Real-Time Supervisory Control for Power Quality Improvement of Multi-Area Microgrids

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Abstract—In this paper, the power quality (PQ) improvement of multi-area microgrids (MAMGs) is addressed. To this aim, mitigation of voltage harmonics and unbalance is considered by using distributed generators (DGs) and active power filters (APFs) in a proper way. As a novel approach, the main goal of the proposed method is to pick out redundant APFs and/or significantly reduce of DGs and APFs compensation workload by making collaboration between areas toward integrated PQ improvement of the MAMG. To achieve the desired PQ indices of different areas, supervisory control is planned for proper utilization of available compensators in time. By supervisory control, harmonic propagation between areas and the system unbalance are dealt with and systemic PQ improvement of the MAMG is provided. To this aim, scheduling framework is used to track the PQ situation of each area. Evaluation of the proposed control is carried out by a comprehensive simulation study in MATLAB/Simulink.

Index Terms—Active power filter (APF), distributed generator (DG), multi-area microgrid (MAMG), real-time power quality (PQ) tracking, supervisory control (SC), voltage unbalance/harmonic compensation.

I. INTRODUCTION

Ombination of distributed generators (DGs), energy storage systems, and loads in a small-scale grid forms a microgrid (MG). MGs may operate connected to the main grid (grid-connected) or isolated from that (islanded). As multifunctional converters, DGs interface converters can be controlled to supply power and improve power quality (PQ).

Among many strategies proposed for voltage harmonic and unbalance compensation of the MG by proper control of DGs converters, some of them consider common point (CP) of loads or sensitive load bus and some others address the quality of DGs terminal [1]–[11] (a brief explanation of some approaches is discussed in [8]). However, PQ of other points except for the considered point might become distorted severely by these methods. In general, if voltage compensation occurs locally, the other points except for the considered compensating point might be distorted. This phenomenon is known as “whack a mole” [12]. Voltage distortion at DGs terminal might damage some consumers in electrical proximity of those areas so PQ improvement of both DGs terminal and CPs should be attended. Using active power filters (APFs) for PQ improvement is the subject of many research works, e.g., [13]–[26]. Simply, shunt APFs (which are much more popular than series one) inject proper harmonic and/or fundamental negative sequence current in the opposite phase of the undesired part of line current to cancel current distortion and consequently voltage harmonics and/or unbalance, respectively. However, based on the APF compensation effort, voltage quality at the points except for the APF installation point might be degraded [12]. To simultaneously compensate voltage harmonics of CP and DGs buses, DGs and APFs are used in a coordinated way in [8], while DGs inverters rated power is also considered in a compensation procedure. In [8], it is tried to reduce APFs rating in a construction phase of a new single-area MG.

With the exponential growth of distributed energy resources, the MG is becoming a multidirectional network interconnecting a vast range of consuming devices. As an effective approach to increase reliability and decrease dependence on energy storage systems, larger scale MGs interconnecting more DGs are recommended, since by extension of power sharing between DGs, it would be possible alleviation of the problems created due to unreliable renewable energy resources. Accordingly, PQ issue of such a wide system needs to be attended more since the PQ situation of a certain point (or area) might significantly affect the other points (or areas) PQ level due to harmonic propagation [27], [28]. Few literature works address the PQ of larger scale power systems [29]–[31]. For example, in [29], a double-resistive APF is proposed to attenuate voltage harmonics and suppress harmonic propagation in radial power systems respectively installed at the end feeder and at a specific place determined based on PQ concerns. The proposed method in [29] is not applicable in interconnected power systems. In [30], a long-feeder simulator-based APF is proposed to reduce harmonic propagation in closed-loop distribution feeders. The proposed APF is recommended to be installed at the middle electrical point of the system. Likewise, the proposed method in [30] cannot be used in interconnected power systems. In [31], an optimal utilization of DGs inverters (as compensators) is proposed. Taking into account the available capacity of each inverter, to utilize inverters toward harmonic suppression as
far as possible, a double-objective optimization approach is considered in [31]. Obviously, there would be no (or weak) compensation in case DGs are operated in full operation or renewable energy is unavailable.

Yet, integrated PQ improvement of larger scale power systems (regardless to topology) is not achievable in [29]–[31] since harmonic propagation is dependent on some uncertain factors such as loading condition and distribution lines [30]. As a result, there is no guarantee that all PQ indices of different points of a multi-area MG (MAMG) are tracked during the time. In other words, continuous PQ improvement of the MAMG, which is divisible based on PQ requirement of each area, as a unified system has not been addressed so far.

