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Article

An Accurate Time Constant Parameter Determination Method for the Varying Condition Equivalent Circuit Model of Lithium Batteries

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Abstract: An accurate estimation of the state of charge for lithium battery depends on an accurate identification of the battery model parameters. In order to identify the polarization resistance and polarization capacitance in a Thevenin equivalent circuit model of lithium battery, the discharge and shelved states of a Thevenin circuit model were analyzed in this paper, together with the basic reasons for the difference in the resistance capacitance time constant and the accurate characterization of the resistance capacitance time constant in detail. The exact mathematical expression of the working characteristics of the circuit in two states were deduced thereafter. Moreover, based on the data of various working conditions, the parameters of the Thevenin circuit model through hybrid pulse power characterization experiment was identified, the simulation model was built, and a performance analysis was carried out. The experiments showed that the accuracy of the Thevenin circuit model can become 99.14% higher under dynamic test conditions and the new identification method that is based on the resistance capacitance time constant. This verifies that this method is highly accurate in the parameter identification of a lithium battery model.

Keywords: lithium battery; Thevenin model; resistance capacitance time constant; parameter identification

1. Introduction

The microscopic physical parameters of lithium batteries are difficult to measure directly by sensors or measurement techniques [1–3]. Parameter identification in equivalent models of lithium battery is an important issue in battery management [4–7]. The battery model can be divided into an electrochemical model [8], black box model and equivalent circuit model in terms of its different building mechanisms [9–12]. The electrochemical model is based on the analysis of chemical reactions inside the battery, and the partial differential equation is established to describe the electrodes and electrolyte dynamics [13,14]. It is suitable for optimum design and the safety analysis of the battery [15–17]. The black-box model is a linear or non-linear function that can describe the response characteristics of voltage of batteries [18–21]. However, it usually needs a data-driven algorithm as support, including the neural network method, support vector regression method, and genetic particle filter method [22–24].

The black-box model can establish the model structure and parameter optimization flexibly, but it lacks the significance of physics [25–27]. The equivalent circuit model consists of capacitors and resistors to simulate the dynamic voltage response characteristics of batteries [28–30]. The relationship between the parameters in this model is direct and obvious [31] and there are fewer model parameters, which makes the mathematical description of state space easier [32,33]. Therefore, it is widely used in system simulation and practical engineering [34].

The commonly used equivalent circuit models are the Rint model, Thevenin model, RC model, The Partnership for a New Generation of Vehicles (PNGV) model and the General Non-Linear (GNL) model. In these models [35–37], Thevenin model is often chosen as a battery model in battery State of Charge (SOC) estimations because of its simple circuit structure and moderate difficulty in parameter identification [38]. In the process of identifying the Thevenin model parameters, the Thevenin model generally uses a first-order or second-order structure, and rarely uses a high-order structure [39]. This is because the increase in order has little contribution to improving the accuracy of the model, and it also increases the difficulty of parameter identification [40]. In order to get accurate model parameters, it is necessary to study the influence of working current, SOC and temperature on the model parameters, as well as the identification method of model parameters.

In reference [41], a first-order equivalent circuit model of Thevenin based on self-healing characteristics is proposed and verified on the experimental platform. In reference [42], the parameter identification method of the second-order Thevenin model with different discharge rate is studied. At a low discharge and charge rate (below 0.5 C), the parameter identification method of the valve regulated lead-acid (VRLA) and the LiFePO₄ (LFP) battery model is used in reference [40]. The Thevenin model with a self-discharge effect is proposed in reference [43], and its parameters are identified within the SOC range of 20%–80%. In reference [44], the application of charge–discharge cycling electrochemical impedance spectroscopy in model parameter identification was proposed. In this paper, based on the first-order Thevenin model, the load resistance is introduced. The influence of load resistance on the RC time constant of a Thevenin model in the process of discharge and shelving is analyzed in detail. At the same time, the dynamic equation and identification method of each parameter of the model are given with accuracy. The model parameters are identified by hybrid pulse power characterization (HPPC) experiments, and the accuracy of the identification method is verified by simulation.

