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Unified Modular State-Space Modeling of Grid-Connected Voltage-Source Converters

Dongsheng Yang , Senior Member, IEEE, and Xiongfei Wang , Senior Member, IEEE

Abstract—This article proposes a modular state-space modeling framework for grid-connected voltage-source converters, where the different control loops, including the ac current control, the phase-locked loop, the dc-link voltage control, and the ac voltage magnitude control, can be modeled separately as building blocks. Moreover, the mathematical relationship between state-space models in the rotating (dq -) frame and the stationary ($\alpha\beta$ -) frame is explicitly established, and, thus, the modal analysis can be performed directly in the $\alpha\beta$ -frame, which allows intuitive interpretation of voltage and current oscillation modes in the $\alpha\beta$ -frame. Experimental tests of a 3-kW back-to-back converter system validate the effectiveness of the unified modular state-space modeling and analysis.

Index Terms—Component connection method (CCM), frequency coupling, sensitivity analysis, state-space model, stationary frame.

I. INTRODUCTION

VOLTAGE-SOURCE converters (VSCs) are widely used in power grid applications, for e.g., renewable power generations [1], flexible power transmission and distributions, and energy-efficient consumptions [2], [3]. The ever-increasing use of VSCs brings in more control flexibility and improved efficiency, but does also pose a number of new challenges to stability and power quality of the power system [4].

Many research efforts have thus been made to address VSC-grid interactions. The impedance-based modeling approach has been recently reported in [5] and [6] to analyze the dynamic effects of different control loops on the VSC-grid interactions. For the inner current loop, the multiple-input multiple-output (MIMO) system model can be simplified into single-input single-output (SISO) transfer functions based on complex space vectors. This SISO impedance model not only provides an intuitive insight into the interactions among the paralleled VSCs and weak power grids, but also enables to reshape the output impedances of VSCs for stabilizing the power system [7], [8].

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However, the frequency coupling effects will be induced by the inherent asymmetry of the outer control loops, such as the phase-locked loop (PLL), the dc-link voltage control (DVC), and the ac voltage magnitude control (AVC), which significantly complicate the analysis of converter dynamics. Instead of the SISO impedance transfer function, the impedance matrix has to be used to model the terminal dynamics of converters [9]–[11]. Consequently, the generalized Nyquist criterion is utilized for the stability assessment, and the stability analysis results usually provide little insight into the controller design and the system damping.

To facilitate the controller-design-oriented analysis, research works on transforming the MIMO impedance model as a closed-loop SISO system have been reported recently [12]. However, the approach requires prior knowledge on the grid impedance, which is varying over time in practice, and it is difficult to predict.

Alternatively, the state-space modeling and modal analysis can also be employed to design controllers for stabilizing VSC-grid interactions [13]. The eigenvalues and eigenvectors of the state matrix provide a complete overview of the system oscillatory modes and their damping factors [14]. The participation factors and sensitivity analysis further reveal the dynamic contributions of state variables and system parameters and, thus, help to identify the root causes of critical oscillations [15]. Moreover, differing from the impedance-based analysis, which reflects the input-output dynamic relationship locally, the state-space modeling gives a global view of the system dynamics and is thus generally preferred for large-scale interconnected systems [16].

In spite of the advantages of the modal analysis, the basic state-space modeling approach features less modularity and scalability than the impedance-based method, with respect to analyzing the control impacts of VSCs [17]. Moreover, the nonlinear dynamics of the outer control loops and the PLL adds more interconnections among control loops [18]–[20], which complicate the derivation of the state matrix of the whole control system.

To simplify the modeling process, many efforts have been devoted to modularize the state-space modeling method. In [21], each control loop of the VSC is modeled separately as a substate-space model, and then the models are combined together based on their interconnections. However, there are shared state variables among substate-space models, which have to be merged together to obtain the right state variables for the state matrix of the overall system. Therefore, without a clear definition of the combination rule, considerable efforts

are needed to reformulate the substate-space models for them to be incorporated into the system model. Hence, to tackle this challenge, the rules for combining two substate-space models with different interconnection forms, i.e., the parallel, the concatenation, the feedback, and the common input or output, are introduced in [22]. The shared state variables can be represented by a single state variable with interconnections between the submodules. Thus, the overall system model can be readily derived without the reformulations of substate-space models. Those rules only apply to two subsystems with a well-defined interconnection form, whereas the control loops of VSCs are cross coupled with each other, which makes those rules difficult to apply.

