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Published in:

I E E E Transactions on Sustainable Energy

DOI (link to publication from Publisher): 10.1109/TSTE.2018.2825361

Publication date: 2019

Document Version Accepted author manuscript, peer reviewed version

Link to publication from Aalborg University

Citation for published version (APA): Ding, T., Yang, Q., Liu, X., Huang, C., Yang, Y., Wang, M., & Blaabjerg, F. (2019). Duality-Free Decomposition Based Data-Driven Stochastic Security-Constrained Unit Commitment. *I E E Transactions on Sustainable Energy*, *10*(1), 82-93. Article 8334604. https://doi.org/10.1109/TSTE.2018.2825361

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# Duality-Free Decomposition Based Data-Driven Stochastic Security-Constrained Unit Commitment

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Abstract— To incorporate the superiority of both stochastic and robust approaches, a data-driven stochastic optimization is employed to solve the security-constrained unit commitment model. This approach makes the most use of the historical data to generate a set of possible probability distributions for wind power outputs and then it optimizes the unit commitment under the worst-case probability distribution. However, this model suffers from huge computational burden, as a large number of scenarios are considered. To tackle this issue, a duality-free decomposition method is proposed in this paper. This approach does not require doing duality, which can save a large set of dual variables and constraints, and therefore reduces the computational burden. In addition, the inner max-min problem has a special mathematical structure, where the scenarios have the similar constraint. Thus, the max-min problem can be decomposed into independent sub-problems to be solved in parallel, which further improves the computational efficiency. A numerical study on an IEEE 118-bus system with practical data of a wind power system has demonstrated the effectiveness of the proposal.

Index Terms—Data-driven stochastic optimization; duality-free decomposition; security-constrained unit commitment; distributionally robust optimization

### NOMENCLATURE

$t\in \mathcal{T}$	Hourly periods, running from 1 to $T= \mathcal{T} $ .
$l\in\mathcal{L}$	Transmission lines, running from 1 to $L= \mathcal{L} $ .
$b\in \mathcal{B}$	Buses, running from 1 to $B= \mathcal{B} $ .
$q \in \mathcal{Q}$	Wind units, running from 1 to $Q= Q $ .
$g \in \mathcal{G}$	Thermal units, running from 1 to $G= G $ .
$\omega \in \Omega$	Wind power scenarios, running from 1 to $N= \Omega $ .
$s \in \mathcal{S}_a$	Startup segments, running from 1 (hottest) to
9	$S_q =  S_q $ (coldest).

This work was supported in part by National Key Research and Development Program of China (2016YFB0901900), in part by National Natural Science Foundation of China (Grant 51607137), in part by China Postdoctoral Science Foundation (2017T100748), in part by the project of State Key Laboratory of Electrical Insulation and in part by Power Equipment in Xi'an Jiaotong University (EIPE16301). This work was performed under the auspices of the U.S. Department of Energy by Lawrence Livermore National Laboratory under Contract DE-AC52-07NA27344 with Release Number LLNL-JRNL-TBD.

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- $\psi$  Confidence set for uncertain probability distribution of wind power.
- f(b), t(b) Transmission lines subset starting from bus b or ending at bus b.
- G(b), W(b) Thermal or wind units subset located at bus b.
  - $P_{gt\omega}$  Power output of thermal unit g at period t under scenario  $\omega$  [MW].
  - $W_{qt\omega}$  Forecasted power output of wind unit q at period t under scenario  $\omega$  [MW].
  - $L_{bt\omega}^{\rm shed}$  Load shedding imposed on bus b at period t under scenario  $\omega$  [MW].
  - $PL_{lt\omega}$  Power flow on transmission line l at period t under scenario  $\omega$  [MW].
- $\theta_{at\omega}$ ,  $\theta_{bt\omega}$  Phase angle of bus a and bus b at period t under scenario  $\omega$  [rad].
  - $r_{gt\omega}$  Spinning reserve provided by thermal unit g at period t under scenario  $\omega$  [MW].
  - $u_{gt}$  Commitment status that is equal to 1 if thermal unit g is online at period t.
  - $v_{gt}$  Startup status that is equal to 1 if thermal unit g starts up at period t.
  - $z_{gt}$  Shutdown status that is equal to 1 if thermal unit g shuts down at period t.
  - $\delta_{gst}$  Startup type *s* of thermal unit *g*, which is equal to 1 at the period *t* where the unit starts up and has been offline within  $[T_{gs}^{SU}, T_{g,s+1}^{SU})$  hours.
  - $\pi_{\omega}$  Probability of wind power scenario  $\omega$ .
- $\pi_{\omega}^{0}$  Probability of wind power scenario  $\omega$  from data  $C_{g}^{\text{NL}}$ ,  $C_{g}^{\text{SD}}$  No-load cost and shutdown cost of thermal unit g [\$].
  - C<sup>LOL</sup> Load shedding cost [\$/MWh].
  - $C_{gs}^{\rm SU}$  Startup cost of thermal unit g when the unit starts up and has been offline within  $[T_{gs}^{SU}, T_{g,s+1}^{SU})$  hours [\$].
  - $L_{bt}$  Load demand located at bus b at period t [MW].
- $PL_l^{\text{max}}$  Capacity of transmission line l [MW].
  - $x_{ab}$  Reactance of transmission line from bus a to bus b [per unit].
  - $R_t$  Spinning reserve requirement at period t [MW].
- $TU_g$ ,  $TD_g$  Minimum uptime and minimum downtime of thermal unit g [h].
- $P_g^{\text{max}}$ ,  $P_g^{\text{min}}$  Maximum and minimum power output of thermal unit g [MW].
- $SU_g$ ,  $SD_g$  Startup capability and shutdown capability of thermal unit g [MW].
- $RU_g$ ,  $RD_g$  Ramp-up rate and ramp-down rate of thermal

unit g [MW/h].

- $\alpha$  Pre-designed confidence level.
- $\beta$  Controllable parameter for confidence set.
- $N_s$  The Number of scenarios.
- K The Number of historical data.

#### I. INTRODUCTION

C ecurity constrained unit commitment (SCUC) is one of the important functions for scheduling generators in day-ahead power system operation [1]-[3]. It determines the on/off status of all dispatchable units over a given number of horizons while satisfying all the physical constraints of generators and the power network. However, with a high penetration of wind power into the power grid, many challenging issues arise [4]. The wind power output is highly stochastic and volatile, which hinders their efficient and secure large-scale deployment and challenges the SCUC of power systems. Thus, the uncertainty of the wind power output should be considered in the SCUC scheduling problem. With this, many studies have been done in the literature [5-21]. They can be categorized into three groups: 1) interval constrained unit commitment (ISCUC) [5-6], 2) stochastic security-constrained unit commitment (SSCUC) [7-14], and 3) robust security-constrained unit commitment (RSCUC) [15-21].

