HisRect: Features from Historical Visits and Recent Tweet for Co-Location Judgement

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Abstract—Enabled by smartphones, social media users are increasingly going mobile. This trend fosters various location based services on social media platforms (e.g., Twitter). Many services like friends notification and community detection benefit from co-location judgement, i.e., to decide whether two Twitter users are co-located in some point-of-interest (POI). This problem is challenging due to the limited information in tweets and the lack of explicit geo-tags in tweets that can be used as labeled data. Our approach to this problem is based on a novel concept of HisRect features extracted from users’ historical visits and recent tweets: The former has impacts on where a user visits in general, whereas the latter gives more hints about where a user is currently. In practice, labeled data is scarce. Therefore, we design a semi-supervised learning (SSL) framework that leverages unlabeled data to extract HisRect features. Moreover, we employ an embedding neural network layer to process HisRect features of two users, which decides co-location based on the embedding difference between the two features. Our model is extensively evaluated on two large sets of real Twitter data from more than one million users. The experimental results demonstrate that our HisRect features and SSL framework are highly effective at deciding co-locations. In terms of multiple metrics, our approach clearly outperforms alternative approaches using state-of-the-art techniques.

Index Terms—Twitter, POI, Co-Location Judgement, Semi-Supervised Learning

1 INTRODUCTION

Driven by smartphones and mobile Internet, social media users are increasingly going mobile [1], [2]. For example, Twitter had approximately 257 million mobile active users monthly as per the first quarter in 2016 [1]. Along with this trend is the emergence of location based services deployed on social media. Most of such location based services require accurate or coarse user locations to decide the service results for users. However, many people actually do not share their precise locations in their social posts [3], [4]. It is thus necessary to bridge this gap in order for the relevant location based services to take full effect.

In this work, we study a co-location judgement problem, i.e., to judge if two Twitter users are at the same point-of-interest (POI) in a period of time. We stipulate that two tweets are sent in the same time period if their time difference is less than a threshold \( \Delta t \). Many important applications today need to know how to acquire the information about “if two users stay together” or “who are in the same place among a group of users”. For example, friends notification [5] is a very popular service on social media, which notifies a user that one of his/her friends is also present at the same POI in the same time. As another example, many social network platforms also offer local people recommendation [6], [7], which can recommend users who are close to and share the same interest with a user in need. Furthermore, “followship” measurement in the real world [8] investigates when a person visits a POI due to the influence of another person. Other examples include community detection and group analysis [9], [10], [11] that aim to find users sharing interests and appear in the same place at the same time.

Such people may form communities in an online-to-offline fashion to fulfill different purposes. All aforementioned applications can clearly benefit from co-location judgement. Existing works usually requires the input data to be geotagged, i.e., tweets must be associated with coordinates or place names. However, geo-tagged tweets only occupy a small fraction in all tweets [3]. Solving the problem of co-location judgement provides a better way to enable these applications as it can deal with non-geotagged tweets. Traditional location inference approaches [12] also work in these tasks—we just infer the location of every user and then judge if users in question are in the same location. However, as our experiments show, such a method results in low inference accuracy whereas our co-location judgement approach achieves high judgement accuracy.

The problem of co-location judgement on Twitter data is challenging. On the one hand, the content length of each tweet is limited to 140 characters and thus a tweet conveys little information in general. As Twitter users often use non-standard and shorthand terms, tweets are often vague and noisy. Thus, it is difficult to find location clues from short, noisy tweets. On the other hand, as tweets are mostly not geo-tagged [13], and even fewer tweets are explicitly associated to POIs, the labeled data across each POI, on average, is scarce.

Since only a small fraction of tweets are geo-tagged, it is not possible to directly know if two Twitter users are co-located or not. We have to make use of other information available for the users. Fortunately, people often send location-related tweets when they get to new POIs. Also, the places a user has ever visited tend
to have an impact on where they are now or where they are going. Therefore, our approach to the co-location judgement problem is based on historical visits and recent tweet contents.

To address the challenges, our solution integrates users’ visit history and recent tweets in feature selection. A user’s historical visits can be regarded as a kind of prior information, whereas her/his recent tweet is often related to where she/he is (or heading to). We deliberately extract features from historical visits and recent tweets (HisRect for short), which combine Twitter user visit history and recent tweet contents. Furthermore, we decide if two users are co-located based on the difference between their HisRect features.

To alleviate the issue of data scarcity, we further propose a semi-supervised learning (SSL) framework [14] that leverages unlabeled data, those geo-tagged tweets which are not explicitly associated to any POI, to train the HisRect featurizer. Subsequently, we feed the HisRect features of two users to another embedding neural network layer and calculate the difference of the two embeddings. Finally, we construct our co-location judger as a feed-forward neural network that only takes the embedding difference as input.

Our HisRect featurizer and co-location judgement are experimentally evaluated on large real datasets. The experimental results demonstrate that our HisRect based approach is effective at finding co-located users and it clearly outperforms alternative approaches. Furthermore, our HisRect features result in more accurate POI inference than the state-of-the-art techniques.

Our contributions are summarized as follows.

- We formulate the problem of co-location judgement on Twitter data. To the best of our knowledge, this is the first work to address this problem.
- We design HisRect features which quantify the spatial and temporal aspects in Twitter users’ visit history and address the local features in recent tweets.
- We develop a novel semi-supervised embedding learning framework to train the HisRect featurizer such that unlabeled data can be exploited in our solution. The framework includes a carefully-designed affinity graph that considers both spatial and temporal distances between HisRect feature instances. Relevant experimental results demonstrate the effectiveness of the proposed semi-supervised method.
- We conduct extensive performance evaluation using real-world Twitter data. The results verify the effectiveness of our HisRect features and semi-supervised framework.

The rest of this paper is organized as follows. Section 2 reviews the related work. Section 3 formulates the research problem. Section 4 describes how to build HisRect features and presents the semi-supervised learning framework for training the featurizer. Section 5 details our approach for co-location judgement. Section 6 reports the experimental results. Finally, Section 7 concludes the paper and points to future work directions.

## 2 Related Work

To the best of our knowledge, there exists no work on the co-location judgement problem on Twitter data. A straightforward solution works as follow. For two twitter users who sent tweets in the same period of time, we infer two respective locations based on their tweet contents or their historical visits and check if the two inferred locations are the same. Therefore, we briefly review location inference or recommendation methods in Section 2.1. Also, we review semi-supervised learning techniques briefly in Section 2.2.

### 2.1 Location Inference or Recommendation

To infer locations for individual tweets, most existing approaches rely on tweet contents. Kinsella et al. [15] create language models of locations using geo-tagged tweets, measure the Kullback-Leibler divergence between such a model and a tweet, and infer the tweet location at the neighborhood and city level. Doran et al. [16] build smoothed language models to estimate tweet locations at the neighborhood level. Friedhorsky et al. [17] propose a two-dimensional Gaussian Mixture Model to infer the city of a tweet. Zubiaga et al. [13] extract features from user profiles and tweet contents, following a weighted maximum entropy classifier to determine the country for a tweet in real-time. Flatou et al. [18] use a Gaussian model to capture the location distributions of n-grams and associate geographic scope to such n-grams.

