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**Optimal Design of a Wide Area Measurement System Using Hybrid Wireless Sensors and Phasor Measurement Units**

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**Abstract:** Real-time monitoring of the power system by phasor measurement units (PMUs) leads to the development of such devices in a wide area measurement system (WAMS). However, the power system observability cannot be obtained by employing only PMUs. The communication infrastructure (CI) is a significant part of the WAMS that has to be optimally designed and implemented to collect data from PMUs and deliver them to control centers. In this paper, a novel hybrid wireless sensor network is proposed for the connection of PMUs throughout the system to enable convenient and low-cost communication media. The problem of observability in the communication system is checked along with the optimal placement of PMUs in the power system to reach full observability. A hybrid wireless sensor network including plug-in powered sensor nodes (PPSNs) and energy harvesting sensor nodes (EHSNs) is utilized for increasing the reliability of the communication system. In the proposed co-optimal PMU-sensor placement problem, the main objective is to minimize the total cost of PMU placement and the related communication system, considering full observability of the power system and CI. To achieve better results, the zero-injection bus (ZIB) effect and system observability redundancy index (SORI) are considered as a constraint in the objective function. A binary-coded genetic algorithm is used for solving the proposed mixed-objective optimization problem subject to different technical operating constraints. The proposed method is examined on IEEE 13-bus and IEEE 37-bus test feeder systems. The results show the applicability and effectiveness of the proposed method compared with the conventional methods in this subject area.

**Keywords:** wide area measurement system (WAMS); phasor measurement unit (PMU); communication infrastructure; observability; hybrid wireless sensor

1. Introduction

Today’s increasing electricity consumption, together with the restructuring of power systems, causes new challenges in the operation, control, and monitoring of such networks. In this regard, the use of a supervisory control and data acquisition (SCADA) system is not sufficient to ensure the stability and security of the system. SCADA systems usually do not enable a synchronous data set [1]. Also, the sampling rate is not high in such systems. Thus, the information of SCADA systems displays the system’s semi-stable status, and the operators in control centers do not have the right information about the system’s dynamic conditions [2].
To enable reliable data measurement, the wide area measurement system (WAMS) has been developed to compensate for the disadvantages of the SCADA system [3,4]. The phasor measurement unit (PMU) is the main part of a WAMS. In fact, by measuring the voltage and current angles and increasing the sampling rate and simultaneous measurement capability, the previous disadvantages could be eliminated [5].

In order to estimate the true state of a system, observability is a must [6], meaning that if all the state variables of a network are determined, the network will be fully observable. PMU can measure the voltage phasor and related current phasors of a bus. Using this characteristic, the number of buses that need to be measured will be reduced [7,8]. However, owing to the high cost of PMU installation, determination of the minimum number of PMUs for observability of a system is an important issue that needs further attention [9].

In recent research works, many methods have been presented to solve the optimal PMU placement (OPP) problem while considering the observability of the system [10]. The main goal is to reduce the WAMS cost by minimizing the number of PMUs [11]. The proposed methods for solving the OPP are divided into two groups: mathematical-based approaches and heuristic methods. One of the most applicable methods of the first type is integer linear programming (ILP) [12]. Heuristic algorithms, such as genetic algorithm [13], Tabu search [14], and binary particle swarm [15], are also used frequently for solving the OPP problem.

All of the aforementioned methods follow the aim of minimizing the number of PMUs that guarantee the full observability of the power system subject to several aspects such as contingency [16], redundancy [17], reliability assessment [18], and so on. In the work of [19], an integer linear programming model is proposed for the OPP. This research shows that the optimal solution of the OPP cannot be achieved without considering the zero-injection buses (ZIB). Also, with regard to multiple solutions of the OPP, two indices are defined for the ranking of solutions; the bus observability index (BOI) and system observability redundancy index (SORI). The same problem is addressed in the work of [20], where the effect of ZIBs in contingency constrained OPP is investigated using an auxiliary variable.

Conventional measurement (CM) assets in a network such as injection measurement (IM), voltage measurement (VM), and power flow measurement (PFM) units also play an important role in the OPP problem, as pepper modeling of CMs and ZIBs can decrease the number of PMUs for the observability of WAMS. To this end, some studies have invested a great deal of effort into efficiently using CMs and ZIBs to reduce the required number of PMUs for full observability of a system. The effect of ZIBs and PFM on the OPP is considered in the work of [21]. In the work of [22], the effects of VM, IM, PFM, and ZIBs in the OPP are proposed using a modified bus merging method. A combination of SCADA and the WAMS measurements for the OPP problem with respect to the voltage magnitude estimation and voltage controllability is proposed in the work of [23]. The objective of this paper is state estimation with the minimum number of measurement devices.

Individual placement of PMUs and communication infrastructures cannot provide a globally optimal solution to WAMS. Therefore, a bunch of research works has been dedicated to considering the optimal PMU and communication infrastructure placement, simultaneously. In the work of [24], optimal PMU-communication link placement has been proposed and demonstrated that such co-placement could end in system-wide optimality. In the work of [25], the optimal placement of the phasor data concentrator (PDC) has been added to the objective function, and a combined approach based on binary imperialistic competition algorithm and Dijkstra algorithms has been used to solve the optimization problem. Likewise, optimal PMU-communication link placement is done in the work of [26], considering the bandwidth cost of the communication system. Data security in PMU communication system is considered in the work of [27]. A microwave communication technology instead of the conventional fiber-based links is proposed in the work of [28], where the objective is to minimize the propagation delay in the optimal placement of PMUs, PDC, and communication links. The authors in [29] have implemented the optimal micro-PMU placement for distribution networks using the greedy algorithm.
They showed that the proposed model could be effectively used for observability analysis at the distribution level.

