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Comprehensive Comparison of Rotor Permanent Magnet and Stator Permanent Magnet Flux-Switching Machines

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Abstract—This paper compares two flux-switching machines, namely, one stator permanent-magnet flux-switching (SPM-FS) machine and one rotor permanent-magnet flux-switching (RPM-FS) machine, with the same overall dimensions, main material properties and current density. The characteristics comparison is conducted from two perspectives, i.e. electromagnetic torque production mechanisms and torque (power)-sizing equations. The harmonics contribution to average electromagnetic torque is analyzed based on the modulation principle and gearing effect, which reflects the similarities and differences between two FS machines in torque production mechanism. Moreover, torque performances are investigated from the viewpoints of magnetic parameters and electrical parameters. Then, electromagnetic performances including overload capability, flux-weakening capacity, and efficiency are analyzed and compared further. The predicted results indicate the RPM-FS machine exhibits larger torque capability, lower torque ripple, and improved flux-weakening capacity. The finite element analysis (FEA) predicted results are validated by experiments on two prototype machines.

Index Terms— Rotor permanent magnet, stator permanent magnet, flux switching, permanent magnet machine.

I. INTRODUCTION

In recent years, stator-permanent magnet (PM) (SPM) flux-switching (SPM-FS) machines have attracted considerable attentions, due to the dramatic improvements of power (torque) density, efficiency and thermal dissipation ability, and are considered as a promising candidate for electric vehicle (EV) and hybrid electric vehicle (HEV) applications [1]-[2]. However, due to the co-existence of PMs and armature windings in stator as shown in Fig. 1(a), the electrical loading of SPM-FS machines is significantly reduced, meanwhile, the magnetic saturation is serious in stator teeth with the reduced available space for both armature windings slots and stator iron laminations [3]. Then the torque capability is limited especially for the applications of EVs and HEVs, where normally a large armature current density is required due to the limited DC-link voltage supplied by batteries. To address the issues above, currently a novel rotor-permanent magnet flux-switching (RPM-FS) machine was proposed as shown in Fig. 1(b), which inherits the “flux-switching” principle of SPM-FS machines. The torque density can be enhanced further by removing the magnets from stator to rotor for the better usage of the rotor space and releasing the stator space to avoid serious iron saturation [4].

In preliminary design stage of electrical machines, the electromagnetic torque production mechanism and torque (power)-sizing equation are mostly important to investigate the operation principle and evaluate the torque capability, respectively. Recently, the torque production mechanism of flux-switching machines is investigated based on a novel perspective, namely magnetic field modulation principle [5]-[6], where it is found that the electromagnetic torque is not only contributed by the primitive harmonics of PM field and armature reaction field, but also produced by the corresponding modulated harmonic components [7]. The field modulation principle and gearing effect reveal the electromagnetic torque proportion of harmonic components, which is helpful to investigate the differences of flux-switching machines with novel topologies. On the other hand, the torque (power)-sizing equations are particularly important to promptly provide the relationship between key initial geometric dimensions and performance specifications [8]. Numerous research on the torque (power)-sizing equations of different machines are conducted, e.g. conventional interior-PM machines, vernier PM machines, double salient PM machines, axial-flux PM machines and out-rotor flux-switching PM machines, etc. [9]-[11]. In addition, the torque (power)-sizing equation also reflects the torque production mechanism, i.e. the interaction of magnetic loadings and electrical loadings.

In this paper, the electromagnetic torque characteristics of
flux-switching machines are investigated from two perspectives, namely, torque production mechanism and torque (power)-sizing equation. Meanwhile, a comparison of torque capability between two flux-switching machines with stator-PM and rotor-PM respectively is conducted in section II. Then, the electromagnetic performance of a pair of RPM- and SPM-FS machines are analyzed and compared further in section III, which reveals the merits and disadvantages of two machines comprehensively. The predicted results indicate the RPM-FS machine exhibits larger torque capability, lower torque ripple, and wider range of speed regulation. In section IV, the predicted results are verified by experiments on the two prototypes of RPM- and SPM-FS machines with the same stator outer diameter and stack length, followed by conclusions in section V.

II. TORQUE PRODUCTION MECHANISM AND TORQUE-SIZING EQUATION

The topologies of a pair of flux-switching machines with stator-PM and rotor-PM respectively are shown in Fig. 1, and key geometric parameters, including stator outer diameter, stack length, air-gap, and rotor pole-pair number, are kept the same, and the material properties of magnets, stator and rotor irons are also identical. In addition, the effective armature current density of two flux-switching machines at the rated torque and the DC-link bus voltage are equal, i.e., \( J_{dm} = 5 \text{A/mm}^2 \) and \( U_{dc} = 600 \text{V} \), respectively.