Some studies consider not only content and metadata in user profiles but also temporal information. Yuan et al. [19] propose a probabilistic topic model to exploit micro-blogging data to detect spatio-temporal topics, and then they use the topics to model user mobility behavior and infer tweet locations. Dredze et al. [20] also consider the impact of time on tweet locations, taking time as a feature and using a linear classifier trained on geo-tagged tweets to infer tweet locations at the city level. Palpanas and Parasevopoulos [21], [22] exploit the similarities in the contents between a tweet and a set of geo-tagged tweets posted at the same time in order to decide if the given tweet is from the same location as others. Besides, Noulas et al. [23] and Ryoo et al. [24] exploit users mobility to predict their next places. McGee et al. [25], [26], Yamaguchi et al. [27] and Kong et al. [28] consider temporal spatial aspects when making location inference.

Some recent POI/location recommendation models are able to predict the location or POI for a given user at a given time period. Recent studies [29], [30], [31], [32], [33] focuses on leveraging the geographical and social influences to improve recommendation accuracy. Studies [34], [35], [36] make use of temporal cyclic patterns and temporal sequential patterns. Besides, semantic information is adopted by many recommendation approaches to alleviate the data sparsity problem. Yin et al. propose LCA-LDA [37] and Geo-SAGE [38] models to exploit the content information of checked-in POIs to infer both personal interests and local preferences. Also, SPORE [39] fuses sequential influence with personal interests in the latent and exponential space, TPM [40] utilizes cyclic patterns, and GE [41] embeds four corresponding relational graphs into a shared low dimensional space to capture the sequential effect, geographical influence, temporal cyclic effect and semantic effect. ST-LDA [42] learns region-dependent personal interests according to the contents of their checked-in POIs at each region. SH-CDL [43] jointly performs deep representation learning for POIs from heterogeneous features and hierarchically additive representation learning for spatial-aware personal preferences. However, unlike our HisRect-based approach, these models requires a user’s historical data in the training process in order to make recommendations for the user. That said, these models can hardly deal with new users, i.e., those users whose historical data is not available in the training dataset. Furthermore, they require semantic information about POIs (such as tags or descriptions). Moreover, most of these models focus on building static features.
for users and POIs/items. Thus, they will predict the locations of a user at two time periods to be the same. Although some models consider the temporal information when making predictions, they only concern time, days or hours, e.g., if a user posts two tweets of 2 o’clock but on two different Saturdays, the two times are regarded as the same and the user will most likely receive the same POI recommendations. Also, they do not utilize the textual information of relevant tweets when predicting the locations of users. In summary, those recommendation methods fall short for our co-location judgment problem as their design characteristics are different from what is needed by our problem.

2.2 Graph-based Semi-Supervised Learning

Semi-supervised learning (SSL) aims to leverage unlabeled data to improve performance when labeled data is scarce. Graph-based SSL uses a matrix to describe the similarities between any two instances. Let $L$ and $U$ be the numbers of labeled and unlabeled instances, respectively. Let $x_{1:L}$ and $x_{L+1:L+U}$ denote the input vectors of labeled and unlabeled instances, respectively, and $y_{1:L}$ are the labels of $x_{1:L}$. Graph-based SSL learns a classifier $f: x \rightarrow y$. The mainstream approaches usually need an affinity graph, which is a $(L + U) \times (L + U)$ matrix $A$. Each entry $a_{ij}$ indicates the similarity between instances $i$ and $j$ that are either labeled or unlabeled. The matrix can be derived from distances between instances [14], [44], [45], [46], or from external data such as knowledge graphs [47], document citation networks [48] and social networks [49]. In this paper, our matrix $A$ is constructed based on the spatial and temporal distances between instances.

Generally, the loss function of graph-based SSL can be written as follows [14]:

$$\mathcal{L} = \sum_{i=1}^{l} \ell_i(f(x_i), y_i) + \sum_{i,j=1}^{l+u} \ell_u(f(x_i), f(x_j), a_{ij})$$

In particular, $f(\cdot)$ is the prediction function to be learned that maps input $x$ to labels $y$, $\ell_i$ is some proper loss function for supervised loss on labeled data, and $\ell_u$ for unsupervised loss on both labeled and unlabeled data. Specifically, $\ell_u$ incurs a large penalty when similar instances with a large $a_{ij}$ are predicted to have different labels.

Different graph-based SSL algorithms define unsupervised loss $\ell_u$ in different ways. Zhu et al. [45] use label propagation to force $f$ to agree with $y_{1:L}$, where $f$ is a label lookup table for unlabeled instances in the graph and can be obtained with a closed-form solution. Talukdar et al. [49] propose a variant of label propagation called modified adsorption that allows prediction on labeled instances to vary and incorporates node uncertainty. Zhou et al. [44] define $\ell_u$ as squared loss. Belkin et al. [14] use the Laplacian Eigenmaps regularizer and parameterize $f$ in the Reproducing Kernel Hilbert Space with $\ell_u$ being squared loss or hinge loss.

Different from aforementioned approaches, Yang et al. [50] present an SSL framework based on graph embeddings. Weston et al. [46] propose to learn an embedding function instead of a prediction function. In their proposal, $f(x) \in \mathbb{R}^d$ is the embedding for a given instance $x \in \mathbb{R}^n$. In this case, $\ell_u$ is defined as $a_{ij}\|f(x_i) - f(x_j)\|_2$ for any instances $x_i$ and $x_j$.

In this paper, we adopt the idea of semi-supervised embedding. Nevertheless, we use a neural network to fit the embedding function $f$ because neural networks have powerful expression ability [51]. As the dimension of the embeddings is high (up to 512) in our setting, the Euclidean distance is not a feasible measure for similarity [52]. Instead, we use the cosine distance to calculate $\ell_u$.

3 Problem Formulation and Framework

This section formulates the research problem and gives our solution framework.

3.1 Notations and Problem Formulation

It is very difficult to directly know if two Twitter users are co-located as the geo-tagged tweets are scarce. Thus, we consider utilizing other information available to solve the problem. According to our observations, the places a user has ever visited tend to have impact on where they are now or where they are going. Also, people usually send location-related tweets when they get to new POIs. In this study, we make use of geo-tagged tweets that are posted with geo-locations captured as latitude and longitude. Such a tweet implies a visit of a place by the corresponding Twitter user. With the help of an appropriate geographic information service like OpenStreetMap⁷, we are able to decide if a geo-tagged tweet was posted in a POI. In addition, we also consider the contents of the most recent tweets of Twitter users. By taking into account the visit histories and the recent tweet contents, we expect to identify if two Twitter users are currently located in the same POI or not.

The notations used throughout the paper are given in Table 1.

<table>
<thead>
<tr>
<th>$P$</th>
<th>Set of POIs</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_L$</td>
<td>Labeled profiles</td>
</tr>
<tr>
<td>$R_U$</td>
<td>Unlabeled profiles</td>
</tr>
<tr>
<td>$R_{U_{train}}$</td>
<td>Labeled profiles of training dataset</td>
</tr>
<tr>
<td>$R_{L_{train}}$</td>
<td>Labeled profiles of testing dataset</td>
</tr>
<tr>
<td>$F_L$, $F_U$</td>
<td>Labeled pairs</td>
</tr>
<tr>
<td>$F^{+}$, $F^{-}$</td>
<td>Positive and negative pairs with $F^{+} \cup F^{-} = \Gamma_L$</td>
</tr>
<tr>
<td>$F_{U_{train}}$</td>
<td>Labeled pairs of training dataset</td>
</tr>
<tr>
<td>$F_{U_{test}}$</td>
<td>Labeled pairs of testing dataset</td>
</tr>
<tr>
<td>$\Delta t$</td>
<td>The time period</td>
</tr>
</tbody>
</table>

**Definition 1 (POI).** A POI $p$ is a 4-tuple $p = (pid, bp, lat, lon)$, where $pid$ is $p$’s identifier, $bp$ is $p$’s bounding polygon formed by connecting $N$ coordinate points, and $(lat, lon)$ is the central point of the polygon $bp$.