SSCUC models generate several wind power scenarios associated with various probabilities to describe uncertainties. These models minimize the expected total cost while satisfying all operational constraints under all the scenarios [7]. In contrast, the RSCUC models are immune against the wind power uncertainties within a predefined uncertainty set [15]. These models essentially minimize the total cost under the worst-case scenario. The computational burden of the RSCUC models mainly depends on the definition of their uncertainty sets [20]. It should be noted that both the SSCUC and RSCUC models can be cast as a two-stage optimization problem. The first-stage decisions find the optimal unit commitment that cannot be changed once they are optimized before the true wind power realization; the second-stage decisions are adjusted to the realization of the wind power generation, which provides the recourse for the system. The difference of the two models is that the RSCUC expects to find the solution that can fully guarantee the feasibility for any possible realization within the uncertainty set, while the SSCUC only protects the system under the selected scenarios.

Nevertheless, compared with the SSCUC models, the RSCUC models may give relatively conservative solutions. Recently, the concept of uncertainty budget has been proposed to reduce over-conservative decisions. Several methods to construct the proper uncertainty sets based on historical data were introduced in [22] to reduce the conservativeness while maintaining the robustness of the solutions. In addition, [23] introduced a risk-constrained robust unit commitment model, where the uncertainty set was divided into several probability-blocks with respect to the data sets. A multistage adaptive robust unit commitment model was set up in [24],

where dynamic uncertainty sets were utilized to capture the temporal and spatial correlations of renewable energy as well as the sequential nature of the dispatch process. Furthermore, a two-stage min-max regret robust unit commitment was established in [25] to reduce the conservativeness, where the maximum regret in the robust optimization framework was considered. Moreover, adjustable uncertainty sets according to different system-risk levels were adopted to achieve the operational flexibility for day-head unit commitment [26]. Then, a novel unified stochastic and robust unit commitment model was proposed in [27] to reduce the expected cost by adjusting the weights in the objective function.

Compared with the RSCUC models, although the SSCUC models can avoid the conservative total cost, the system security cannot be sufficiently guaranteed. Therefore, many efforts were devoted into the chance-constrained security-constrained unit commitment (CSCUC) [28-30]. The CSCUC model ensures the feasibility for the constraints with stochastic variables in a certain probability. Since the chance constraints generally lead to the non-convexity, the CSCUC problem is usually solved by means of a sample-average approximation approach [28]. Only certain CSCUC models can be equivalently transformed into deterministic SCUC models [29], which leads to the notion of risk-averse SCUC models that include the operational risk. In general, the risk exposure of the power system is considered in the objective function or in the constraints of the SCUC model. Typically, the considered risk includes the loss-of-load and the wind curtailment [30]. The risk-averse SCUC model allows a tradeoff between the expected dispatch costs and the operational risks caused by uncertainties [31]. Recently, several risk measures have been applied to SCUC models, such as the mean-variance [32], shortfall probability [33], and conditional value-at-risk (CVaR) [31, 34].

Generally, stochastic programming methods cannot cover all possible realizations of uncertainties. A particular probability distribution of random parameters is usually assumed, which may be biased in practice. Although the robust optimization can take all realizations into consideration and protect the system against a pre-defined uncertainty set, it gives a more conservative solution than the stochastic approach. The chance-constrained framework is usually reformulated as a large-scale mixed integer programming model, depending on the number of scenarios considered in the model, which increases the computational burden. Also, as one of the stochastic approaches, it shares the same disadvantages with the SUC—it is not possible to enumerate all the scenarios and the solution depends on the assumed distribution in the model.

To achieve a more reasonable unit commitment with the superiority of stochastic and robust optimization models, the data-driven framework can be adopted to find a more suitable solution. It should be robust but less conservative. Based on the historical data, a series of possible probability distribution of wind power can be constructed. This model takes advantage of data information and considers the worst-case distribution of the uncertainties. When comparing with the case considering the worst-case scenario in the robust optimization approach, the

data-driven model yields less conservativeness. It aims to find an optimal solution under the worst probability distribution, known as "distributionally robust optimization" or "data-driven optimization" [35]-[38]. Recently, this approach is also used to solve the UC problem [39], [40]. More importantly, it does not require probabilistic distribution assumption. Instead, it allows an ambiguous distribution within the confidence set. This leads to a more robust solution compared with the stochastic optimization.

However, the model in [39] has difficulties in solving large-scale problems. More specifically, due to the "max-min" duality, it is difficult to find the worst-case scenario. Clearly, a larger number of scenarios will lead to a more precise optimal solution, while increasing the complexity and computational burden. In that case, the problem becomes intractable or even unsolvable. In the prior-art work, the decomposition method has been proposed to tackle this issue [41], [42]. For instance, in [41], the augmented Lagrangian relaxation method was employed to decompose the large-scale problem into several small sub-problems (one for each scenario). However, this is only applicable to single-level stochastic programming models. In this paper, the proposed data-driven distributionally robust optimization is essentially a "min-max-min" tri-level model to efficiently solve the above issues. To our best knowledge, how to decompose the tri-level optimization model has not been addressed yet in the literature.

The main contributions of this paper are summarized as:

- (i) A data-driven stochastic SCUC model is set up using the practical data that incorporates the superiority of stochastic and robust optimization models. Meanwhile, the practical wind speed is analyzed under four seasons during one year, which facilitates the stochastic SCUC model.
- (ii) A novel decomposition approach is proposed to solve the tri-level data-driven stochastic unit commitment model. This approach does not require dualization, which can save a large set of dual variables and constraints and thus reduce the computational burden. Additionally, due to its special structure, the inner max-min problem can be decomposed into independent sub-problems and then solved in parallel, which further improves the computational efficiency.

The rest of the paper is organized as follows: Section II investigates the modeling of wind power generation scenarios. In Section III, a data-driven stochastic security-constrained unit commitment (SCUCU) model is set up considering the uncertain probability distribution of wind power. A duality-free based Bender's decomposition algorithm is then proposed to solve the data-driven stochastic SCUC model in Section IV. In Section V, numerical results and comparisons on a standard IEEE 118-bus system demonstrate the effectiveness of the proposed model and method. Finally, conclusions are drawn in Section VI.

#### II. WIND POWER SCENARIO GENERATION

Wind power generation scenarios are usually generated with Monte Carlo simulations using a predefined wind power distribution. However, in order to describe a precise wind power distribution, wind speed characteristics should be analyzed according to the wind farm historical data. In this paper, the wind speed is characterized by four seasons in a year. Taking one real-field wind farm in China as an example, where the wind speed data in the past 10 years is utilized:

Fig. 1 depicts the wind speed in one day (24 hours) and one month (720 hours). It can be observed that the wind speed is stochastic and volatile. However, the wind speed is relatively periodic and the daily wind speed distribution over a long period is similar.

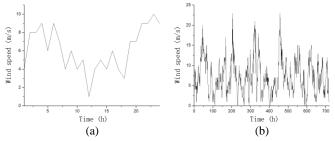


Fig. 1. Wind speed distribution in the wind farm located in Northwest China for: (a) one day and (b) one month.

For one day, Fig. 2 shows the wind speed distribution at 00:00 AM and 12:00 PM. It can be observed that the wind speed distribution has a "double-peak" nature, where the peak values are near 0 m/s and 5 m/s, respectively. The number of scenarios becomes smaller with the increase in wind speed. Meanwhile, a comparison of Fig. 2(a) and (b) implies that the average wind speed at 12:00 PM is higher than that at 00:00 AM. Moreover, the number of scenarios with high wind speeds (more than 18 m/s) is larger at 12:00 PM than that at 00:00 AM. As a result, the wind speed modeling should consider the daily time-series characteristics.