2. Mathematical Analysis

2.1. Dynamic Thevenin Mode

Considering the demands of engineering application, the dynamic characteristics of a lithium battery should be characterized by uncomplicated equivalent model [45,46], so the Thevenin model of lithium battery equivalent circuit model is selected in this paper. The Thevenin model is composed of a resistance capacitance (RC) circuit in series with ohm internal resistance [47–49]. Its basic idea is to use ohm internal resistance to characterize the instantaneous change in terminal voltage in the charging and discharging process [50–52], and an RC parallel circuit to characterize the polarization effect of the battery in the using process [53,54]. This model can accurately characterize the dynamic characteristics of lithium battery in the working process. A description of the model is shown in Figure 1a.

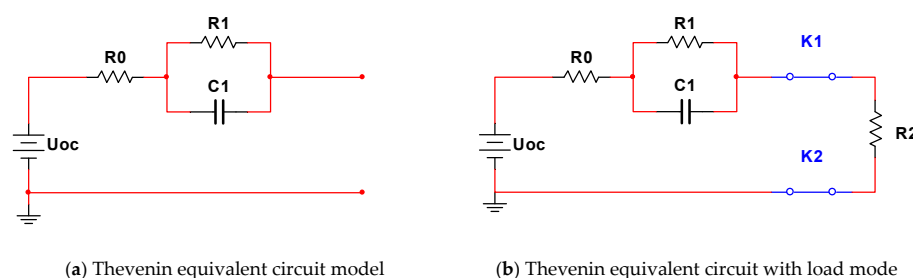


Figure 1. Thevenin equivalent circuit and load mode.

In Figure 1a, U_{OC} represents the open circuit voltage of the battery, and R_0 represents the ohmic internal resistance of the battery, it can characterize the change in voltage response at the moment of battery charging and discharging. R_1 and C_1 represent the polarization resistance and polarization capacitance inside the battery, respectively. The circuit formed by R_1 and C_1 can reflect the gradual change in battery voltage during and after charging and discharging.

We will then discuss the different working states of the circuit when switches $K1$ and $K2$ are closed and opened at the same time. In Figure 1b, we specify the discharge direction as the reference positive direction of the circuit.

When switches $K1$ and $K2$ are not closed, the circuit is in the initial state. The capacitor in the circuit has no electric energy and the voltage on the capacitor is zero. When switches $K1$ and $K2$ are closed, the battery will work with load and start discharging. Equation (1) can be obtained according to

$$U_2 = U_{OC} - U_C - R_0 \times i \tag{1}$$

In Equation (1), i is the discharge current, U_C is the voltage at both ends of polarization capacitor C_1 , R_2 is the load resistance, and U_2 is the load resistance voltage. For polarization capacitor C_1 , when switches $K1$ and $K2$ are closed, it is the zero-state response, as expressed in Equation (2).

$$U_C = i \times R_1 (1 - e^{-\frac{t}{\tau_1}}) \tag{2}$$

In Equation (2)

$$\tau_1 = R_{eq1} \times C_1 \tag{3}$$

by connecting R_0 and R_2 in series and R_1 in parallel. Its evaluation expression is Equation (4).

$$R_{eq1} = \frac{(R_0 + R_2) \times R_1}{(R_0 + R_2) + R_1} \tag{4}$$

When switches $K1$ and $K2$ are closed for t_1 s, they are turned on again. At this time, for capacitor C_1 , it is a zero-input response. The circuit diagram is shown in Figure 2b. At this point, the voltage on the capacitor is shown as expressed in Equation (5).

