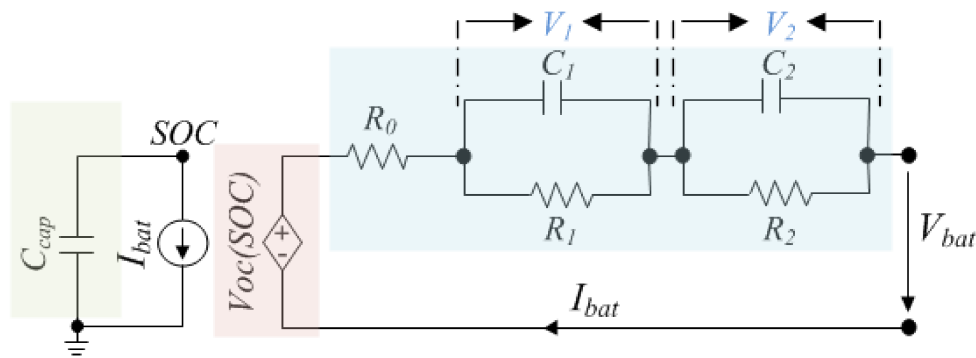


Figure 1. Proposed equivalent electrical model.

On the left-hand side, the capacitor C_{cap} and the current-controlled source are used to model the capacity and the SOC of the battery cell. On the right-hand side, the electrical circuit representation consists of a controlled voltage source, a series resistor, and two RC networks. The resistor, R_0 represents the battery ohmic resistance, and it is responsible for the instantaneous voltage drop during charging/discharging [34]. The parameters, R_1 , R_2 , C_1 , C_2 , are used to describe the transient behavior of the battery cell. The R_1 and C_1 are responsible for the fast voltage response and represents the charge transfer resistance and electrochemical double layer capacitance, respectively, while R_2 and C_2 are responsible for the slow voltage response and are used to the model for the diffusion process. All the EEC parameters are dependent on SOC, temperature and current. The two parts are connected by the voltage source V_{OC} (SOC), which is used to model the OCV of the battery that is dependent on SOC.

In this proposed dynamic model of the LTO-based battery cell, the self-discharge was not considered, mainly because it does not affect the dynamic response of Li-ion batteries. Meanwhile, the terminal voltage of the proposed model, V_{bat} , was calculated for discharging conditions as follows:

$$V_{bat} = V_{OC} - V_1 - V_2 - R_0 I_{bat}, \quad (1)$$

where V_{OC} represents the open circuit voltage, V_1 and V_2 is the voltage across the $R_1 C_1$ network, $R_2 C_2$ network, respectively, I_{bat} is the instantaneous battery current, whose sign is taken to be positive when the battery is charging and negative during discharging.

The battery SOC was defined according to the following mathematical relationship:

$$\text{SOC} = \text{SOC}_i + \frac{1}{C_{\text{cap}}} \int_0^t I_{\text{bat}} dt, \quad (2)$$

where SOC_i represents the initial SOC, C_{cap} is the nominal battery capacity.

From Equation (2), it is noted that SOC calculation is based on the integration of current. The obtained SOC is used further as the reference SOC during the EKF estimation method.

2.1. Experimental Set-Up

This research work was carried out on a commercially available 13 Ah high-power LTO ($\text{Li}_4\text{Ti}_5\text{O}_{12}$)-based Li-ion battery cell. The electrical and thermal parameters of this LTO-based battery cell are summarized in Table 1.

During the experiments, the LTO-based Li-ion battery cell was placed in a temperature chamber, as illustrated in Figure 2. The temperature of the battery cell was monitored using a type-K thermocouple; furthermore, the temperature values referred in this analysis are the ones measured on the surface of the LTO-based Li-ion battery cell.

Table 1. Specification of the Li-ion battery cell used in this study.

Property	Title 2
Nominal capacity	13 Ah
Nominal voltage	2.26 V
Voltage range	1.5–2.9 V
Current range	± 130 A
Operating temperature range	−40 °C to 55 °C

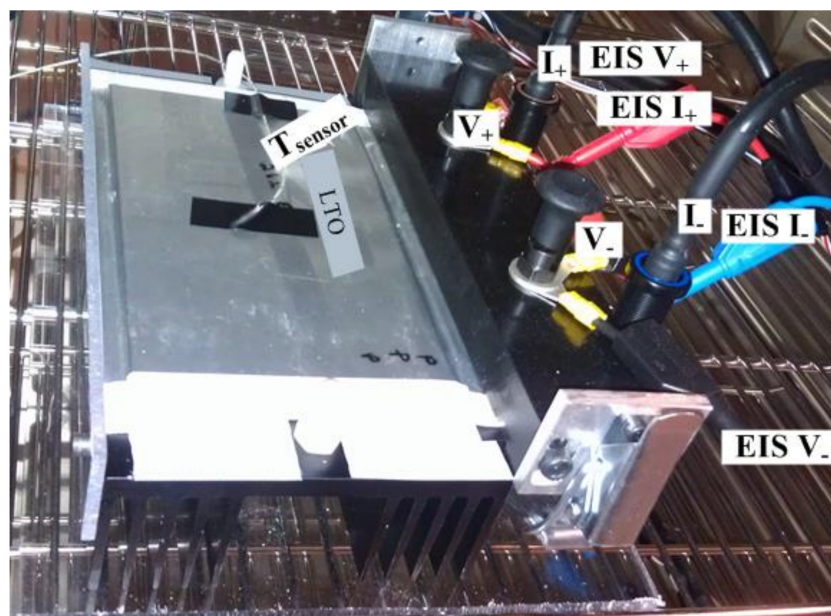


Figure 2. LTO-based Li-ion battery cell placed in a temperature chamber.

2.2. Battery Capacity

The capacity of the battery is influenced by the C-rate and temperatures. Thus, the capacity of the studied LTO-based battery cell was measured for different temperatures (i.e., 5–45 °C in steps of 10 °C) and 8 different C-rates (i.e., from C/4 to 9 C). During charging, the capacity was measured

considering a constant current–constant voltage procedure, while during discharging a constant current procedure was applied. Figure 3 illustrates the impact of the C-rate on the voltage during the capacity measurements at 25 °C for different C-rates.

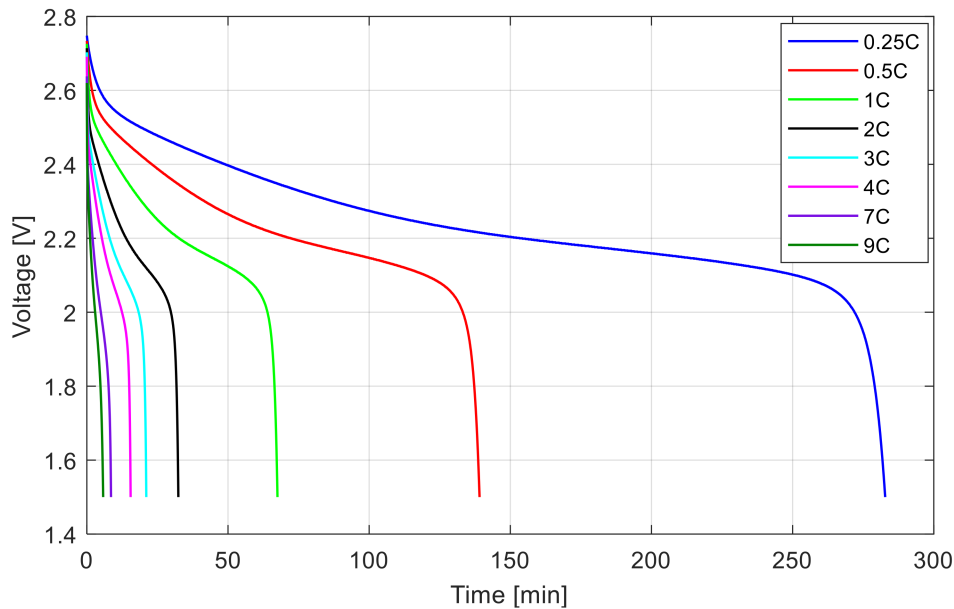


Figure 3. Voltage changes with discharging rates.