In line with previous efforts toward simultaneous PQ improvement of DGs terminal and CPs, the present paper’s contributions can be listed as follows.

1) PQ improvement under the existing unbalance-nonlinear load condition.

2) PQ improvement of the interconnected MAMG while areas are distinguished by their PQ requirements. As a novel approach, the proposed strategy is implementable in any topology of power systems.

3) The proposed strategy can be implemented either in a construction phase of a new MAMG or for operation of an established MAMG. The proposed method is able to increase the efficiency of APF placement that might carry out in the construction phase of the MAMG. In addition, the proposed method can be used to improve the PQ of new sensitive load buses (or CPs) without installation of a new APF in the respective buses in an established MAMG. It is because integrated PQ improvement of the MAMG is addressed utilizing available compensators.

4) Taking into consideration the loading condition of areas in a PQ improvement process so that the MAMG is improved by the least number of available compensators. Due to harmonic propagation and mutual effects of unbalances between areas, the loading condition of each area is of great importance and this concern is addressed by using a scheduling framework in the proposed method.

Noteworthy to mention that the paper approach can be considered as a further step to the previous work [8] specialized for the MAMG that is a different scenario, entirely.

In what follows, the general scheme of the proposed control and CP compensation by DGs and APFs are described in Section II. Section III is dedicated to the proposed supervisory control (SC). Simulation study is provided in Section IV, and the paper is concluded in Section V.

II. GENERAL SCHEME OF THE PROPOSED CONTROL

Fig. 1 illustrates an interconnected MAMG and the general structure of the proposed control. The areas of the MAMG are connected by interarea lines and each area might contain several DGs, APF, and a variety of loads (including linear, nonlinear, unbalanced, and unbalance-nonlinear loads). The subscript $ij$ represents the $j$th power component in the $i$th area. Two points are represented in each area with subscripts $T_{ij}$.

![Fig. 1. General scheme of the proposed control. (a) Power stage. (b) Control stage.](image)

(DG$_{ij}$ terminal) and CP$_i$ as the coupling point of areas where there might be high amount of loads including sensitive loads. In Fig. 1, voltage distortion rate (VDR) might be a collection of voltage unbalance factor (VUF), voltage total harmonic distortion (THD), and voltage individual harmonic distortion (VHD) including both positive and negative sequences of harmonic components. By remote terminal units, $i_{APF}$ and VDR of all areas are calculated by the following equations [12]:

$$VHD = \sqrt{\frac{\sum_{h=2}^{\infty} V_h^2}{V_1^{rms} o\alpha}}, \quad VUF = \frac{V_{1+}^{rms} o\alpha}}{V_{1-}^{rms} o\alpha}, \quad THD = \frac{1}{V_1} \sqrt{\frac{\sum_{h=2}^{\infty} V_h^2}{V_1^2}} = 1 + \sqrt{V_{d}^2 + V_{q}^2}$$

$$i_{APF} = \sqrt{(i_{f,dq}^{1+})^2 + \sum_{h=3,5,7} (i_{f,dq}^{h+})^2}$$

where $V_{1+}^{rms} o\alpha}$, $V_{1-}^{rms} o\alpha}$, and $V_{h+}^{rms} o\alpha}$ are fundamental positive sequence, fundamental negative sequence, and $h$th harmonic components (positive and negative sequences) of voltage rms ($o\alpha$-axis in a stationary framework), respectively. $V_{d}$ and $V_{q}$ are oscillatory components of voltage in the $d$- and $q$-axis, respectively, and $V_1$ is the rms value of phase voltage (fundamental component). Finally, $i_{f,dq}^{1+}$ and $i_{f,dq}^{h+}$ are fundamental negative
sequence and harmonic components of the filter output current in the \(dq\) framework. Thereafter, the VDR of \(CP_i\) and \(T_{ij}\) is, respectively, represented by \(VDR_{CP_i}\) and \(VDR_{T_{ij}}\).

\(VDR_{CP_i}\) is recommended to be pretty low to provide high quality of power for high amount of sensitive loads and reduce harmonic propagation between areas. Meanwhile, satisfactory \(VDR_{T_{ij}}\) should be considered based on the PQ indices determined by the sensitivity of the loads located close to DGs terminals.