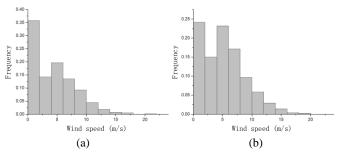


Fig. 2. Wind speed distribution of the wind farm in one day at: (a) 00:00 AM and (b) 12:00 PM.

However, for one year, Fig. 3 depicts the distribution of wind speeds, which shows that the high wind speed condition is more frequent in spring and winter than that in summer and autumn. In spring, the peak wind speed is around 7.5 m/s and there are several scenarios with the wind speed higher than 12.5 m/s; in summer, the peak is around 5 m/s and the number of scenarios with the wind speed higher than 10 m/s is small. The statistics from historical data suggest that four seasons have different wind speed characteristics. As a consequence, daily time-series characteristics should be modeled separately.

Based on the historical data, the daily wind power density can be estimated through various prior-art probabilistic forecast approaches. Meanwhile, in [43], a method that can generate statistical scenarios of the wind power generation considering spatial-temporal interdependence was introduced, and it is also used in this paper. Then, 1000 wind power scenarios are set up at the beginning according to the estimated probability density function describing the uncertainty in forecasts. Furthermore, the scenario generation technique is based on building joint predictive densities from the marginal ones. The interdependent structure of wind power generation through time and space is modeled by the covariance matrix of the multivariate Gaussian distribution. Finally, it is known that a large number of scenarios are required to fully characterize the wind power uncertainty. However, increasing the number of scenarios makes the stochastic SCUC modelling become computationally intractable. To retain the tractability and maintain the statistical information, the probability distance-based scenario-reduction technique [44] is employed in this paper.

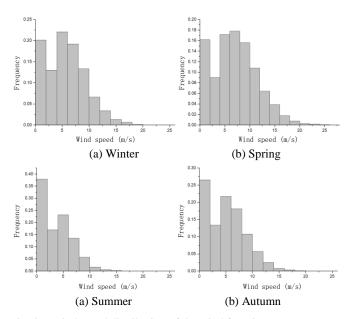


Fig. 3. Wind speed distribution of the wind farm in a year.

#### III. DATA-DRIVEN STOCHASTIC SCUC MODEL

# A. General Stochastic SCUC Model

In this section, the general stochastic SCUC model is set up in a tight and compact MILP formulation [39]. It was discussed in [39] that the tight and compact formulation could improve the computational efficiency of stochastic UC models, since a smaller searching space and a faster searching process for the branch-and-cut algorithm are enabled.

The stochastic SCUC optimization problem aims to minimize the expected operational cost over a given number of time horizons while satisfying various physical constraints. Specifically, the objective function should include: (i) the fixed production cost; (ii) startup cost; (iii) shutdown cost; (iv) production cost; and (v) loss-of-load cost, such that

$$\min \sum_{t \in T} \sum_{g \in \mathcal{G}} \left( C_g^{NL} u_{gt} + \sum_{s \in \mathcal{S}_g} C_{gs}^{SU} \delta_{gst} + C_g^{SD} z_{gt} \right)$$

$$\begin{split} + \sum_{\omega \in \Omega} \pi_{\omega} \Biggl( \sum_{t \in T} \sum_{g \in \mathcal{G}} F_g (P_{gt\omega}) + \sum_{t \in T} \sum_{b \in \mathcal{B}} C^{LOL} L_{bt\omega}^{shed} \Biggr) (1) \\ s.t. \quad \delta_{gst} \leq \sum_{i = T_{gs}^{SU}} z_{g,t-i} \quad \forall g,t \in [T_{g,s+1}^{SU},T], s \in [1,S_g) \ (2) \\ \sum_{s \in \mathcal{S}_g} \delta_{gst} = v_{gt} \qquad \forall g,t \quad (3) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq u_{gt} \quad \forall g,t \in [TU_g,T] \quad (4) \\ \sum_{i = t - TU_g + 1} z_{gi} \leq 1 - u_{gt} \quad \forall g,t \in [TU_g,T] \quad (5) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gt} \quad \forall g,t \in [TU_g,T] \quad (5) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gt} \quad \forall g,t \quad (6) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gt} \quad \forall g,t \quad (6) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gt} \quad \forall g,t \quad (6) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gt} \quad \forall g,t \quad (6) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gt} \quad \forall g,t \quad (7) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gt} \quad \forall g,t,\omega \quad (7) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gt} \quad \forall g,t,\omega \quad (7) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gt} \quad \forall g,t,\omega \quad (12) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (13) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (14) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (15) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (15) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (16) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (16) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (16) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (16) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (16) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (16) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (16) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (16) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (16) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (16) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (16) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (16) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (16) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi} \quad \forall g,t,\omega \quad (16) \\ \sum_{i = t - TU_g + 1} v_{gi} \leq 1 - u_{gi$$

In the above formulation, constraints (2) and (3) are startup cost constraints. They choose the suitable startup-type variable  $\delta_{gst}$  that activates the corresponding startup cost  $C_{gs}^{SU}$  in the objective function of (1). Constraints (4) and (5) are the minimum uptime and downtime constraints. Constraint (6) is a logical constraint guaranteeing that  $v_{gi}$  and  $z_{gi}$  have proper values at the startup and shutdown time. Constraints (7), (8) and (9) are to meet the power balance and network transmission security requirements. Constraint (10) describes the load shedding. Constraints (11), (12) and (13) refer to the ramping limitation and spinning reserve requirement. Constraints (14), (15) and (16) denote the minimum and maximum generation limitations.

# B. Proposed Data-driven Stochastic SCUC Model

It should be noted that the probability distribution of wind power is important to generate scenarios. However, the uncertainties should be considered in the system modeling. In this way, the unknown probability distribution of wind power follows any possible probability distribution within a pre-defined confidence set built up upon the historical data.

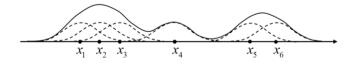


Fig. 4. Uncertain probability distribution functions.

As shown in Fig. 4, the possible probability distributions are fully covered by the confidence set. Here, we consider that the pre-defined confidence set  $\Psi$  is convex, which can facilitate the computation. In the prior-art research, two methods were reported to construct the confidence set. One is based on the first- and second-order moments (e.g., mean and variance). The other is to utilize the density information (e.g., norm-1 and norm-*inf*). In this paper, the latter is adopted for illustration and the two confidence sets can be expressed as

$$\begin{split} \Psi_{1} &= \{\pi_{\omega} | \|\pi_{\omega} - \pi_{\omega}^{0}\|_{1} \leq \beta\} \\ &= \left\{\pi_{\omega} \left| \sum_{\omega \in \Omega} |\pi_{\omega} - \pi_{\omega}^{0}| \leq \beta\right\} \right. \\ \Psi_{\infty} &= \{\pi_{\omega} | \|\pi_{\omega} - \pi_{\omega}^{0}\|_{\infty} \leq \beta\} \\ &= \left\{\pi_{\omega} \left| \max_{\omega \in \Omega} |\pi_{\omega} - \pi_{\omega}^{0}| \leq \beta\right\} \right. \end{split} \tag{17a}$$