2.3. Battery OCV

Despite the linear model of the LTO battery, the static relationship between VOC and SOC is intrinsically nonlinear [35]. SOC represents the amount of charge remained in the battery compared with the full capacity, and the relationship between OCV and SOC is a static characteristic of the battery, which is not changing with the load profile, but changes with temperature and age.

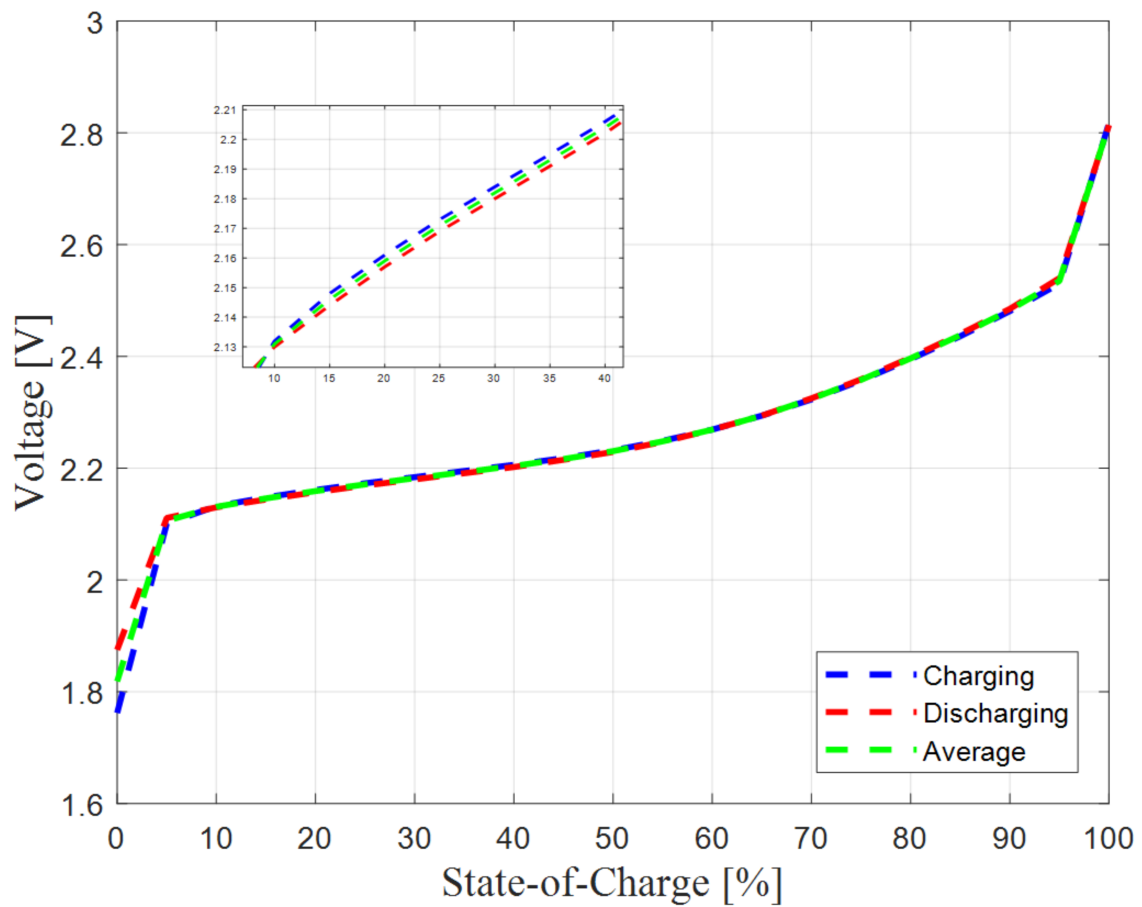
The nonlinearity of the model increases the complexity of the performance analysis of the estimators [35]. To deal with this problem, a high order polynomial function is introduced. The quadratic optimization is applied to guarantee the diminishing of OCV with the decrease of SOC [36].

The relationship between the SOC and OCV was determined by charging and discharging with 0.5C (i.e., 6.5 A) the LTO-based battery cell at different temperatures (5, 15, 25, 35, 45 °C). Based on the OCV-SOC curves obtained experimentally for the LTO-based battery (see Figure 4), the average between the charge and discharge curves is taken as the relationship between OCV and SOC. The average between charge and discharge of the OCV-SOC characteristic at different temperatures is presented in Figure 5. Further on, the average of OCV-SOC curves was approximated by a polynomial function, as shown in Equation (3), where the coefficients are given in Table 2 for all considered temperatures. The mean absolute error considering the experimental results at 25 °C is 0.0073 V, which proves the accuracy of the curve fitting method:

$$V_{oc} = f(\text{SOC}) = \sum_{i=0}^8 p_i \text{SOC}^i, \quad (3)$$

Table 2. Polynomial approximation of the OCV-SOC characteristic.

Coefficient	Title 3				
	5 °C	15 °C	25 °C	35 °C	45 °C
p ₀	2.1243	2.0301	1.8160	1.8778	1.860
p ₁	0.1511	2.1737	7.9113	6.1879	6.667
p ₂	7.3333	-1.365×10^1	-7.341×10^1	-5.680×10^1	-6.177×10^1
p ₃	-8.047×10^1	3.177×10^1	3.455×10^2	2.689×10^2	2.947×10^2
p ₄	3.784×10^2	3.906×10^1	-8.888×10^2	-7.004×10^2	-7.767×10^2
p ₅	-9.307×10^3	-3.292×10^2	1.283×10^3	1.033×10^3	1.166×10^3
p ₆	1.251×10^3	6.321×10^2	-1.0004×10^3	-8.355×10^2	-9.722×10^2
p ₇	-8.693×10^2	-5.262×10^2	3.643×10^2	3.283×10^2	4.0437×10^2
p ₈	2.439×10	1.648×10^2	-3.739×10^1	-4.279×10^1	-6.055×10^1