SC is used to suppress VDR of the MAMG by proper exploitation and management of DGs and APFs so that the least number of them are used. Beside power sharing, the commands from SC put into effect using operational control. Operational control consists of DGs and APFs control stages. Comprehensive details corresponding to the control stage of DGs and APFs are available in [7], [8], and [14]. Yet, CP compensation of each area might be carried out by the cooperation of respective DGs and APFs.

Fig. 2 shows the equivalent circuit of a typical area from compensation point of view. DGs, as voltage-controlled voltage source inverters, and APFs, as current-controlled current source inverters, try to compensate CP. \(V_{VDR_{CP_i}}\) and \(V_{VDR_{T_{ij}}}\) (voltage distortion components at \(CP_i\) and \(T_{ij}\), respectively) should be compensated. For instance, the negative sequence of the third harmonic component of \(CP_i\) voltage might be considered as \(V_{VDR_{CP_i}}\).

\[ V_{VDR_{CP_i}} = V_{VDR_{T_{ij}}} - V_{Load} \]  

\[ V_{VDR_{CP_i}} = \frac{i_s - Y_{eq}}{Y_{Load} \cdot Y_{Line}} \]  

\[ V_{VDR_{CP_i}} = i_s + i_f \]

Using the above-mentioned equations, the following equation can be easily derived:

\[ (V_{VDR_{CP_i}} - V_{VDR_{T_{ij}}}) \cdot Y_{Load} = (1 + K) \cdot i_L - K \cdot i_f \]  

where \(K = Y_{Load} / Y_{Line}\). In addition, the following function can be applied for DGs and APF:

\[ V_{VDR_{T_{ij}}} = G_{DG} \cdot (-V_{VDR_{CP_i}}) \]  

\[ i_f = G_{APF} \cdot i_L \]

where \(G_{DG}\) and \(G_{APF}\) are, respectively, compensation gain of DG and APF. Replacing (8) and (9) into (7), the following equation is achieved:

\[ (G_{DG} + 1) \cdot V_{VDR_{CP_i}} = (1 + K - K \cdot G_{APF} \cdot V_{Load} \cdot Y_{Line}) \]  

where \(V_{Load} = i_L / Y_{Load}\).

Normally, \(Y_{Line} \gg Y_{Load}\) (or \(K \ll 1\)) [5]. Thus, \(K\) is negligible in comparison with 1 and the following equation can be achieved with a good accuracy:

\[ (G_{DG} + 1) \cdot \frac{V_{VDR_{CP_i}}}{V_{Load}} = (1 - K \cdot G_{APF}) \]  

\[ G_{DG} = \frac{V_{VDR_{CP_i}}}{V_{Load}} \]  

\[ G_{APF} = \frac{V_{VDR_{CP_i}}}{V_{Load}} \]  

In (11), the term \(V_{VDR_{CP_i}} / V_{Load}\) results VDR\(_{CP}\). Based on (11), Fig. 3 illustrates CP compensation by DG and APF. When \(G_{DG} = 0\), compensation is only carried out by the APF, and when \(G_{APF} = 0\), compensation is merely carried out by the DG. VDR\(_{CP}\) is attenuated when DG or APF compensation gain is increased. Hereby, it can be induced that the vertical axis of Fig. 3 is the compensation rate of CP.

As mentioned before, CP compensation might be carried out by so called the “cooperation” of DGs and APF. To better illustrate the cooperation, another interpretation of (11) is represented in Fig. 4. In this figure, compensation gain of CP by DG and APF is shown in per unit. In other words, DG and APF compensation gains are theatrically normalized based on their maximum values. Hereby, it would be possible assuming a general relationship between compensation effort and the percentage of VDR. This way, complete compensation can be estimated as VDR = 0%; likewise no compensation can be
estimated as \( VDR = 100\% \). It should be mentioned that these estimations are helpful for better realization of the cooperation although they are achieved by general assumptions.