$$U_c = U_{c0} e^{-\frac{t}{\tau_2}} \tag{5}$$

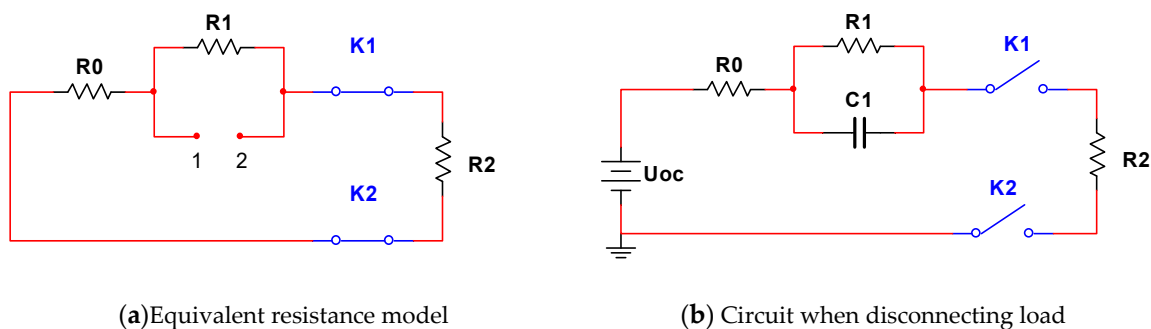


Figure 2. Equivalent circuit.

In Equation (5)

$$\tau_2 = R_{eq2} \times C_1 \tag{6}$$

As can be seen from Figure 2b, R_{eq2} is resistance R_1 .

Since the voltage on the capacitor cannot be abruptly changed, when the switch is changed from the closed state to the open state, U_{c0} is the value of the capacitor at the time t_1 before the switch is opened. Its expression is as shown in Equation (7).

$$\begin{cases} R_{eq2} = R_1 \\ U_{C0} = i \times R_1 (1 - e^{-\frac{t_1}{\tau_1}}) \end{cases} \quad (7)$$

From the theoretical analysis above, the following two conclusions can be obtained.

First, when Thevenin equivalent circuit model works in discharge state and shelved state, the RC time constants in the shelved state and discharge state are different due to the unequal equivalent resistance. The RC time constant τ_2 of shelved state is larger than that of discharge state τ_1 .

The second point is that when the switches $K1$ and $K2$ are closed and opened, the expression of Thevenin's equivalent circuit model is a piecewise function, and the function expression is in Equation (8).

$$\begin{cases} U_2 = U_{OC} - i \times R_0 - i \times R_1 (1 - e^{-\frac{t}{\tau_1}}) & 0 \leq t \leq t_1 \\ U_2 = U_{OC} - i \times R_1 (1 - e^{-\frac{t_1}{\tau_1}}) e^{-\frac{t}{\tau_2}} & t_1 \leq t < t_2 \end{cases} \quad (8)$$

In Equation (8), 0 to t_1 indicate the switch closing time; t_1 to t_2 indicate the time when the switch is turned on.

2.2. Parameter Identification

According to the American freedom vehicle battery experiment manual [55], the HPPC experiment is conducted on lithium batteries at 10 points when SOC equals 0.1 to 1.0. The discharge rates of lithium batteries are all set at 1C. In the single-cycle step, 10 s of constant current discharge, 40 s shelved and 10 s constant current charge are arranged in turn, and the interval between 10 SOC points is 40 min. Figure 3 shows the current pulse curve and the corresponding voltage change curve in the HPPC experiment.

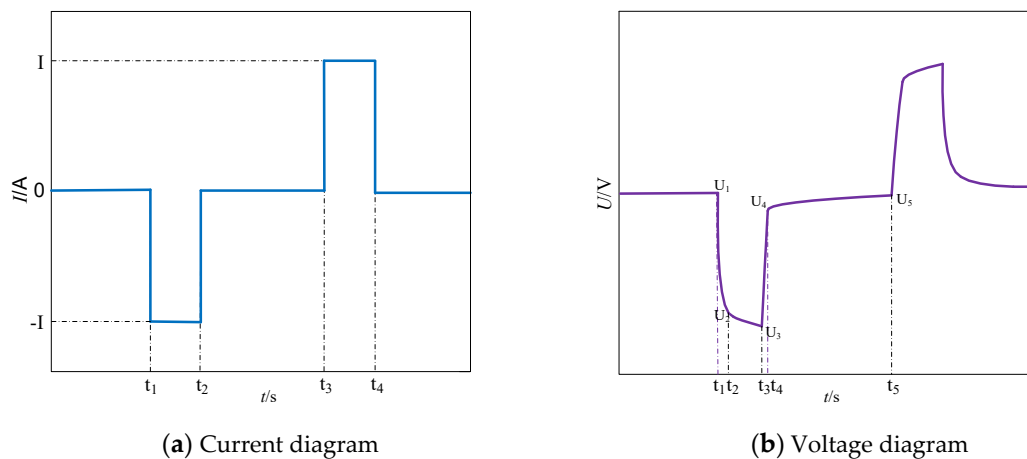


Figure 3. Current and voltage diagram during HPPC experiment.