**Figure 4.** The OCV-SOC characteristic of the LTO-based battery measured at $T = 25\text{ }^{\circ}\text{C}$.

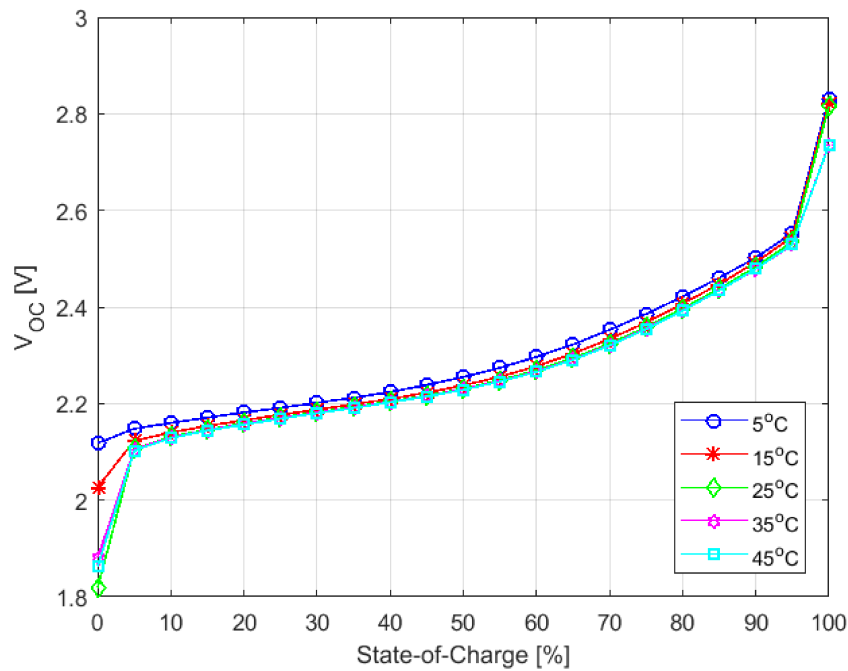


Figure 5. The OCV-SOC characteristic of the LTO-based battery measured at different temperatures.

Considering the equivalent circuit model for the LTO battery, presented in Figure 1, the state-space equation can be written as given in Equation (4):

$$\begin{bmatrix} \dot{V}_1 \\ \dot{V}_2 \\ \dot{\text{SOC}} \end{bmatrix} = \begin{bmatrix} -\frac{1}{R_1 C_1} & 0 & 0 \\ 0 & -\frac{1}{R_2 C_2} & 0 \\ 0 & 0 & 0 \end{bmatrix} \cdot \begin{bmatrix} V_1 \\ V_2 \\ \text{SOC} \end{bmatrix} + \begin{bmatrix} \frac{1}{C_1} \\ \frac{1}{C_2} \\ \frac{1}{C_{cap}} \end{bmatrix} \cdot I_{bat}, \quad (4)$$

In this equation, the SOC of the battery and the voltages across the two RC networks are selected to be system state variable. The battery parameters which need to be estimated are R_0 , R_1 , C_1 , R_2 , and C_2 .

3. Parameter Identification

Apart from the OCV, the other parameters of the EEC (R_0 , R_1 , R_2 , C_1 , C_2) have been estimated using the hybrid pulse power characterization (HPPC) method. The HPPC profile, which was applied to the LTO-based battery cell, is shown in Figure 6. The current pulse characterization method consists in applying a constant current pulse of a certain amplitude, ΔI to the battery and measuring the resulting change in the battery voltage, ΔV , either during and after the pulse.

The parameters of the EEC have been identified for SOC between 5% and 95% with a 5% SOC resolution. At each SOC, both charging and discharging current pulses of various amplitudes were applied. Based on the voltage response to a current pulse (see Figure 7), the parameters R_0 , R_1 , R_2 , C_1 , and C_2 have been identified.

When there is a sudden change in the current, a voltage drop, (ΔV_0) caused by the ohmic polarization appears instantaneously; then the voltage drop completes the transient process with an exponential approximation until the voltage will return to a steady state value. Therefore, the ohmic resistance, R_0 , was determined according to Equation (5), considering that the voltage before the current pulse changes is V_0 , the voltage at the end of the instantaneous voltage drop (i.e., after 0.1 s) is V_1 .

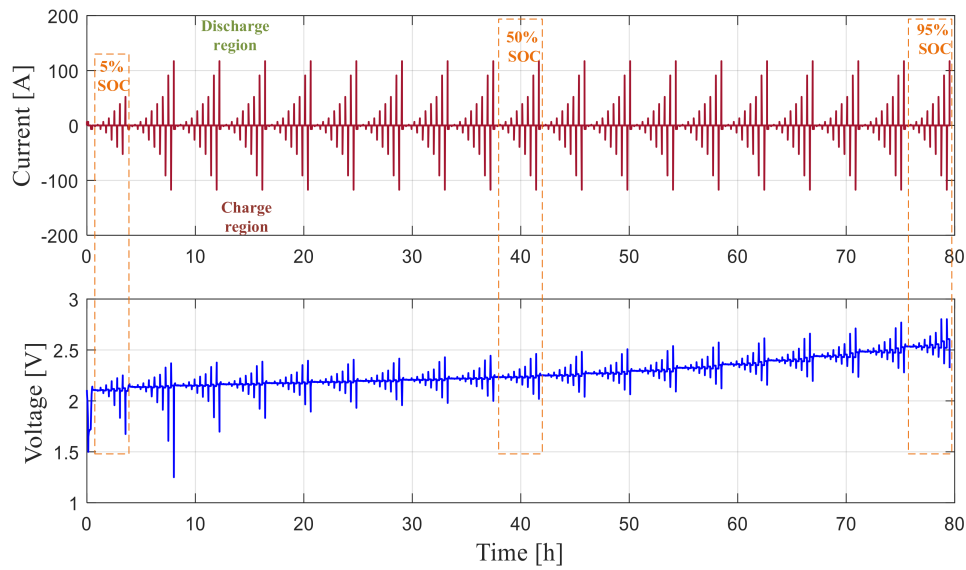


Figure 6. Current pulse and voltage profiles.

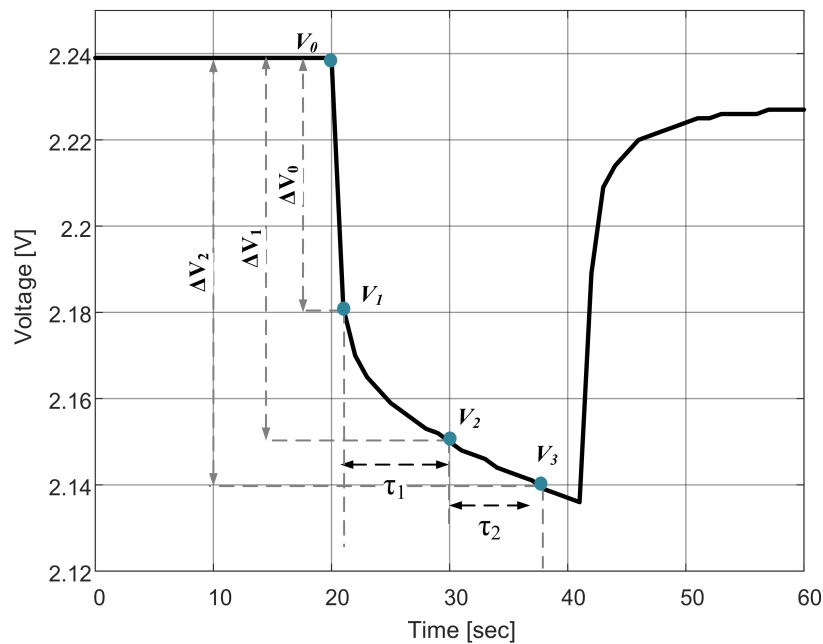


Figure 7. Voltage response of LTO-based Li-ion battery cell for a 1 C-rate current pulse at 25 °C.