Briefly, based on the cooperation principle, CP compensation rate is properly shared between DG and APF while DG is prior to APF. The sharing ratio is determined according to \( VDR_{CP}^{-} \). Typically, if 60\% of complete compensation (reducing \( VDR_{CP} \) to zero) is determined to yield the PQ indices of \( CP_{i} \) (\( VDR_{CP_{i},ref} \)), based on the cooperation principle, it might be shared between APF and DG by the ratio of 1:3 (red lines in Fig. 4). For instance, considering \( VDR_{CP_{i},ref} = THD_{CP_{i},ref} = 5\% \), to reduce \( THDCP_{i} \) from the current value to 5\%, the required compensation effort, e.g., 0.8 p.u., might be shared between DG and APF by the ratio of 1:1.67 (blue lines in Fig. 4). Anyway, APF, and DG\(_{ij} \) compensation gains are assigned as \( S_{i}^{m,±1} \) and \( G_{ij}^{m,±1} \), respectively [8].

III. PROPOSED SUPERVISORY CONTROL

Generally speaking, SC manages the compensation process so that PQ indices of all \( T_{ij} \) and CPs of the MAMG are achieved by the least number of DGs and APFs when redundant compensators are picked out. In other words, based on loading condition and VDR of different points of the MAMG, SC provides a proper arrangement of available compensators to suppress VDR and obtain PQ indices so that no extra compensator is operated. It means that the arrangement is set in accordance with the VDR of the MAMG.

Note that the scenario here is completely different from a single-area MG since there are multiple areas connected together; therefore, PQ improvement of each area might significantly affect other areas’ PQ level [12], as shown in Section IV. Simply, SC responsibility is to get benefit from this effect and cause further reduction in the number of the compensators operating in time. Remember that the first reduction is achieved by the cooperation between DG(s) and APF of each area. To meet SC contribution and track load changes (\( VDR_{T_{ij}} \), \( VDR_{CP_{i}} \)) of all areas, the paper approach is to implement SC in a time-series-based model (so called “scheduling framework”), as represented in Fig. 5 [32].

According to Fig. 5, SC can be operated in two modes: CP compensation mode (PCM) and \( T_{ij} \) compensation mode (TCM). Note that these modes take place in a series while the PCM is prior to the TCM. In other words, primarily SC improves all CPs, then it deals with \( T_{ij} \) when all CPs meet specified PQ indices.

A. SC in the PCM

As shown in Fig. 1, the data acquired by remote terminal units are transferred to SC by a low-bandwidth communication network. Fig. 6 shows SC in the PCM. First, all \( VDR_{CP_{i}} \) are compared with the reference value. Noteworthy that PQ indices of all CPs are set to the same value to make effective collaboration between areas. The reference PQ indices might be set based on the most sensitive CP; however, high level of PQ is preferred for CPs to achieve more efficient collaboration. Then, the errors \( e_{CP_{i}} \) are fed to the detection block. The following simple if-else loop function is considered in this block:

\[
\text{For } i = 1: m; \text{ For } j = 1: m \text{ if } j \neq i \text{ then } \\
\quad \text{if } e_{CP_{i}} > e_{CP_{j}} ; B_{i} = 1; \\
\text{else: } B_{i} = 0; \text{ break; End;}
\]

End \( (F1) \)

where \( m \) is the number of areas.

Based on F1, the area with the highest \( VDR_{CP_{i}} \) is detected, then the command signal \( B_{i} = 1 \) is specified for that area. Note that other areas’ respective signals are \( B_{j} = 0 \). It means that the CP compensation of those areas is not initiated yet. The signals are multiplied with the respective DGs and APF compensation gains generated by the cooperation (i.e., \( S_{i}^{m,±1} \) and \( G_{ij}^{m,±1} \)). The final gains are represented as \( D_{ij}^{m,±1} \) (DG\(_{ij} \) compensation gain) and \( F_{ij}^{m,±1} \) (APF\(_{ij} \) compensation gain) in Figs. 1 and 6. The new gains are transferred to operational control. As shown in Fig. 6, SC regenerates the commands during time. In other words, after each time period, the signals \( D_{ij}^{m,±1} \) and \( F_{ij}^{m,±1} \) are regenerated and sent to the operational control (see Fig. 1), meaning that the next area starts to compensate respective CP if it is needed. By this policy, SC in the PCM meets its obligation that is reducing compensators rating. In fact, PQ improvement of the considered area can significantly reduce the workload of the compensators in other areas. Consequently, in comparison with a conventional strategy that the compensators of the power system are individually operated merely based on the VDR of an installation point, there might be some spare compensators by this workload reduction. Using the proposed SC, the redundant compensators are automatically picked out from a compensation process. In addition, it is planned in SC shutting down of low operating APFs and transferring their compensation burden to other APFs (in the other areas) operating in normal operation. It results in further reduction in the applied compensators (more details are discussed below). That is why we say “collaboration” between areas.