It has been studied in [39] that the estimated probability distribution will approach the true probability distribution if more historical data can be obtained. For a pre-designed confidence level  $\alpha$  and the controllable parameter for the confidence set  $\beta$  can be calculated as

$$\beta_{\Psi_1} = \frac{\dot{N}_s}{2K} \ln \frac{2N_s}{1-\alpha} \,, \quad \beta_{\Psi_\infty} = \frac{1}{2K} \ln \frac{2N_s}{1-\alpha}$$
 (18)

For each given probability distribution, the stochastic SCUC model can be solved by (1)-(16). The confidence set actually gives a series of estimated probability distributions of wind power that will give a series of stochastic SCUC solutions. In order to protect the system against all the possible stochastic SCUC solutions resulted from the uncertain probability distribution of wind power. A data-driven stochastic SCUC model aims to find the optimal solution under the worst-case probability distribution, such that

$$\min_{u_{gt}, v_{gt}, \delta_{gst}, z_{gt}} \sum_{t \in \mathcal{T}} \sum_{g \in \mathcal{G}} \left( C_g^{NL} u_{gt} + \sum_{s \in \mathcal{S}_g} C_{gs}^{SU} \delta_{gst} + C_g^{SD} z_{gt} \right) + \\
\max_{\pi_{\omega} \in \Psi} \min_{P_{gt\omega}, L_{bt\omega}^{Shed}} \sum_{\omega \in \Omega} \pi_{\omega} \sum_{t \in \mathcal{T}} \left( \sum_{g \in \mathcal{G}} F_g (P_{gt\omega}) + \sum_{b \in \mathcal{B}} C^{LOL} L_{bt\omega}^{Shed} \right) (19) \\
\text{s.t. (2)-(16)}$$

The above proposed data-driven stochastic SCUC model can be essentially cast as a two-stage optimization problem. Here, the first-stage optimizes the unit commitment, while the second-stage optimization is to find the worst-case operational cost and the load loss under different probability distributions of wind power.

#### IV. DUALITY-FREE DECOMPOSITION METHOD

The data-driven stochastic unit commitment model proposed in this paper can be solved by the Bender's decomposition method or the standard column-and-constraint generation method [20], [23], [45]-[46], which is implemented in a master sub-problem framework. That is, the sub-problem aims to find the critical scenario of the uncertain set that provides an upper bound. Then, new variables and constraints are added to the master problem to obtain a lower bound. The master problem and sub-problem are solved iteratively and the method stops

until the gap between the upper and lower bounds is smaller than a pre-set convergence tolerance.

#### A. Sub-problems

For a given set of specific first-stage variables in the k-th iteration as  $(u_{gt}^*, v_{gt}^*, \delta_{gst}^*, z_{gt}^*)$ , we can establish a second-stage bi-level "max-min" model from (19)-(20) to find the worst-case scenario, yielding

$$\begin{split} \max_{\pi_{\omega} \in \Psi} \min_{\substack{P_{gt\omega}, \, t_{bt\omega}^{\text{shed}}, \\ P_{L_{lt\omega}}, \theta_{t\omega}, r_{gt\omega}}} \sum_{\omega \in \Omega} \pi_{\omega} \sum_{t \in T} \left( \sum_{g \in \mathcal{G}} F_g (P_{gt\omega}) + \sum_{b \in \mathcal{B}} C^{LOL} L_{bt\omega}^{\text{shed}} \right) \end{aligned} \\ s.t. \sum_{g \in \mathbf{G}(b)} P_{gt\omega} + \sum_{q \in \mathbf{W}(b)} W_{qt\omega} - \left( L_{bt} - L_{bt\omega}^{\text{shed}} \right) \\ &= \sum_{l \in \mathbf{f}(b)} PL_{lt\omega} - \sum_{l \in \mathbf{t}(b)} PL_{lt\omega} \quad \forall b, t, \omega \quad (22) \\ PL_{lt\omega} &= (\theta_{at\omega} - \theta_{bt\omega}) / x_{ab} \qquad \forall l, t, \omega \quad (23) \\ -PL_{lt\alpha}^{\text{max}} \leq PL_{lt\omega} \leq PL_{lt\alpha}^{\text{max}} \qquad \forall l, t, \omega \quad (24) \\ 0 \leq L_{bt\omega}^{\text{shed}} \leq L_{bt} \qquad \forall b, t, \omega \quad (25) \\ \left( P_{gt\omega} + r_{gt\omega} \right) - P_{g,t-1,\omega} \leq RU_{g} \qquad \forall g, t, \omega \quad (26) \\ -P_{gt\omega} + P_{g,t-1,\omega} \leq RD_{g} \qquad \forall g, t, \omega \quad (27) \\ \sum_{g \in \mathcal{G}} r_{gt\omega} \geq P_{g}^{\min} u_{gt}^{**} \qquad \forall g, t, \omega \quad (29) \\ P_{gt\omega} + r_{gt\omega} \leq P_{g}^{\max} u_{gt}^{*} - \left( P_{g}^{\max} - SU_{g} \right) v_{gt}^{*} \quad \forall g, t, \omega \quad (30) \\ P_{gt\omega} + r_{gt\omega} \leq P_{g}^{\max} u_{gt}^{*} - \left( P_{g}^{\max} - SD_{g} \right) z_{g,t+1}^{**} \quad \forall g, t, \omega \quad (31) \end{split}$$

The sub-problem is a "max-min" bi-level problem and we can dualize the inner "min" model to obtain its equivalent "max" model based on the strong duality theory. Then, the bi-level model can be reformulated as a single "max" linear programming model. However, the dual problem is actually a large-scale optimization model, especially when the number of scenarios is large. It may significantly affect the computational performance and online applications.

Fortunately, it has been found that the second-stage bi-level "max-min" model has a special structure and thus it can be decomposed into several small sub-problems without the duality information. Since the feasible region enclosed by the second-stage variables is disjoint with the confidence set  $\Psi$ , the summation operator " $\Sigma$ " and "min" operator can be exchanged. Thus, the second-stage "max-min" problem can be formulated as

$$\max_{\pi_{\omega} \in \Psi} \sum_{\omega \in \Omega} \pi_{\omega} \min_{\substack{P_{gt\omega}, L_{bt\omega}^{shed}, \\ PL_{lt\omega}, \theta_{t\omega}, r_{gt\omega}}} \sum_{t \in \mathcal{T}} \left( \sum_{g \in \mathcal{G}} F_g(P_{gt\omega}) + \sum_{b \in \mathcal{B}} C^{LOL} L_{bt\omega}^{shed} \right) (32)$$

$$s.t. \quad (7)-(16) \qquad (33)$$
Furthermore, let  $h_{\omega} = \min_{\substack{P_{gt\omega}, L_{bt\omega}^{shed}, \\ PL_{lt\omega}, \theta_{t\omega}, r_{gt\omega}}} \sum_{t \in \mathcal{T}} \left( \sum_{g \in \mathcal{G}} F_g(P_{gt\omega}) + \sum_{b \in \mathcal{B}} C^{LOL} L_{bt\omega}^{shed} \right)$  and the model (32)-(33) becomes
$$\max_{\pi_{\omega} \in \Psi} \sum_{\omega \in \Omega} \pi_{\omega} h_{\omega} \qquad (34)$$

$$s.t. \quad h_{\omega} = \min_{\substack{P_{gt\omega}, L_{bt\omega}^{shed}, PL_{lt\omega}, \theta_{t\omega}, r_{gt\omega}}} \sum_{t \in \mathcal{T}} \left( \sum_{g \in \mathcal{G}} F_g(P_{gt\omega}) + \sum_{b \in \mathcal{B}} C^{LOL} L_{bt\omega}^{shed} \right) (35)$$

If there are  $N_s$  scenarios, the lower-level model of the bi-level problem can be decomposed into  $N_s$  independent optimization models. Especially, the feasible region  $\Psi$  for the upper level and the feasible region for the lower level are absolutely disjoint, resulting in a decoupled strategy.