$$R_0 = \frac{\Delta V_0}{\Delta I} = \frac{|V_0 - V_1|}{I}, \quad (5)$$

In order to extract the parameters of the EEC, related to the battery transient response, R_i and C_i , which are responsible for the fast voltage response (first RC network) and for the slow voltage response (second RC network), the following approach was followed. Resistances R_1 and R_2 were determined according to Ohm's Law, as given in Equations (6) and (7), where V_2 and V_3 are measured during the current pulse after 10 and 18 s, respectively. The capacitances C_1 and C_2 were calculated based on the

time constant of RC parallel networks, which is given in Equation (8). Furthermore, the time constant of the two RC parallel networks was determined according to the methodology presented in [37]:

$$R_1 = \frac{\Delta V_1}{\Delta I} = \frac{|V_1 - V_2|}{I}, \quad (6)$$

$$R_2 = \frac{\Delta V_2}{\Delta I} = \frac{|V_2 - V_3|}{I} \quad (7)$$

$$\tau_i = R_i \cdot C_i, \quad (8)$$

where τ_i represents the time constant of the first and second RC network, R_i and C_i represent the resistance and the capacitance of the RC networks, i is 1 or 2 and corresponds to the first and second RC networks.

Figure 8 shows the results of the EEC parameters' identification process (based on Equations (5)–(8)) that were obtained for different temperatures and various SOC, when the discharging pulse case was considered. Similar results were obtained for the charging pulse case.

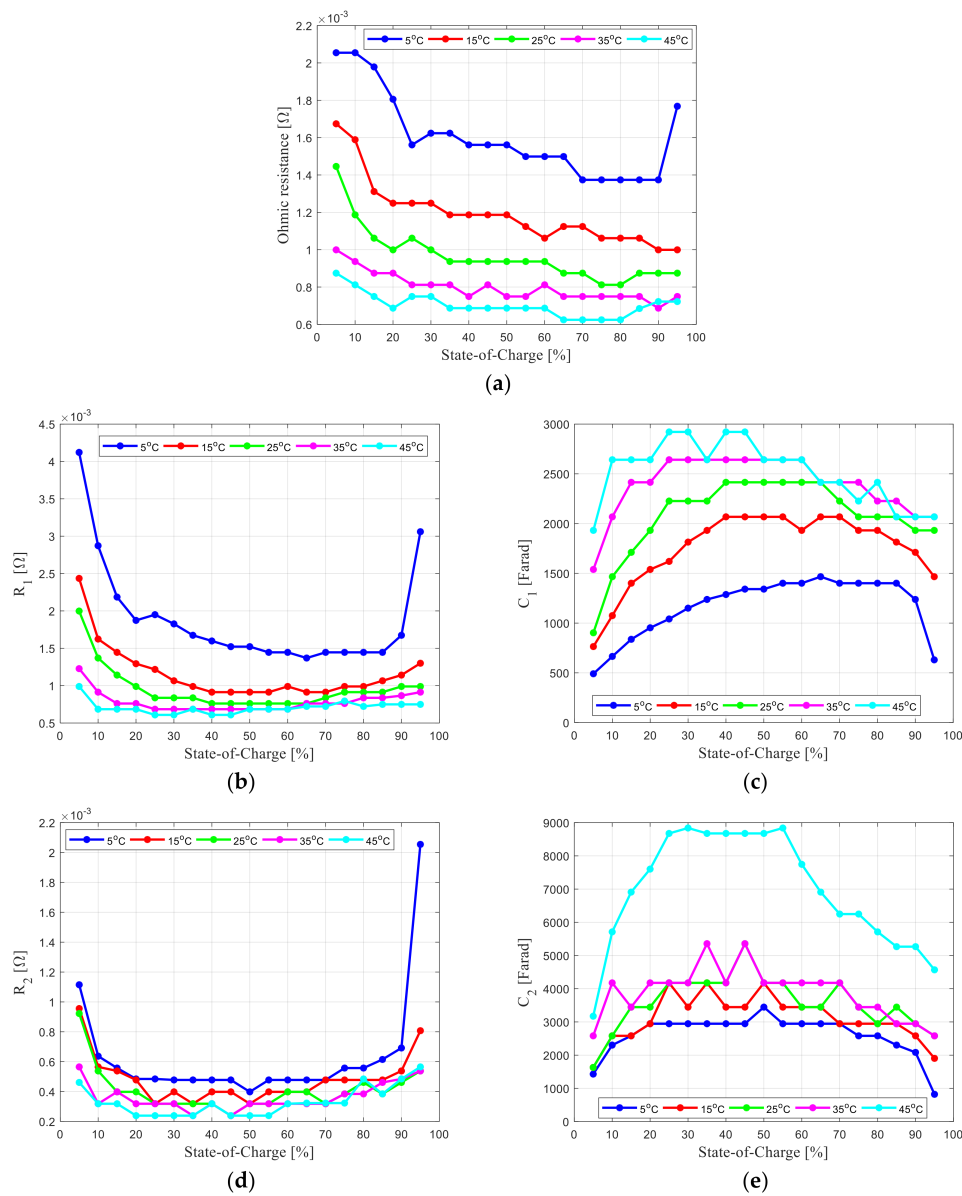


Figure 8. Variation of EEC parameters (a) R_0 ; (b) R_1 ; (c) C_1 ; (d) R_2 ; (e) C_2 with SOC and temperature.

As it can be observed in Figure 8, the ohmic resistance, R_0 , as well as resistances R_1 and R_2 significantly decrease with the increase in temperature. Meanwhile, the capacitances, C_1 and C_2 , are increasing with the increase in temperatures. Furthermore, all five parameters are changing with SOC. These experimental results show dependence between battery parameters and the operating conditions and justify the need to analyze the sensitivity of the battery model to the changes in the parameters.

4. State-of-Charge Estimation Based on Extended Kalman Filter Method

Kalman filters were firstly used in the area of aerospace. They are able to estimate the optimal state of a system on the basis of a series of data observed from the state space equation in the linear space. For the purpose of achieving the states also in a nonlinear system, EKF is proposed. The EKF dynamically linearizes the nonlinear model at the working point by a Taylor Series expansion.

The battery state space function is also a nonlinear system, especially in the lower and higher SOC ranges.

Considering the EEC presented in Figure 1, the battery model is expressed as follows:

$$\begin{cases} V_{bat} = V_{OC} - V_1 - V_2 - I \cdot R_0 \\ I = \frac{V_1}{R_1} + C_1 \cdot \frac{dV_1}{dt} = \frac{V_2}{R_2} + C_2 \cdot \frac{dV_2}{dt} \end{cases} \quad (9)$$

First equation presented in the Equation (9), represents the battery voltage, V_{bat} . From Equation (9), we can obtain the state space function of the two RC model as follows:

$$\begin{cases} X_{k+1} = A \cdot X_k + B \cdot I_k \\ Y_{k+1} = C \cdot X_k + D \cdot I_k \end{cases} \quad (10)$$

where:

$$X_k = \begin{bmatrix} V_1 \\ V_2 \\ SOC \end{bmatrix}_k, A = \begin{bmatrix} -\frac{T}{R_1 \cdot C_1} + 1 & 0 & 0 \\ 0 & -\frac{T}{R_2 \cdot C_2} + 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, B = \begin{bmatrix} \frac{T}{C_1} \\ \frac{T}{C_2} \\ -\frac{T}{C_{cap}} \end{bmatrix},$$

$$C = \begin{bmatrix} -1 & -1 & \frac{\partial f(OCV)}{\partial SOC} \end{bmatrix}, D = R_0, Y_k = U_{t,k}.$$

where T is the step time response. In this equation, the SOC of the battery and the voltages across the two RC circuit are selected to be system state variable. The EKF computes the Jacobian matrix from (9), then the matrix C is obtained. In Equation (10), the approximation $e^{A \cdot T} \approx I + A \cdot T$ is using to discrete the battery state space equation [5].