In most of the reviewed literature, studies have assumed that the communication links are based on conventional optical fiber cables. The fiber-link communication needs a major infrastructure and a very high investment cost would be inevitable. As an alternative, wireless sensors can be effectively used to yield a low-cost communication system with a simple infrastructure.

Today, wireless sensors are extensively used in different applications such as medical care [30], environment monitoring [31], smart city [32], various industries automation [33], and smart homes [34]. However, most conventional wireless sensors are driven by batteries with limited lifetimes, making the maintenance and replacement of battery-powered sensor nodes (BPSNs) a very difficult or even impossible task [35]. Many types of research have been done to minimize the energy consumption of these sensors or to maximize battery lifetime [36]. Energy harvesting sensor nodes can be used to solve the lifetime problem of battery-based sensors. EHSN can harvest energy from environmental sources and convert it into usable electrical energy for wireless sensors [37]. Another group of wireless sensors is the plug-in powered sensor nodes (PPSNs) that can be energized from an external source.

In this paper, the optimal PMU and their communication links’ placement is done using a combination of PPSNs and EHSNs. The objective function includes the total cost minimization subject to power system observability and communication constraints. The cost of this system relates to PMU cost and communication system cost. The effect of ZIBs and SORI are also included in the model to get a more practical, yet optimal result. A binary-coded genetic algorithm is used for solving the proposed mixed-objective optimization problem. In this problem, there are two major constraints: communication constraint and observability constraints, both from the power system (PMUs) and communication network (WSNs) perspectives. As a whole, the main motivations and contributions of this study can be summarized as follows:

- An efficient and low-cost communication infrastructure is proposed based on PPSNs and EHSNs to enable secure communications among PMUs and the control center,
- The combination of PPSNs and EHSNs for setting up the communication infrastructure in the power system is analyzed in terms of economy and observability,
- The impacts of ZIB and SORI are simultaneously investigated in designing a communication infrastructure.

The rest of this paper is organized as follows. A problem definition is presented in Section 2. The problem formulation and the proposed optimization method are detailed in Section 3. The numerical study and simulation results are presented in Section 4, while conclusions are drawn in Section 5.

2. WAMS Structure

Along with the SCADA system, WAMS has been developed to compensate for the shortcomings of the SCADA system. PMUs are the main component of the WAMS that can measure the voltage and current phasors with high precision (less than 0.1% error) and high speed (up to 60 samples per second). PMUs use the global positioning system (GPS) to synchronize measured data. If enough PMUs are installed in different buses, the system will be observable and the system operator can truly estimate the state of the system. Therefore, one of the important issues is finding the optimal number and location of the PMUs to have a fully observable system, while being economic and viable in practice.

Generally, there are three levels in WAMS: data acquisition, data transferring, and data processing. In the first step, the measured data are provided by the measuring devices such as PMU, IM, VM, and PFM. The second level is transferring and delivering data to the control center through communication infrastructure, which can vary according to the type of network. The last level is the energy management system (EMS). In this step, the provided data are processed and optimal actions in terms of state estimation (SE), optimal power flow (OPF), load flow (LF), and so on will be determined based on the required output.
In this paper, for the first level, the PMU is utilized. In order to model the power system, there are two node sets: the nodes with load or generation that is called a non-zero-injection bus, and the set of nodes without associated load or generation, so-called ZIBs. The existence of PMUs and considering the effect of ZIBs can decrease the number of measurement devices that are needed for full observability of the power system. These issues will be described in the next section.

In the second level, a combined wireless sensor structure is proposed for setting up communication infrastructure. The PPSNs and EHSNs are used for delivering data to the PDC. It is assumed that the location of the PDC is determined and fixed. In fact, unlike conventional communication networks such as optic fiber links, a combination of PPSNs and EHSNs is used for communication infrastructure.

The provided data by the measurement system and CI can be processed in the third level to fulfill the objectives of the system operator. In the next section, the formulation of the proposed method is presented.

3. Problem Formulation

In this paper, OPP and the related communication system using wireless sensors are studied. The minimization of measurement units and wireless sensor-based communication considering the system constraints is the objective. To this end, the OPP problem considering ZIBs and redundancy is initially defined and formulated. Then, the communication system requirements are discussed. In the next step, the observability aspects of the wireless sensor network are presented. Finally, the structure of the proposed solution method based on a binary-coded genetic algorithm is described.

3.1. Optimal PMU Placement

Because of the high price of PMUs, it is not economical to set up all system nodes with such devices. Thus, the right direction for optimizing the placement of PMUs in a power grid is to use the least number of measuring devices corresponding to the minimum cost and to establish full observability of the network with the mentioned measurements.

A power grid is fully observable if all of its buses can be observed. By definition, a node in the power system is observable if that node or any of its adjacent nodes (which are connected to the target node) is equipped with a PMU. In other words, the presence of a PMU in a bus is adequate for the observability of all adjacent buses. Accordingly, the OPP problem can be derived as follows [19]:

\[
\begin{align*}
\text{Min} & \quad \sum_{i=1}^{n} \omega_i x_i, \\
\text{s.t.} & \quad f_i \geq 1 \quad i \in I,
\end{align*}
\]

where \( n \) is the number of buses, \( \omega_i \) is the cost of purchasing and installing PMUs, and \( I \) is the set of buses. \( f_i \) is the observability function at the bus \( i \), which is defined as follows:

\[
f_i = \sum_{j \in I} A_{i,j} x_j \quad \forall i \in I,
\]

where \( A \) is the connectivity matrix and \( X \) is the PMU installation matrix. If the number of network buses is equal to \( n \), then the connectivity matrix of the system will be \( n \times n \), which is formed as follows:

\[
A_{n \times n(i,j)} = \begin{cases} 
1 & i = j \\
1 & \text{if bus } i \text{ and } j \text{ are connected} \\
0 & \text{otherwise}
\end{cases}
\]
Moreover, the existence of a PMU in a bus can be represented mathematically as follows:

\[ x_i = \begin{cases} 
1 & \text{if a PMU is installed at bus } i \\
0 & \text{otherwise} 
\end{cases} \quad (5) \]

The \( X \) vector contains all the \( x_i \) variables.

\[ X = [x_1 \ x_2 \ldots x_n]^T \quad (6) \]

For full observability of the power system, all of the indices in Equation (2) should be 1 or greater than 1, meaning that each bus should be observable by at least one PMU.