Based on the flux-switching operation principle, phase PM flux linkages and consequently, back-electro motive forces (back-EMFs) of both FS machines due to magnets solely are essentially sinusoidal [4]. Hence, the electromagnetic power \( P_e \) of two machines can be expressed in a unified form as,

\[
P_e = \frac{m}{T} \int_0^T c(t) \cdot i(t) \, dt = \frac{m}{2} E_{am} \cdot I_{am} \cos \theta
\]

where, \( m \) is phase number, \( T \) is the period of phase back-EMF, \( E_{am} \) and \( I_{am} \) are the amplitudes of the fundamental phase back-EMF and armature current, respectively, and \( \theta \) is the phase angle between phase back-EMF and armature current.

The amplitude of the fundamental phase back-EMF yields

\[
E_{am} = N_{ph} \cdot P_r \cdot \Phi_{PM}\text{ms}
\]

where, \( N_{ph} \) is winding turns per phase, \( \omega_0 \) is rotor speed, \( P_r \) is rotor pole-pair number, \( \Phi_{PM}\text{ms} \) is the fundamental amplitude of PM flux.

Since the \( d \)-axis inductance \( L_d \) is approximately equal to the \( q \)-axis inductance \( L_q \) in both RPM-FS and SPM-FS machines [4], the reluctance torque is negligible and \( L_d = 0 \) control is suitable for both machines, i.e. \( \theta = 0^\circ \). Then, the electromagnetic torque can be expressed as:

\[
T_e = \frac{P_r}{\omega_0} = \frac{m}{2} N_{ph} P_r \Phi_{PM}\text{ms} I_{am}
\]

It can be found that electromagnetic torque of RPM-FS and SPM-FS machines are significantly determined by the key magnetic parameter \( \Phi_{PM}\text{ms} \) and electrical parameter \( I_{am} \).

Table I: Key Specifications and Dimensions of Two Flux-Switching Machines

<table>
<thead>
<tr>
<th>Specifications</th>
<th>RPM-FS</th>
<th>SPM-FS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum air-gap length ( g ) (mm)</td>
<td>0.35</td>
<td>0.35</td>
</tr>
<tr>
<td>Stator outer diameter ( D_{st} ) (mm)</td>
<td>128</td>
<td>128</td>
</tr>
<tr>
<td>Stator inner diameter ( D_{in} ) (mm)</td>
<td>76.8</td>
<td>70.4</td>
</tr>
<tr>
<td>Stack length ( la ) (mm)</td>
<td>10.6</td>
<td>7.2</td>
</tr>
<tr>
<td>PM width ( w_{PM} ) (mm)</td>
<td>4.54</td>
<td>4.6</td>
</tr>
<tr>
<td>PM height ( h_{PM} ) (mm)</td>
<td>10.62</td>
<td>28.8</td>
</tr>
<tr>
<td>IRON LAMINATION TYPE</td>
<td>50WW470</td>
<td>N35SH</td>
</tr>
<tr>
<td>Iron lamination type</td>
<td>50WW470</td>
<td>N35SH</td>
</tr>
</tbody>
</table>

A. Analysis of Magnetic Parameters

The fundamental amplitude of phase PM flux \( \Phi_{PM}\text{ms} \) satisfies

\[
\Phi_{PM}\text{ms} = 4 B_{\text{max}} w_{r} l_{e} k_{sio} k_{i1} k_{i2}
\]

\[
= 2 B_{\text{max}} D_{s} w_{r} c_{i1} k_{sio} k_{i1} k_{i2}
\]

where, \( w_{r} \) is rotor-tooth-width, \( l_{e} \) is the effective stack length, \( k_{sio} \) is split ratio (the ratio of stator inner diameter \( D_{si} \) to stator outer diameter \( D_{so} \) for inner-rotor outer-stator machines), \( P_r \) is PM pole-pair number, which is defined as the fundamental
harmonic order of the PM-MMF distribution. \( c_i \) is stator pole-arc coefficient, and \( B_{\text{gmax}} \) is the peak value of air-gap flux density, marked as \( B_{\text{gmax}} \) of A1 in Figs. 2(a) and 3(a), respectively. It should be emphasized that the general peak value (marked as “Peak value”) is ignored due to the localized saturation effect [12]. \( k_{\text{HC}} \) is the harmonic coefficient of phase flux to take harmonics influence into consideration, which is determined as the ratio of \( \Phi_{\text{PM}} \) to the peak value of phase flux. \( k_{\text{FL}} \) is the flux leakage coefficient, and \( k_d \) is the fundamental winding distribution factor. Since the parameters \( D_{\alpha\alpha}, I_n, \) and \( P_{\text{FS}} \) are determined in the preliminary design process, \( \Phi_{\text{PM}} \) is dominantly influenced by the variables \( B_{\text{gmax}}, k_{\text{sis}}, \) and \( c_i \) in equation (4).