After establishing the state space equation, the steps for SOC estimation by EKF are listed in Table 3.

Table 3. The process of EKF for SOC estimation.

Prediction	
State Prediction	$X_{k+1 k} = A \cdot X_k + B \cdot I_k$
Covariance Prediction	$P_{k+1 k} = A \cdot X_k \cdot A^T + Q_k$
Update	
Kalman Gain Matrix	$K_k = P_{k+1 k} \cdot C^T \cdot (C \cdot P_{k+1 k} \cdot A^T + W_k)^{-1}$
State Estimation	$X_{k+1}^* = X_{k+1 k} + K_k \cdot (y_k - C \cdot X_k - D \cdot I_k)$
Covariance Estimation	$P_{k+1} = (I - K_k \cdot C) \cdot P_{k+1 k}$

In Table 3, Q is the covariance of the process noise, W is the covariance of observation noise, and P is the error covariance. The initial values of the three covariance matrices should be set before the EKF

estimation. After giving initial values, the EKF is capable of converging to the optimal SOC through the iterative process summarized in Table 3. $X_{k+1|k}$ and $P_{k+1|k}$ are the estimated state and covariance matrix, respectively. Afterward, the Kalman filter gain and the covariance matrix are updated, and the estimated state is corrected by the updated gain. The update step utilizes the information from the new measurement for improving the a posteriori state estimation. In this way, the EKF can achieve the best tradeoff between sensor measurement and model output for an accurate state estimation. The parameter X_{k+1}^* from Table 3, is the final state estimation of the EKF. The structure of the EKF calculating steps is presented in Figure 9a. The EKF is able to estimate the battery's SOC on the basis of only the former state and the current measurement. Thus, it does not rely on the battery historical data and has a much higher computation efficiency. Moreover, according to the closed structure of the EKF, the algorithm is insensitive to the initial SOC value. The flowchart of the EKF-based SOC estimation is shown in Figure 9b.

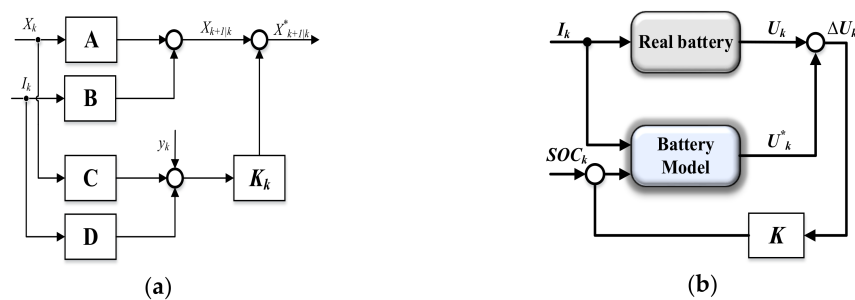


Figure 9. (a) The structure for EKF calculation; (b) The schematic diagram of EKF on SOC estimation.

5. State-of-Charge Estimation Results

The SOC of the LTO-based Li-ion battery is estimated using the EKF method, which is presented in Figure 9b. The structure of the SOC estimation method is illustrated in Figure 10. The EKF utilizes the voltage measurement from the battery and the load current profile applied to the battery, in order to estimate the SOC. Then, in order to improve the accuracy of the battery model, the estimated SOC and the battery current are substituted into the established battery model for updating parameter. In order to test the proposed SOC estimation method for the LTO-based battery, a step discharge profile was used. The considered battery cell was discharged, from a totally charged state, with 6.5 A (0.5C-rate) in steps of 5% Δ SOC. During the experiment, the data (i.e., current and voltage) were recorded with a sampling time of five seconds.

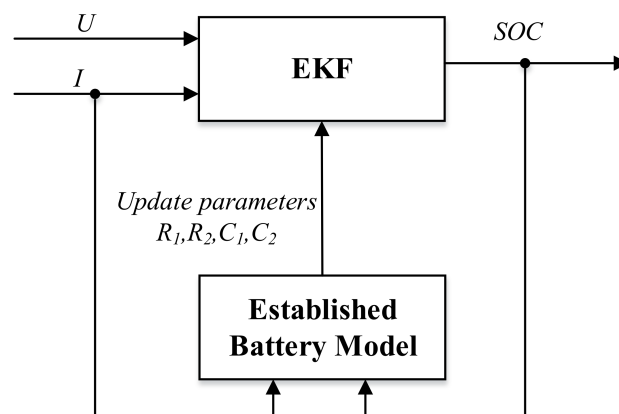


Figure 10. The structure of the SOC estimation method.

The result of the EKF based SOC estimation, for a temperature of 25 °C is shown in Figure 11a. Furthermore, a comparison between the laboratory measured battery voltage and the estimated battery voltage by the model is presented in Figure 11b. In order to test the SOC estimation, the initial SOC of the EKF method was arbitrarily set to 0.7 (70%) for further analysis in this paper.

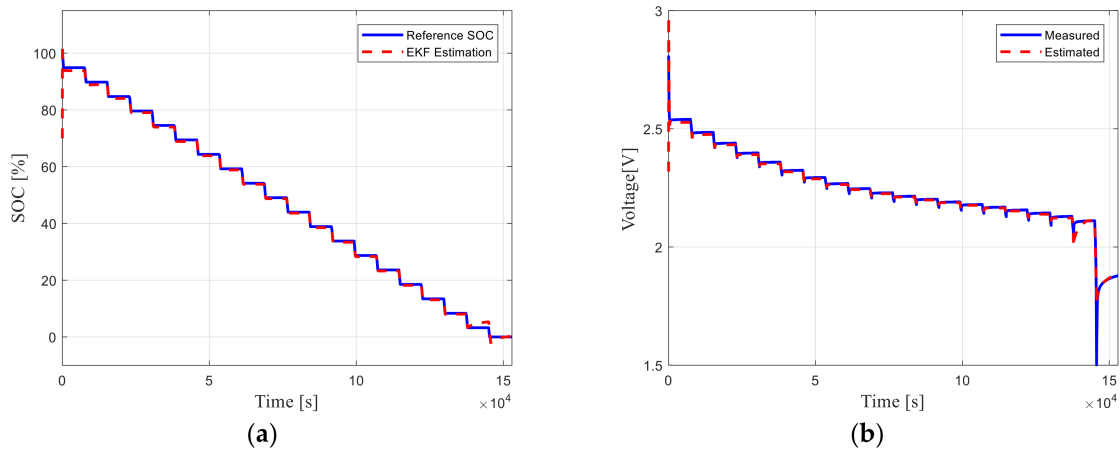


Figure 11. (a) SOC estimation results at 25 °C when the initial SOC is set to 70%; (b) Comparison between measured and estimated voltage 25 °C.