The dead band block in Fig. 6 is for removing compensated CPs from the loop and prohibiting CP compensation of those areas with no violation from \( VDR_{CP_{i},ref} \). Furthermore, operation
of SC in the PCM terminates when all CPs meet specified PQ indices. In further details, in case of no violation of the indices from the beginning, SC in the PCM would be bypassed (due to the dead band). In that case, according to the cooperation principles, CP compensation might be carried out only by DGs.

Considering all possible cases, if we have significant increase at \( \text{VDR}_{CP} \) due to nonlinear load increase, an additional area might join to the compensation process according to PCM control function (F1). In this case, other areas’ collaboration had not been sufficient to meet \( \text{VDR}_{CP,ref} \). On the other hand, in case of decreasing \( \text{VDR}_{CP} \), there might be a decrease in compensators rating as explained below.

### B. SC in the TCM

After the PCM, SC proceeds with the TCM. Fig. 7 shows SC in the TCM. Generally speaking, the main purpose of SC in the TCM is picking out redundant APFs by making collaboration between operating APFs scattered in the MAMG. Simply, the strategy here is to remove low operating APFs from the compensation process and devoting their influence to one of them located in the area with the highest \( \text{VDR}_{ij} \). It is achievable by using two successive control phases: appropriate elimination of APF(s) as phase I (\( T_1 \) in Fig. 7) and counteracting the reduced compensation effort as phase II (\( T_2 \) in Fig. 7).

1) **Phase I of the TCM (\( T_1 \))**: It is assumed that those APFs operating in less than half of their rated power are low operating filters. Of course, this assumption can be easily modified according to the technical concerns of each APF. Based on Fig. 7, \( e_{APF} \), and \( e_{VDR_{ij}} \) are calculated and fed to the block “appropriate elimination of APF(s).” The following math function is applied in this block:

\[
\begin{align*}
\text{For } i = 1 \text{ to } m; \text{ For } j = 1 \text{ to } n \\
\text{if } e_{APF} \leq 0 \text{ and } e_{VDR_{ij}} \leq 0; \ B_i = 0; \\
\text{else; } B_i = 1; \ break; \ End;
\end{align*}
\]

End  (F2)

where \( n \) is the number of \( T_{ij} \) in the considered area. Based on F2, after detecting low operating APF(s), shutdown command \( (B_i = 0) \) is applied to the gain of the extracted APF(s) to be eliminated from the compensation process [see Figs. 1(b) and 7]. Note that the inequality constraint \( e_{VDR_{ij}} \leq 0 \) joins the loop in the next time period, basically.

2) **Phase II of the TCM (\( T_2 \))**: By the removal of one or more APFs, VDR at one or more of \( T_{ij} \) will be increased especially those \( T_{ij} \) being in the same area with the removed APF(s) due to smaller electrical distance between the respective CP and \( T_{ij} \). To tackle this inconsistency, one of the APFs is called to counteract the reduced compensation effort.

First, \( e_{VDR_{ij}^+} \) is fed to the block “required compensation calculation.” Then, \( C^{h,1} \) (see Fig. 7), as the total compensation effort required by all DGs due to the removal of one or more APFs, can be calculated by F3

\[
C^{h,1} = 0; \text{ For } i = 1 \text{ to } m; \text{ For } j = 1 \text{ to } n \\
\text{if } e_{VDR_{ij}^+} > 0; \ C^{h,1} = C^{h,1} + C^{h,1, ij}_i; \\
\text{else; } C^{h,1} = C^{h,1}; \ break; \ End; \ End.
\]

End.  (F3)

Generally, the fittest APF for neutralization is the one located in the area with the highest \( e_{VDR_{ij}} \) due to the smallest electrical distance between \( T_{ij} \) and the APF \( Z_{ij} \) in Fig. 1(a). Thus, detecting the fittest APF is carried out by using the following math function (see Fig. 7):

\[
\begin{align*}
\text{For } i = 1 \text{ to } m; \text{ For } j = 1 \text{ to } n; \text{ For } k = 1 \text{ to } m \& k \neq i; \\
\text{if } e_{VDR_{ij}^+} > e_{VDR_{ij}^+}; S^{h,1, ij}_i = C^{h,1} + S^{h,1, ij}_i; \\
\text{else; } S^{h,1, ij}_i = S^{h,1}; \ break; \ End; \ End.
\end{align*}
\]