\[
\Phi_{\text{PM}} = \Phi_{\text{PMm}1}\left[1 + \frac{B_{\text{gmax}}}{\Phi_{\text{PMm1}}} k_{\text{HC}} \cos(\frac{n_{\text{PPM}}}{2} + \frac{\pi}{2})ight]
\]

where \( n_{\text{PPM}} \), \( P_{\text{FS}} \), \( k_{\text{HC}}, k_{\text{HC}}^\prime \cos(\frac{n_{\text{PPM}}}{2} + \frac{\pi}{2}) \) are the harmonic order of the PM-MMF distribution, and it is a key parameter to influence \( \Phi_{\text{PM}} \), which can be identified as:

\[
c_i = \frac{B_{\text{gmax}}}{\Phi_{\text{PMm}}} = \frac{\beta_{\text{PM}} \beta_{\text{PMm}}}{\pi / P_{\text{FS}}} = \frac{P_{\text{FS}} \beta_{\text{PM}}}{\pi}
\]

where \( B_{\text{gmax}} \) is the average flux density under one PM pole, and \( \beta_{\text{PM}} \) is PM teeth arc as shown in Fig. 4.

It can be found that the PMs in RPM-FS machines is inserted between two adjacent rotor cores, and then, \( \beta_{\text{PM}} \) is identical to rotor teeth arc \( \beta_{\text{r}} \) as shown in Fig. 4. Since the PMs in RPM-FS machines are magnetized with the same direction, \( P_{\text{PM}} \) is 10, and then the corresponding pole arc coefficient \( c_i \) can be calculated to be 0.5. However, for SPM-FS machines, since the PMs are sandwiched by “C-type” stator cores, and magnetized in the opposite direction as shown in Fig. 1(a), \( P_{\text{PM}} \) is equal to 6. So, \( \beta_{\text{PM}} \) is identical to the stator teeth arc, i.e. \( \beta_{\text{PM}} = \beta_{\text{r}} \), and consequently, \( c_i = 0.25 \) can be obtained.

Based on the Fourier analysis, the flux-density harmonic distributions of two flux-switching machines are shown in Figs. 2(b) and 3(b). For the SPM-FS machine, the dominant harmonic components are 6th and 18th, produced by the primitive PM-MMF \( (n_{\text{PPM}}, n^1=1 \text{ and } 3) \), whereas the other harmonics with 4, 8, 16 and 28 pole-pairs \( (n_{\text{PPM}} \pm k_{\text{F}} P_{\text{FS}}), n^1 = 1, k=1, \text{ and } n^3=3, k=1 \) are generated since the PM-MMF is modulated by the salient rotor teeth in air-gap field [7]. Similarly, for the RPM-FS machine, the dominant harmonics produced by the PM-MMF only are 10th and 50th components \( (n_{\text{PPM}}, n^1=1 \text{ and } 5) \), meanwhile, if the modulation of salient stator teeth to rotor PM-MMF is taken into consideration, the harmonics of 14th and 34th components \( (n_{\text{PPM}} \pm k_{\text{F}} P_{\text{FS}}), n^1 = 1, k=1 \) are generated [13]. It is worth noting that the primitive PM-MMF of RPM-FS machine contains the harmonics with 20 and 40 pole-pairs, i.e. \( n_{\text{PM}} = 2, \text{ and } 4 \), which is different from the SPM-FS machine. Because the PMs in RPM-FS machines are magnetized with the same direction, and the rotor slot width \( \beta_{\text{PM}} \) is not equal to rotor cell gap \( \beta_{\text{r}} \) as listed in Table I, which means that the even harmonic orders in PM-MMF cannot be cancelled, and then the corresponding harmonic components are produced in the air-gap flux density distribution as shown in Fig. 3(b).

Fig. 4 The air-gap flux density distribution. (a) One PM pole-pair of RPM-FS machine. (b) Single PM pole of SPM-FS machine.
machine is higher than that of the SPM-FS one. In addition, the split ratio \(k_{dio}\) of RPM-FS machine is 0.6, which is slightly higher than that of the SPM-FS machine (0.55). Consequently, although the value of \(B_{pmu}\) in the SPM-FS machine (2.2T) is about 2 times of that of the RPM-FS machine (1.1T), the peak value of phase PM flux is slightly larger than that of RPM-FS machine as shown in Fig. 5. Furthermore, the PM flux of RPM-FS machine contains harmonics with odd pole-pair numbers, and the total harmonic distortion (THD) is higher (3.8%). Hence, the harmonic coefficient \(k_{HC}\) should be taken into consideration to precisely calculate \(\Phi_{Pamu}\) in equation (4).

harmonic distortion (THD) is 4.36% and 1.70%, respectively.