### 3.2. Effect of Zero-Injection and Redundancy

In a ZIB, there is no generation and load. In fact, no current is injected in a ZIB. A ZIB and its adjacent buses are called a set of zero injection bus (SOZIB) \([22]\). Observability of \( N \) nodes of SOZIB is adequate for full observability of a SOZIB. Therefore, the existence of a ZIB can decrease the number of PMUs that is needed for the observability of a system. For example, in Figure 1, if none of the nodes are ZIBs, at least two PMUs are needed for full observability of the network. They can be placed, as an example, on node 1 and 5. However, if bus 2 is assumed to be a ZIB, then one PMU will be enough to make the system observable (i.e., one PMU at node 5) and SOZIB can be realized as follows:

\[ \text{SOZIB}_2 = \{1, 2, 3, 5\} \quad (7) \]

![Six-node test system.](image)

In the case of modeling the ZIBs in the objective function, an integer linear programming model can be used, where a new variable \( u_i \) is defined for observability of node \( i \) \([19]\) (i.e., \( u_i = 1 \) if the node is observable, and \( u_i = 0 \) otherwise). In this regard, if \( N-1 \) nodes of SOZIB are observable, then the entire nodes with the set are observable. Thus, an equation will be added to the model as follows:

\[ \sum_{k \in \text{SOZIB}_i} u_k \geq |\text{SOZIB}| - 1 \quad \forall \ i \in Z, \quad (8) \]

where \( Z \) is the set of zero injection buses. Now, in Figure 1, and supposing that node 2 is a ZIB, the additional constraint in the ILP formulation is as follows:

\[ u_1 + u_2 + u_3 + u_5 \geq 3. \quad (9) \]

This equation means that out of the four nodes, 1, 2, 3, and 5, at least three nodes should be observable. Considering the effect of zero injection buses, the mathematical model in Section 3.1 can be modified as below:

\[ \text{Min} \ \sum_{i=1}^{n} w_i x_i, \quad (10) \]
\[ s.t. \quad A \cdot X \geq u, \quad (11) \]
\[ u_j = 1 \quad \forall j \notin \text{SOZIB}_1 \cup \text{SOZIB}_2 \ldots \cup \text{SOZIB}_z, \quad (12) \]
\[ \sum_{k \in \text{SOZIB}_i} u_k \geq |\text{SOZIB}| - 1 \quad \forall i \in Z. \quad (13) \]

There are multiple solutions for OPP in a given power system. For example, without considering ZIBs in Figure 1, we can place PMUs at node 2 and 5 or 1 and 5. For selecting a better result, a bus observability index (BOI) is defined [19]. BOI\(_i\) is the number of PMUs that can observe the \(i\)-th bus. The sum of BOIs for all nodes of the network is called the system observability redundancy index (SORI). SORI can be defined as follows:

\[ \text{SORI} = \sum_{i=1}^{n} \text{BOI}_i. \quad (14) \]

In the six-node test system described earlier, if the PMUs are located at nodes 2 and 5 (case a), the BOIs for nodes 1 to 6 are 1, 2, 2, 1, 2, 1. But if the PMUs are located at nodes 1 and 5 (case b), the BOIs for nodes 1 to 6 are 1, 2, 1, 1, 1, 1. Hence, SORIs for the two cases are equal to SORI\(_a\) = 9 and SORI\(_b\) = 7, respectively. From a technical perspective, the first case (i.e., case a with higher SORI value) is the best choice for PMU placement. In fact, maximizing this index relates to maximizing the remaining observable buses in case of missing a PMU. For example, missing the PMU installed at node 5 results in the unobservability of nodes 4 and 6 in case a. However, in case b, nodes 3, 4, 5, and 6 will be unobservable, as the mentioned PMU is lost. Thus, the redundancy of observability can be measured with SORI.

### 3.3. Communication System

In this study, wireless sensor networks are used as the communication system. There are some sensor nodes in this network. Each sensor has characteristics similar to the measurement of the required data and processing and sensing them to adjacent nodes [38]. A given sensor node consists of five elements: sensor unit, processing unit, receiving and sending unit, energy management unit or power supply unit, and eventually accessory equipment. Moreover, each sensor could be used in the role of a router with sending the collected information by the sensor itself and the received information from the adjacent nodes to the sink node (i.e., control center).

Most conventional wireless sensors are battery-driven. Given the fact that switching or replacing these sensors is very difficult or almost impossible in some cases, their energy consumption is a fundamental issue. EHSN can be used to solve the lifetime problem of battery-based sensors. EHSN can harvest energy from available environmental sources such as vibration, solar energy, and wind. The harvested energy can be then converted into usable electrical energy for wireless sensors. Owing to new EHSNs technology, some types of these sensors benefit from a hybrid structure, having both battery-powered and energy-harvested features at the same time.

In this paper, the connection of PMUs is performed using a combination of PPSNs and EHSNs. To achieve this goal with the highest reliability, the network is divided into two categories: the nodes measured by PMU, and the router nodes. In the first group, PPSNs are used as the sensor can be fed directly by the PMUs. The second group benefits from the EHSNs to assure longer lifetimes. By doing so, the reliability of the system can be improved [39].