End.  (F4)

Based on F4, the fittest APF is detected then its compensation gain is increased by \( C^{h,1} \), while there is no change for the rest. Note that only those APFs that were candidates for appropriate elimination (F2), are in the game. In fact, these APFs had been operating in low operation so they are more likely to have enough capability to counteract the total reduced compensation effort. However, in case of overloading the fittest APF, it is axiom that compensation effort of the APF would be limited to its maximum operation.

In rare cases, if the fittest APF is operating in the maximum operation, SC continues with the next time period (see Fig. 5), the PCM is bypassed, and finally, since there is one or more \( e_{VDR_{ij}^+} > 0 \), the fittest removed APF returns to the compensation process (F2).
C. Overview of SC

Fig. 8 presents a flowchart of the proposed control. In total, there are two important points regarding SC: First, due to higher current propagation of a fundamental negative sequence in comparison with harmonic components (in order to lower interarea line impedance at a fundamental component), SC individually deals with VUF and THD (or VHD) at the same time. Second, three successive steps are contrived in SC to reduce compensators rating:

1) The first reduction is obtained by making cooperation between DGs and APFs.
2) The second reduction occurs by making collaboration between areas (compensating areas sequentially; PCM).
3) The third reduction gains making collaboration between APFs of areas (TCM).

IV. SIMULATION STUDY

The test MAMG is shown in Fig. 9. Nominal voltage and frequency of the system are 230 V (per-phase rms value) and 50 Hz, respectively, and the switching frequency of DGs and APFs inverters is 10 kHz. To entirely evaluate the proposed control in different areas with different load conditions, four areas with different PQ requirements of $T_{ij}$ are considered in the system. It should be mentioned that the considered MAMG system is the most complex system with four areas. Hereby, other possible configurations of the four-area MG (also three-area, two-area, and single-area MGs) can be realized as the subsystems of the considered system.

Diode rectifier is used to make nonlinear load as it is configured in Fig. 10. Thus, by disconnecting one phase of the nonlinear load, there will be unbalanced-nonlinear load. In addition, to avoid complexity, APFs are considered the same.

**TABLE I**

<table>
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<th>Power Quality References</th>
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<tr>
<td>$V_{DR_{CP}}$</td>
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<td>VUF</td>
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Further to voltage unbalance suppression, compensation of both positive and negative sequences of third, fifth, and seventh harmonics (the main orders) of $T_{ij}$ and CPs voltages is carried out. PQ references of $T_{ij}$ and CPs are presented in Table I. In the present simulation study, PCM-scheduling, $T_1$, and $T_2$ (related to the TCM) are set to 5 s. Note that these terms are set to a short value to reduce simulation run time. Three scenarios are planned to evaluate SC in PCM and TCM under different loading conditions. Note that these scenarios are only distinguished by the loading condition of the MAMG, while control and power parameters are the same as presented in Table II.

A. First Scenario, SC in the PCM

In this scenario, areas 1 and 2 contain unbalance-nonlinear and linear loads and areas 3 and 4 include nonlinear and linear loads. Fig. 11 shows $VDR_{CP_i}$ and $VDR_{T_{ij}}$. Among all CPs,
This article has been accepted for inclusion in a future issue of this journal. Content is final as presented, with the exception of pagination.

TABLE II

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<th>Distribution Lines</th>
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**Fig. 11.** VDR CPs (PCM). (a) THD. (b) HD. (c) VUF.

Based on Fig. 11(a), at \( t = 5 \) s, the highest VDR (both THD and VUF) belongs to CP_1. Thus, compensation of area 1 is carried out in period 1 so VDR_{CP_1,ref} and VDR_{T_{11},ref} are achieved based on Fig. 11(b). At the end of period 1, CP_1 and CP_2 are in the highest THD and VUF, respectively. Therefore, harmonic compensation of CP_1 and voltage unbalance suppression of CP_2 are done in period 2. It can be seen that HD_{CP_2,ref}, THD_{T_{11},ref}, VUF_{CP_2,ref}, and VUF_{T_{21},ref} are achieved in this period [see Fig. 11(b)]. During periods 3 and 4, only harmonic compensation of areas 2 and 3 is carried out, respectively. It is shown that HD_{CP_2,ref} and THD_{T_{31},ref} in period 3 and HD_{CP_2,ref} and THD_{T_{31},ref} in period 4 are obtained. Note that before period 1, there were VUF-violation at areas 3 and 4; however, after period 2, there is no violation at these areas although neither their DGs nor their APFs are used for VUF suppression. By precise exploration of Fig. 11, two notes can be deduced.