For each scenario, it gives a linear programming model as

$$h_{\omega}^{k*} = \min_{\substack{P_{gt\omega}, I_{bt\omega}^{Shed}, \\ PL_{lt\omega}, \theta_{t\omega}, r_{gt\omega}}} \sum_{t \in T} \left( \sum_{g \in \mathcal{G}} F_g (P_{gt\omega}) + \sum_{b \in \mathcal{B}} C^{LOL} L_{bt\omega}^{Shed} \right) (37)$$

$$s.t. \quad (7)-(16)$$

$$(38)$$

When the optimal solution  $(h_1^{k*}, ..., h_{\omega}^{k*} ..., h_{N_s}^{k*})$  is obtained, it gives

$$\max_{\pi_{\omega} \in \Psi} \sum_{\omega \in \Omega} \pi_{\omega} h_{\omega}^{k*} \tag{39}$$

Thus, the original bi-level model can be solved by  $N_s+1$  small linear programming models, where  $N_s$  models described in (4) can be handled in parallel. The proposed method does not need to dualize the inner model when solving the bi-level sub-problem, and thus it is referred to as a duality-free decomposition method. A simple example for the "max-min" sub-problem is shown in Appendix to verify the proposed duality-free decomposition method.

### B. Master Problem

When the sub-problem is solved, an optimal value  $\vartheta(P_{gt\omega}^{k*}, L_{bt\omega}^{shed,k*}, PL_{lt\omega}^{k*}, \theta_{t\omega}^{k*}, r_{gt\omega}^{k*})$  and the worst-case probability  $(\pi_1^{k*}, ..., \pi_{\omega}^{k*} ..., \pi_{N_s}^{k*})$  are obtained. In fact, this gives an upper bound for the original model. Then, a set of extra variables  $(P_{gt\omega}^{k+1}, L_{bt\omega}^{shed,k+1}, PL_{lt\omega}^{k+1}, \theta_{t\omega}^{k+1}, r_{gt\omega}^{k+1})$  and associated constraints are generated and added into the master problem by fixing the optimal probability  $(\pi_1^{k*}, ..., \pi_{\omega}^{k*} ..., \pi_{N_s}^{k*})$  from the above model in (32)-(33).

If the sub-problem is feasible, we can create variables  $(P_{gt\omega}^{k+1}, L_{bt\omega}^{shed,k+1}, PL_{lt\omega}^{k+1}, \theta_{t\omega}^{k+1}, r_{gt\omega}^{k+1})$  and assign the following constraints to the master problem with the fixed optimal probability at the k-th iteration  $(\pi_1^{k*}, ..., \pi_{\omega}^{k*} ..., \pi_{N_s}^{k*})$ , which are called "optimality cuts".

$$\eta \geq \sum_{\omega \in \Omega} \pi_{\omega}^{k*} \sum_{t \in T} \left( \sum_{g \in \mathcal{G}} F_{g} (P_{gt\omega}^{k+1}) + \sum_{b \in \mathcal{B}} C^{LOL} L_{bt\omega}^{shed,k+1} \right) (40)$$

$$\sum_{g \in G(b)} P_{gt\omega}^{k+1} + \sum_{q \in W(b)} W_{qt\omega} - \left( L_{bt} - L_{bt\omega}^{shed,k+1} \right)$$

$$= \sum_{l \in f(b)} PL_{lt\omega}^{k+1} - \sum_{l \in t(b)} PL_{lt\omega}^{k+1} \quad \forall b, t, \omega \quad (41)$$

$$PL_{lt\omega}^{k+1} = \left( \theta_{at\omega}^{k+1} - \theta_{bt\omega}^{k+1} \right) / x_{ab} \quad \forall l, t, \omega \quad (42)$$

$$-PL_{lt}^{max} \leq PL_{lt\omega}^{k+1} \leq PL_{lt\omega}^{max} \quad \forall l, t, \omega \quad (43)$$

$$0 \leq L_{bt\omega}^{shed,k+1} \leq L_{bt} \quad \forall b, t, \omega \quad (44)$$

$$\left( P_{gt\omega}^{k+1} + r_{gt\omega} \right) - P_{g,t-1,\omega}^{k+1} \leq RU_{g} \quad \forall g, t, \omega \quad (45)$$

$$-P_{gt\omega}^{k+1} + P_{g,t-1,\omega}^{k+1} \leq RD_{g} \quad \forall g, t, \omega \quad (46)$$

$$\sum_{g \in \mathcal{G}} r_{gt\omega}^{k+1} \geq R_{t} \quad \forall t, \omega \quad (47)$$

$$\begin{split} P_{gt\omega}^{k+1} &\geq P_g^{\min} u_{gt} & \forall g,t,\omega \quad (48) \\ P_{gt\omega}^{k+1} + r_{gt\omega}^{k+1} &\leq P_g^{\max} u_{gt} - \left(P_g^{\max} - SU_g\right) v_{gt} & \forall g,t,\omega \quad (49) \\ P_{gt\omega}^{k+1} + r_{gt\omega}^{k+1} &\leq P_g^{\max} u_{gt} - \left(P_g^{\max} - SD_g\right) z_{g,t+1} & \forall g,t,\omega \quad (50) \\ \text{where } \eta \text{ is a dummy continuous variable.} \end{split}$$

If the sub-problem is infeasible, it is possible to create variables  $(P_{gt\omega}^{k+1}, L_{bt\omega}^{shed,k+1}, PL_{lt\omega}^{k+1}, \theta_{t\omega}^{k+1}, r_{gt\omega}^{k+1})$  and assign the following constraints to the master problem with the fixed optimal probability at the k-th iteration  $(\pi_1^{k*}, \dots, \pi_{\omega}^{k*}, \dots, \pi_{N_S}^{k*})$ , which is called "feasibility cuts".

$$\sum_{g \in \mathbf{G}(b)} P_{gt\omega}^{k+1} + \sum_{q \in \mathbf{W}(b)} W_{qt\omega} - \left(L_{bt} - L_{bt\omega}^{shed,k+1}\right)$$

$$= \sum_{l \in \mathbf{f}(b)} PL_{lt\omega}^{k+1} - \sum_{l \in \mathbf{t}(b)} PL_{lt\omega}^{k+1} \quad \forall b, t, \omega$$
(51)
$$(42) - (50)$$

The master problem aims to relax the original optimization model and provide a lower bound. Mathematically, it is a standard mixed integer liner program (MILP) model that can be easily dealt with by the standard commercial solvers.