As illustrated in Figure 2, the connection among PMUs should be made through EHSNs. The dashed-dotted lines between the yellow points represent the connection and the route between the EHSNs to send the PMU data to the control center. Thus, the minimum number of sensors to the control center must be found. Here, a number of assumptions are made. First, it is assumed that wireless sensors can transfer the PMUs data completely, that is, there is no packet loss in data.
transmission. Second, the bandwidth of wireless sensors is supposed to be sufficient for transferring PMUs’ measured data.

Figure 2. Communication system. PMU, phasor measurement unit; EHSN, energy harvesting sensor node; PPSN, plug-in powered sensor node.

With the mentioned assumptions, the structure of the communication system can be well constructed. However, because the wireless sensors are used as the communication system, the observability analysis from the viewpoint of the communication system is necessary. This issue will be considered in the next section.

3.4. Communication System Observability

Transferring the measured data to the control center should be done after the OPP. In conventional systems based on optic fiber-cables, it is not necessary to analyze the observability, because the cables connect the entire nodes. However, in wireless communication systems, similar to the PMUs placement, the observability analysis has to be done to be sure that wireless sensors can communicate with each other and with the control center. A node in the communication system is observable if there is a connection between that node and the reference node. The reference node in this research is the control center. In other words, a wireless node is observable if it is not islanded [39].

For analyzing the communication system observability, a mesh grid of the power network is initially created. The geographical area where the distribution network is located is divided into a set of equal sub-areas/meshes, as shown in Figure 3. Wireless sensors can be placed in any mesh and the presence of a sensor in an area could cover the observability of the adjacent areas. According to Figure 3, the relationship between the transmitting range ($tr$) of the wireless sensors and the length of each mesh ($d$) is as follows:

$$d = \frac{2}{3\sqrt{2}} tr.$$  (15)
As can be seen, the examined eight-bus power system could be observable through the placement of the two PMUs in buses 4 and 8. It is assumed that bus 8 is the control center. However, if the distance between buses 4 and 8 is greater than the transmission range (tr) of PPSNs, the communication system is unable to transmit data to the center. Thus, it will not be observable.

The difference between observability from the power system and communication network perspectives is shown in Figure 4. As can be seen, the examined eight-bus power system could be observable through the placement of the two PMUs in buses 4 and 8. It is assumed that bus 8 is the control center. However, if the distance between buses 4 and 8 is greater than the transmission range (tr) of PPSNs, the communication system is unable to transmit data to the center. Thus, it will not be observable.

![Figure 3. Transmitting range of wireless sensor and its relation to the length of the mesh grid.](image)

![Figure 4. Eight-bus test system for a communication system observability analysis.](image)
The $n_1$ and $n_2$ can be calculated having the length and width of the geographical area, and the mesh grid is created. As can be seen, a router sensor is needed to complete the observation of the communication network. As can be seen in Figure 4, bus 6 is located in the common transmission range of the two sensors, and thus can be selected as a router node. In the larger networks, however, an optimization problem has to be solved for optimal placement of wireless sensors with respect to observability constraint.

A binary genetic algorithm is used in this study for optimal placement of wireless sensors following the optimal placement of PMUs based on the power system observability constraint. The chromosome is coded in such a way to reflect the existence and position of the primary sensor units that are derived from the observability problem of the power system. It is supposed that in each node in which a PMU exists, a PPSN can also be placed. Thus, the number of elements in the chromosome (CR) is equal to the total number of meshes ($N_T$), while each could be assigned a binary value (1 having PPSN, and 0 otherwise):

$$CR = [SN_1 \ SN_2 \ SN_3 \ \ldots \ \ldots \ SN_n]_{1 \times N_T},$$  \hspace{1cm} (18)

$$SN_i = \begin{cases} 1 & \text{with PPSN} \\ 0 & \text{without PPSN} \end{cases}.$$  \hspace{1cm} (19)

For example, vector CR for Figure 4 can be created as follows:

$$CR = [0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0],$$  \hspace{1cm} (20)

Having formed the initial population, the distance matrix has to be determined as follows:

$$L = \begin{bmatrix} L_{11} & L_{12} & \ldots & L_{1n} \\ L_{21} & L_{22} & \ldots & L_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ L_{n1} & L_{n2} & \ldots & L_{nn} \end{bmatrix},$$  \hspace{1cm} (21)

where $L_{ij}$ is the distance of area $i$ from area $j$ in the mesh grid. Two areas $i$ and $j$ are in connection with the two following conditions:

1. Both of them should have wireless sensors ($tr_i \neq 0$ and $tr_j \neq 0$);
2. The wireless node in one region is located in the coverage range of the wireless node of the other area ($tr_i \geq L_{ij}$ or $tr_j \geq L_{ij}$).

In order to determine the connection between the areas, a matrix called the incident matrix (IM) is defined as follows:

$$IM_{ij} = CR_i \times CR_j \times (tr_i \geq L_{ij}) \times (tr_j \geq L_{ij}).$$  \hspace{1cm} (22)

The matrix size is $N_T \times N_T$. If the number of network buses is $N$, the communication observability matrix can be used for observability analysis of communication system [40]. This matrix can be defined as follows:

$$CO = sign(IM^{N-1}).$$  \hspace{1cm} (23)

Matrix CO shows the connectivity of the nodes to the control center. If the control center is in area $S$ and the set of all communication nodes is $Z$, for complete observability of communication system, relation (24) should be met.

$$CO_{sj} = 1 \ \forall j \in Z.$$  \hspace{1cm} (24)

To achieve the lowest cost, the least number of router sensors must be detected. This is done through an optimization process detailed in the next section.
3.5. Proposed Objective Function