We use $(lat, lon) \in p.bp$ to denote that a point $(lat, lon)$ is inside the POI $p$.

**Definition 2 (Tweet).** A tweet $t$ is a 4-tuple $t = (ts, content, lat, lon)$ where $ts$ is the timestamp when $t$ was posted, and $content$ is the content of $t$. If $t$ is a geo-tagged tweet, $lat$ and $lon$ represents the latitude and longitude, respectively. Otherwise, both $lat$ and $lon$ are set to null.

Let $P$ be the set of all POIs. A tweet $t$ is a POI tweet if there is a POI $p \in P$ such that $(t.lat, t.lon) \in p.bp$, i.e., tweet $t$ was posted when the user was at a POI in $P$.

A geo-tagged tweet implies a visit as follows.

**Definition 3 (Visit).** A visit $v$ is a 3-tuple $v = (ts, lat, lon)$, meaning a user visited location $(lat, lon)$ at time $ts$.
In the training phase, we extract \( ts, \) \( lat \) and \( lon \) from all geo-tagged tweets in a user’s timeline, which forms a complete sequence of visits of the user. Each sequence is called the user’s visit history. Furthermore, we build user profiles that combine user visit history and recent tweet.

**Definition 4 (Profile).** A user profile \( r \) is a 4-tuple \( r = (uid, t, v-history, pid) \), where \( uid \) identifies the user who sent the recent tweet \( t \), \( v-history \) is the user’s visit history before \( t.ts \), and \( pid \) is a POI identifier.

For convenience, we use \( r.ts, r.lat, r.lon \) and \( r.content \) to denote \( r.t.ts, r.t.lat, r.t.lon \) and \( r.t.content \), respectively. If \( r \) is a POI tweet at \( p \), \( r.pid \) is set to \( p.pid \) and \( r \) is regarded as labeled; otherwise, \( r.pid \) is set to null and \( r \) is unlabeled.

In the co-location judgement, we consider a pair of users.

**Definition 5 (Pair).** A pair is a 3-tuple \( r_i \) \( r_j \) = \( (r_i, r_j, co-label) \), where \( r_i \) and \( r_j \) are two profiles, \( r_i.uid \neq r_j.uid \), and \( |r_i.ts - r_j.ts| < \Delta t \).

A pair is unlabeled and its co-label is set to null, if either of its profiles is unlabeled. Otherwise, the pair is labeled. In a labeled pair, co-label is set to 1 in the training data if the two users are co-located at the same POI. Such a pair is positive. Otherwise, co-label is set to 0 and the pair is negative. We use \( \Gamma_L^+ \) and \( \Gamma_L^− \) to denote the sets of positive and negative pairs, respectively.

In the rest of this paper, we use \( d(a, b) \) to denote the spatial distance between two objects with location annotations. Specifically, \( a \) or \( b \) can be a profile, a visit or a POI. Besides, we define the spatial distance \( \text{d}(r, P) \) between a profile \( r \) and the POI set \( P \) as the lower bound distance between \( r \) and all POIs in \( P \), i.e., \( \text{d}(r, P) = \min \{ \text{d}(r, p) | p \in P \} \).

Our research problem is formulated as follows:

**Co-Location Judgement:** Given two profiles \( r_i \) and \( r_j \) generated by two new users such that \( r_i.uid \neq r_j.uid \), and \( |r_i.ts - r_j.ts| < \Delta t \), i.e., \( r_i \) and \( r_j \) form a pair, suppose that the two profiles’ \( pids \) are unknown, decide if they are co-located, i.e., if they are from the same POI.

### 3.2 Solution Framework

Fig. 1 shows the framework of our solution to the co-location judgement problem. The core is to extract features from historical visits and recent tweets in profiles. The left part illustrates how it works. The feature, called ‘HisRect’, \( \mathcal{F}(r) \) of the profile \( r \) includes two parts: the fixed dimensional feature \( \mathcal{F}^v(r) \) which quantifies the spatial and temporal aspects of historical visits, and \( \mathcal{F}^c(r) \) which extracts the location clues from the raw recent tweet contents and is also fixed dimensional. To get \( \mathcal{F}^v(r) \), we adopt the skip-gram algorithm [53] to build word vectors first. Then BiLSTM-C [54], an LSTM variant, is used to convert the word vector sequence of the tweet content in a profile into the fixed dimensional feature \( \mathcal{F}^c(r) \). We detail the procedure of building HisRect feature of profiles from Section 4.1 to 4.3. To train this featurizer, we propose a graph-based semi-supervised learning approach, as shown in right upper part in Fig. 1. The SSL framework takes pairs and labeled profiles as input. It needs a similarity matrix \( A \) that measures the ‘distance’ of both profiles in a pair. To create \( A \), we take the spatial and temporal distance of two profiles into consideration (Section 4.4). After that, each profile is expressed as a fixed dimensional feature vector. Finally, the right lower part shows the procedure of judging if a pair \( r_i \) \( r_j \) is co-located or not using the featurizer \( \mathcal{F} \). We calculate the difference of features \( \mathcal{F}(r_i) \) and \( \mathcal{F}(r_j) \) and feed it into a binary classifier composed of fully-connected layers and activation functions only. It is noteworthy that the parameters of \( \mathcal{F} \) are fixed during this stage. Section 5 describes the approach in details.

### 4 HisRect Feature

The HisRect \( \mathcal{F}(r) \) of a profile \( r \) includes two parts: \( \mathcal{F}^v(r) \) features \( r.v-history; \mathcal{F}^c(r) \) is the embedding of \( r.content \). The left part of Fig. 1 shows how to build HisRect feature of a profile.

#### 4.1 Feature of Historical Visits

A straightforward way to featurize a user’s visit history is to use a one-hot encoding vector representing the POI identities [33]. However, this way fails to take into account when the visits to
those POIs took place and neither can this way utilize those visits whose coordinates are not inside any POI. Thus, we need to find a better way to model users’ visit histories.

In a short period of time, a user is unlikely to move from one POI to another that is far away. Therefore, a user’s historical visits have an impact, to some extent, on her/his current locations. Intuitively, more recent visits tend to have a higher impact. It is thus beneficial to utilize a user’s visit history by considering both temporal and spatial aspects. More specifically, we want to know thus beneficial to utilize a user’s visit history by considering both some places close to some POI from the definition of $F$ and time-concerned smoothing factors, respectively. It is evident one POI to another that is far away. Therefore, a user’s historical results are reported in Section 6.

