Voltage Stability and Transient Symmetrical Fault Current Control of Voltage-Controlled MMCs

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Published in:
IEEE Transactions on Power Delivery

DOI (link to publication from Publisher):
10.1109/tpwrd.2020.2970247

Publication date:
2020

Document Version
Accepted author manuscript, peer reviewed version

Link to publication from Aalborg University

Citation for published version (APA):

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Abstract—This paper presents a design-oriented analysis on the voltage stability and the transient fault current limitation of voltage-controlled modular multilevel converter (MMC) with L-filters. First, a dual-loop voltage control based on the L-filter plant is systematically designed, where the upper limits of controller parameters for ensuring the small-signal stability are identified. Then, considering the transient current limitation during faults, the lower boundaries of inner current controller parameters are derived. Within the region of allowed controller parameters, the optimization is further made to minimize the output voltage stiffness against the load current disturbance. Lastly, time-domain simulations corroborate the theoretical analysis.

Keywords—Modular Multilevel Converter (MMC), voltage control, controller design, fault current

NOMENCLATURE

\[ P_w, Q_w \] Active power and reactive power of wind farm
\[ u_{eq}, i_w \] Voltage and current at grid connection point of wind farm
\[ Z_w \] Impedance of the transmission line
\[ u_c \] Voltage of PCC of MMC
\[ u_{dc}, i_c \] Voltage output by MMC and current input into MMC
\[ u_g \] Voltage at the location of the fault
\[ u_{ao}, u_{gs} \] Voltage in two-phase stationary frame
\[ i_w, i_f \] Current in two-phase stationary frame
\[ i_{dc}, u_{dc} \] DC current and DC voltage of MMC
\[ L_{eq}, R_{eq} \] Equivalent inductance and resistance of MMC
\[ L_g \] Equivalent inductance from fault point to PCC of MMC
\[ f_c, \omega_c \] Crossover frequency and angular frequency
\[ \alpha_0 \] Resonant frequency of PR controller
\[ i_r, i'_r \] Reference value of voltage and current.
\[ I_{max} \] Maximum value of the current limiter
\[ T_{abc2a, \phi} \] Clarke transformation
\[ G_d, T_d \] Time delay and time constant
\[ H_s, T_{d1} \] Filter of voltage feedforward and time constant
\[ G_s, G_v \] Transfer function of inner current loop regulator and outer voltage loop regulator.
\[ K_{pu}, K_{ii} \] Proportional gain and resonant gain of inner current loop regulator
\[ K_{pv}, K_{iv} \] Proportional gain and resonant gain of outer voltage loop regulator
\[ \delta_{1%}, t_s \] Overshoot and convergence time

I. INTRODUCTION

The modular multilevel converter (MMC) high voltage direct-current (HVDC) transmission systems have recently drawn increasing attentions in the grid integration of large-scale wind farms. Compared with the line-commutated converters (LCC)-HVDC, the MMC-HVDC is expected to have better dynamic performance when feeding to weak [1], [2] or passive [3], [4] ac power networks. On the wind farm side, the MMC needs to operate as a voltage source, forming the system voltage and frequency. Consequently, both the high-performance ac voltage control and the fast overcurrent limiting capability during ac faults become critical [5], [6]. Moreover, due to the versatile nature of wind, the load current of the voltage-controlled MMC can be fluctuated, and thus the output voltage of the MMC needs to be stiff against the load current disturbances.

The controller parameters have a significant impact on the stability and transient performance of MMCs. Designing the voltage controller for voltage-source converters (VSCs) has been thoroughly discussed, considering the phase margin (PM), the gain margin (GM) and the steady-state error [7], [8]. Yet, those studies are mainly based on the LC-filtered VSCs, where the dual voltage-current control loops can be readily designed based on the second-order LC-filter plant [9]. In contrast, only the L-filter is used with MMCs, and hence no LC-filter resonance needs to be considered when designing the voltage controller [10], [11]. Further, differing from the capacitor voltage of the LC-filtered VSCs, the PCC voltage of the MMC cannot be treated as a state variable, due to the lack of capacitance. Therefore, the controller design for the LC-filtered VSCs cannot be directly extended to MMCs.