From the voltage response curve of HPPC experimental battery, the characteristics of each SOC point can be obtained as follows.

The voltage of the battery terminal of t_1 - t_2 drops instantaneously. This is because the battery discharge current increases abruptly from 0 to 1C, resulting in a sudden change in voltage on the ohmic internal resistance. The terminal voltage of the t_2 - t_3 battery decreases slowly during the process of discharging the current charging polarization capacitor, which is caused by the zero-state response of the RC loop. The terminal voltage of t_3 - t_4 battery rises instantaneously, which is caused by the sudden

change in the discharge current to 0 and the disappearance of voltage on ohmic internal resistance. During the t_4 - t_5 period, the slow rise in battery terminal voltage is the process of polarization resistance discharging by the polarization capacitor, which is caused by the zero-input response of the RC circuit. t_5 time is the charging phase of the battery. There is a phase of sudden voltage increase and a phase of slow voltage increase during the charging. According to the above characteristics, the following methods can be used to identify the parameters of the Thevenin equivalent model.

2.2.1. Open Circuit Voltage Identification

The open circuit voltage U_{OC} is the voltage that keeps the battery stable at both positive and negative terminals when the battery is left for a long time. The experiments show that the terminal voltage of the battery after standing for 1 h is basically equal to the open circuit voltage of the battery. Therefore, the battery is discharged at a 1C constant current for 6 min and then shelved for 1 h. At this time, the voltage at both ends of the battery can be considered as the open circuit voltage of the battery under SOC state;

2.2.2. Identification of R_0 , R_1 , C_1

This curve of t_2 - t_3 is a zero-state response curve, as expressed in Equation (9)

$$U_2 = U_{OC} - i \times R_0 - i \times R_1(1 - e^{-\frac{t}{\tau_1}}) \quad (9)$$

Simplify Equation (9) to Equation (10)

$$y = a - b - c(1 - e^{-\frac{x}{d}}) \quad (10)$$

The curve from t_4 - t_5 is a zero-input response curve, as expressed in Equation (11)

$$U_2 = U_{OC} - i \times R_1(1 - e^{-\frac{10}{\tau_1}})e^{-\frac{t}{\tau_2}} \quad (11)$$

Simplify Equation (11) to Equation (12)

$$y = a - g \times e^{-\frac{x}{h}} \quad (12)$$

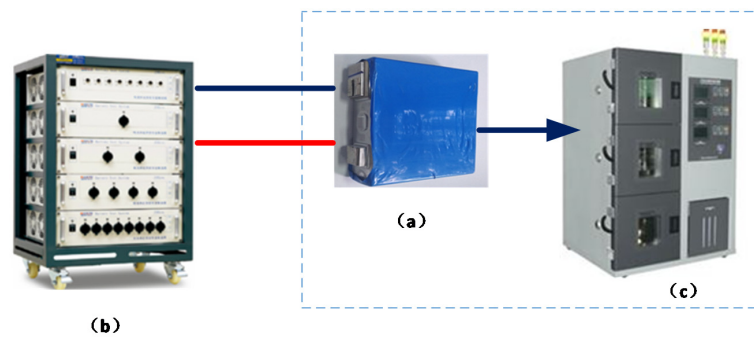
In Equations (8)–(12), y represents the terminal voltage U_2 , and x represents the time t ; the six parameters a , b , c , d , h , and g correspond to U_{OC} , $i \times R_0$, $i \times R_1$, τ_1 , τ_2 and $i \times R_1(1 - e^{-\frac{10}{\tau_1}})$, respectively.

According to the identified open-circuit voltage U_{OC} and load current i measured by the current sensor, R_0 , R_1 , and i can be identified by using cftool toolbox in MATLAB. When the time constant τ_2 is obtained, C_1 can be obtained by using $C_1 = \tau_2/R_1$.