**B. Analysis of Electrical Parameters**

The armature reaction MMF is produced by injecting 3-phase symmetrical and sinusoidal currents. The back-EMF vectors distributions of the slot conductors in two flux-switching machines are shown in Fig. 8. Based on the fundamental star vector theory [14], the armature winding pole-pair number \(P_s\) of the 24s/10p RPM-FS machine is equal to \(P_{ps} \times P_s = 10\), and then it can be deduced that the armature reaction MMF contains the harmonics with (2i-1) pole-pair multiplied by the greatest common divisor (GCD) of \(P_s\) and \(P_r\), i.e. 4i-2 (i=1, 2…, but without triple multiples).

However, for the 12s/10p SPM-FS machine, the definition of \(P_s\) should be redefined, which is different from that of RPM-FS machine. Since the PMs are inserted between two adjacent stator cores and the slot number \(P_s\) is equal to 2\(P_{ps}\), it can be deduced that the GCD(\(P_s\), \(P_R\)) is \(P_s\). If \(P_s\) is defined the same as that of the RPM-FS machine, namely, \(P_{ps} = P_{ps}\), then the corresponding spoke number \(N_{sp}\) of back-EMF vectors distributions in slot conductors can be obtained by \(N_{sp} = P_{ps}/(\text{GCD}(P_s, P_R))\), which is identically equal to 2. Obviously, the result cannot match the combination condition of \(P_s\) and \(P_r\), namely \(N_{sp}\) must be an integer multiplied by the phase number \(m=3\) [13]-[14]. Therefore, for SPM-FS machines \(P_s\) is redefined as \(P_{ps} = P_{ps}/(\text{GCD}(P_s, P_R))\), and then the modulated PM-MMF harmonic components can be utilized to produce electromagnetic torque. The armature reaction harmonic orders of the 12s/10p SPM-FS machine are expressed as \(4i\) (\(i=1, 2…\) without triple multiples).

In addition, since the rotor topologies of two flux-switching machines are both salient structures, the armature reaction MMF will be modulated by the rotor teeth. Then, the modulated harmonic orders of RPM-FS and SPM-FS machines can be identified as \(4i\) and \(4i\) (\(i=0, 1, 2…\), respectively, which can be verified by the results shown in Figs. 9(a) and (b).

Correspondingly, the open-circuit phase back-EMF waveforms per turn at the based speed of 1500r/min are shown in Fig. 6. By applying Fourier analysis, it can be found that the phase back-EMF waveform of the RPM-FS machine has the higher odd-order harmonics especially the 3rd-order component, which is agreed with the PM flux-linkage analysis. However, the 3rd-order harmonic can be cancelled by “Y”-connected armatures windings, and thus the line back-EMF waveform is more sinusoidal as shown in Fig. 7, where the fundamental amplitudes of the line back-EMF of the RPM-FS and SPM-FS machines is 5.4V and 7.19V, and the corresponding total harmonic distortion (THD) is 4.36% and 1.70%, respectively.

The amplitude of phase current \(I_{wm}\) in equation (3) yields,

\[
I_{wm} = \sqrt{2} J_{a, rms} A_{sl}, k_{sf} P_r \frac{8mN_{ph}}{A_{sl, k_{sf}}}
\]

where, \(A_{sl}\) is the armature slot area, and \(k_{sf}\) is the slot fill factor. Since the two machines are designed under air cooling condition, the rated phase current density is set to \(J_{a, rms}=5A/mm^2\). Hence, \(I_{wm}\) is mainly determined by the slot effective area \(A_{sl, k_{sf}}\) and the phase turns number \(N_{ph}\). It should
be emphasized that \( N_{ph} \) can be cancelled further in torque-sizing equation, and then electromagnetic torque \( T_e \) is mainly influenced by \( A_{slot,kf} \) from the electrical loading perspective. Moreover, the value of \( A_{slot,kf} \) in the RPM-FS machine is 78.4mm\(^2\), which is 1.5 times of that of the SPM-FS one due to removed PMs from stator to rotor.

For the 12s/10p SPM-FS machine, \( T_e \) is mainly attributed to 6 harmonic components, including \( 4^\text{th} \), \( 6^\text{th} \), \( 8^\text{th} \), \( 16^\text{th} \), \( 18^\text{th} \), and \( 28^\text{th} \). From the magnetic loadings perspective, the primitive harmonic components, namely \( 6^\text{th} \) and \( 18^\text{th} \), produces 18\% and 28.9\% of the electromagnetic torque respectively, whereas the contributions by modulated harmonics with \( 4^\text{th} \), \( 8^\text{th} \), \( 16^\text{th} \), and \( 28^\text{th} \) is 28.5\%,-14\%, 29.2\% and 9.5\%, respectively. From the electrical loadings perspective, the primitive harmonics of armature reaction MMF \( (4i, \text{where } i=1, 2...\text{without triple multiples}) \) and the modulated harmonics \( (4i\pm jPr) \), where \( i=1, 2...\text{without triple multiples}, j=1, 2...\) are both utilized to generate \( T_e \). In general, the SPM-FS machine not only uses primitive harmonics in PMs and armature reaction fields, but also the modulated harmonics, which is different from that of RPM-FS machines.