Generally, $r.content$ can be defined as a sequence of words $r.content = (w_1, ..., w_T)$ with length of $T$. Since processing words directly is difficult, we convert $r.content$ into a sequence of fixed-dimensional vectors. In particular, we extract the content of all tweets of each timeline in our training data $C_{train}$ and use the skip-gram algorithm [53] to train these word vectors. Consequently, each word is expressed as an $M$-dimensional vector of float numbers, where $M$ is an empirical value that has little impact on the overall model performance. It is set to 512 in our experiments. Subsequently, we express the word sequence of $r.content$ as a word vector sequence $X = (x_1, ..., x_T)$. This $X$ serves as the vectorization for $r.content$. Each $x_i$ in $X$ is the word $w_i$’s $M$-dimensional vector and the length of the sequence $X$, i.e., $|X|$, is $T$. This way, we convert $r.content$ into $X$.

Bidirectional Long short-term memory (BLSTM) [55] is specialized for sequential data. It takes $X$ as input and computes the $N$-dimensional hidden state sequences $\overrightarrow{H} = (h_0, ..., h_T)$ and $\overleftarrow{H} = (\overleftarrow{h}_0, ..., \overleftarrow{h}_T)$ bidirectionally. However, BLSTM take the sequence of individual word vectors as input. Sometimes, an individual word cannot give clear location clues but word groups or phrases have close ties with some particular locations. For example, “statue” or “liberty” can be used everywhere, whereas “Statue of Liberty” is the landmark of New York City. Motivated as such, we combine word groups in the hope of extracting such local features that are more powerful for location inference.

To address this idea, we use $BiLSTM$-$C$ [54], a variant of LSTM which adds a convolution layer above the BLSTM layer, to exploit the local features inside the word groups. It concatenates every vector in $\overrightarrow{H}$ and $\overleftarrow{H}$ and converts the combination of them into a $T \times N \times 2$-dimensional tensor $H$ that can be viewed as a 2-channel image with height $T$ and width $N$. Using one filter $K \in \mathbb{R}^{3 \times N}$ to convolve $H$, followed by a nonlinear rectified linear unit (Relu) operation, $BiLSTM$-$C$ gets a $(T-2) \times N$-dimensional output “feature map”. By computing the mean of elements in this “feature map” across the first dimension, we get the fixed $N$-dimensional feature $F^v(r)$ of $r.content$:

$$H_{i,0} = \begin{bmatrix} \overrightarrow{h}_0 \\ \overrightarrow{h}_1 \\ \vdots \\ \overrightarrow{h}_T \end{bmatrix} \quad H_{i,1} = \begin{bmatrix} \overleftarrow{h}_0 \\ \overleftarrow{h}_1 \\ \vdots \\ \overleftarrow{h}_T \end{bmatrix} \quad F^v(r) = \text{Mean}(\text{Relu}(K \ast H)) \quad (3)$$

The architecture of $BiLSTM$-$C$ is shown in the bottom-left part of Fig. 1.

### 4.3 Combination of $F^v(r)$ and $F^c(r)$

To obtain the final HisRect $F(r)$, we merge $F^v(r)$ and $F^c(r)$ through vector concatenation and feed $[F^v(r), F^c(r)]$ to a feed-forward neural network which is composed of some stacked fully connected layers followed by nonlinear rectified linear units ($\text{Relu}(x) = \max(0, x)$). Combining Eq. (2) and (3), we obtain the representation of HisRect feature $\overrightarrow{F}(r)$:

$$F(r) = h^{Q_f} \bigg( ... h^2 (h^1 (F^v(r), F^c(r))) \bigg) ,$$

where $Q_f$ is the total number of fully connected layers in $F$. The probabilistic estimates of a profile located in every POI and their actual labels. However, a supervised method falls short when there lacks sufficient training data. In our case, out of the total 1,904,227 profiles, only 533,400 are associated to a POI. In other words, the amount of unlabeled data is almost three time larger than that of the labeled data. This motivates us to employ a graph-based semi-supervised learning (SSL) method to leverage unlabeled data to generate better features.

### 4.4 Semi-Supervised HisRect Training

The HisRect feature is the bridge between raw profiles and POIs. It is natural to train $F$ by feeding HisRect features to a POI inference classifier. As we have a labeled profile set $R_L$, a straightforward way is to use a supervised learning method. Such a method estimates the probabilities of a profile located in every POI and builds a supervised loss function based on the probabilities and their actual labels. However, a supervised method falls short when there lacks sufficient training data. In our case, out of the total 1,904,227 profiles, only 533,400 are associated to a POI. In other words, the amount of unlabeled data is almost three time larger than that of the labeled data. This motivates us to employ a graph-based semi-supervised learning (SSL) method to leverage unlabeled data to generate better features.
Our SSL approach aims to solve the following optimization problem:

\[
\begin{align*}
    f^* &= \arg \min_{f \in \mathcal{N}} L_{\text{poi}} + L_u \\
    \text{where } L_u &= \sum_{i,j=1}^{l+u} a_{ij} \left(1 - \langle \mathcal{E}(\mathcal{F}(r_i)), \mathcal{E}(\mathcal{F}(r_j)) \rangle \right) \\
    \text{with } \mathcal{E}(x) &= \text{normalize} \left(h^{Q_3}(...h^2(h^1(x)))\right)
\end{align*}
\]

Above, \( f \) is the objective function, \( \mathcal{N} \) is a normalized vector function space, and \( L_{\text{poi}} \) is the supervised loss of the POI classifier \( \mathcal{P} \), a feed-forward neural network taking the labeled profiles set \( R_L \) as input which is just the cross entropy in our setting. \( \mathcal{E} \) is a normalized feed-forward network to embed the HisRect features of profiles into \( \mathbb{R}^E \) space in which \( E \) is the dimensionality of embeddings and \( Q_3 \) is the number of fully connected layers. The unsupervised loss \( L_u \) takes the labeled and unlabeled pairs sets \( \Gamma_L \) and \( \Gamma_U \) as input, and \( a_{ij} \) is the similarity between profiles \( r_i \) and \( r_j \). \( L_u \) gives a large penalty when the cosine distance\(^{3}\) is large between the embeddings of two similar profiles. In Fig. 1, the top-right part illustrates the joint training of the semi-supervised HisRect feature \( \mathcal{F} \) and the POI classifier \( \mathcal{P} \).

The most important thing is how to measure the similarity between two profiles. As each profile contains latitude and longitude, it is natural to use the spatial distance between two profiles to compute their similarity. Also, the time dimension should be taken into consideration as two profiles tend to be less similar if they were posted at different times. By considering the spatial and temporal aspects, we derive the similarity matrix \( \Theta \) as follows:

\[
a_{ij} = \begin{cases} 
1, & \text{if } r_i \sim r_j \in \Gamma_U, \\
-1, & \text{if } r_i \sim r_j \in \Gamma_U \text{ and } d(r_i, r_j) < \rho, \\
c_i^d + d(r_i, r_j)^{\Delta t}, & \text{if } r_i \sim r_j \in \Gamma_U \text{ and } d(r_i, r_j) > \rho, \\
0, & \text{otherwise},
\end{cases}
\]

In particular, \( \rho \) and \( \Delta t \) are the thresholds for spatial and temporal distances, respectively; \( c_i^d \) is another smoothing factor.

Two profiles should be similar if they are associated to the same POI in the same time period. In contrast, two profiles in a negative pair are supposedly different, as they are associated to different POIs. Accordingly, a penalty should be given if the distance is large between features of profiles in a positive pair. Otherwise, it gives a reward, i.e., a negative penalty. Therefore, we set the similarity item \( a_{ij} \) for profiles in positive and negative pairs to be 1 and -1, respectively.