In the previous sections, the model of the power system and communication network used in this paper was presented. The cost of communication infrastructure is as essential as PMU placement costs in the WAMS. So, in the proposed method, the communication infrastructure and PMU placement are simultaneously optimized. Cost function includes the minimization of PMU-communication links’ placement costs, as defined in (25), considering the communication and observability constraints.

\[
Total \ Cost = Cost_{PMU} + Cost_{WSN},
\]

where \(Cost_{PMU}\) is the total cost of OPP in the network and \(Cost_{WSN}\) is the cost of sensors placement that is necessary for complete data transferring. As there exist multiple solutions for OPP, the SORI index is defined for observability ranking and solution selection. This index is presented as a constraint in the optimization problem. Depending on how important the SORI is, the constraint could be tightened. Thus, the objective function can be written as below:

\[
\begin{align*}
\text{Min} & \sum_{i=1}^{N} C_i X_i + C_{P} NP + C_{E} NE \\ 
\text{St.} & AX \geq 1, \\
& \sum_{k \in SOZIB} u_k \geq |SOZIB| - 1 \ \forall i \in Z, \\
& CO_{n-1,j} = 1 \quad j = 1,2,\ldots,m, \\
& SORI \geq R_{\text{min}},
\end{align*}
\]

where

- \(C_i\): cost of PMU in bus \(I\);
- \(X_i\): status of installing a PMU in bus \(I\);
- \(N\): number of buses;
- \(C_{P}\): cost of PPSN;
- \(NP\): number of PPSNs;
- \(C_{E}\): cost of EHSN;
- \(NE\): number of EHSNs;
- \(m\): total number of wireless sensors;
- \(R_{\text{min}}\): a coefficient that shows the impact of SORI.

Equation (27) represents the observability of the power system that is described in Section 3.1. The effect of zero-injection buses is considered as a constraint in Equation (28) that is defined in Section 3.2. As described before, for proper implementation of the wireless sensor, the observability analysis of these sensors should be done. Thus, Equation (29) describes the communication infrastructure observability that is defined in Section 3.4. Equation (30) is the SORI constraint. The effectiveness of this constraint relates to the \(R_{\text{min}}\) coefficient. For example, if the SORI importance is very high, the coefficient is increased according to the operator’s requirement.

A flowchart of the proposed method is illustrated in Figure 5, where three main steps are defined to reach a solution. At the first step, the optimal placement of PMUs is calculated with regard to the full observability, ZIBs, and SORI constraints.
Figure 5. Flowchart of the proposed method. ZIB, zero-injection bus; SORI, system observability redundancy index.
In the second step, the optimal placement of wireless sensors (PPSNs and EHSNs) is determined with respect to the communication observability constraint. In the last step, all possible co-optimal placement solutions are evaluated to achieve the best one in terms of the minimum total cost. A detailed review of each step is given below.

**Step 1**: The algorithm is initialized in block A with a set of input data including the number of buses, distance, and connections. Optimal PMU placement is implemented in block B considering the observability constraint and ZIBs and SORI index using Equations (10)–(14). It is important to note that more than one optimal solution might be found at this stage. However, all the candidate solutions will be evaluated in block I to reach the best optimal one.

**Step 2**: In block C, the mesh grid for proper placement of the wireless sensors is formed according to Equations (15)–(17). On the basis of the OPP result, the initial population is formed according to Equations (18) and (19) in block D. To transfer the data to the control center, a wireless sensor as the sink node should be selected, which is done in block E. It is assumed that the location of the control center is predetermined and remains unchanged during the program iterations. In block F, minimization of the number of wireless sensors (Equation (26)) is done with respect to communication observability constraints (Equation (29)). The cost of each possible solution with respect to constraints is calculated in block G. It should be noted that block H represents the stop criterion (which is set to a maximum number of iterations) for the genetic algorithm.

**Step 3**: For achieving the best solution, all possible solutions stored in the repository should be evaluated. As noted before, PMU placement can usually be done in multiple ways, and each plan of action has a related communication cost. In the last step, after optimization of wireless sensor placement in all possible cases, the best solution in terms of the minimum total cost is reported. It should be noted that block I denotes the stop condition for exploring different OPP solutions.

4. Case Study and Discussion

In this section, the proposed method is implemented on sample networks to examine the advantages of using hybrid wireless sensors in WAMS. The IEEE test systems are utilized to test the proposed method. The sample networks are IEEE 13-node and 37-node test feeders [41]. In each case, genetic algorithm parameters are set (calibration was done by trial and error), as reported in Table 1, where PC is the probability of crossover and PM is the probability of mutation. The population size is also a tradeoff between the exploration capability and computational burden. In this paper, the population size is selected by running the program and tracking the ability to obtain a global solution and satisfying the constraints.

<table>
<thead>
<tr>
<th>Network</th>
<th>Population Size</th>
<th>PC</th>
<th>PM</th>
</tr>
</thead>
<tbody>
<tr>
<td>IEEE 13 node</td>
<td>100</td>
<td>0.8</td>
<td>0.3</td>
</tr>
<tr>
<td>IEEE 37 node</td>
<td>150</td>
<td>0.75</td>
<td>0.35</td>
</tr>
</tbody>
</table>

4.1. IEEE 13-Node Test Feeder

The schematic of this test system is illustrated in Figure 6. The network is considered in two cases: Case I, where co-optimal placement is done regardless of the ZIB effect; and Case II, while considering ZIBs.
4.1.1. Case I: Co-Optimal Placement without ZIB Effect

A binary-coded genetic algorithm (BCGA) is used to determine the multiple solutions of OPP with a binary variable, according to the method presented in the work of [42]. The choice of BCGA is mainly owing to its simplicity of implementation and the fact that the algorithm could provide alternative solutions with the adjustment of tunable parameters such as population, generation, and EliteCount, which in turn provides the system planner with a portfolio of different solutions among which to choose. Multiple solutions and related SORI for this network with respect to power system observability constraint are shown in Table 2. Using the simultaneous optimization process (Equations (26)–(30)), the best position of PMUs and wireless sensors considering the communication and power systems observability and SORI constraints could be obtained. If it is assumed that $R_{\text{min}} = 22$, according to Table 2, only solutions 4, 6, 7, and 8 can be considered with respect to the SORI constraint.