3. Experimental Design

In order to get the parameters of the Thevenin equivalent model, HPPC experiments were carried out. At the same time, the open-circuit voltage was measured for lithium batteries under different SOC conditions, then the variation rule of the parameters of the model with the working state was obtained through experimental analysis and calculation.

The experimental object used was a lithium ternary polymer battery, and its appearance is shown in Figure 4a. The battery has a nominal capacity of 40 Ah and an actual capacity of 39.37 Ah. The instruments used in the experiment included a charge and discharge instrument and a three-layer independent temperature control experiment box. Their appearance is shown in Figure 4b,c. In order to avoid the influence of temperature change on model parameters, the experiment was carried out at 25 °C. A constant temperature of 25 °C will be maintained by a temperature-controlled test chamber.



(a) Ternary polymer lithium battery (b) Charge and discharge instrument (c) Three independent temperature control test boxes

Figure 4. Appearance diagram of experimental equipment.

The HPPC experiment is to stimulate the battery with continuous discharge pulses, then acquire the battery parameters by experimental data. This experiment added two discharge experimental points to the base of the standard HPPC experiment. The two points were SOC, equal to 0.95 and 0.05, respectively. The complete HPPC experimental steps are as follows.

1. The lithium batteries were discharged by IC, and then the batteries were shelved for 2 h after discharging. The batteries were charged to SOC 100% by constant current and voltage;
2. Let the battery stand for 10 h, then measure and record the open circuit voltage of the battery;
3. Discharge at 1C for 3 min, then shelve it for 40 min;
4. Steps 3 and 4 were performed at four points where the SOC equaled 1, 0.95, 0.1, and 0.05, respectively;
5. A current pulse experiment was performed on a lithium battery. First, it was discharged at 1C for 10 s, then shelved for 40 s, charged at 1C for 10 s thereafter, then shelved for 40 s;
6. The battery was discharged at 1C for 6 min, then left to stand for 40 min;
7. Steps 6 and 7 were performed at eight points where the SOC was equal to 0.9, 0.8, 0.7...0.3, and 0.2, respectively.

Discharge experiments of lithium batteries were carried out according to the above experimental steps. The current and voltage during the experiment were shown in Figure 5.

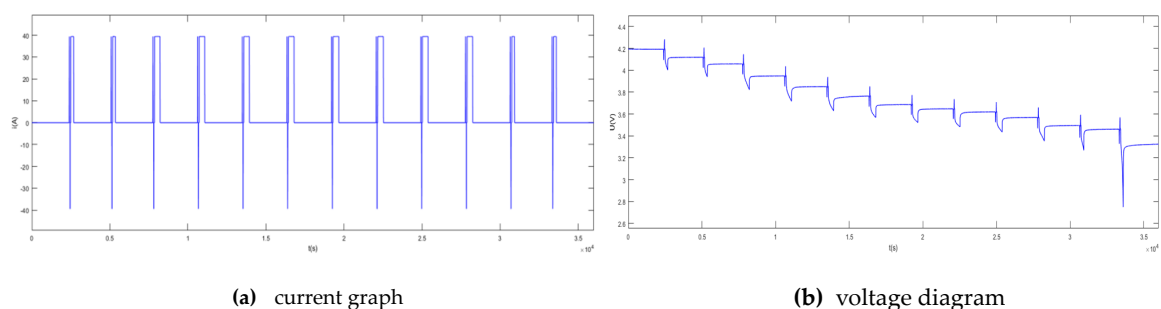


Figure 5. HPPC experiment of the discharge process.

With the HPPC experimental data, the corresponding relationship between different SOC points and various parameters can be drawn when the Thevenin equivalent model is at 25 °C, as shown in Table 1.

Table 1. Model parameters under different SOC states.