For the 24s/10p RPM-FS machine, \( T_e \) is dominantly produced by the harmonics with 10\% pole-pair, and \( A_{vph} \) is the corresponding harmonic component of electrical loadings in armature windings with \( 10 \) pole-pair, and \( \phi \) is the phase angle shift between \( B_{gy} \) and \( A_{vph} \). Based on the harmonic distributions of PM-MMF and armature reaction MMFs in Figs. 2, 3 and 9, the electromagnetic torque \( T_e \) contributions by air-gap field harmonics are shown in Fig. 10.

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The electromagnetic torque is produced by the interaction between the harmonic components of magnetic loadings and electrical loadings as revealed by equation (7), which exhibit the same orders and rotating speeds [14].

\[
T_e = -\frac{D_{gy}}{4} \int_{0}^{\frac{\pi}{2}} B_{gy}(\theta) A_{vph}(\theta) d\theta = \frac{\pi D_{gy}}{4} \sum_{v=1}^{\text{orders}} B_{gy} A_{vph} \cos \phi
\]  

(7)

where, \( B_{gy} \) is the harmonic component of magnetic loadings with \( v \) pole-pair, and \( A_{vph} \) is the corresponding harmonic component of electrical loadings in armature windings with \( v \) pole-pair, and \( \phi \) is the phase angle shift between \( B_{gy} \) and \( A_{vph} \). Based on the harmonic distributions of PM-MMF and armature reaction MMFs in Figs. 2, 3 and 9, the electromagnetic torque \( T_e \) contributions by air-gap field harmonics are shown in Fig. 10.

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From equation (8), it can be seen that \( T_e \) is mainly influenced by the magnetic parameters \( B_{max}, k_{ios}, \text{ and } c_{e} \) in equation (4), and the electrical parameters \( A_{slot,kf}, k_{FL} \) in equation (6). However, both the magnetic and electrical parameters are determined by the geometric dimensions shown in Table II. Hence, geometric parameters sensitivity are analyzed to explicitly reflect the influence of each design variable on the optimization objectives, i.e. electromagnetic torque and torque ripple.

\[
T_e = \frac{\sqrt{2}}{8P_{PM}} \sum_{j=1}^{\text{orders}} \sum_{r=1}^{\text{polarities}} |4R_{PM} \pm jPr| A_{slot,kf} c_{e} k_{ios} c_{t} k_{FL}
\]  

(8)

On the other hand, based on the analysis of magnetic parameter \( \Phi_{PM} \) in equation (4) and electrical parameter \( I_{sw} \) in equation (6), the electromagnetic torque equation can be evolved as equation (8), which can be utilized to estimate the electromagnetic torque directly.

According to equation (8), the directly predicted electromagnetic torque \( T_e \) of the RPM-FS machine is 17.36Nm, and the error between the 2D-FEA estimation is 10.8\%. For the SPM-FS machine, the directly obtained \( T_e \) is 16.9Nm, which is about 1.14 times of the 2D-FEA result. For both machines, the error between the analytical results and the 2D-FEA results can be attributed to the ignorance of magnetic saturation effect and the estimation of the flux leakage coefficient \( k_{FL} \).

## Table II

<table>
<thead>
<tr>
<th>Item</th>
<th>Geometric parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>RPM-FS</td>
<td>SPM-FS</td>
</tr>
<tr>
<td>( B_{max} )</td>
<td>( \beta_{ios} ), ( \beta_{ios} ), ( \beta_{ios} ), ( \beta_{ios} )</td>
</tr>
<tr>
<td>( k_{ios} )</td>
<td>( k_{ios} )</td>
</tr>
<tr>
<td>( c_{e} )</td>
<td>( c_{e} )</td>
</tr>
<tr>
<td>( A_{slot,kf} )</td>
<td>( \beta_{ios}, \beta_{ios} ), ( \beta_{ios} )</td>
</tr>
<tr>
<td>( \beta_{ios} )</td>
<td>( \beta_{ios} ), ( \beta_{ios} )</td>
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From equation (8), it can be seen that \( T_e \) is mainly influenced by the magnetic parameters \( B_{max}, k_{ios}, \text{ and } c_{e} \) in equation (4), and the electrical parameters \( A_{slot,kf}, k_{FL} \) in equation (6). However, both the magnetic and electrical parameters are determined by the geometric dimensions shown in Table II. Hence, geometric parameters sensitivity are analyzed to explicitly reflect the influence of each design variable on the optimization objectives, i.e. electromagnetic torque and torque ripple.
D. Sensitivity Analysis of Geometric Parameters

Based on the derivation of torque-sizing equation (8), the key geometric parameters in flux-switching machines can be determined given the specification requirements. Meanwhile, the key geometric variables will impact on torque performances significantly, hence, the sensitivity analysis on electromagnetic torque $T_e$ and torque ripple $T_{ripple}$ are conducted based on the local sensitivity analysis (LSA) [15] and global sensitivity analysis (GSA) [16], and the result are shown in Table III.