Moreover, Figure 12a shows a discharged pulse, where random SOC values have been assigned to initialize the EKF estimation method. The initial SOC used in EKF method has been 50%, 70%, and 100%, while the SOC reference is actually 100%. The results of these experiments show that in the beginning there is a high error in the SOC estimation (50%, 30%), then the estimated SOC converge to the reference (steady-state value) after an acceptable settling time (up to 100 s). Then the SOC stays with the reference, overlapping with very small errors. The error band of the SOC estimation method has to be between the $\pm 2\%$ [21,38]. The obtained SOC estimation error, when the initial SOC for the EKF has been set 50%, 70% and 100% are showed in Figure 12b.

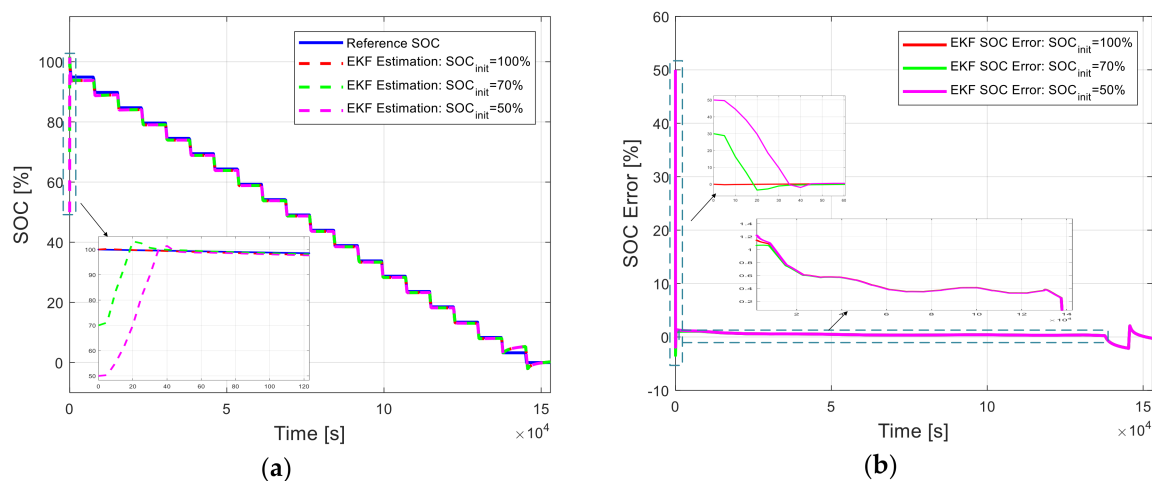


Figure 12. (a) Experimental results of EKF method at 25 °C considering different initial SOC assignments (50%, 70%, 100%); (b) SOC estimation error curves at 25 °C.

Furthermore, the mean absolute error between the measured and estimated SOC and voltage profiles were computed according to Equation (10):

$$|\bar{\varepsilon}| = \left| \overline{x_{ref}(i) - x_{est}(i)} \right|, \quad (11)$$

where x_{ref} represents the voltage measured, and the reference SOC, respectively and x_{est} represents the modeled voltage, and the SOC estimated, respectively. The SOC and voltage estimation mean errors are summarized in Table 4, while the maximum SOC and voltage estimation errors are summarized in Table 5.

Using the proposed model based on the EKF, the SOC and voltage of the battery were estimated also for a similar discharge profile at four other temperatures, i.e., 5 °C, 15 °C, 35 °C, 45 °C. The obtained SOC and voltage mean estimation errors are also summarized in Table 4. As it can be observed the proposed model estimates with very good accuracy both the SOC and voltage of the LTO-based battery; the highest mean estimation error was 0.0144 V (at T = 45 °C) for voltage and 1.16% (at 35 °C) for SOC. The maximum SOC and voltage estimations errors (i.e., 5.57% and 0.55 V, respectively) were obtained for a temperature of 5 °C; nevertheless, for all the considered temperatures the maximum voltage and SOC estimation errors were obtained in the beginning of the simulations, when the SOC estimator was not able yet to capture the reference SOC.

Table 4. SOC and voltage mean estimation errors.

Mean Error	Temperature				
	5 °C	15 °C	25 °C	35 °C	45 °C
SOC [%]	0.4440	0.8422	0.5437	1.1569	1.1422
Voltage [V]	0.083	0.0087	0.0058	0.0172	0.0144

Table 5. SOC and voltage maximum estimation errors.

Max. Error	Temperature				
	5 °C	15 °C	25 °C	35 °C	45 °C
SOC [%]	5.5703	1.7172	2.1326	3.3254	2.2291
Voltage [V]	0.5588	0.0570	0.272	0.1380	0.1242

As one can observe in Figure 11, the proposed model is not able to estimate the voltage and the SOC of the studied LTO-based battery for SOC values close to 0%. This lack of accuracy is caused by the fact that the model was parametrized considering a 5% SOC resolution, as previously mentioned; however, for SOC values below 10%, the voltage behavior of the battery changes steeply (i.e., decreases drastically), which suggests that for this interval, the battery model has to be parameterized considering a higher SOC resolution, e.g., 2% SOC steps instead of 5% SOC.

6. Sensitivity Analysis of Estimated SOC and Battery Voltage

The sensitivity, of the proposed SOC estimation model, on the parameters of the battery model, was also analyzed. As previously mentioned, the parameters of the EEC were obtained for SOC between 5% and 95% with 5% SOC resolution. In order to perform this sensitivity analysis, each parameter of the EEC was kept constant at a time (at the average value between the values obtained for each SOC at 0.5C), while the other parameters were varying with the SOC. This analysis was repeated for all the considered five temperatures.

The obtained SOC and voltage estimation errors are summarized in Table 6. Furthermore, the measured and estimated voltage profiles, for the sensitivity analysis performed at 25 °C, are presented in Figure 13. In Table 6, the highlighted (grey shade) values represent the instances when the obtained errors for the case when the average for the parameter was used are higher than the errors for the case when the dependence on the SOC was considered. Moreover, Figure 14 shows the obtained errors in terms of SOC and voltage, respectively, when the initial SOC of the EKF method is set to be 70%.

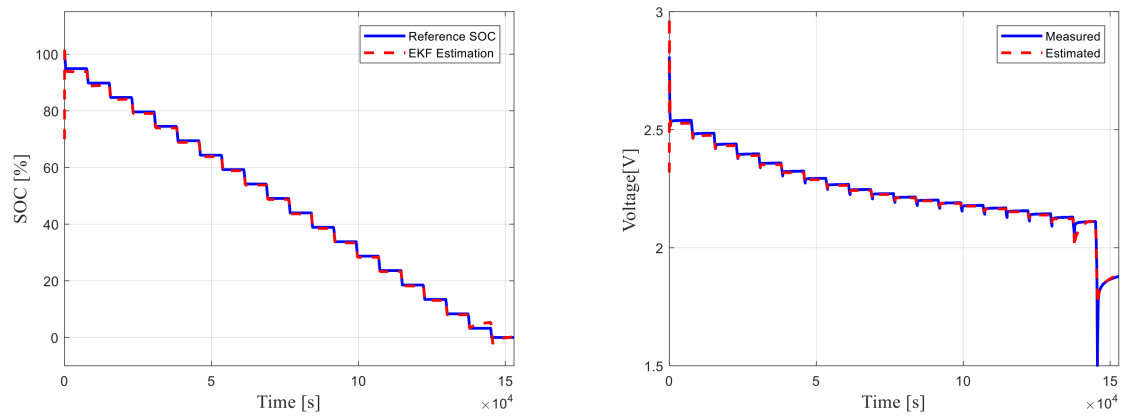
As one can observe, the SOC estimation is most sensitive with the changes in the values of the resistances and the capacitances of the RC-networks, while the battery voltage is most sensitive to the capacitance, C_1 .