SOC	τ_1/s	τ_2/s	$R_0/m\Omega$	$R_1/m\Omega$	C_1/F	U_{oc}/V
0.05	7.773	8.765	2.445	1.2510	7006.3948	3.4616
0.1	8.99	10.47	2.229	0.8389	12,480.6294	3.4951
0.2	10.26	13.43	2.071	0.6871	19,545.9176	3.5686
0.3	10.33	12.60	2.019	0.6200	20,322.5806	3.6201
0.4	9.877	12.15	1.988	0.5833	20,829.7617	3.6480
0.5	8.842	12.33	1.956	0.5780	21,332.1799	3.6867
0.6	9.441	12.08	1.947	0.7818	15,451.5221	3.7648
0.7	9.388	11.93	1.936	0.7674	15,545.9995	3.8504
0.8	8.785	11.62	1.948	0.7212	16,112.0355	3.9487
0.9	8.515	11.22	1.953	0.6715	16,708.8608	4.0584
0.95	8.684	12.72	1.976	0.6590	19,301.9727	4.1192
1	9.033	12.79	1.994	0.7220	17,714.6814	4.1917

From the identified parameters, it can be seen that when the Thevenin equivalent circuit model works in discharge and shelf state, τ_2 is larger than τ_1 . When SOC is 0.05 and 0.1 respectively, the ohmic internal resistance, polarization resistance and polarization capacitance of the battery will change rapidly, but they are relatively stable in other discharge stages. With SOC as the independent variable and each parameter in Table 1 as the dependent variable, we can obtain fitting Equations (13)–(16), where R_0 , R_1 , C_1 and U_{OC} vary with SOC through polynomial fitting.

$$R_0 = -0.04868 \times SOC^7 + 0.2129 \times SOC^6 - 0.3831 \times SOC^5 + 0.3659 \times SOC^4 - 0.1996 \times SOC^3 + 0.06241 \times SOC^2 - 0.01078 \times SOC + 0.002851 \quad (13)$$

$$R_1 = 0.2345 \times SOC^8 - 1.438 \times SOC^7 + 3.497 \times SOC^6 - 4.409 \times SOC^5 + 3.135 \times SOC^4 - 1.277 \times SOC^3 + 0.2909 \times SOC^2 - 0.03471 \times SOC + 0.002402 \quad (14)$$

$$C_1 = 1.139 \times 10^7 \times SOC^8 - 4.641 \times 10^7 \times SOC^7 + 7.585 \times 10^7 \times SOC^6 - 6.355 \times 10^7 \times SOC^5 + 2.875 \times 10^7 \times SOC^4 - 6.515 \times 10^6 \times SOC^3 + 3.539 \times 10^5 \times SOC^2 + 1.356 \times 10^5 \times SOC - 107.2 \quad (15)$$

$$U_{OC} = 5.062 \times SOC^5 - 15.72 \times SOC^4 + 18.57 \times SOC^3 - 9.559 \times SOC^2 + 2.508 \times SOC + 3.333 \quad (16)$$

4. Model Verification

After identifying the parameters of the model, the dynamic simulation model of the Thevenin equivalent circuit was constructed in Simulink. The identified parameters were put into the simulation model, then different working currents were input, the output voltage response of the model was compared with the actual voltage data, and the model was verified. The built model validates the Simulink simulation structure, as shown in Figure 6.

To calculate SOC with discharge current, the method of the ampere-hour (AH) integral is applied. Its internal structure is shown in Figure 7.

The internal structure of Thevenin's equivalent circuit model is shown in Figure 8, where each circuit component is a controllable parameter that changes over time. The model has five inputs and one output. The inputs are i , R_0 , R_1 , C_1 and U_{OC} , and the output is the terminal voltage U . This model can simulate the working condition of the lithium battery.

In order to evaluate the accuracy of the model parameters, the variable operating current is added to the model and the difference between the model output voltage and the time output voltage is compared. The variable operating current is shown in Figure 9.