From Table III some conclusions can be summarized:

1. $k_{st}$ has dominant influence on $T_e$ and $T_{ripple}$ in both flux-switching machines, since it is not only the key variable in torque-sizing equation (8), but also it directly determines the magnetic loadings $B_{pmax}$ and armature winding slot area $A_{slotf}$ under a given stator outer diameter, which can further determine the torque capability.

2. $k_{so}$ exhibits the highest sensitivity on $T_e$ in the RPM-FS machine due to the significant influence of PM volume and $B_{pmax}$. However, for the SPM-FS machine, $k_{st}$ has little impact on $T_e$ and $T_{ripple}$ since the rotor structure is simple and robust, and $k_{so}$ can change the magnetic saturation in rotor yoke only.

3. From the topology of RPM-FS machines in Fig. 1(b), $\beta_{rt}$ and $\beta_{rs}$ are constrained by each other in the circumferential direction, and are analyzed comprehensively by GSA [16]. $\beta_{rt}$ and $\beta_{rs}$ are the key dimensions to determine $c_r$ and $B_{pmax}$ in torque-sizing equation, and consequently, $T_e$ will be affected further. It is worth noting that $\beta_{rt}$ and $\beta_{rs}$ have the highest sensitivity on torque ripple, which indicates that $T_{ripple}$ can be significantly reduced by optimizing the corresponding variables. Similarly, the sensitivity values of $w_{PM}$ and $w_{r}$ are also calculated by GSA, which have little impacts on $T_{ripple}$. For the SPM-FS machine, the rotor structure is mainly determined by $\beta_{rt}$ and $\beta_{rs}$, where $\beta_{rt}$ has remarkable influences on $T_e$ and $T_{ripple}$, and $\beta_{rs}$ only has effect on $T_{ripple}$.

4. From Figs. 1(a) and (b), the stator structure of RPM-FS machines is more complicated than that of RPM-FS machines, and the parameters $\rho_{rt}$ and $w_{PM}$ are constrained by each other in the circumferential direction. The combined sensitivity analysis results are listed in Table III. It can be seen that $\rho_{rt}$ and $w_{PM}$ have considerable influences on $T_e$ and $T_{ripple}$, since they determine both magnetic and electrical loadings parameters in torque-sizing equation, i.e. $B_{pmax}$, $c_r$, and $A_{slotf}$. However, for the RPM-FS machine, the stator structure parameter $\rho_{rt}$ only has impact on $A_{slotf}$, which affects $T_e$ further.

III. ELECTROMAGNETIC PERFORMANCES COMPARISON

In this section, based on 2D-FEA, the electromagnetic performances of the RPM-FS machine and the SPM-FS machine are investigated and compared comprehensively.

A. Torque Performances

The rated electromagnetic torque versus rotor position waveforms of two flux-switching machines are shown in Fig. 11(a). It can be found that the average torque and torque ripple of the RPM-FS machine is 16.05Nm and 11%, respectively. However, the torque ripple without cogging torque is only 5%, hence, the predicted cogging torque waveform in Fig. 11(b) is the main reason for torque ripple and can be reduced by optimization further. For the SPM-FS machine, the average torque is 14.8Nm, which is 8% lower than that of the RPM-FS one. Meanwhile, the torque ripple of the SPM-FS machine is 22%, which is 2 times of that of the RPM-FS machine. However, the torque ripple without cogging torque can be dramatically reduced to 6% only as shown Fig. 11(a), since the peak-peak cogging torque of the SPM-FS machine is 3.4Nm, which is much higher than the RPM-FS machine as shown in Fig. 11(b).

The output torques versus armature current angles ($\beta$) at the current density of $J_{st,max}=5A/mm^2$ are shown in Fig. 12, where the RPM-FS and SPM-FS machines reach the maximum torque...
when $\beta$ is $0^\circ$ and $5^\circ$, respectively, which means the $dq$-axes inductances $L_d/L_q$ are approximately equal in both machines. Hence, the reluctance torques are negligible and $i_d=0$ control is suitable for both machines.

Fig. 13 shows the average torque versus current densities. It can be found that the output torque of RPM-FS machine is always larger than that of SPM-FS machine and the torque ripple ratio is smaller. Moreover, the output torque of RPM-FS machine increases linearly, as the armature current density rises, which is almost parallel to that of the SPM-FS machine. Hence, both of RPM-FS machine and SPM-FS machine have satisfactory overload capacity.