The single-loop voltage control is implemented with the MMC in [12], yet the fault current of the MMC cannot be limited in this case, when there is a short circuit fault in the ac side of voltage-controlled MMC. Considering the limited overcurrent capability of MMCs [13], [14], a fast fault current control is important. To limit the fault current, fault current limiters are employed in [6], [15], [16]. In practice, the dual-loop control that consists of the outer voltage loop and the inner current loop is generally used for the fault current control.
However, in those works, the transient fault current is always assumed to be equal to the limit value of the current limiter [18], [19]. The parametric effect of current controller on the transient fault current is often overlooked. Since the limit value is merely a steady-state value of the fault current, the fault current can be much higher than the limit during the transient process, which affects the safe operation of MMC.

The reliable operation of wind farm depends on a stable voltage formed by the MMC station. The small-signal stability of voltage-controlled MMC has been explored in [20], [21], but what is not yet clear is the impact of parameters on the stiffness of MMC output voltage under the power fluctuations of wind farms. In [22], the voltage stiffness is improved when a severe fault occurs by adjusting the reactive power output of the voltage-controlled MMC. To address the large power and voltage disturbances, the voltage stiffness is enhanced by an additional frequency control loop [6]. However, the effects of the inner current regulator and outer voltage regulator on the voltage stiffness of the MMC are not addressed.

The voltage feedforward control is commonly used in the control of grid-connected VSCs [23] and MMCs [24]. The grid impedance is introduced to the control system through the feedforward loop and the influence of voltage feedforward on the voltage stability of grid-connected converters is studied in [25], [26], [27]. It can be seen that voltage feedforward has an important impact on the control and operation characteristic of converter. However, when the MMC is connected with wind farms, $u_s$ is formed by MMC, while the effects of voltage feedforward on the stiffness of the voltage and fault current limitation of the MMC need to be clarified.

This paper thus presents a systematic controller design guideline for the dual-loop voltage-controlled MMC-HVDC. The proportional-resonant (PR) regulators are used in both the outer voltage and inner current loops. Considering the effect of the voltage feedforward, the upper limits of controller parameters are identified first based on the small-signal model and stability analysis of the dual-loop voltage control. Then, the parametric effects of the current controller on the current overshoot and settling time are analyzed, which yields the lower limits of current controller parameters. Next, within the region of permitted controller parameters, the optimization is further made to minimize the closed-loop output impedance of MMC, in order to enhance the voltage stiffness against the power fluctuations from the wind farms. Lastly, time-domain simulations validate the effectiveness of the design guideline.

II. PARAMETERS DESIGN BASED ON THE STABILITY REQUIREMENT

A. System Description

Fig. 1 illustrates the single-line diagram of the MMC with the dual-loop voltage control system implemented in the stationary frame. It is noted that the stationary-frame PR controller can be mathematically derived from the P-Integral (PI) controller in the synchronous ($dq$-) reference frame [28], [29]. The purpose of selecting the stationary-frame is to control both the positive- and negative-sequence components, and meanwhile avoid using the sequence decomposition algorithm and Park transformations. Thus, the phase variation of PCC voltage, which may affect the dynamics of the dq-frame control [28], can be avoided in the stationary frame.

In Fig. 1, $u_s$ denotes the voltage at the point of common connection (PCC), $u_s$ is the output voltage of MMC, $i_s$ is the current injected into MMC, $L_{eq}$ is the equivalent inductance, and "*" represents the reference of the current and voltage. A constant dc-link voltage of the MMC is assumed and the timescale of internal dynamics is well decoupled from the external ac voltage control dynamics. With these assumptions, the MMC power stage can be approximated as a linear time-invariant (LTI) plant [30], [31].

B. Controller Parameters Design of Inner Loop

Fig. 2 shows the control block diagram of the inner current loop, where $G_i$ is the current regulator and $G_d$ represents the time delay. Since the internal control dynamic of MMC has little effect at the crossover frequency of the inner loop $f_c$, it is not considered in the parameter tuning of dual-loop voltage control [30].