When a pair of profiles are not from the labeled set \( \Gamma_L \), we cannot measure their similarity in the aforementioned way. For profile pairs from \( \Gamma_L \), we utilize the \( \text{lat, lon} \) and \( ts \) in the profiles. Intuitively, the shorter the spatial distance between two profiles, the larger the similarity between them is. Given a profile pair, if their spatial distance is larger than \( \rho \) or their temporal distance is larger than \( \Delta t \), we set their similarity to be 0. Furthermore, if a profile \( r \) was posted in a place close to no POI, i.e., \( d(r, P) > \rho \), we think it offers little useful information and set all the similarities involving \( r \) to be 0. Those relevant profiles are unlabeled and we are less confident to say that their features are totally different. Therefore, we do not set them to -1.

We train \( \mathcal{F} \), \( \mathcal{E} \) and \( \mathcal{P} \) as follows. First, we build the sets \( \Gamma_L \) and \( \Gamma_U \) from labeled profile set \( R_L \) and unlabeled profile set \( R_U \), respectively, and calculate the similarity matrix \( \Theta \). For \( \Theta \), we only need to consider those pairs of profiles in \( R_L \cup R_U \), as the weights of the pairs not in \( \Gamma_L \cup \Gamma_U \) are all 0. These pairs have no impact on the penalty \( L_u \). After we obtain the aforementioned data, batches are sampled from \( R_L \) and \( \Gamma_L \cup \Gamma_U \) according to the proportion of \( R_L : \Gamma_L \cup \Gamma_U \). Subsequently, we feed the samples to the network to calculate \( L_{\text{poi}} \) and \( L_u \). Finally, by updating \( \Theta_{\mathcal{F}} \), \( \Theta_{\mathcal{P}} \) and \( \Theta_{\mathcal{E}} \)—the parameters of \( \mathcal{F} \), \( \mathcal{E} \) and \( \mathcal{P} \), respectively, we perform a stochastic gradient descent step with mini-batch Adam [56] to optimize the supervised loss \( L_{\text{poi}} \) and the unsupervised loss \( L_u \). The whole procedure is repeated for a number of iterations until \( L_{\text{poi}} \) and \( L_u \) are convergent. The whole training process is formalized in Algorithm 1.

**Algorithm 1** Semi-supervised HisRect feature training

**Input:** \( R_L, \Gamma_L, \Gamma_U, A, B \)

1. set \( \Omega = |R_L| + |\Gamma_L \cup \Gamma_U| \)
2. set \( \gamma_{\text{poi}} = \frac{|\Gamma_U|}{|\Omega|}, \gamma_u = \frac{|R_U|}{|\Omega|} \)
3. repeat
4. generate a random number \( \gamma \in [0, 1] \)
5. if \( \gamma < \gamma_{\text{poi}} \) then
6. sample a batch of labeled profiles \( B_e \in R_L \) of size \( B \)
7. \( L_{\text{poi}} = -\frac{1}{B} \sum_{e \in B} \log(p_{\text{poi}}[r, p]) \)
8. Take a gradient step to optimize \( L_{\text{poi}} \), update \( \Theta_{\mathcal{F}} \) and \( \Theta_{\mathcal{P}} \)
9. else
10. sample a batch of pairs \( B_p \in \Gamma_L \cup \Gamma_U \) of size \( B \)
11. \( L_u = -\frac{1}{B} \sum_{(e, p) \in B_p} a_{ij} \left(\frac{E(H(r_i))}{E(H(r_j))}\right)^2 \)
12. Take a gradient step to optimize \( L_u \), update \( \Theta_{\mathcal{F}} \) and \( \Theta_{\mathcal{E}} \)
13. until \( L_{\text{poi}} \) and \( L_u \) all converge or are sufficiently small

## 5 HisRect-based Co-Location Judgement

The HisRect feature is suitable to solve the problem of co-location judgement. If two users have similar historical visits or send tweets from the same POI, they are more likely to be co-located. On the contrary, two users with very different visits histories are very likely to be in different places.

In order to judge if two profiles \( r_i \) and \( r_j \) are co-located, a simple method called Comp2Loc uses the classifier \( \mathcal{P} \) to infer the POIs for both profiles and see if the two inferred POIs are identical. However, this method only considers part of the original HisRect feature and utilizes the features of \( r_i \) and \( r_j \) separately. It lacks insight on the intrinsic properties of co-located pairs.

A more sophisticated method should consider the difference between the features of \( r_i \) and \( r_j \) and thus capture the intrinsic relationship between \( r_i \) and \( r_j \). The bottom-right part of Fig. 1 shows the framework of our approach to the co-location judgement problem. We use an embedding layer \( \mathcal{E}' \) to embed the HisRect features of \( r_i \) and \( r_j \). Also, we construct a feed-forward neural network \( \mathcal{C} \) whose input is the difference vector between the two embeddings. On top of \( \mathcal{C} \) follows a binary softmax layer. It is basically a logistic regression with sigmoid function and the corresponding cross entropy is reducible to a log loss function. The formula of \( \mathcal{E}' \), \( \mathcal{C} \), co-location probability estimate \( p_{\text{co}} \) and the supervised loss are shown as follows.

\[
\begin{align*}
    \mathcal{E}'(x) &= h^{Q_3}(...h^2(h^1(x))) \quad \mathcal{C}(x) = h^{Q_3}(...h^2(h^1(x))) \\
    p_{\text{co}}(r_i, r_j) &= \sigma \left( \mathcal{C} \left( \mathcal{E}'(\mathcal{F}(r_i)) - \mathcal{E}'(\mathcal{F}(r_j)) \right) \right)
\end{align*}
\]
\[ \mathcal{L}_{co} = - \sum_{r_i \epsilon \mathcal{L}} \log(p_{co}(r_i)) - \sum_{r_j \epsilon \mathcal{L}} \log(1 - p_{co}(r_j)) \]

Above, \( Q'_c \) and \( Q_c \) are the numbers of fully connected layers in \( \mathcal{E}' \) and \( \mathcal{C} \), respectively. When \( p_{co}(r_{ij}) \) is larger than a threshold (it is set to 0.5 generally), the profiles \( r_i \) and \( r_j \) are regarded as co-located.

To train \( \mathcal{E}' \) and \( \mathcal{C} \), we only need the labeled pairs set \( \Gamma_L \). In each training iteration, we sample batches from \( \Gamma_L \), calculate corresponding \( \mathcal{L}_{co} \), and take a gradient descent step until \( \mathcal{L}_{co} \) converges. Note that the parameters \( \Theta_{\mathcal{F}} \) of \( \mathcal{F} \) are fixed at this stage.

We can also connect the HisRect feature with \( \mathcal{E}' \) and \( \mathcal{C} \) directly and take \( \mathcal{L}_{co} \) as loss objective to train the parameters \( \Theta_{\mathcal{F}}, \Theta_{\mathcal{E}}', \) and \( \Theta_{\mathcal{C}} \) jointly using labeled pairs \( \Gamma_L \). This approach, called One-phase, omits the process of HisRect feature training. As some profiles in \( R_L \) may not show in any pair in \( \Gamma_L \), One-phase may fail to exploit useful information. Also, One-phase cannot be trained in a semi-supervised way since it does not use unlabeled data. Experiments show that our approach outperforms One-phase.