Finally, for a given gap  $\varepsilon$ , the complete procedure of the duality-free decomposition method for the data-driven stochastic unit commitment problem can be described as

Step 1: Let  $LB = -\infty$ ,  $UB = +\infty$ , K = 0;

**Step 2: Solve the master problem model:** 

$$\min \sum_{t \in \mathcal{T}} \sum_{g \in \mathcal{G}} \left( C_g^{NL} u_{gt} + \sum_{s \in \mathcal{S}_g} C_{gs}^{SU} \delta_{gst} + C_g^{SD} \mathbf{z}_{gt} \right) + \eta \quad (53)$$
s.t. (3)-(7) (54)
$$(40)-(50) \qquad k=1,...,K \qquad (55)$$

Solve the above model and derive the optimal solution (  $u_{gt}^*, v_{gt}^*, \delta_{gst}^*, z_{gt}^*, \eta^*; P_{gt\omega}^{1*}, L_{bt\omega}^{shed,1*}, PL_{lt\omega}^{1*}, \theta_{t\omega}^{1*}, r_{gt\omega}^{1*}; ...; P_{gt\omega}^{K*}, L_{bt\omega}^{shed,K*}, PL_{lt\omega}^{K*}, \theta_{t\omega}^{K*}, r_{gt\omega}^{K*})$  as well as the optimal objective value  $O^{K*}$ . Then, update the lower bound as  $LB = O^{K*}$ ;

Step 3: Fix  $(u_{gt}^*, v_{gt}^*, \delta_{gst}^*, z_{gt}^*)$  and solve the sub-problem model in parallel by (37)-(39), respectively. If the sub-problem is feasible, let the optimal objective value be  $\vartheta^*$ ; otherwise set  $\vartheta^* = +\infty$ . Furthermore, update the upper bound as  $UB = \min\{UB, \sum_{t \in \mathcal{T}} \sum_{g \in \mathcal{G}} \left(C_g^{NL} u_{gt}^* + \sum_{s \in \mathcal{S}_g} C_{gs}^{SU} \delta_{gst}^* + C_g^{SD} z_{gt}^*\right) + \vartheta^*\}$ ;

Step 4: If  $(UB-LB) \le \varepsilon$ , return  $(u_{gt}^*, v_{gt}^*, \delta_{gst}^*, z_{gt}^*)$  and stop. Otherwise, add the cuts as

- (a) If the sub-problem in Step 3 is feasible, obtain the optimal probability  $(\pi_1^{k*},...,\pi_{\omega}^{k*}...,\pi_{N_s}^{k*})$ . Create variables  $(P_{gt\omega}^{k+1},L_{bt\omega}^{shed,k+1},PL_{tt\omega}^{k+1},\theta_{t\omega}^{k+1},r_{gt\omega}^{k+1})$  and assign the constraints (40)-(50) to the master problem;
- (b) If the sub-problem in Step 3 is infeasible, create variables  $(P_{gt\omega}^{k+1}, L_{bt\omega}^{shed,k+1}, PL_{lt\omega}^{k+1}, \theta_{t\omega}^{k+1}, r_{gt\omega}^{k+1})$  and add the constraints (51)-(52) to the master problem;

Step 5: Update K=K+1 and go back to Step 2.

#### V. NUMERICAL ANALYSIS

In this section, three unit commitment models with wind power generation uncertainties are designed and compared with the proposed data-driven stochastic SCUC model (DSSCUC):

- WSSCUC: It is a worst-case stochastic SCUC model. Solve the general stochastic SCUC model (1)-(16) and fix the first-stage decision variables. Then, we randomly generate 1000 different probabilities from the confidence set and solve the second-stage problem for each given probability. Then, choose the solution with the maximum objective value is served as the worst-case scenario for the stochastic approaches.
- RSCUC: It is a two-stage robust SCUC model. Using the historical data, we can give the uncertainty set of robust optimization with respect to central limit theorem.
- SSCUC: It is a two-stage stochastic SCUC model.

The computation is carried on a computer with an Intel® Core<sup>TM</sup> i7 Duo Processor (2.4 GHz) and 4-GB RAM in MATLAB by the CPLEX 12.6 commercial solver. It should be noted that the series of sub-problems in the proposed method have independent mathematical structures, enabling the parallel computation. Due to the lack of hard-ware platform of high-performance computing, we use the "for" loop to simulate the parallel computation and take the worst computing time of the sub-problems as the parallel computational time.

#### A. Test on the IEEE 118-bus System

At first, the proposed duality-free decomposition based DSSCUC is studied on the IEEE 118-bus test system including 54 generators and 186 transmission lines [47]. The spinning reserve requirement is equal to 5% of the load demand. The cost of load shedding is \$3500/MWh. Five 300-MW wind farms are located at bus #10, #25, #26, #37, and #38. Here, the historical wind data from the real-life wind farms in Northwestern China is used, as shown in Figs. 1-3.

The comparison of the three methods is presented in Table I with  $N_s = 5$ . It is obvious that the RSCUC model optimizes the solution that is immune against all the possible realizations, which leads to the highest optimal total cost. The SSCUC method considers the probability of scenarios, which therefore yields the lowest optimal total cost. In contrast, the proposed DSSCUC model using either  $\beta_{\Psi_1}$  or  $\beta_{\Psi_{\infty}}$  is greater than the SSCUC, while smaller than the WSSCUC approach. When  $\beta$  is large enough, the solution will tend to that of the RSUCU model. On the contrary, when  $\beta$  is small, the solution will approach that of the SSUCU model. The DSSCUC model is between RSCUC and SSCUC. As a result,  $\beta$  can be considered as a budget parameter that can control the size of uncertainty sets and further a trade-off between the robust and stochastic optimization can be made. With the increase of  $\beta$ , the uncertainty set becomes larger and the optimal solution is more conservative.

Moreover, the worst-case total cost from the stochastic approach is computed by the WSSCUC model considering uncertain probability distribution of about 9.5%~17.2% larger than the traditional two-stage SCUC model. It is obvious that a larger confidence level  $\alpha$  will enlarge the confidence set (i.e.,  $\beta$  becomes large), and the worst-case solution will thus become

larger. The results suggest that the traditional SSCUC model suffers from the uncertain probability distribution of wind power. However, the proposed DSSCUC model takes into account the uncertainty from the statistics, so the solution will be benefited.

Finally, the stochastic SCUC models including the SSCUC, WSSCUC and DSSCUC models are always better than the robust SCUC model. This is because the robust optimization neglects the probability of scenarios and the probability of the worst-case scenario may be very small in practice. Thus, the extreme worst case will sacrifice much cost (about 24%) to protect the system from the worst case with small probabilities. In the framework of the two-stage stochastic optimization, the expected total cost is optimized which gives the optimal solution under the given probability distribution.

Table I. Performance of Different SCUC Models.