Table 2. Phasor measurement unit (PMU) placement solutions for a 13-node test feeder without the zero-injection bus (ZIB) effect. SORI, system observability redundancy index.

<table>
<thead>
<tr>
<th>Solution</th>
<th>PMU Installation Nodes</th>
<th>SORI</th>
<th>Solution</th>
<th>PMU Installation Nodes</th>
<th>SORI</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2, 4, 7, 8, 12, 13</td>
<td>20</td>
<td>13</td>
<td>2, 4, 7, 11, 12, 13</td>
<td>15</td>
</tr>
<tr>
<td>2</td>
<td>2, 4, 5, 7, 8, 12</td>
<td>21</td>
<td>14</td>
<td>3, 4, 7, 11, 12, 13</td>
<td>17</td>
</tr>
<tr>
<td>3</td>
<td>3, 4, 7, 8, 12, 13</td>
<td>21</td>
<td>15</td>
<td>2, 4, 7, 9, 11, 13</td>
<td>17</td>
</tr>
<tr>
<td>4</td>
<td>3, 4, 5, 7, 8, 12</td>
<td>22</td>
<td>16</td>
<td>3, 4, 7, 9, 11, 13</td>
<td>19</td>
</tr>
<tr>
<td>5</td>
<td>2, 4, 7, 8, 9, 13</td>
<td>21</td>
<td>17</td>
<td>2, 4, 7, 11, 12, 13</td>
<td>18</td>
</tr>
<tr>
<td>6</td>
<td>2, 4, 5, 7, 8, 9</td>
<td>22</td>
<td>18</td>
<td>3, 4, 7, 11, 12, 13</td>
<td>19</td>
</tr>
<tr>
<td>7</td>
<td>3, 4, 7, 8, 9, 13</td>
<td>22</td>
<td>19</td>
<td>2, 4, 5, 7, 9, 11</td>
<td>19</td>
</tr>
<tr>
<td>8</td>
<td>3, 4, 5, 7, 8, 9</td>
<td>23</td>
<td>20</td>
<td>3, 4, 5, 7, 9, 11</td>
<td>20</td>
</tr>
<tr>
<td>9</td>
<td>1, 3, 5, 7, 8, 9</td>
<td>19</td>
<td>21</td>
<td>1, 3, 5, 7, 9, 11</td>
<td>17</td>
</tr>
<tr>
<td>10</td>
<td>1, 3, 5, 7, 8, 12</td>
<td>18</td>
<td>22</td>
<td>1, 3, 5, 7, 11, 12</td>
<td>16</td>
</tr>
<tr>
<td>11</td>
<td>1, 3, 7, 8, 12, 13</td>
<td>17</td>
<td>23</td>
<td>1, 3, 7, 9, 11, 13</td>
<td>16</td>
</tr>
<tr>
<td>12</td>
<td>1, 3, 7, 8, 9, 13</td>
<td>18</td>
<td>24</td>
<td>1, 3, 7, 11, 12, 13</td>
<td>15</td>
</tr>
</tbody>
</table>

According to Section 3.2, there is one PPSN in each bus in which PMU is installed. On the basis of the configurations tabulated in Table 2, the network is observable from the power system’s viewpoint. However, it lacks observability features in the communication network. To handle this issue, EHSNs, as router nodes, must be placed throughout the network for transferring data to the control center. Node 4 is chosen as the control center.

It is assumed that the transmitting range ($tr$) of each PPSN and EHSN is equal to 100 meters. The length and width of the network are about 900 m and 400 m. With these data, the mesh grid for...
communication observability analysis is constructed using Equations (15)–(17). The calculated values are as follows:

\[
d = 47.6 \text{ m}
\]

\[
n_1 = \left[ \frac{W_1}{d} \right] + 1 = \left[ \frac{400}{47.6} \right] + 1 = 9
\]

\[
n_2 = \left[ \frac{W_2}{d} \right] + 1 = \left[ \frac{900}{47.6} \right] + 1 = 19
\]

\[
N_T = n_1 \times n_2 = 171
\]

The simultaneous optimization process is coded in genetic algorithm again for co-optimal placement of PMUs and wireless sensors with regard to the mentioned constraints. Because there are 171 sections in the mesh grid, the chromosome (CR vector) has 171 genes. EHSNs are placed in each area, as a router, according to the optimization problem. The results of the optimization problem for this network are shown in Table 3. In this case study, it is assumed that the price of each PMU is about $40,000 and the prices of each PPSN and EHSN are about $80 and $100, respectively. Note that the PPSNs are installed at the same nodes where PMUs exist, thus there is no special infrastructural need. However, the EHSNs need additional structures to be set up. The cost of each infrastructure is assumed to be $150. Therefore, the price of each EHSN is regulated as $250 [43].

Table 3. Optimization problem result. PPSN, plug-in powered sensor node; EHSN, energy harvesting sensor node.