In addition, the consumed PM material mass (kg) and utilization ratio (torque per magnet mass) are listed in Table IV. It can be found that the PM utilization ratio of the RPM-FS machine is 59.4(Nm/kg), which is about 3.6 times of that of SPM-FS machine. The core losses and PM losses are listed in Table IV, where the core losses are analyzed based on the improved Yamazaki’s model [17, 18], and the PM eddy current losses are calculated by the 3D-FEA. The predicted efficiencies of two machines at rated operation point are almost same, being 90.2% and 90.9%, respectively.

### B. Flux Weakening Capability

The constant-power speed range is another key characteristic of traction machines for EV and HEV applications. Generally, the flux-weakening ability of the PM brushless machines can be expressed by a flux-weakening coefficient $k_{f_w}$ [11]

$$k_{f_w} = \frac{N_{ph}\Phi_{ph, m}}{N_{ph}\Phi_{ph, m} - L_d i_d}$$  \hspace{1cm} (9)

where, $L_d$ and $i_d$ is the $d$-axis inductance and armature current, respectively. From Table IV, the flux-weakening capacities of two machines can be evaluated by equation (9). The coefficient $k_{f_w}$ of RPM-FS and SPM-FS machines is 2.47 and 1.51, respectively. Since both flux-switching machines can not realize completed flux-weakening, the maximum speed $n_{max}$ can be evaluated as [19],

$$n_{max} = \frac{60}{2\pi P_{cu}} \frac{U_{lim}}{N_{ph}\Phi_{ph, m} - L_d i_d}$$  \hspace{1cm} (10)

where $U_{lim}$ is the limited voltage, which is determined by the DC-bus voltage. It can be found that the magnetic parameter $N_{ph}\Phi_{ph, m}$, i.e., the $d$-axis PM flux linkage of the SPM-FS machine is larger than that of the RPM-FS one from Table IV, whereas the $d$-axis armature reaction flux-linkage $L_d i_d$, which is related to the electrical performance parameter $I_{lim}$, is lower. Hence, the maximum speed of the RPM-FS machine can be obtained to be 4600r/min as shown in Fig. 14, which is about 1.8 times of that of the SPM-FS machine under the same DC-bus voltage. Meanwhile, the constant power range of the RPM-FS machine is also wider.

In addition, at the beginning of flux-weakening control, a higher $i_d$ of the SPM-FS machine is utilized to offset the PM flux linkage due to the limited $U_{dc}$, which leads to a sharp reduction of $i_d$. Since the reluctance torque in both machines is negligible, the electromagnetic torque is approximately equal to the PM torque. Hence, $T_e$ reduces significantly as shown in Fig. 14, and then, the peak power of the SPM-FS machine is lower that of the RPM-FS machine. In addition, the speed regulation range of RPM-FS machine can be improved further by adjusting the key geometric parameter $k_{f_w}$ (the ratio of $D_r$ to $D_o$ as shown in Fig. 1(b)). In the case of $k_{f_w}=0.73$, $D_r=55.6$mm and $D_o=76.1$mm, the output torque of RPM-FS machine is reduced as 14.8Nm due to the lower PM volume utilization, which is the same as rated torque of SPM-FS machine. Then, $k_{f_w}$ is calculated as 2.75, and a larger maximum speed 5300r/min can be obtained.

\begin{table}[h]
\centering
\caption{Performance Comparison of Two Flux-Switching Machines}
\begin{tabular}{|c|c|c|}
\hline
Specifications & RPM-FS & SPM-FS \\
\hline
Mass of stator iron (kg) & 2.49 & 2.39 \\
Mass of rotor and shaft (kg) & 2.13 & 1.62 \\
Mass of copper mass (kg) & 0.27 & 0.9 \\
Mass of PM (kg) & 6.15 & 6.15 \\
Total mass (kg) & 6.89 & 6.15 \\
PM flux linkage (Wb) & 8.80 & 11.64 \\
$q$-axis inductance (Lm) & 9.22 & 14.97 \\
$h_{max}$ & 2.47 & 1.51 \\
Peak value of cogging (Nm) & 3.4 & 3.4 \\
Output torque (Nm) & 16.05 & 14.8 \\
Torque ripple (%) & 11% & 22% \\
$k_{f_w}$ (Nm/kg) & 59.4 & 59.4 \\
Cooper loss (W) @90°C & 158.8 & 103.8 \\
$T_{in}P_{cu}$ & 0.101 & 0.142 \\
Core loss (W) & 59.74 & 51.47 \\
PM loss (W) & 3.92 & 30.95 \\
Output power (W) & 2520.9 & 2324.6 \\
Efficiency (%) & 90.2% & 90.9% \\
Power factor & 0.89 & 0.91 \\
\hline
\end{tabular}
\end{table}