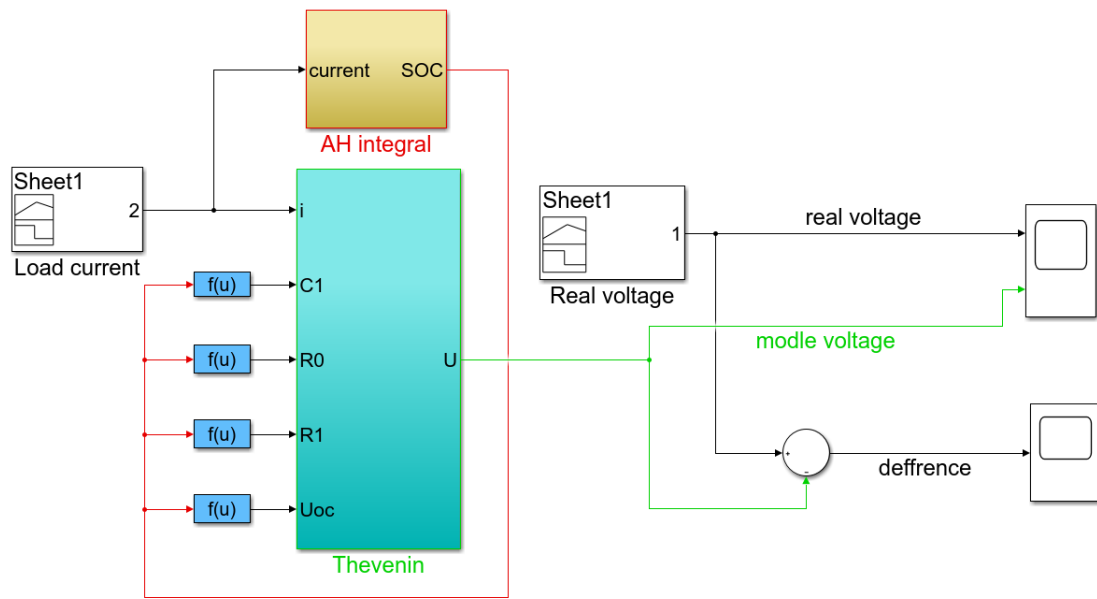


Figure 6. Simulink Model Verification Structural Diagram.

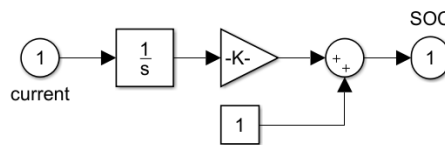


Figure 7. The internal structure of ampere-hour (AH) integral.

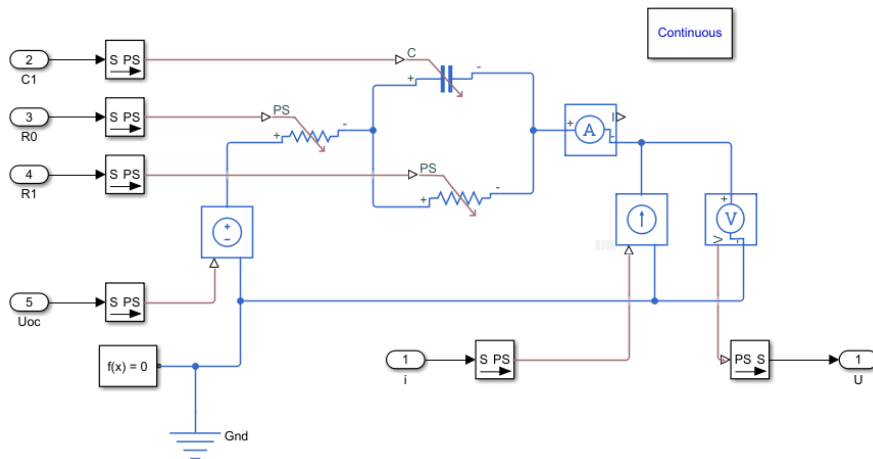
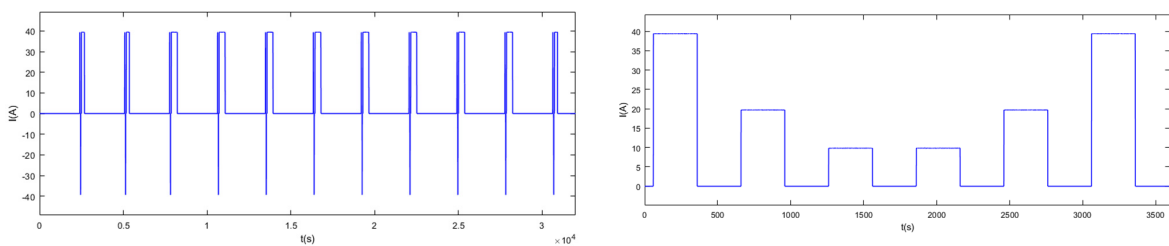


Figure 8. The internal structure of Thevenin model.