<table>
<thead>
<tr>
<th>Solution</th>
<th>PMU Installation Node</th>
<th>PPSN Installation Node</th>
<th>EHSN Area Number</th>
<th>SORI</th>
<th>Total Cost (in US $)</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>3,4,5,7,8,12</td>
<td>3,4,5,7,8,12</td>
<td>39,51,53,69,70,88,106,124,131,133,151</td>
<td>22</td>
<td>243,230</td>
</tr>
<tr>
<td>6</td>
<td>2,4,5,7,8,9</td>
<td>2,4,5,7,8,9</td>
<td>39,43,59,67,85,103,121,131</td>
<td>22</td>
<td>242,480</td>
</tr>
<tr>
<td>7</td>
<td>3,4,7,8,9,13</td>
<td>3,4,7,8,9,13</td>
<td>40,43,59,77,87,105,123,131</td>
<td>22</td>
<td>242,480</td>
</tr>
<tr>
<td>8</td>
<td>3,4,5,7,8,9</td>
<td>3,4,5,7,8,9</td>
<td>40,43,59,77,87,105,125,131</td>
<td>23</td>
<td>242,480</td>
</tr>
</tbody>
</table>

As can be seen, solutions 6, 7, and 8 have a lower total cost. However, given that the SORI index in solution 8 is more than others, this case is chosen as the global best result. In fact, this result has a lower cost and higher SORI.

4.1.2. Case II: Co-Optimal Placement Considering the ZIB Effect

In this case, it is assumed that node 5 is a ZIB. For the determination of multiple solutions, a genetic algorithm is used according to Equations (10)–(13). In this case, because of the ZIB effect, using five PMUs is adequate for full observability of the network. The multiple solutions and related SORI for this network concerning observability constraints are shown in Table 4.

Table 4. PMU placement solutions for a 13-node test feeder considering ZIB effect.

<table>
<thead>
<tr>
<th>Solution</th>
<th>PMU Installation Nodes</th>
<th>SORI</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2,4,7,8,12</td>
<td>19</td>
</tr>
<tr>
<td>2</td>
<td>3,4,7,8,12</td>
<td>20</td>
</tr>
<tr>
<td>3</td>
<td>2,4,7,8,9</td>
<td>20</td>
</tr>
<tr>
<td>4</td>
<td>3,4,7,8,9</td>
<td>21</td>
</tr>
<tr>
<td>5</td>
<td>3,4,7,9,11</td>
<td>18</td>
</tr>
<tr>
<td>6</td>
<td>2,4,7,9,11</td>
<td>17</td>
</tr>
<tr>
<td>7</td>
<td>3,4,7,11,12</td>
<td>16</td>
</tr>
<tr>
<td>8</td>
<td>2,4,7,11,12</td>
<td>15</td>
</tr>
</tbody>
</table>

Given \( R_{\text{min}} = 20 \), only solutions 2, 3, and 4 will be chosen according to the SORI constraint. Similar to the previous section, the results of optimization for each possible solution are listed in Table 5.
Table 5. Optimization problem result (zero-injection effect).

<table>
<thead>
<tr>
<th>Solution</th>
<th>PMU Installation Node</th>
<th>PPSN Installation Node</th>
<th>EHSN Area Number</th>
<th>SORI</th>
<th>Total Cost (in US $)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>3,4,7,8,12</td>
<td>3,4,7,8,12</td>
<td>40,58,67,85,95,113,123,141,151</td>
<td>20</td>
<td>202,560</td>
</tr>
<tr>
<td>3</td>
<td>2,4,7,8,9</td>
<td>2,4,7,8,9</td>
<td>39,57,75,93,111,129</td>
<td>20</td>
<td>201,810</td>
</tr>
<tr>
<td>4</td>
<td>3,4,7,8,9</td>
<td>3,4,7,8,9</td>
<td>40,58,76,94,112,130</td>
<td>21</td>
<td>201,810</td>
</tr>
</tbody>
</table>

As can be seen, solutions 3 and 4 have a lower total cost. However, given that the SORI in solution 4 has a higher value, this scenario is chosen as the global best solution.

Comparing Tables 3 and 5 shows that considering zero-injection nodes can decrease the number of PMUs. The number of EHSNs is decreased in case II as a result of reducing the number of PMUs, and thus the total cost of the network is less than that in Case I.

4.2. IEEE 37-Node Test Feeder

The IEEE 37-node test feeder is shown in Figure 7. For more simplicity, the nodes are numbered from 1 to 37. Similar to the previous test system, two cases are considered: Case I, without the ZIB effect; and Case II, where co-optimal placement is done considering the ZIB effect. Here, it is assumed that nodes 5, 14, and 16 are zero-injection nodes. In this network, the PPSN and EHSN with higher transmitting range ($tr$) and higher price are chosen. The $tr$ is 150 meters and the price of each PPSN and EHSN and their infrastructure are about $120 and $300, respectively. According to the IEEE segment data, the values of Equations (15)–(17) can be calculated. Thus, in this case, $d = 70.17$, $n_1 = 11$, $n_2 = 24$, and $NT = 264$. Thus, the number of genes in each chromosome is equal to 264. The simulation results are listed in Table 6. The control center is chosen at node 2.

![Figure 7. IEEE 37-node test feeder.](image-url)
Table 6. Optimization problem result.

<table>
<thead>
<tr>
<th>Without ZIB Effect</th>
<th>Zero-Injection Effect</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>PMU Installation Node</strong></td>
<td>2,4,5,8,11,14,18,22,24, 27,32,35</td>
</tr>
<tr>
<td><strong>PPSN Installation Node</strong></td>
<td>2,4,5,8,11,14,18,22,24, 27,32,35</td>
</tr>
<tr>
<td><strong>EHSN Area Number</strong></td>
<td>59,66,87,88,92,94,95,114, 124,146,168,202,223,224,236</td>
</tr>
<tr>
<td><strong>SORI</strong></td>
<td>46</td>
</tr>
<tr>
<td><strong>Total Cost (in US $)</strong></td>
<td>485,940</td>
</tr>
<tr>
<td><strong>PMU Installation Node</strong></td>
<td>2,4,8,11,14,18,22,24, 27,32,35</td>
</tr>
<tr>
<td><strong>PPSN Installation Node</strong></td>
<td>2,4,8,11,14,18,22,24, 27,32,35</td>
</tr>
<tr>
<td><strong>EHSN Area Number</strong></td>
<td>54,63,83,88,92,94,95, 118,126,170,192,201,226,238</td>
</tr>
<tr>
<td><strong>SORI</strong></td>
<td>45</td>
</tr>
<tr>
<td><strong>Total Cost (in US $)</strong></td>
<td>445,520</td>
</tr>
</tbody>
</table>

It can be seen that in Case I, 12 PMUs and 15 EHSNs are needed for full observability of power system and communication network, while 11 PMUs and 14 EHSNs are needed in the second case. In other words, considering ZIBs leads to a decreased number of required PMUs.