	Total cost/10 <sup>6</sup> \$					
$\alpha$	DSSCUC		RSCUC	SSCUC	WSSCUC	
	$\psi_1$	$\psi_{\mathrm{inf}}$	KSCUC	SSCUC	Wascuc	
0.5	1.5167	1.5035			1.6288	
0.6	1.5331	1.5201			1.6391	
0.7	1.5502	1.5496			1.6536	
0.8	1.5795	1.5732	1.8453	1.4871	1.6712	
0.9	1.6111	1.5943			1.6934	
0.95	1.6348	1.6132			1.7158	
0.99	1.6584	1.6380			1.7433	

In order to investigate the influence of the load demand and wind power output on the solution decision, we consider four seasons to study where a typical day is selected in each season. In spring, the wind power is high and the load demand is low. In summer, the wind power is low and the load demand is high. In autumn, both the wind power and load demand are low. In winter, both the wind power and load demand are high. The solutions are presented in Table II. Observations show that the total cost in spring is the lowest and the solution in summer is the highest. More importantly, the gap between DSSCUC and other methods is small when the wind power output is low, whereas it is large in the case of a high penetration of wind power.

Furthermore, the proposed duality-free decomposition method (PM) and the traditional Benders decomposition method (TM) in [39] were explicitly compared considering scenarios and the results can be found in Table III. It can be observed that for the same  $N_s$ , the PM and TM generate the same objective value (obj.). In contrast, the PM preforms an order of magnitude faster than the TM. This is because the PM needs 2-4 iterations for convergence, whereas the TM needs 9-15 iterations. Moreover, the PM yields a decomposition structure for the second-stage problem that can be handled in parallel, which can significantly reduce the computational time, especially for the problem with a large number of scenarios.

Table II. Impact of Seasons on Different SCUC Models.

	Total cost/10 <sup>6</sup> \$						
Seasons	DSSCUC		RSCUC	SSCUC	WSSCUC		
	$\psi_1$	$\psi_{\mathrm{inf}}$	KSCUC	SSCOC	WSSCUC		
Spring	1.6348	1.6132	1.8453	1.4871	1.7158		
Summer	2.4045	2.3895	2.5101	2.3347	2.4690		
Autumn	2.0832	2.0787	2.1576	2.0333	2.1112		

|--|

Table III. Comparison of the traditional and proposed methods

	<i>D</i> -1				D-inf			
$N_s$	Obj. (10 <sup>6</sup> \$)		Time (min)		Obj. (10 <sup>6</sup> \$)		Time (min)	
	TM	PM	TM	PM	TM	PM	TM	PM
5	1.63	1.63	36	4	1.61	1.61	34	5
10	1.58	1.58	44	4	1.55	1.55	43	5
15	1.56	1.56	53	4	1.51	1.51	57	6
20	1.55	1.55	75	5	1.50	1.50	81	9
25	1.54	1.54	90	6	1.49	1.49	103	11

Moreover, the comparison of computational performance among the three approaches is shown in Table IV. The SSCUC is a standard MILP that can be directly handled by CPLEX. However, the computational time increases significantly with a large number of scenarios. This is because the SSCUC model contains  $N_s$  sets of decision variables and constraints. The RSUCU approach needs 7 iterations while the challenge is in the inner bi-level "max-min" problem, where a large-scale MILP is performed by the use of duality. In addition, the computational time of the SSUCU will increase significantly when the number of scenarios is increased. Among the three methods, the proposed DSSCUC model consumes the least computational time due to the duality-free decomposition method, where the second-stage "max-min" problem is decomposed into several small-scale linear programs that are handled in parallel. It should be noted that the increase of  $N_s$ will increase its computational time. The reason is that the master problem will become larger with a large number of scenarios.

Table IV. Comparison of computational efficiency by three methods on 118-bus test system (min).

M	DSSCUC		RSCUC	SSCUC	
1 V S	D-inf	D-1	RSCOC	SSCOC	
5	4	5		12	
10	4	5		19	
15	4	6	10	29	
20	5	9		47	
25	6	11		78	

#### B. Test on the Practical Hainan Power Grid in China

To verify the proposed method on a large-scale test system, the Hainan power grid in China is used, which is depicted in Fig. 5. This power grid contains 82 generators with the total capacity being 5300 MW, 7 wind farms with the total capacity being 800 MW, and the load demand is 4200 MW. The transmission network is operated on two voltage levels, i.e., 220 kV and 500 kV, where there are 34 high-voltage substations and 404 transmission corridors.

The per unit values of the forecasted load demand and wind power generation over 24 hours are shown in Fig. 6, which are defined by  $P^t/P^0$ . Here,  $P^t$  is the value at the time period t and  $P^0$  is the value at 1:00 AM. We consider the true wind power follows a multivariate normal distribution with the variance equivalent to 1/3 of the forecasted value. Furthermore, 1000 samples are generated as the set of the historical data. The sensitivity analysis of parameters on the four models is presented in Table V. For each group, we consider four points

for comparison. The results reveal that with the increase of the number of scenarios  $N_s$  and confidence level  $\alpha$  and with the decrease of the number of historical data K, the total cost will become larger since the uncertainty set becomes larger. Thus, it is suggested that for a given confidence level and the number of scenarios, more historical data can narrow the region of the uncertainty set and reduce the conservativeness. Similarly, for a given number of scenarios and historical data, improving the confidence level indicates that the system requires higher estimation precision for the possible probability distributions. In that case, the confidence set and the uncertainty set become larger. Moreover, it can be observed in Fig. 7 that the gap between WSSCUC and DSSCUC will become smaller if  $\alpha$  and K are increased while decreasing  $N_s$ .

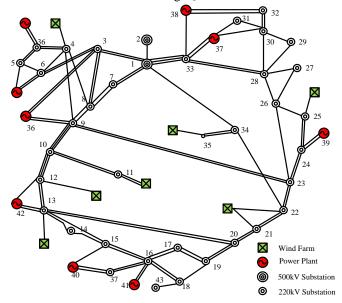


Fig. 5. Layout of the Hainan power grid in China.

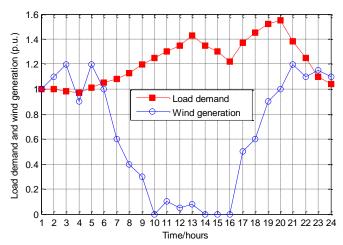


Fig. 6. Load demand and wind generation over 24 hours

Finally, the computational performance among the three approaches on the Hainan power grid is shown in Table VI. The comparison demonstrates that the simulation results in Table IV are similar to those in Table VI. The computational time increases significantly with a large number of scenarios. As for the MILP problem, the computational time mainly depends on

the number of variables and constraints. If  $N_s = 25$ , the traditional method cannot find the optimal solution within 1000 minutes. If  $N_s = 50$ , the number of variables is more than one million and the number of constraints are more than five millions. Hence, the traditional method for the DSSCUC cannot be solved due to the limited memory space. In contrast, the proposed duality-free decomposition based method can still handle the DSSCUC and the computational speed is improved up to two orders of magnitudes, since the large-scale problem is decomposed into several small-scale sub-problems.

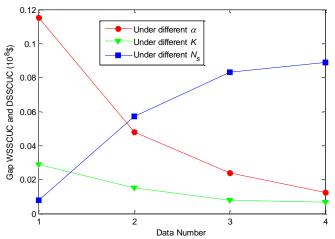


Fig. 7. Gap between WSSCUC and DSSCUC.