1) First, PQ of other areas except for the considered area is also improved while compensation is not initiated for them. For example, from period 1 to period 3, THD_{CP_3} is decreased from 4.5% to less than 2.5% while harmonic compensation has not been initiated in area 3 (it is the same for VUF suppression).

2) Second, since VDR reduction is initiated in the respective period, corresponding VDR_{T_{ij}} is increased to the reference value based on Table I. Simply, it can be seen in Fig. 11(a) that in the last period (20 < \( t < 25 \)), all the curves less than 1% are related to CPs and the others are related to DGs terminals. It shows that the cooperation between APFs and DGs is accomplished properly since compensation sharing is done so that DGs are prior to APFs (see Section II).

**B. Second Scenario, SC in the TCM (Unbalance-Nonlinear Load Reduction)**

In this scenario, areas 1–3 contain unbalance-nonlinear and linear loads, while area 4 includes nonlinear and linear loads. Fig. 12 represents voltage harmonics of the system. Before \( t = 8 \) s, the reference values of CPs and T_{ij} are achieved and SC proceeds with the TCM. At \( t = 8 \) s, an unbalance-nonlinear load reduction (R_{NL} from 33 to 100 \( \Omega \)) occurs at CP_2. In this situation (\( t = 10 \) s), APF_2, APF_3, and APF_4 are operated in low operation situation, while APF_1 is operated in normal operation so shutdown commands (\( B_2 = B_3 = B_4 = 0 \)) are sent to APF_2 to APF_4 in T_1 (10 < \( t < 15 \)). Accordingly, VDR_{T_{31}} and VDR_{T_{41}} are increased. It is because APF_2, APF_3, and APF_4 are switched OFF and only DG_21, DG_31, and DG_41 compensate CP_2, CP_3, and CP_4, respectively. On the other hand, VDR_{T_{11}} (both THD_{T_{11}} and VUF_{T_{11}}) almost remains without change after \( t = 10 \) s since APF_1 is operated during T_1. At the end of T_1 (\( t = 15 \) s), T_2 is detected as the terminal with the highest violation from the reference value (see Fig. 12). Thus, APF_2 (the closest APF to T_2) is chosen as the fittest APF to counteract the reduced compensation effort. From \( t = 15 \) s (T_2), APF_2 is returned to the compensation process, while the compensation effort of APF_3 and APF_4 is added to the compensation effort of
From Fig. 12, it can be seen that since APF\(_2\) is returned to the compensation process, all the PQ indices (including area 3 and area 4) are achieved. Note that APF\(_3\) and APF\(_4\) are switched OFF. Meanwhile, VDR\(_{T_{11}}\) is almost unchanged since area 1 does not contribute in the collaboration between APFs due to SC principles (see Section III). In addition, VDR\(_{CP}\) have not been changed because there have not been any violation from any CP.

It should be mentioned that VUF of all CPs and DGs terminals is in the allowable range so no collaboration between areas is required in this regard [see Fig. 12(b)]. Note that during \(T_1\) that APF\(_2\) is switched OFF, VUF\(_{T_{21}}\) is increased but it is still in the allowable range. Therefore, during \(T_2\) that APF\(_2\) is returned to the compensation process, VUF\(_{T_{21}}\) is also returned to the previous value (\(T_1\)) since APF\(_2\) does not compensate unbalanced voltage.

As a more tangible figure, Fig. 13 shows voltage and current waveforms of different points of the MAMAG when SC is in the TCM. Comparatively, it can be seen that CP\(_1\)-current is under the lower unbalanced condition. It is because area 4 is free of unbalanced load; however, due to the imbalance of the MAMG as a unified system, CP\(_1\)-current is slightly unbalanced.