The genetic algorithm will convergence in about 90 iterations in an IEEE 37-node test feeder, while this takes only 50 iterations in an IEEE 13-node test system. In this research, because of the simultaneous optimization of the power system and communication network, the complexity of the problem and the volume of calculations are increased. The population size is equal to the mesh grid number \(N_T\). In larger networks, given that the numbers of mesh grids are high, the required computations will increase. However, because of off-line programming, the computational burden is not a significant issue.

The results of the case studies showed that co-placement of the hybrid wireless sensors and PMUs can decrease the total cost of the system, while satisfying technical constraints in both power and communication systems. Moreover, the proposed communication infrastructure has relatively lower costs compared with the cost of a conventional system based on optical fiber cables or even the cost of PMU installation. For example, in the 37-node test system, the PMU placement cost considering the ZIB effect is $440,000. However, the communication infrastructure cost is $5520. The results of the work of [25] show that the optic fiber cables cost is considerable compared to PMU cost.

The results show that considering the ZIBs can decrease the total of WAMS. Comparing Tables 3 and 5 shows that considering the zero injection bus effect can decrease the total cost from $242,480 to $201,810. The difference is $40,670 (16.7%) in this case. Also, in the IEEE 37-node test feeder, the results of Table 6 show that the difference between the two cases (considering ZIBs and without considering ZIBs) is about 8.3%.

In addition to the economic aspect, reliability considerations are also of outstanding significance in co-optimal placement problems. The reliability of wireless sensors can be considered in two parts: sensor node reliability and wireless link reliability.

5. Conclusions

This paper presented a hybrid wireless sensor network as a communication infrastructure for the PMU placement problem. The wireless sensors were used as the links of the WAMS. The applicability and advantages of this communication system were evaluated. The main advantages of this system were identified as low placement and installation costs and simple infrastructure. The results also showed that using the proposed method, the communication infrastructure cost is not only much lower than the PMU installation costs, but also lower than those of conventional fiber-link optic communication systems. However, for proper implementation of the proposed communication infrastructure, high-level wireless sensors are needed.

In smart energy systems, where data measurement and processing is vital for secure and optimal operation and control of the system, more studies should be carried out on measurement devices,
their connections, and interoperability. The reliability and security of such devices are also significant for better performance of the systems. In future works, more focus will be given to the mentioned aspects of monitoring energy systems. Also, more detailed analyses will be made on bandwidth and data transferring capability of the high-tech wireless sensors as the backbone of the proposed communication infrastructure in this work.

**Abbreviation**

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>PMU</td>
<td>Phasor Measurement Unit</td>
</tr>
<tr>
<td>WAMS</td>
<td>Wide Area Measurement System</td>
</tr>
<tr>
<td>PPSN</td>
<td>Plug-In Powered Sensor Node</td>
</tr>
<tr>
<td>EHSN</td>
<td>Energy Harvesting Sensor Node</td>
</tr>
<tr>
<td>ZIB</td>
<td>Zero-Injection Bus</td>
</tr>
<tr>
<td>CI</td>
<td>Communication Infrastructure</td>
</tr>
<tr>
<td>SORI</td>
<td>System Observability Redundancy Index</td>
</tr>
<tr>
<td>SCADA</td>
<td>Supervisory Control and Data Acquisition</td>
</tr>
<tr>
<td>OPP</td>
<td>Optimal PMU Placement</td>
</tr>
<tr>
<td>CM</td>
<td>Conventional Measurement</td>
</tr>
<tr>
<td>IM</td>
<td>Injection Measurement</td>
</tr>
<tr>
<td>ILP</td>
<td>Integer Linear Programming</td>
</tr>
<tr>
<td>BOI</td>
<td>Bus Observability Index</td>
</tr>
<tr>
<td>VM</td>
<td>Voltage Measurement</td>
</tr>
<tr>
<td>PFM</td>
<td>Power Flow Measurement</td>
</tr>
<tr>
<td>PDC</td>
<td>Phasor Data Concentrator</td>
</tr>
<tr>
<td>BPSN</td>
<td>Battery-Powered Sensor Node</td>
</tr>
<tr>
<td>GPS</td>
<td>Global Positioning System</td>
</tr>
<tr>
<td>EMS</td>
<td>Energy Management System</td>
</tr>
<tr>
<td>SE</td>
<td>State Estimation</td>
</tr>
<tr>
<td>OPF</td>
<td>Optimal Power Flow</td>
</tr>
<tr>
<td>LF</td>
<td>Load Flow</td>
</tr>
<tr>
<td>SOZIB</td>
<td>Set of Zero Injection Bus</td>
</tr>
</tbody>
</table>

**Author Contributions:** Conceptualization, A.B. and M.A.; formal analysis, A.B. and A.A.-M.; methodology, A.B., M.A., and A.A.-M.; validation, A.B., A.A.-M., and M.A.; writing—original draft preparation, A.B.; review and editing, A.A.-M., M.A., and J.P.S.C.

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**Conflicts of Interest:** The authors declare no conflict of interest.

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