Another modular state-space modeling approach that has been applied to power systems is the component connection method (CCM) [23], where the system is decomposed into multiple components, whose interconnections are modeled as a linear algebra matrix based on the algebraic relations of their inputs and outputs. Thus, the system state-space model can be obtained by combining the linear algebra matrix with the individual state-space models of components [24]. This method features better modularity and scalability than that reported in [22] and remarkably reduces the computational effort for the power networks in which the interconnections of equipment can be explicitly defined. However, the CCM is still not readily used for modeling the control loops of VSCs, since the linearization of the outer control loops introduces additional substate-space models and interconnections, which are implicit as opposed to the physical substate-space model and interconnections. Therefore, a modular state-space modeling method that can characterize the effects of control loops is still missing.

Besides the modeling complexity, another obstacle that impedes the widespread use of the state-space modeling method is the lack of a unified mathematical relationship between the state-space models in different reference frames.

To obtain the time-invariant operating point, the state-space models of VSCs are generally developed in the dq -frame [25]. However, with the dq -frame state-space model, it is difficult to link the oscillation modes in the dq -frame to actual oscillation modes in the $\alpha\beta$ -frame. The relations between the oscillation modes in the two frames can be either frequency shifted, for e.g., the symmetric dq -frame current control, or frequency-coupled, for e.g., the asymmetric dq -frame dynamics of the PLL [11], [26], [27]. It is worth noting that this limitation of the dq -frame state-space model is also imposed on the dq -frame impedance model, and recent studies have thus been devoted to developing the $\alpha\beta$ impedance model [28], [29]. In [27], the unified impedance model is introduced, which bridges the mathematical relationships between the impedance models in the dq - and $\alpha\beta$ -frame. It is shown that the $\alpha\beta$ -frame impedance-based analysis can explicitly reveal the frequency couplings between the sub- and supersynchronous oscillations. However, the $\alpha\beta$ -frame state-space model of VSCs still remains an open issue.

To address the abovementioned challenges, this study provides an improved modular state-space modeling framework as compared with the work presented in [23], which enables us to model the system with implicit subsystems and connections

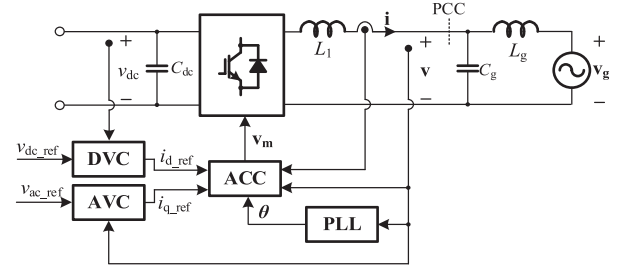


Fig. 1. Control scheme of the grid-connected VSC.

caused by linearization of control loops. Another major contribution of this study is to establish the mathematical relationship between the state-space models in the dq -frame and the $\alpha\beta$ -frame, which allows the straightforward stability analysis and intuitive interpretation of voltage and current oscillation modes in the $\alpha\beta$ -frame.

The remainder of this article is organized as follows. Section II describes the configuration of the studied system and also proposes the improved framework of modular state-space modeling. The substate-space models and interconnections used in the framework are derived in Section III and IV. Based on which, the system state-space model is established first in the dq -frame in Section V, and the mathematical relationships between the state-space models in the dq - and $\alpha\beta$ -frame are proposed in Section VI. Then, the stability analysis based on the unified state-space model is presented in Section VII. In Section VIII, Experimental tests on a 3-kW back-to-back converter system are conducted to validate the effectiveness of the unified modular state-space modeling approach. Finally, Section IX concludes this article.

II. SYSTEM DESCRIPTION AND MODELING METHOD

A. System Configuration

The control scheme of the grid-connected VSC is shown in Fig. 1. Basically, the control scheme can be divided into four parts, including the ac current control (ACC), PLL, DVC, and AVC. C_{dc} is the dc-link capacitor; L_1 is the converter filter inductor; and C_g and L_g are equivalent grid capacitance and grid inductance seen from point of common connection (PCC), respectively.