In addition, \(T_{21}\) voltage waveform at \(t = 15\) s is severely distorted in comparison with those at the times \(t = 10\) and 20 s. It is due to the fact that APF\(_2\) is switched OFF during \(T_1\) so DG\(_{21}\) is the only compensator of area 2 during this time period (see Fig. 12). As a result, the DG compensation effort is increased; accordingly, the DG voltage distortion is increased. Generally, lower current and voltage distortion of CPs compared with those of \(T_{ij}\)'s can be seen. It is because CPs PQ level is higher than that of \(T_{ij}\)’s.

C. Third Scenario, SC in the TCM (Unbalance-Nonlinear Load Increase)

Like the second scenario, in the third scenario, areas 1–3 contain unbalance-nonlinear and linear loads when area 4 includes nonlinear and linear loads. As shown in Table II, the second scenario loading condition is followed by the third
scenario; therefore, APF$_1$ and APF$_2$ are on when the compensation burden of APF$_3$ and APF$_4$ is devolved to APF$_2$.

Fig. 14 shows VDR at different points of the system. At $t = 6$ s, there is a severe increase in the unbalance-nonlinear load of area 3 ($R_{NL3}$ from 40 to 13 !). Thus, APF$_2$ workload is increased. However, it is in the maximum operation during $T_2$, as a result, area 2 (APF$_2$) collaboration with area 3 (APF$_3$) is limited. Accordingly, $T_{31}$-VDR (both VHD and VUF) is increased during this period (see Fig. 14). Finally, at $t = 10$ s, since there is a violation from a DG terminal ($T_{31}$), the respective APF (that is, APF$_3$ due to closeness to $T_{31}$), the respective APF is returned to the compensation process based on F2 control function. Note that the PCM is bypassed since there is no violation from any VDR$_{CP,ref}$ even from VDR$_{CP2,ref}$ (see Fig. 14). It can be seen that since APF$_3$ is returned to the compensation process, the violations are removed. It is in the situation that the VDR of the other areas remains unchanged because it does not play any role in the new collaboration between areas 2 and 3.

Fig. 15 shows DG$_{31}$ and DG$_{41}$ output currents. As expected from Fig. 14, since APF$_3$ is operated, the negative sequence of the fundamental component of current at $T_{31}$ is decreased because DG$_{31}$ workload is decreased. Considering harmonic currents of $T_{31}$, it can be seen that the fifth order of harmonic current is decreased, while the seventh order is increased. It shows that there had been a violation at VHD of the fifth order. Even though the seventh order of VHD is increased, this parameter is still in the allowable range [see Fig. 14(a)]. However, based on Fig. 15, the output current of DG$_{41}$ remains unchanged as it was expected from Fig. 14. In what follows, a brief summary is presented demonstrating the paper contribution by the simulation study.

Based on the loading condition of each scenario, from nine compensators (five DGs and four APFs) in the test system:
1) For VUF suppression
   a) In the first scenario, DG$_{31}$, DG$_{41}$, APF$_3$, and APF$_4$ are removed from the compensation process.
   b) In the second scenario, APF$_2$, APF$_3$, and APF$_4$ are removed from the compensation process.
   c) In the third scenario, APF$_4$ is removed from the compensation process.
2) For voltage harmonic mitigation
   a) In the first scenario, all nine compensators are utilized.
   b) In the second scenario, APF$_3$ and APF$_4$ are removed from the compensation process.
   c) In the third scenario, APF$_4$ is removed from the compensation process.

Noteworthy to remind that by the conventional method, all nine compensators are operated since no plan is contrived in the conventional method reducing compensators rating based on VDR of the MAMG.

V. CONCLUSION

A real-time SC scheme is proposed in this paper to improve the PQ of an MAMG when the areas PQ requirements are different. Both DGs terminal and CP of each area are attended in PQ improvement. Voltage unbalance and harmonic compensation, including positive and negative sequences of selected harmonics, are addressed in the proposed method. The main contribution of the proposed method is applying an efficient arrangement of available compensators in the compensation process so that the least number of them are used for integrated PQ improvement of the MAMG. To this aim, DGs inverters and APFs are considered as compensators. Briefly, three items are influential to develop the best arrangement: the cooperation between DG(s) and APF of each area, the collaboration between areas and the collaboration between the APFs of areas.
Furthermore, the arrangement is adaptively modified based on the VDR of the MAMG. The proposed method is evaluated by MATLAB/Simulink when a complex four-area MG is considered as the test system.

REFERENCES


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