Table 6. Sensitivity analysis of the error of the SOC and battery voltage. Mean errors.

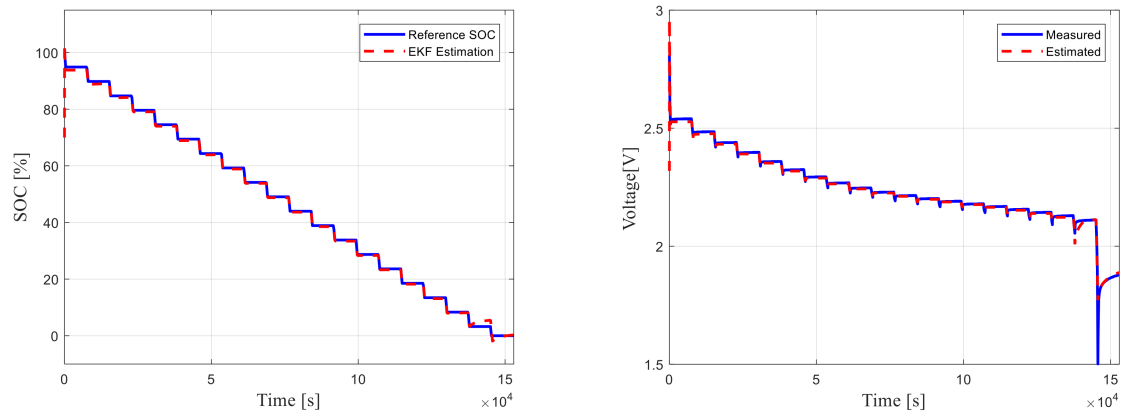
Condition	Mean Error	Temperature				
		5 °C	15 °C	25 °C	35 °C	45 °C
R_0 constant	SOC [%]	0.4463	0.8390	0.5420	1.543	1.1442
	Voltage [V]	0.0084	0.0088	0.0058	0.0172	0.0144
R_1 constant	SOC [%]	0.5166	0.8457	0.5221	1.1738	1.1235
	Voltage [V]	0.0083	0.0086	0.0056	0.0017	0.0136
C_1 constant	SOC [%]	0.8676	0.8675	0.5790	1.1561	1.2407
	Voltage [V]	0.0074	0.009	0.0085	0.0175	0.0161
R_2 constant	SOC [%]	0.3637	0.8782	0.6101	1.1755	1.1459
	Voltage [V]	0.0086	0.0089	0.0068	0.0169	0.00136
C_2 constant	SOC [%]	0.9623	0.8510	0.4341	1.1830	1.2193
	Voltage [V]	0.0077	0.0089	0.0054	0.0169	0.0153

However, by comparing the results summarized in Tables 4 and 6, it can be concluded that generally, the differences between the two cases are rather small. This behavior suggests that the variation of the parameters of the EEC with the LTO-based Li-ion battery SOC has only a small impact on the accuracy of the SOC and voltage estimation.

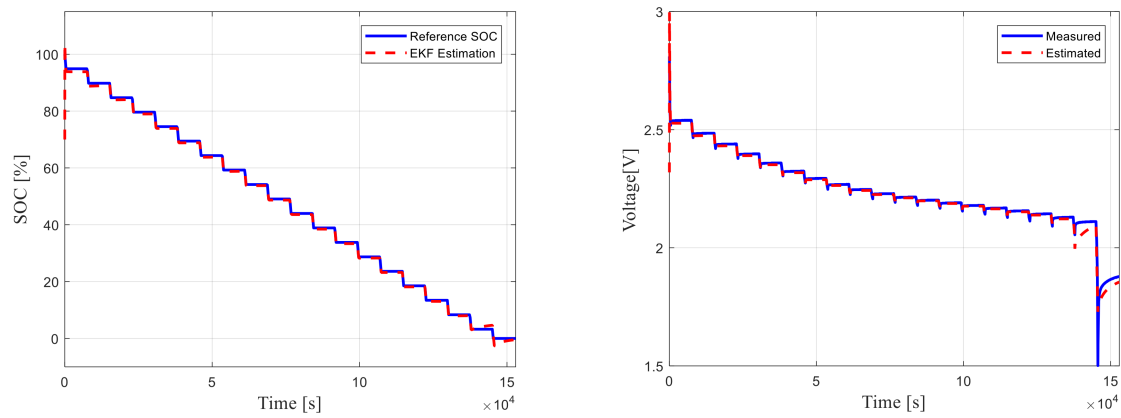
The same conclusion can be drawn by comparing the maximum error values obtained for the two cases, which are summarized in Table 5 (parameters values changing with SOC) and Table 7 (parameters values constant with SOC). From Table 6, one can see that the SOC estimation error is below the acceptable error (2%) in all the considered study cases.



(a)



(b)



(c)

Figure 13. Cont.