As shown in [8], the real space vectors are usually denoted with italic letters, for e.g., $x_{dq} = [x_d, x_q]^T$, whereas complex space vectors are denoted with boldface letters, for e.g., $\mathbf{x}_{dq} = x_d + jx_q$, $\mathbf{x}_{dq}^* = x_d - jx_q$. To avoid the confusion between real space vector (such as x_{dq}) and scalar (such as x_d), the vectors in this article are accented with a right arrow, i.e., $\vec{x}_{dq} = [x_d, x_q]^T$ and $\vec{\mathbf{x}}_{dq} = [\mathbf{x}_{dq}, \mathbf{x}_{dq}^*]^T$.

In Fig. 1, the complex space vectors of converter output current and voltage are denoted by \mathbf{i} and \mathbf{v} , respectively, whereas the complex space vector of grid voltage is denoted by \mathbf{v}_g .

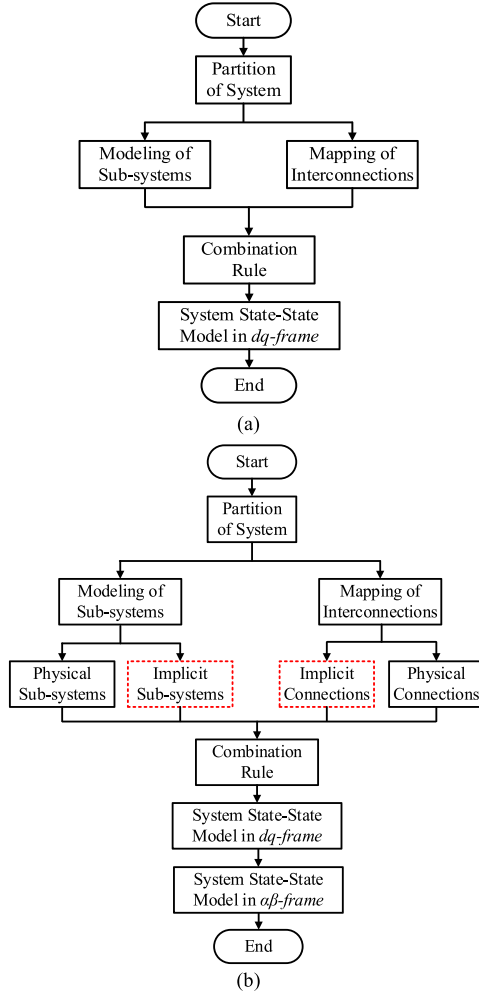


Fig. 2. Modular state-space modeling methods. (a) Conventional CCM method. (b) Proposed method.

B. Modular State-Space Modeling Method

The flowchart of the CCM-based modular state-space modeling is shown in Fig. 2(a). First, the system can be partitioned to n subsystems. Then, the subsystems are modeled separately. Assuming that the substate-space model of i th component can be given by a set of nonlinear equations as follows:

$$\dot{\vec{x}}_i = f_i(\vec{x}_i, \vec{a}_i) \quad (1a)$$

$$\vec{b}_i = g_i(\vec{x}_i, \vec{a}_i) \quad (1b)$$

where \vec{x}_i , \vec{a}_i , and \vec{b}_i denote the state variables, input variables, and output variables, respectively. The small-signal state-space model of the i th component can be obtained by linearizing (1)

$$\Delta \dot{\vec{x}}_i = F_i \Delta \vec{x}_i + H_i \Delta \vec{a}_i \quad (2a)$$

$$\Delta \vec{b}_i = J_i \Delta \vec{x}_i + K_i \Delta \vec{a}_i. \quad (2b)$$

For simplicity, the prefixes Δ in (2) are disregarded in the following.