Our proposed co-location approach can be easily wrapped into an efficient clustering algorithm. Given \( N \) profiles, we can get an \( N \times N \) probability matrix \( S \) with each item \( S_{i,j} \) representing the similarity of profiles \( r_i \) and \( r_j \). By taking each profile as a node and linking an edge between node \( i \) and \( j \) if \( S_{i,j} \) is larger than a threshold (in general, it is set to 0.5), this matrix is converted into an undirected graph. Consequently, the clusters are just the connected components of the graph. We do not even need to designate the number of clusters. The experimental results demonstrate that our approach works well on clustering tasks.

6 EXPERIMENTS

6.1 Experimental Settings

6.1.1 Datasets

We use the open-source library twitter4j to access Twitter’s open API to crawl data. We crawl timelines of Twitter users whose profile location is in one of New York’s five boroughs (NYC for short) or Clark County (including Las Vegas, LV for short) in Nevada. Totally, there are 892,172 NYC and 207,682 LV Twitter user timelines, involving 992,390,010 and 148,021,872 tweets, respectively. Only 2.2 percent of NYC tweets and 2.0 percent of LV tweets are geo-tagged. In addition, we download NYC and LV OpenStreetMap data dump and extract all POI bounding polygons. By checking the coordinates in those geo-tagged tweets against the POI bounding polygons, we identify all POI tweets, i.e., those sent in a POI. In the data we use, most POIs involve no tweets. Therefore, we only consider the top 1000 POIs in NYC and top 250 POIs in LV that have the most tweets. We filter out the user timelines that contain no POI tweet and obtain 58,966 and 10,844 user timelines in NYC and LV, respectively. We randomly select \( \frac{1}{3} \) of these timelines to form the testing dataset. The remaining timelines are split into training and validation data in the ratio of 9 : 1.

We obtain labeled profiles set \( R_{L}^{train} \), labeled pairs set \( \Gamma_{L}^{train} \), and unlabeled pairs set \( \Gamma_{U}^{train} \) for the training dataset. The testing or validation dataset, only the labeled profiles set \( R_{L}^{test} \) and labeled pairs set \( \Gamma_{L}^{test} \) are needed. More details about the datasets are given in Table 2.

6.1.2 Training and Implementation

Each stopword in the content of all profiles is replaced with a \(<s/>\) symbol firstly. Since the ratio between the numbers of negative/unlabeled and positive pairs is very large, we use \( \frac{1}{20} \) of negative and unlabeled pairs only in every training epoch, i.e., negative and unlabeled pairs can be gone through in every 10 epochs.

It is noteworthy that our approach design is independent of the \( \Delta t \) in the problem setting. We conduct some preliminary experiments using different \( \Delta t \) values. The performance results are very stable despite the varying \( \Delta t \). Therefore, for both training and testing datasets, we set \( \Delta t = 1 \) hour in subsequent experiments.

Other important details are as follows:

- We replace each stop word with a \(<s/>\) and only consider those words appearing more than 10 times when training word embeddings.
- The parameters of the LSTM and all the fully connected layers are initialized with Gaussian noise with mean being 0 and standard deviation set to be 0.01.
- We initialize the initial state of the LSTM with 0.
- To avoid exploding gradient problem, we enforced a hard constraint on the norm of gradient by scaling it when its norm exceeds a threshold \([0, 5]\).
- We use dropout and the configuration is set to keep probability of 0.8 [57] at the LSTM layer and before every fully connected layer during training. These are not involved when applying the model on testing dataset.
- We use three Adam optimizers to minimize \( \mathcal{L}_{poi}, \mathcal{L}_u \) and \( \mathcal{L}_{co} \) respectively. To avoid overfitting, we add a \( l^2 \) regularization term on these three loss functions.
- We perform SGD with mini-batch Adam, started with learning rates of 0.01 for all the three optimizers. The coefficients of learning rates and \( l^2 \) regularization terms all decrease with the number of training iterations increasing.
- We set \( \Delta t = 1h \), \( \epsilon_u = 1000m \), \( \epsilon_d = 50m \) and \( \rho = 1000m \), respectively.

6.1.3 Evaluation Metrics and Approaches

For performance comparison with other co-location judgement approaches, we apply four widely-used metrics, i.e., Acc (accuracy), Rec (recall), Pre (precision) and F1 (F1-score, \( F_1 = \frac{2 \cdot \text{Pre} \cdot \text{Rec}}{\text{Pre} + \text{Rec}} \)).

Table 3 summarizes the differences among all approaches in our experiments. HV is short for historical visits. Our proposed approach is called HisRect; HisRect-SL is the same but uses the supervised HisRect training only. An approach is FF (short for Feature-first) if it extracts features for both profiles in a pair first, followed by using the features to make the judgement. One-phase is not a FF approach as it does not use an explicit step to extract features.

A Naive approach infers the locations of two profiles and checks if the two locations are identical. In our experiments, we implement three naive approaches: Comp2Loc and two exiting tweet location inference approaches called TG-TI-C [22] and 7. https://www.ranks.nl/stopwords
omits the convolution layer from BiLSTM model, named BiLSTM the architecture with HisRect.

In addition, to study the effect of the convolution layer of the architecture BiLSTM-C, we build another neural network model, named BLSTM, that only uses bidirectional LSTM and omits the convolution layer from BiLSTM-C. Moreover, we implement ConvLSTM [58] which uses convolutional structures instead of fully-connected layers in both the input-to-state and state-to-state transitions. Unlike our HisRect, these two approaches use bidirectional LSTM or ConvLSTM without the following convolution layer when extracting features of tweet contents.

The original testing set contains significantly more negative pairs than positive pairs. In order to have clear comparison, we split the negative pairs into 10 parts, merge each of them with the positive pairs to form 10 testing sets instead. The reported results of each approach are the average over the 10 testing sets.

6.2 Experimental Results on Co-Location Judgement

Table 4 reports the overall performance results of all the eleven approaches. The results show that our HisRect approach is overall the best in terms of all metrics. Moreover, the ROC-curves of all approaches but the three naive ones are presented in Figure 2. The naive approaches are excluded because it is impossible to set the thresholds of the false positive rates for them. All of the tested approaches are trained with the same training dataset and their parameters are tuned to the best separately. It is also evident from Figure 2 that our HisRect performs best. Its AUC values are 0.974 and 0.957 in NYC and LV datasets, respectively. In Co-location judgement problems, judging the co-located pairs rightly matters more, i.e., we hope to get a higher recall on the prerequisite of a relatively high accuracy. Considering the low rate of positive pairs, we use $\frac{1}{3}$ of negative and unlabeled pairs only in every training epoch to increase the proportion of labeled pairs. Similarly, we split the negative pairs into 10 parts and merge each of them with the positive pairs to form 10 testing sets in order to have clear comparison (Section 6.1.1). Overall, the approaches that based on “historical visits + tweet contents” type feature almost get high AUC values and performs much better than other methods. Our HisRect outperforms the state-of-the-art alternatives. Subsequently, we further compare the performance differences and disclose the reasons behind.