The open-loop transfer function of the inner current loop can be obtained as

$$G(s) = G_i G_d \frac{1}{s L_{eq}}$$

(1)

where $G_i$ and $G_d$ are expressed as

$$G_i = K_i \frac{s}{s + \alpha_i}$$

(2)

$$G_d = e^{-s t_d}$$

$K_i$ is proportional coefficient, $K_i$ is resonant gain of inner current loop regulator, and $T_d$ is time constant of time delay. Assuming that the crossover frequency $\omega_c$ is much greater than $\omega_{ac}$, $G_i$ can be approximated as
\[ G_i(\omega) \approx K_p + \frac{K_i}{j\omega} \quad (3) \]

In order to guarantee the system stability, \( PM > 0 \) and \( GM > 0 \) are required at the crossover frequency. If the proportional gain of the PR regulator is designed to have a dominant effect at the crossover frequency, i.e.,
\[
K_p = 10 \cdot \frac{K_u}{2\pi f_c} \quad (4)
\]

The loop gain and its phase response can be approximated as (5).
\[
L(\omega_c) \approx 20 \log\left[ \frac{K_p}{(2\pi f_c) L_{eq}} \right] \quad (5)
\]
\[
\phi(\omega_c) \approx -90 - 57.3\beta(2\pi f_c) \]

To ensure \( PM > 0 \) and \( GM > 0 \), the parameters should be designed as
\[
f_c < \frac{90}{104.6\pi T_d} \quad (6)
\]
\[
K_p < \left(2\pi f_c\right) L_{eq} \]

If the integral gain of the current regulator is designed to have a dominant effect at the crossover frequency, i.e.,
\[
\frac{K_u}{2\pi f_c} = 10 \cdot K_p \quad (7)
\]

The loop gain and its phase response can be approximated as (8).
\[
L(\omega_c) \approx 20 \log\left[ \frac{K_i}{(2\pi f_c) L_{eq}} \right] \quad (8)
\]
\[
\phi(\omega_c) \approx -180 - 57.3\beta(2\pi f_c)
\]

From (8), it can be seen that \( PM \) is always smaller than 0. Hence, the inner loop controller can’t be designed with the integral gain playing a dominant role at \( f_c \), and it can only be designed with the proportional gain dominating the crossover frequency, where (6) is satisfied.

C. Controller Parameters Design of Outer Loop

In the islanded system, the MMC is controlled as a voltage source forming the \( u_s \). And the influence of voltage feedforward is investigated in this part.

1) With the voltage feedforward loop

The mathematical model of outer voltage loop control can be obtained as (9).
\[
\left\{ \begin{array}{l}
\dot{i}_u \approx G_{ei} \cdot (u_{sa} - u_{sa}^*) \\
\dot{i}_{ip} \approx G_{ei} \cdot (u_{ip} - u_{ip}^*) 
\end{array} \right.
\]

where
\[
G_{ei} = K_{pv} + \frac{s \cdot K_{pv}}{s^2 + \alpha_1 \omega_1} \quad (10)
\]

Combining (9) with Fig. 2, the block diagram of the outer loop and the inner loop in the \( \alpha\beta \) frame is shown as Fig. 3, where \( H_g \) represents the filter of the voltage feedforward, i.e.,
\[
H_g = \frac{1}{1 + sT_{di}} \quad (11)
\]

From Fig. 3, the transfer function can be obtained as
\[
u_{sa} = \frac{G_G G_G G_G}{1 + G_G G_G G_G - G_G H_g} u^*_{sa} + \frac{G_G G_G}{1 + G_G G_G G_G - G_G H_g} i_{sa} \quad (12)
\]

Then, the open-loop transfer function is expressed as
\[
G_{i1}(s) = G_G G_G G_G - H_g \quad (13)
\]

If the proportional gain of the PR voltage regulator is designed to have a dominant effect at the crossover frequency of the voltage loop, i.e.,
\[
K_{pi} = 10 \cdot \frac{K_u}{2\pi f_c} \quad (14)
\]

Then, the amplitude-frequency characteristic and phase-frequency characteristics can be approximated as (18), which is shown in the bottom of this page.

From (6) and (18), to ensure the PM > 0 and GM > 0, the satisfactory region can be obtained as
\[
K_{pi} K_{pv} \leq 1 \quad (15)
\]

If the integral gain of the PR regulator is designed to have a dominant effect at the crossover frequency, i.e.,
\[
K_{pv} = 10 \cdot \frac{K_u}{2\pi f_c} \quad (16)
\]

Then, the amplitude-frequency characteristic at crossover frequency can be approximated as
\[
L(\omega_c) \approx 20 \log\left[ \frac{K_{pi} K_{pv}}{1 + \frac{K_{pi} K_{pv}}{1 + (\omega_c T_{di})^2} + \frac{K_{pi} K_{pv}}{\omega_c}} \right] \quad (17)
\]