Table V. Sensitivity analysis of parameters

	The state of parameters							
$\alpha$			Total cost/	Total cost/10 <sup>8</sup> \$				
(K=1000	DSSCUC		RSCUC	SSCUC	WSSCUC			
$N_s = 10$ )	$\psi_1$	$\psi_{\mathrm{inf}}$	RSCOC	33000	WSSCOC			
0.5	3.5629	3.5432			3.6783			
0.90	3.6649	3.6513	4.5158	3.2494	3.7130			
0.95	3.7031	3.6943	4.3136	3.2494	3.7271			
0.99	3.7806	3.7745			3.7932			
K			Total cost/	10 <sup>8</sup> \$				
$(\alpha = 0.95)$	DSS	CUC	RSCUC	SSCUC	WSSCUC			
$N_s = 10$ )	$\psi_1$	$\psi_{\mathrm{inf}}$	KSCUC		WSSCUC			
1000	3.7031	3.6619		3.2494	3.7321			
3000	3.4313	3.4106	4.5158		3.4465			
6000	3.3586	3.3417	4.3136		3.3663			
10000	3.2989	3.2833			3.3056			
$N_s$			Total cost/10 <sup>8</sup> \$					
$(\alpha = 0.95)$	DSSCUC		RSCUC	SSCUC	WSSCUC			
<i>K</i> =1000)	$\psi_1$	$\psi_{\mathrm{inf}}$	RSCOC	SSCOC	WSSCUC			
5	3.4854	3.341			3.4933			
10	3.7031	3.562	4.5158	3.2494	3.7603			
25	4.0515	3.918	4.5156		4.1345			
50	4.3054	4.195			4.3942			

Table VI. Comparison of computational efficiency by three methods on Hainan power grid in China (min).

$N_s$	DSCUC		RSCUC	SSCUC	
	TM	PM	RSCOC	33000	
5	92	12		34	
10	342	12		78	
25	>1000	13	78	375	
50	out of memory	13		>1000	
100	out of memory	15		out of memory	

#### **CONCLUSIONS**

To address the uncertain probability distribution of wind power resultant from the historical data, a data-driven stochastic security-constrained unit commitment was set up to optimize the unit commitment under the worst probability distribution in this paper. Furthermore, a novel duality-free decomposition method was proposed for the data-driven stochastic security-constrained unit commitment. The key point is that the second-stage sub-problem has a special structure that can be decomposed into several parallel sub-problems without the duality information. However, it is required by the traditional Bender's decomposition method. Numerical results have shown that the proposed method performs better than the Benders decomposition method especially for the problem with a large number of scenarios.

#### **APPENDIX**

### A Simple Example for the Sub-problem

In order to verify the proposed duality-free decomposition method, we set up a simple example with two variables  $(x_1, x_2)$ under three scenarios to show the detail numerical results. The bi-level sub-problem is formulated as

$$\max_{p_1, p_2, p_3} \min_{x_1, x_2} \left(2x_1^1 + 3x_2^1\right) p_1 + \left(2x_1^2 + 3x_2^2\right) p_2 + \left(2x_1^3 + 3x_2^3\right) p_3 \text{ (A1)}$$

s.t. 
$$x_1^1 + x_2^1 = 1$$
,  $x_1^2 + x_2^2 = 2$ ,  $x_1^3 + x_2^3 = 3$   
 $x_1^1, x_1^1, x_1^2, x_2^2, x_1^3, x_2^3 \ge 0$  (A2)

$$p_1 \in [0.1, 0.3], \ p_2 \in [0.4, 0.7], \ p_3 \in [0.2, 0.6],$$
 
$$p_1 + p_2 + p_3 = 1 \tag{A3}$$

Traditional method dualizes the inner "min" model to obtain its equivalent "max" model based on the strong duality theory. Then, the bi-level model can be reformulated as a single "max" linear programming model, such that

$$\max_{\lambda_1, \mu_2, \mu_3, \lambda_4, \lambda_5, \lambda_5} \lambda_1 + 2\lambda_2 + 3\lambda_3 \tag{A4}$$

s.t. 
$$\lambda_1 \leq 2p_1$$
,  $\lambda_1 \leq 3p_1$ ,  $\lambda_2 \leq 2p_2$ ,  $\lambda_2 \leq 3p_2$ ,  $\lambda_3 \leq 2p_3$ ,  $\lambda_3 \leq 3p_3$  (A5)

$$p_1 \in [0.1, 0.3], \ p_2 \in [0.4, 0.7], \ p_3 \in [0.2, 0.6],$$
 
$$p_1 + p_2 + p_3 = 1 \tag{A6}$$

where  $\lambda_1$ ,  $\lambda_2$  and  $\lambda_3$  are multipliers to the constraints (A2). It can be found that the above optimization model is a simple linear problem that can be solved to the global optimal solution with  $(p_1=0.1, p_2=0.4, p_3=0.5, \lambda_1=0.2, \lambda_2=0.8, \lambda_3=1.0)$  and the optimal objective value is 4.8.

For the proposed duality-free decomposition method, we can solve three small models by (37)-(38) in parallel, such that

$$\min_{\substack{x_1^1, x_2^1 \\ s.t.}} 2x_1^1 + 3x_2^1$$
 (A7-a)  
s.t.  $x_1^1 + x_2^1 = 1, x_1^1, x_2^1 \ge 0$  (A7-b)

s.t. 
$$x_1^1 + x_2^1 = 1$$
,  $x_1^1, x_2^1 \ge 0$  (A7-b)

The global optimal solution is  $(x_1^1 = 1, x_2^1 = 0)$  and the optimal objective value is  $h_1$ =2.

$$\min_{\substack{x_1^2, x_2^2 \\ x_1^2 = x_2^2}} 2x_1^2 + 3x_2^2 \tag{A8-a}$$

s.t. 
$$x_1^2 + x_2^2 = 2$$
,  $x_1^2, x_2^2 \ge 0$  (A8-b)

The global optimal solution is  $(x_1^2 = 2, x_2^2 = 0)$  and the optimal objective value is  $h_2$ =4.

$$\min_{x_1^3, x_2^3} 2x_1^3 + 3x_2^3$$
(A9-a)
$$s.t. \quad x_1^3 + x_2^3 = 3, \ x_1^3, x_2^3 \ge 0$$
(A9-b)

s.t. 
$$x_1^3 + x_2^3 = 3$$
,  $x_1^3, x_2^3 \ge 0$  (A9-b)

The global optimal solution is  $(x_1^3 = 3, x_2^3 = 0)$  and the optimal objective value is  $h_3$ =6.

Furthermore, we solve another small linear program by (39), using the information from (A7)-(A9), such that

$$\max_{p_1, p_2, p_3} h_1 p_1 + h_2 p_2 + h_3 p_3 \tag{A10-a}$$

s.t. 
$$p_1 \in [0.1, 0.3], p_2 \in [0.4, 0.7], p_3 \in [0.2, 0.6],$$
  
 $p_1 + p_2 + p_3 = 1$  (A10-b)

The optimal solution of the above model is  $(p_1=0.1, p_2=0.4,$  $p_3$ =0.5) and the optimal objective value is 4.8, which is the same as the traditional method.

It can be concluded that the optimal solution and optimal objective value by the proposed method is absolutely the same as those by the traditional method, which verifies the effectiveness of the proposed method. Moreover, it can be observed that the models (A7), (A8) and (A9) are independent that can be solved in parallel. Besides, the proposed model only needs to solve 4 small linear programs comparing to the traditional method that needs to solve one large-scale optimization model.

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