(a) The variable operating current 1

(b) The variable operating current 2

Figure 9. The variable operating current.

As shown in Figure 10, the blue curve is the output voltage of the model, and the red curve is the actual output voltage of the battery. It can be seen that the output voltage of the model is in good agreement with the actual value, which indicates the feasibility and reliability of the parameter identification method.

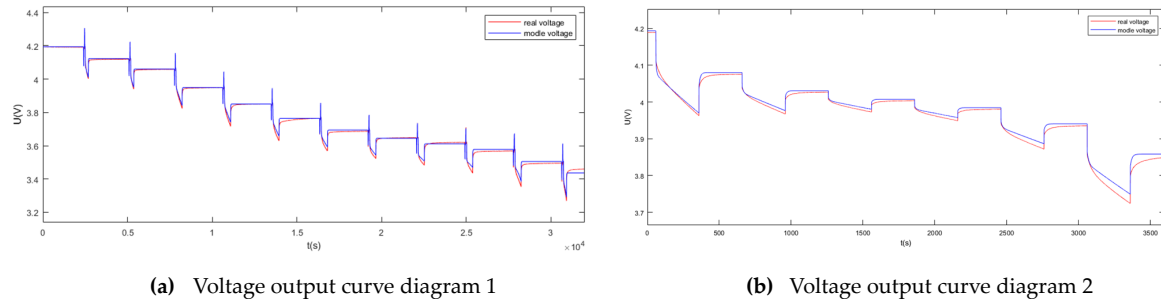


Figure 10. Voltage output curve diagram.

The difference between the output voltage of the model and the actual output voltage of the battery is defined as the model error. Model accuracy is defined as the percentage of model error to the actual output voltage of the battery. From the curve error in Figure 11, it can be seen that the maximum error of the output voltage of the model is 0.0361 and 0.0326 V, respectively. The model accuracy is 99.14% and 99.22% when the maximum voltage of the lithium battery is 4.2 V.

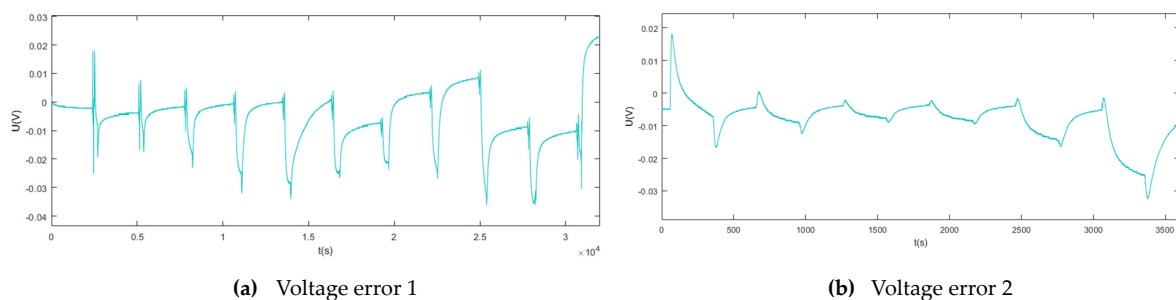


Figure 11. Voltage error.

5. Conclusions

The accurate identification of parameters of lithium battery model is an important part of the SOC estimation of lithium battery. In this paper, the classical Thevenin equivalent circuit model is selected to identify the parameters. Through detailed circuit analysis, the accurate expressions of the RC time constant and terminal voltage of lithium batteries are derived. After HPPC experiments that identify the parameters accurately, the Simulink model is established in MATLAB, and the model is verified by simulation with HPPC experimental data. The parameter identification method adopted in this paper can make the accuracy of the Thevenin model reach more than 99.14%. The parameter identification achieved good results. The research content of this paper can provide an accurate identification method for the parameter identification of a lithium battery mathematical model, and it is also an important theoretical basis for the accurate estimation of SOC in a battery management system.

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