From (17), the GM is always smaller than 0. Therefore, the outer voltage loop regulator can only be designed with the proportional gain dominated at the crossover frequency, in which (15) must be satisfied.
II.PARAMETERS DESIGN BASED ON THE FAULT CURRENT LIMITATION

Short-circuit faults in the ac system increasingly arise as the power scale of wind farm is enlarged. Due to the limited overcurrent capability of the MMC, the fault current control is critical, and the fault current overshoot needs to be effectively suppressed. In this work, only the symmetrical three-phase short circuit fault at the ac-side of the MMC is considered.

A. With the voltage feedforward loop

Fig. 5 shows the control block diagram of the inner current loop after the short circuit fault on the ac side. $u_{gs}$ is the voltage of the location of the fault, $L_d$ is the equivalent fault inductance.

Based on Fig. 5, the transfer function of the inner current loop can be obtained as

$$i_{sa} = \frac{G_G G_d}{s(L_q + L_g - L_{gd} H_d) + G_G G_d} i^{*}_{sa} \nonumber$$

$$+ \frac{1-G_d H_d}{s(L_q - L_g - L_{gd} H_d) + G_G G_d} u_{gs}$$

(25)

Considering a severe three-phase short-circuit fault, the voltage amplitude at the fault location reduces to zero. The reference current amplitude reaches the maximum of the limiter. Since the control system is a linear system, $i_{sa}$ is the superposition of the two step responses, which are

$$G_{i_{sa, step}} = \frac{G_G G_d}{s(L_q + L_g - L_{gd} H_d) + G_G G_d}$$

$$+ \frac{1-G_d H_d}{s(L_q - L_g - L_{gd} H_d) + G_G G_d}$$

(26)

Without loss of generality, the analysis is carried out at the initial current of 0 and the initial phase of 0 degree of $u_{gs}$. According to the characteristic of PR controller, the phase of reference current is opposite to the voltage of $u_{gs}$ after the fault. Thus, the reference current and voltage can be given by

$$i_{sa} = -I_{s_{max}} \cos (\omega t) u(t)$$

$$u_{gs} = |u_{gs}| \cos (\omega t) [u(t + t_0) - u(t)]$$

(27)

where $I_{s_{max}}$ is the maximum of the limiter.

With the Laplace transformation, (25) can be transformed as

$$i_{sa}(s) = -I_{s_{max}} \frac{s}{s^2 + \alpha_0^2} G_{i_{sa, step}}$$

$$+ \left( e^{a_0 t_0} - 1 \right) u_{gs} \frac{s}{s^2 + \alpha_0^2} G_{i_{sa, step}}$$

$$= G_1 e^{a_0 t_0} G_2 + G_2$$

(28)

Considering that

$$L^{-1}(e^{a_0 t_0} G_2) = u(t + t_0) f_2(t + t_0)$$

(29)

which has little effect on the $i_{sa}(t)$ at time $t = 0$, and thus it can be ignored. Then, (28) can be approximated as

$$i_{sa}(s) = -I_{s_{max}} \frac{s}{s^2 + \alpha_0^2} G_{i_{sa, step}}$$

$$+ \left( e^{a_0 t_0} - 1 \right) u_{gs} \frac{s}{s^2 + \alpha_0^2} G_{i_{sa, step}}$$

$$= G_1 e^{a_0 t_0} G_2 + G_2$$

(28)

III. PARAMETERS DESIGN BASED ON THE FAULT CURRENT LIMITATION

This article has been accepted for publication in a future issue of this journal, but has not been fully edited. Content may change prior to final publication. Citation information: DOI 10.1109/TPWRD.2020.2970247, IEEE Transactions on Power Delivery.
\[ i_{sa} (t) = L^{-1} \left( \frac{1}{s} G_{s, step} \right) \]  
(32)

The amplitude changes of current and voltage can be equivalent to the step response of \( G_{step} \), where the overshoot and convergence time can be obtained. Since the order of \( G_{step} \) is too high to express \( i_{sa}(t) \) analytically, it is directly calculated through the MATLAB, and the parametric effect of the inner current regulator and the time delay on the overshoot are illustrated in Fig. 6.