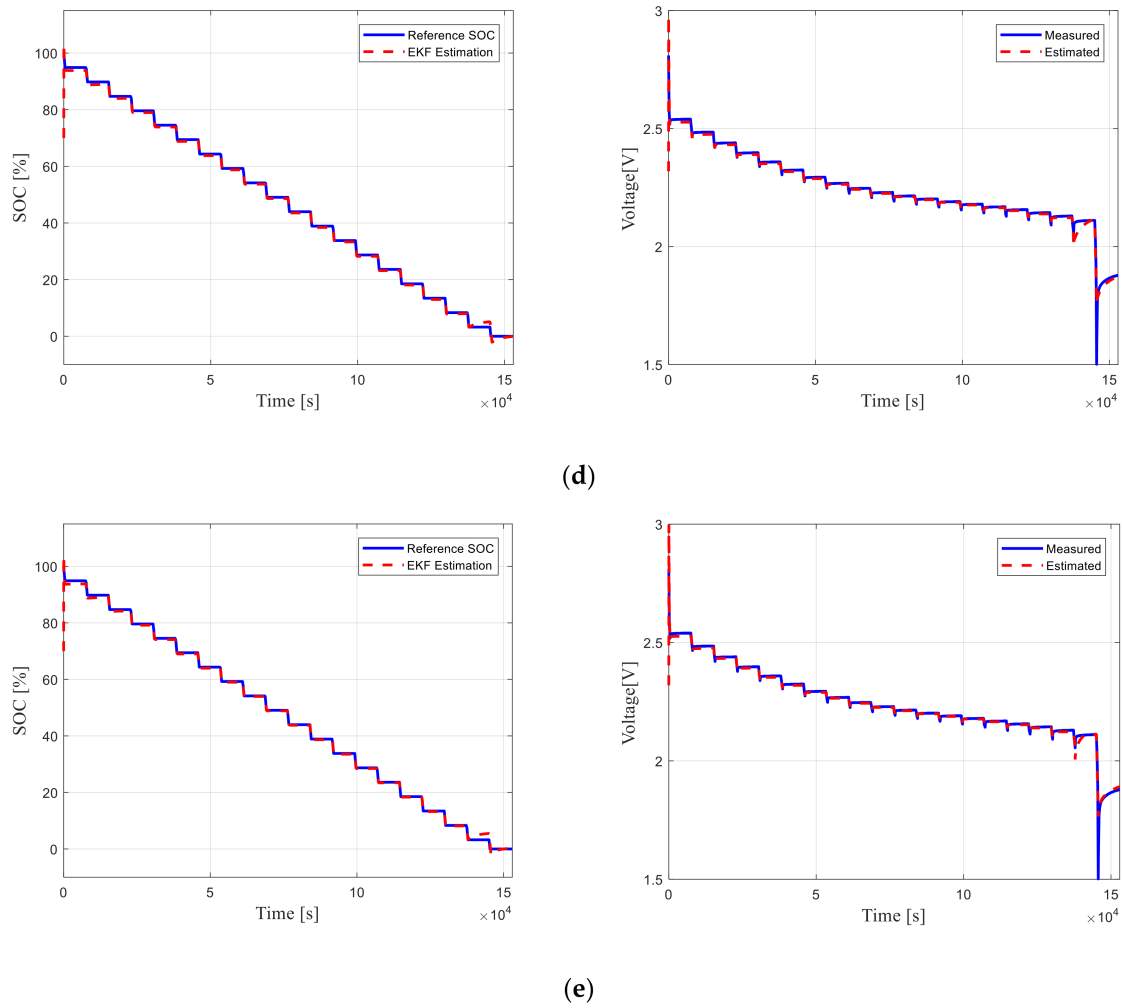


Figure 13. Comparison between the measured and estimation SOC (left) and voltage (right) profiles obtained during sensitivity analysis performed at 25 °C for: (a) R_0 constant; (b) R_1 constant; (c) C_1 constant; (d) R_2 constant; (e) C_2 constant.

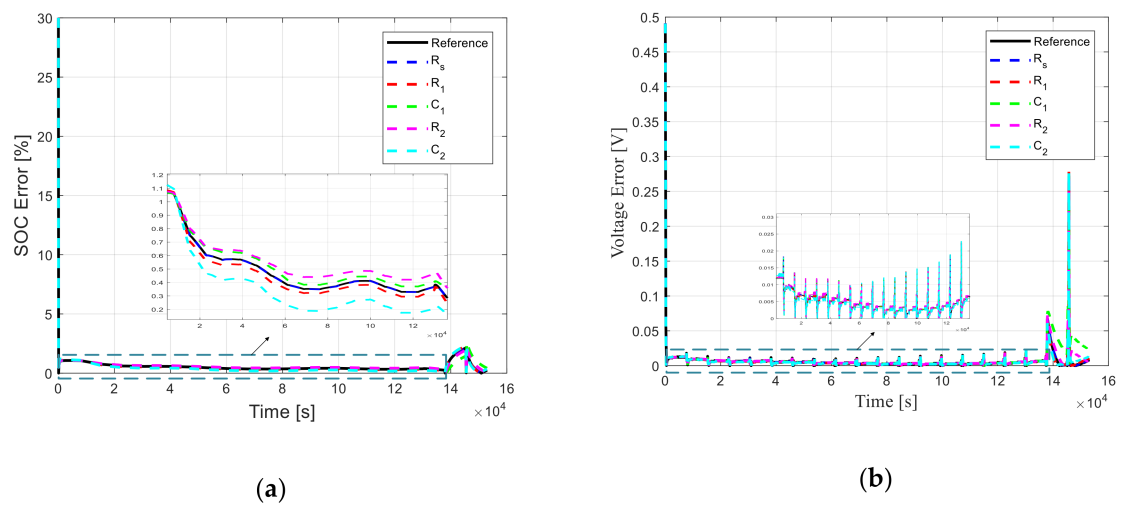


Figure 14. Estimation error curves at 25 °C obtained during sensitivity analysis in terms of: (a) SOC; (b) Voltage.

Table 7. Sensitivity analysis of the error of the SOC and battery voltage. Maximum error values (the shaded values represent the instances when the obtained errors, for the case when the average for the parameter was used, are higher than the errors for the case when the dependence on the SOC was considered).

Condition	Mean error	Temperature				
		5 °C	15 °C	25 °C	35 °C	45 °C
R_0 constant	SOC [%]	5.5756	1.7125	2.1296	3.3240	2.2414
	Voltage [V]	0.5597	0.0553	0.2716	0.1357	0.1225
R_1 constant	SOC [%]	5.7070	1.6713	2.284	3.2537	2.1477
	Voltage [V]	0.5613	0.0448	0.2781	0.1318	0.1126
C_1 constant	SOC [%]	5.6378	1.8295	2.6402	3.4126	2.4001
	Voltage [V]	0.5412	0.0580	0.2398	0.1407	0.1389
R_2 constant	SOC [%]	5.2382	1.7274	2.1197	3.2550	2.3199
	Voltage [V]	0.5613	0.0448	0.2781	0.1318	0.1126
C_2 constant	SOC [%]	6.5139	1.8620	2.2949	3.4093	2.2162
	Voltage [V]	0.5554	0.0584	0.2776	0.1406	0.1330

Figure 14 illustrates the estimation errors obtained for SOC and battery voltage at 25 °C. As it can be observed, only at the beginning, there is a high error (30%) due to the fact that initial SOC of the EKF method is set to 70%. After estimated SOC converge to its reference, the estimated SOC stay close to the reference, overlapping with small errors in all the cases. From Figure 14a, it can be observed that R_2 and C_2 are the most sensitive parameters, and from Figure 14b that C_2 is the most sensitive parameter. For example, keeping the parameter C_2 constant at its average value for the entire SOC interval will result in an increase in the voltage estimation error of about 10 mV in comparison with the case when C_2 varies with SOC.

7. Conclusions

In this paper, a battery model-based on EKF SOC estimation algorithm was developed and verified for an LTO-based Li-ion battery. A second order RC-EEC was used to model the dynamics of the battery. The EEC was fully parameterized, based on extended laboratory measurements, by considering the variation of the circuit parameters with SOC, temperature, and C-rate. Furthermore, in order to estimate the battery SOC using the EKF method, a polynomial function has been used in order to map the VOC-SOC function and afterward used it for an optimal observer.

The proposed SOC estimation algorithm based on the EKF method is able to converge very fast, in a maximum of 100 s, from the initial SOC used for initialization to the reference SOC that is based on Coulomb counting with known initial SOC. Accurate estimation results have been obtained when the SOC estimated by the developed model was compared with a reference SOC obtained using the Coulomb counting method for a step discharge profile; the mean absolute error varied between 0.444 to 1.1422%, depending on the temperature, which is well below the 2% SOC estimation error mentioned in literature. Moreover, with the developed model it was also possible to predict accurately the battery voltage with a mean absolute error below 0.02 V, independent of the considered temperature.

By performing a sensitivity analysis, it was shown that the SOC estimation is most sensitive to the variation with the SOC of the parameters of the two RC networks, while the voltage estimation is most sensitive to the change of capacitance C_1 with SOC; nevertheless, both SOC and voltage estimation are only slightly dependent on the changes of the EEC parameters with the SOC.

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