6.2.1 Comparison with Existing Approaches

HisRect performs much better than TG-TI-C and N-Gram–Gauss on all of the three metrics. Even Comp2Loc, another naive approach, also outperforms them. Compared with HisRect, Comp2Loc yields worse results on these metrics except Pre. Comp2Loc judges a pair to be co-located only when $P$ classifies both profiles in the pair into the same POI. In this case, the HisRect features of both profiles are very similar and thus Comp2Loc achieves high Pre by using the features. However, the HisRect features of the two profiles which are involved in the same POI may focus on different aspects. As a result, Comp2Loc cannot understand the intrinsic relationships. Therefore, it performs worse in terms of Ace, Rec and F1.

6.2.2 The Effect of HisRect Features

Compared to History-only and Tweet-only, HisRect-SL and HisRect clearly improve the performance of co-location judgement. These results indicate that our HisRect features are more powerful than those features that only consider either visit history or recent tweets. Besides, HisRect outperforms One-hot. Thus, it is reasonable to say that HisRect utilizes the historical visits in a better way. Moreover, HisRect achieves better performance than BLSTM and ConvLSTM. This shows that the BiLSTM-C structure in HisRect features is more suitable for extracting features of tweet contents and our complete HisRect features model the historical visits more effectively.

6.2.3 The Effect of Semi-supervised Training

Both HisRect-SL and One-phase are inferior to HisRect on these four metrics. Such performance differences clearly demonstrate the power of semi-supervised learning framework that leverages unlabeled data in our approach.

6.3 The Power of HisRect Features

To understand the power of HisRect features in different settings, we also design more experiments and report relevant results.

6.3.1 Historical Visits or Tweet Contents Are Not Available

In order to verify the power of HisRect features, we investigate whether HisRect can work well if only historical visits or tweet contents are used in the features. We carry out experiments with variants of relevant approaches. We remove the visit history of
TABLE 4: Performance of different approaches

<table>
<thead>
<tr>
<th>Approach</th>
<th>NYC Dataset</th>
<th>LV Dataset</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Acc</td>
<td>Rec</td>
</tr>
<tr>
<td>TG-TL-C</td>
<td>0.7367</td>
<td>0.4388</td>
</tr>
<tr>
<td>N-Gram-Gauss</td>
<td>0.7769</td>
<td>0.5110</td>
</tr>
<tr>
<td>CompLoc</td>
<td>0.9106</td>
<td>0.7274</td>
</tr>
<tr>
<td>History-only</td>
<td>0.7942</td>
<td>0.5366</td>
</tr>
<tr>
<td>Tweet-only</td>
<td>0.8355</td>
<td>0.7316</td>
</tr>
<tr>
<td>One-phase</td>
<td>0.9017</td>
<td>0.8045</td>
</tr>
<tr>
<td>HisRect-SL</td>
<td>0.9222</td>
<td>0.8446</td>
</tr>
<tr>
<td>One-hot</td>
<td>0.8805</td>
<td>0.7424</td>
</tr>
<tr>
<td>BLSTM</td>
<td>0.9186</td>
<td>0.8252</td>
</tr>
<tr>
<td>ConvLSTM</td>
<td>0.9135</td>
<td>0.8266</td>
</tr>
<tr>
<td>HisRect</td>
<td>0.9341</td>
<td>0.8618</td>
</tr>
</tbody>
</table>

Fig. 2: The ROC-curve and AUC of different approaches. (a): NYC dataset; (b): LV dataset

### 6.3.3 POI Inference Based on HisRect

We also investigate the performance of HisRect features on the POI inference problem, i.e., to infer the POI of a tweet without geo-tag. We compare the inference accuracy of HisRect with the following approaches:

- **History-only** only utilizes visit histories in profiles. The rest is the same with HisRect.
- **Tweet-only** only utilizes the contents of tweets in profiles. The rest is the same with HisRect.
- **One-hot** model the visit histories using one-hot encoding vectors.
- **HisRect-SL** does not leverage unlabeled pairs when training HisRect features. The rest is the same with HisRect.
- **BLSTM** uses bidirectional LSTM when training features of tweet contents. The rest is the same with HisRect.

It is apparent that HisRect performs badly if the testing dataset is composed by historical visits or tweet contents only. Its results are even worse than that of History-only when tweet contents are missing. Without historical visits in \( \Gamma_L^{\text{test}} \), Tweet-only outperforms HisRect. However, HisRect is clearly the best when the dataset is complete, which indicates that HisRect is able to establish useful linkages between historical visits and tweet contents. As most profiles’ \( v\text{-}history \) are not empty in real word data, our proposed approach can work well in real world applications.

### 6.3.2 HisRect Visualization

In order to better understand why HisRect works well, we leverage labeled and unlabeled data together to generate HisRect features and observe if such features are good expressions of raw data or not. We get the HisRect features \( \mathcal{F}(r) \) for every profile \( r \) in the top-5 POIs in the testing dataset. Due to the high number of dimensions, we use t-SNE [59] transformation to visualize HisRect features, as shown in Figure 3.

It can be seen from Figure 3 that only a small central part mixes many different POIs and results in chaos. According to our observation, the contents in the profiles displayed in the center either have no tie with any POIs or are noises, and the corresponding visit histories offer little information. Local clues can be hardly found in these profiles. Except for the slight chaos, most profiles that come from the same POIs are adjacent to each other and form clusters as shown in Figure 3. Therefore, it is reasonable to say that HisRect featurizer \( \mathcal{F} \) are able to extract good features of profiles.

### 6.3.1 POI Inference Based on HisRect

It is apparent that HisRect performs badly if the testing dataset is composed by historical visits or tweet contents only. Its results are even worse than that of History-only when tweet contents are missing. Without historical visits in \( \Gamma_L^{\text{test}} \), Tweet-only outperforms HisRect. However, HisRect is clearly the best when the dataset is complete, which indicates that HisRect is able to establish useful linkages between historical visits and tweet contents. As most profiles’ \( v\text{-}history \) are not empty in real word data, our proposed approach can work well in real world applications.

### TABLE 5: Comparison among HisRect-based approaches, History-only and Tweet-only on NYC dataset

<table>
<thead>
<tr>
<th>Approach</th>
<th>Acc</th>
<th>Rec</th>
<th>Pr@1</th>
<th>F1</th>
</tr>
</thead>
<tbody>
<tr>
<td>HisRect</td>
<td>0.7607</td>
<td>0.4495</td>
<td>0.6539</td>
<td>0.5328</td>
</tr>
<tr>
<td>HisRect-SL</td>
<td>0.8319</td>
<td>0.7721</td>
<td>0.7022</td>
<td>0.7361</td>
</tr>
<tr>
<td>History-only</td>
<td>0.7942</td>
<td>0.5366</td>
<td>0.7143</td>
<td>0.6128</td>
</tr>
<tr>
<td>Tweet-only</td>
<td>0.8735</td>
<td>0.7316</td>
<td>0.8314</td>
<td>0.7783</td>
</tr>
<tr>
<td>HisRect</td>
<td>0.9341</td>
<td>0.8618</td>
<td>0.9162</td>
<td>0.8881</td>
</tr>
</tbody>
</table>
We randomly pick up 10%, 20%, .., 90% and 100% of the user timelines in the NYC training dataset. Figure 6 reports the average computation time of converting raw tweets and timelines into corresponding statistics. We also investigate the scalability of our training procedures. We randomly pick up 10%, 20%, .., 90% and 100% of the user timelines in the NYC training dataset. Figure 6 reports the average training time of two models (the HisRect Featuizer and the HisRect model for co-location judgement) per sample in an episode with respect to different amounts of timelines. Here, a sample illustrates the comparative recalls of the ten approaches with varying amount of training timelines. The figure also reports the ratios between positive, negative, unlabeled pairs and labeled profiles of varying amount of training timelines with respect to the corresponding statistics.