It is seen that the parametric effect on the overshoot has a minimum value when \( K_{ps} = K_{pi1} \) with a certain value of \( T_d \). When \( K_{ps} < K_{pi1} \), the larger the \( K_{ps} \), the smaller the overshoot of fault current is obtained. In contrast, when \( K_{ps} > K_{pi1} \), the larger the \( K_{ps} \), the larger the overshoot of fault current is seen. From Fig. 6 (b), it is seen that the effect of \( T_d \) on the overshoot has a minimum value when \( T_d = T_{d0} \). When \( T_d < T_{d0} \), the larger the \( T_d \), the smaller the fault current overshoot is. When \( T_d > T_{d0} \), the larger the \( T_d \), the larger the fault current overshoot is. In order to ensure that the system has sufficient damping, the \( K_{ps} \) has a minimum \( K_{ps, min} \) and \( T_d \) has a maximum \( T_{d,max} \).

Considering that the allowed overshoot is \( \delta \% \), the satisfactory region of \( K_{ps} \) can be obtained as

\[
\max(K_{ps, min}, K_{ps, \delta \% max}) \leq K_{ps} \leq K_{ps, \delta \% min} \]  
(33)

where \( K_{ps, \delta \% min} \) and \( K_{ps, \delta \% max} \) are calculated with (32) with the condition of \( \delta \% \).

The parametric effect of the inner current regulator and the time delay on the convergence time are shown as Fig. 7. From Fig. 7 it can be seen that the larger the \( K_{pi} \) and the smaller the \( T_d \), the shorter the convergence time \( t_i \) is obtained. Assuming that the allowed convergence time is \( t_{i1} \), the satisfactory region can be obtained as

\[
K_{pi, t_{i1, min}} \leq K_{pi} \]  
(34)

where \( K_{pi, t_{i1, min}} \) is calculated through with (32) in the condition of \( t_{i1} \).

Considering that the initial phase of the voltage is \( \phi \), (27) can be written as

\[
\begin{align*}
\dot{u}_{sa} &= \dot{u}_{sa}\max \cos (o t + \phi) u(t) \\
n_{sa} &= [\mu_p \cos (o t + \phi)] [u(t + t_0) - u(t)] \\
\end{align*}
\]  
(35)

And (31) should be modified as (36).

The effect of \( \phi \) on the overshoot is shown as Fig. 8. From Fig. 8 (a), it can be seen that the overshoot of \( \alpha \) is related with the initial phase. Thus, the overshoot is largest when the fault occurs at the phase of \( n \pi/3 \) (\( n = 0, 1, 2, 3 \ldots \)), and the overshoot is smallest when the fault occurs at the phase of \( (2n+1)\pi/6 \) (\( n = 0, 1, 2, 3 \ldots \)) as shown in Fig. 8 (b). Hence, both the overshoot and the convergence time of fault current should be calculated with \( \phi = 0 \), which is the most serious condition, and the satisfactory region can be obtained as (37),

\[
\max(K_{ps, min}, K_{ps, \delta \% min}, K_{pi, t_{i1, min}}) \leq K_{ps} \leq K_{ps, \delta \% max} \]  
(37)
with voltage feedforward $T_d = 0$

$$Z_{cl} = \frac{G_i G_d + s L_{eq}}{1 + G_i G_d - H_u G_d} \text{ (39)}$$

First, at the low frequency, $G_d$ and $H_u$ can be simplified as

$$G_d = 1 \quad H_u = 1 \text{ (40)}$$

Consequently, the impedance modulus can be obtained as

$$|Z_{cl}(\omega)| = \sqrt{\frac{K_{pi}^2 + (\omega L_{eq})^2 + (K_{pi} \omega_0)^2}{1 + \omega^2 \omega_0^2 \left[100(-\omega^2 + \omega_0^2)\right] + L_{eq} K_{pi} \omega_0^2 \omega_0^2 \left[5(-\omega^2 + \omega_0^2)\right]}} \text{ (42)}$$

$$|Z_{cl}(\omega)| = \sqrt{\frac{K_{pi}^2 - 2\omega L_{eq} K_{pi} \sin(\omega T_d) + (\omega L_{eq})^2}{1 + (K_{pi} K_{pv})^2 - 2K_{pi} K_{pv} \frac{1 + \cos(-\omega T_d) + (\omega T_d)^2}{1 + (\omega T_d)^2} \cos(-\omega T_d) + 1 - 2 \frac{\cos(-\omega T_d) + \sin(-\omega T_d) \omega T_d}{1 + (\omega T_d)^2}} \text{ (43)}$$
B. Without the voltage feedforward loop

When there is no voltage feedforward loop, according to (19), the impedance of MMC can be obtained as

$$Z_{cl} = \frac{G_{i1} + sL_{eq}}{1 + G_{i0}G_{d}}$$

(44)

The parameters of outer voltage loop regulator can be designed with either the proportional gain or the integral gain of the PR regulator dominating at the crossover frequency.