IV. EXPERIMENTAL VALIDATIONS

To validate the previous analysis and results, two prototypes of the RPM-FS and SPM-FS machines are manufactured, and experiments are carried out in this section. Figs. 15 and 16 show the two prototypes, and the main design dimensions are in accordance with those listed in Table I. The two machines at the rated speed of 1500r/min are shown in Fig. 14, and then, the peak power of the SPM-FS machine is lower than that of the RPM-FS machine. In addition, the speed regulation range of RPM-FS machine can be improved further by adjusting the key geometric parameter $k_{f_w}$ (the ratio of $D_r$ to $D_o$ as shown in Fig. 1(b)). In the case of $k_{f_w}=0.73$, $D_r=55.6$mm and $D_o=76.1$mm, the output torque of RPM-FS machine is reduced as 14.8Nm due to the lower PM volume utilization, which is the same as rated torque of SPM-FS machine. Then, $k_{f_w}$ is calculated as 2.75, and a larger maximum speed 5300r/min can be obtained.
Meanwhile, the measured and FEA-predicted THD values are 9.97% and 11.65%, respectively. For the SPM-FS machine, the fundamental component of the measured back-EMF is 95% of that 3D-FEA result (256V). The THD values from the measurement and FEA prediction is 2.36% and 1.72%, respectively. The minor discrepancies between the measured and 3D-FEA results can be mainly attributed to the imperfection of manufacturing and assembling process.

The output torque and efficiency of two machines versus current density are shown in Fig. 18, where \( I_{\text{d}} = 0 \) control is employed and the PM operating temperature is estimated to be 90°C for 3D-FEA, since the PM demagnetization caused by high temperature will contribute to the discrepancies. These torque values are measured at the speed of 1500r/min. As can be seen, the measured output torques of two machines increase almost linearly as armature current density rises, and the 3D-FEA results agree well with measured results. It can be found from Fig. 18(a) that the measured output torque of the RPM-FS machine at rated current density is 15Nm, which is about 95% of the 3D-FEA prediction. However, for the SPM-FS machine, the measured rated torque is 11.8Nm, which is 91% of the 3D-FEA result at \( J_{\text{d,rms}} = 5\, \text{A/mm}^2 \). The error can be attributed to the manufacturing tolerances and partial irreversible demagnetization in the PMs due to high temperature under over-load experiments. In addition, the measured efficiencies of both machines are lower than the 3D-FEA results, since the mechanical losses in two machine are estimated inaccurately and the output torque decreases as above analysis. At the rated operation point, the measured efficiencies of two machines are almost the same, being about 86.3% and 86.15%, respectively.

V. CONCLUSIONS

In this paper, a comprehensive comparison between a 24s/10p RPM-FS machine and a 12s/10p SPM-FS machine is conducted with the same overall dimensions, main material properties, current density, and DC-link bus voltage. The electromagnetic torque performances of two flux-switching machines are analyzed and compared from two perspectives, i.e., magnetic field modulation and torque-sizing equation. Some conclusions can be summarized as followed.

1) The RPM-FS and SPM-FS machines are both featured with doubly-salient structures. Hence, both the primitive PM-MMF and armature reaction-MMF are modulated by the salient iron cores in air-gap field.

2) The electromagnetic torque of the RPM-FS machine is mainly contributed by the PM-MMF harmonics with rotor-PM pole-pair number (83%). However, for the SPM-FS machine, \( T_e \) is not only produced by the primitive PM-MMF harmonics with 6th and 18th, but also generated by the modulated PM-MMF harmonic components, i.e. 4th, 8th, 16th, and 28th.

3) For RPM-FS machines, the PMs are removed from stator to rotor, which results in a significant alleviation of the slot areas for armature windings. Hence, the electrical loading is improved effectively and the magnetization saturation of stator teeth can be reduced correspondingly. Consequently, the torque characteristics can be significantly improved.

4) The speed regulation range of the SPM-FS machine is unfavorably narrower than the RPM-FS machine, since the former exhibits a higher PM flux linkage and lower \( d \)-axis armature reaction flux-linkage \( L_{dR} \). In addition, the flux-weakening capability of RPM-FS machine can be enhanced further by adjusting the \( k_{hR} \) meanwhile, the output torque sacrifices correspondingly.
5) The PM utilization ratio of the RPM-FS machine is considerably larger than the SPM-FS machine, which dramatically influences the material cost consumed.

6) The PMs of the RPM-FS machines are located in the rotor, and consequently, the rotor structure is more complex than the SPM-FS machines. Further, the mechanical strength investigation of RPM-FS machines especially under high-speed is the work undergoing.

In general, the torque production mechanism of flux switching machines with different topologies can be investigated based on filed modulation principle and magnetic gearing effect. On the other hand, the torque capability and speed regulation capacity are dominantly determined by the magnetic and electoral loadings, which should be improved by optimizing the key geometric dimensions or investigating novel topologies.

REFERENCES


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