Clearly, all the ten approaches work better with more training data. More training data enable them to extract better features that in turn result in more accurate identifications. Nevertheless, HisRect can achieve good performance even when the amount of training dataset is very small. This shows that our model is equipped with a more powerful expression ability and less sensitive to the amount of training data.

**6.4.2 Effect of Deep Learning Parameters**

Since deep learning is used widely, we want to explore if deeper architectures can bring about improvements to the resolving of the research problem in this work. We vary the number of fully connected layers \((Q_f)\) and that of stacked bidirectional LSTM layers in HisRect featurizer \(\mathcal{F}(Q_l)\). Table 7 shows the performance with different neural architectures.

<table>
<thead>
<tr>
<th>(Q_f)</th>
<th>(Q_l)</th>
<th>(Q_e)</th>
<th>(\text{Rec})</th>
<th>(\text{Acc})</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2</td>
<td>3</td>
<td>0.8384</td>
<td>0.8400</td>
</tr>
<tr>
<td>2</td>
<td>3</td>
<td>4</td>
<td>0.8370</td>
<td>0.8583</td>
</tr>
<tr>
<td>3</td>
<td>4</td>
<td>5</td>
<td>0.8354</td>
<td>0.8452</td>
</tr>
</tbody>
</table>

From Table 7, we find that a deeper architecture does not necessarily improve the performance. When \(Q_f = 2\) and \(Q_l = 3\), the corresponding recall and accuracy are the highest. This observation is also seen in the experiments with different \(Q_e\), \(Q_c\) and \(Q_{\text{tr}}\), where the optimal parameter values are 3, 2 and 2, respectively.

**6.4.3 Comparison with Other SSL Alternatives**

We alter the cosine distance with \(f^2\) norm of two embeddings’ difference in calculating the unsupervised loss, which is the case in [46]. The best accuracy and recall on NYC dataset are 0.9232 and 0.8453, respectively. If we remove the embedding \(\mathcal{E}\) in the formula of the unsupervised loss, the corresponding accuracy and recall are 0.9237 and 0.8515, respectively. These results are worse than the performance of HisRect with the best configurations. Therefore, our HisRect has clear advantages over other SSL approach in the problem of co-location judgement.

**6.4.4 Computation Time and Scalability**

Once the HisRect featurizer \(\mathcal{F}\) and the co-location judge \(\mathcal{C}\) are trained, the HisRect feature construction and co-location judgement can both be finished in 1 ms for a given profile pair. Besides, the computation time of converting raw tweets and timelines into profiles and pairs is also very short (less than 1 ms per tweet). Thus, our approach can work in online scenarios. We also investigate the scalability of our training procedures. We randomly pick up 10%, 20%, .., 90% and 100% of the user timelines in the NYC training dataset. Figure 6 reports the average training time of two models (the HisRect Featuizer and the HisRect model for co-location judgement) per sample in an episode with respect to different amounts of timelines. Here, a sample...
is either a pair or a profile, depending on the kind of data fed into models. Specifically, the input samples of HisRect featurizer contain $\Gamma_{L}^{train}$, $\Gamma_{U}^{train}$ and $R_{L}^{train}$. However, those of HisRect co-location model contain $\Gamma_{L}^{train}$ only. Suppose the training time of HisRect featurizer and HisRect co-location model over one episode is $T_F$ and $T_C$, respectively. The average training time per sample of these two models is $\frac{T_F}{|\Gamma_{L}^{train}|} + \frac{T_C}{|\Gamma_{L}^{train}|}$, respectively. Figure 6 shows that the training time per sample of these two models is almost constant, roughly 0.4 and 1.25 ms, respectively.

### 6.5 A Case Study: Using a Co-location Judgement Approach to Cluster User Profiles

In many applications such as local user recommendation [6], community detection [60] and group analysis [10], people often care more about identifying who are in the same POI given a group of profiles. To address this issue, we design an experiment as follows. We sample groups of profiles with each group containing 5 profiles and design 5 typical patterns: 5-0, 4-1, 3-2, 3-1-1, 2-2-1. Pattern 3-2 means 3 out of 5 profiles (numbered a, b and c) are located in one POI and the other two (numbered d and e) are located in another POI. The meanings of other patterns are similar. Given a 3-2 pattern, if an approach can identify that a, b and c are co-located in a POI and d, e are located in another POI, we regard that the approach can identify the group pattern correctly. Specifically, we use HisRect to generate a $5 \times 5$ probability matrix and find all connected components as clusters. We compare if the predicted clusters are the same with the actual ones. We randomly select 2,000 groups of each different patterns. Table 8 shows the accuracy of HisRect and the other three alternative approaches on identifying group patterns on NYC testing dataset.

<table>
<thead>
<tr>
<th>Approach</th>
<th>5-0</th>
<th>4-1</th>
<th>3-2</th>
<th>3-1-1</th>
<th>2-2-1</th>
</tr>
</thead>
<tbody>
<tr>
<td>HisRect</td>
<td>0.8753</td>
<td>0.7915</td>
<td>0.7658</td>
<td>0.6198</td>
<td>0.5821</td>
</tr>
<tr>
<td>Comp2Loc</td>
<td>0.0392</td>
<td>0.0579</td>
<td>0.0703</td>
<td>0.1250</td>
<td>0.1767</td>
</tr>
<tr>
<td>N-Gram-Gauss</td>
<td>0.0113</td>
<td>0.0339</td>
<td>0.0503</td>
<td>0.0838</td>
<td>0.1237</td>
</tr>
<tr>
<td>TG-TI-C</td>
<td>0.0046</td>
<td>0.0189</td>
<td>0.0216</td>
<td>0.0715</td>
<td>0.0984</td>
</tr>
</tbody>
</table>

Referring to Table 8, it can be seen that HisRect yields much higher accuracy than other approaches when identifying group patterns. In particular, the accuracies of HisRect on identifying patterns on these datasets are all larger than 58%. These results demonstrate that HisRect is effective at co-location and clustering tasks, whereas the alternative approaches excel in neither.
7 Conclusion and Future Work
In this paper, we propose a novel approach to judge if two Twitter users stay at the same POI in the same period of time. Our approach profiles each user by taking into account both visit histories and recent tweets. From such profiles, HisRec features are extracted by a HisRec featurizer. A semi-supervised learning framework with profile embedding is employed to train the featurizer. The HisRec features of two user profiles are fed to another embedding layer. Subsequently, a feed-forward network takes their embeddings difference as input and decides whether the pair is co-located in one of those pre-defined POIs. We conduct extensive experiments using large real datasets collected from Twitter. The experimental results demonstrate that our approach achieves high accuracy, recall, precision and F1-score, and clearly outperform alternative approaches.

The proposed approach in this paper uses visit histories and tweet contents. For future work, it is interesting to consider other information such as social relationship among users and frequent patterns shared by users. Such information may be utilized to build better similarities for user profiles and thus help improve the performance of co-location judgement.

Acknowledgments
This research is supported by Natural Science Foundation of China (No.61772460), Ten Thousand Talent Program of Zhejiang Province (No.2018R52039)

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