1) Proportional gain dominating at the crossover frequency.

With the proportional gain dominating at the crossover frequency, the impedance modulus at the low frequency range can be obtained as (47) in the bottom of this page, from which, it can be seen that the larger the $K_{pi}$ and the smaller the $K_{pi}K_{pv}$, the larger the $|Z(o)|$ is obtained.

At high frequencies, the impedance modulus is obtained as (45).

$$|Z_{cl}(o)| = \sqrt{\frac{K_{pi}^2 - 2\alpha L_{eq}K_{pi}\sin(oT_d) + (\alpha L_{eq})^2}{K_{pi}K_{pv}} + 1 + 2K_{pi}K_{pv}\cos(-oT_d)}$$

(45)

where the $\alpha L_{eq}$ is far larger than others, and hence the $K_{pi}$ has little effect on the impedance modulus. Fig. 13 plots the amplitude-frequency responses of $Z_{cl}(o)$.

2) Integral gain dominating at the crossover frequency.

With the integral gain dominating at the crossover frequency, the impedance modulus in the low frequency range is

$$|Z_{cl}(o)| = \sqrt{\frac{K_{pi}^2 + (oL_{eq})^2 + K_{pi}^2 o^2 \omega_l^3 / 100(-\omega^2 + \omega_l^2) + L_{eq}K_{pi}\omega^2\omega_l / 5(-\omega^2 + \omega_l^2)^2}{1 + 2K_{pi}K_{pv} + K_{pi}K_{pv}(1 + K_{pi}K_{pv})\omega_l^2 / 5(-\omega^2 + \omega_l^2)^2 + K_{pi}K_{pv}}[1 + \omega^2 \omega_l^2 / 100(-\omega^2 + \omega_l^2)^2]^2}$$

(46)

and the smaller the $\alpha L_{eq}$ is, the smaller the $K_{pi}$.

TABLE I

<table>
<thead>
<tr>
<th>SYMBOL</th>
<th>DESCRIPTION</th>
<th>VALUE</th>
</tr>
</thead>
<tbody>
<tr>
<td>$u_r$</td>
<td>Rated ac voltage of MMC</td>
<td>230 kV</td>
</tr>
<tr>
<td>$P$</td>
<td>Rated power of the MMC</td>
<td>400 MW</td>
</tr>
<tr>
<td>$L_{eq}$</td>
<td>Equivalent inductance of MMC</td>
<td>0.1 H</td>
</tr>
<tr>
<td>$L_w$</td>
<td>Line inductance</td>
<td>0.05 H</td>
</tr>
<tr>
<td>$I_{lim}$</td>
<td>The limit value of current limiter</td>
<td>1.0 p.u.</td>
</tr>
<tr>
<td>$f_0$</td>
<td>Grid frequency</td>
<td>50 Hz</td>
</tr>
<tr>
<td>$T_d$</td>
<td>Time delay</td>
<td>0.3 ms</td>
</tr>
</tbody>
</table>

is expressed as (48), which is shown in the bottom of this page. From (48), the same effect of $K_{pi}$, and $K_{pi}K_{pv}$ on $|Z(o)|$ as that with the proportional gain can be observed.

In the high frequency range, the impedance modulus can be obtained as

$$|Z_{cl}(j\omega)| = \sqrt{\frac{K_{pi}^2 + oL_{eq}K_{pi}^2 - 2\alpha L_{eq}K_{pi}\sin(oT_d)}{1 - 2K_{pi}K_{pv}/o\sin(oT_d) + \left(K_{pi}K_{pv}/\omega_l\right)^2}}$$

where similarly the $\alpha L_{eq}$ is far greater than others, and $K_{pi}$ has little effect on the impedance modulus.

The amplitude-frequency characteristic of $Z_{cl}(o)$ is shown in Fig. 14. It is clear that the controller parameters only affect the impedance modulus in the low frequency range.

V. SIMULATIONS

The similation study is carried out in PSCAD to verify the effectiveness of the parameters design method. The arm-averaged model of the MMC given in Fig. 1 is adopted in the simulation, in which each bridge is replaced by a controlled voltage source [32]. The wind farm is modeled by a controlled current source with the PLL. The parameters used in the simulation are given in Table I.

Fig. 15 shows the parametric impact of the inner current loop on voltage stability with $T_d = 0.3$ ms. Based on (6), it can be calculated that the stability of the inner current loop requires $f_c < 913$ Hz and $K_{pi} < 523.5$. The simulation result with $f_c = 920$ Hz $> 913$ Hz and $K_{pi} = 577 > 523.5$ is given in Fig. 15 (a), where the unstable operation of the MMC can be clearly observed. In contrast, the MMC can be stabilized when the
Considering the voltage feedforward loop, the stability of the system requires $K_{pv} K_{pp} \leq 1$, which is indicated by (15). Fig. 16 shows the simulation results with $T_d = 0.3 \text{ ms}, T_{rd} = 0.1 \text{ ms}$ and $\omega_n = 4070$, where the unstable operation of the system when $K_{pv} K_{pp} > 1$ can be clearly observed, as shown in Fig. 16 (c), and thus, the correctness of (15) is verified.

For the condition that voltage feedforward is not adopted, either the proportional or the integral gain of the PR regulator of the voltage loop can be designed to have dominant effect at crossover frequency. In former case, Eq. (22), i.e., $K_{pi} K_{pv} < 1$, should be satisfied. This is verified by Fig. 17, which illustrates the unstable operation of the MMC system when $K_{pi} K_{pv} > 1$ (see Fig. 17 (c)) and the stable operation when $K_{pi} K_{pv} < 1$ (see Fig. 17 (a) and (b)). In the latter case, (24) should be met in order for the stable operation of the system, which is verified by Fig. 18.

Table II shows the simulated and calculated overshoot of the fault current with different parameters under a three phase short circuit fault with $L_p = 0.01 \text{ H}$ and $T_d = 0.3 \text{ ms}$. From TABLE II, it can be seen that the error between simulation and the time-domain waveform of the simulated and calculated fault
TABLE II
OVERSHOOT OF FAULT CURRENT IN DIFFERENT PARAMETERS WITH VOLTAGE FEEDFORWARD

<table>
<thead>
<tr>
<th>K_{pi}</th>
<th>simulation/p.u.</th>
<th>( I_{max} ) calculation/p.u.</th>
<th>error/%</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>1.30</td>
<td>1.24</td>
<td>4.61</td>
</tr>
<tr>
<td>20</td>
<td>1.21</td>
<td>1.18</td>
<td>2.4</td>
</tr>
<tr>
<td>30</td>
<td>1.17</td>
<td>1.14</td>
<td>2.56</td>
</tr>
<tr>
<td>40</td>
<td>1.15</td>
<td>1.13</td>
<td>1.73</td>
</tr>
<tr>
<td>50</td>
<td>1.11</td>
<td>1.11</td>
<td>2.63</td>
</tr>
<tr>
<td>60</td>
<td>1.13</td>
<td>1.08</td>
<td>4.42</td>
</tr>
<tr>
<td>70</td>
<td>1.12</td>
<td>1.05</td>
<td>6.25</td>
</tr>
</tbody>
</table>

VI. CONCLUSIONS

This paper presents a systematic parameters tuning guideline for the dual-loop voltage-controlled MMC considering the requirement of voltage stability, transient fault current limitation and stiffness of voltage against load current change. The impact of voltage feedforward on stability and fault current limitation is investigated. It is found out that the overshoot of the fault current increases significantly if the voltage feedforward is not used. Within the satisfactory region of the parameters, the smaller \( K_{pi} \) will lead to higher stiffness of the output voltage of the MMC against load current change. Based on the proposed method, the controller parameters can be calculated directly without trial and error. The effectiveness of the proposed method is verified by time domain simulation.

REFERENCES


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This article has been accepted for publication in a future issue of this journal, but has not been fully edited. Content may change prior to final publication. Citation information: DOI 10.1109/TPWRD.2020.2979247, IEEE Transactions on Power Delivery
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