Moreover, the interconnections among different components have to be obtained and expressed by algebraic equations as

follows:

$$\vec{a} = L_1 \vec{b} + L_2 \vec{u} \quad (3a)$$

$$\vec{y} = L_3 \vec{b} + L_4 \vec{u} \quad (3b)$$

where $\vec{a} = [\vec{a}_1, \dots, \vec{a}_i, \dots, \vec{a}_n]^T$ and $\vec{b} = [\vec{b}_1, \dots, \vec{b}_i, \dots, \vec{b}_n]^T$ are input and output vectors of all components, respectively; \vec{u} and \vec{y} are system's input and output vectors, respectively. L_1 , L_2 , L_3 , and L_4 are parameter matrices that map the interconnection relationships among different components.

The combination rule for obtaining the system state-space model can be given as follows.

The composite system model can be formulated by combining all the substate-space models of components

$$\dot{\vec{x}} = F \vec{x} + H \vec{a} \quad (4a)$$

$$\vec{b} = J \vec{x} + K \vec{a} \quad (4b)$$

where F , H , J , and K are the diagonal parameter matrices of the composite system model, $F = \text{diag}(F_1, \dots, F_i, \dots, F_n)$, $H = \text{diag}(H_1, \dots, H_i, \dots, H_n)$, $J = \text{diag}(J_1, \dots, J_i, \dots, J_n)$, and $K = \text{diag}(K_1, \dots, K_i, \dots, K_n)$; $\vec{x} = [\vec{x}_1, \dots, \vec{x}_i, \dots, \vec{x}_n]^T$.

Then, the overall state-space model of the system can be expressed as follows:

$$\dot{\vec{x}} = A \vec{x} + B \vec{u} \quad (5a)$$

$$\vec{y} = C \vec{x} + D \vec{u} \quad (5b)$$

where A , B , C , and D are the parameter matrices of the overall state-space model of the system, which are expressed as follows:

$$A = F + H L_1 (I - K L_1)^{-1} J \quad (6a)$$

$$B = H L_1 (I - K L_1)^{-1} K L_2 + H L_2 \quad (6b)$$

$$C = L_3 (I - K L_1)^{-1} J \quad (6c)$$

$$D = L_3 (I - K L_1)^{-1} K L_2 + L_4 \quad (6d)$$

where I is the identity matrix with the same dimension as $K L_1$.

However, the traditional CCM-based modular state-space modeling method can only be applied to the system in which the interconnections among its subsystems can be explicitly defined. Therefore, a modular state-space modeling method is developed in this paper to deal with implicit substate space models and interconnections that are introduced by linearizing of the outer loops, as shown in Fig. 2(b). Moreover, mathematical relationships between the system-state-space model in the dq -frame and that in the $\alpha\beta$ -frame are also incorporated to facilitate the system stability analysis.

III. PHYSICAL SUBSTATE-SPACE MODELS

A. AC Current Control

The block diagram of the current control in the converter dq -frame without considering the PLL dynamics is shown in Fig. 3, which contains the current controller G_i , the voltage feed-forward controller G_{ff} , the control delay G_d , and the admittance of L filter Y_p . i_{d/q_ref} , i_{d/q_err} are the current reference and error, respectively; $v_{m1d/q}$, $v_{m2d/q}$, and $v_{md/q}$ are modulating signals

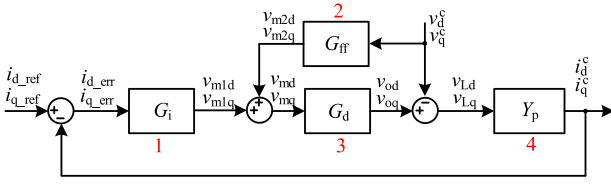


Fig. 3. Block diagram of the current control in the converter dq -frame without considering the PLL dynamics.

generated by the current control, the feedforward controller, and their sum respectively; $v_{od/q}$ and $v_{Ld/q}$ are converter output voltages and the inductor voltages, respectively; $v_{d/q}^c$ and $i_{d/q}^c$ are the voltage and current at the PCC of VSC, respectively. All these variables are defined in the converter dq -frame.

Since the ACC contains multiple components, the CCM will be employed to establish its state-space model. For a clear illustration, G_i , G_{ff} , G_d , and Y_p will be denoted as components 1–4, respectively.

The current controller $G_i(s)$ adopts PI controller, which is given as

$$G_i(s) = k_{pc} + \frac{k_{ic}}{s}. \quad (7)$$

Active damping is implemented by a first-order high-pass filter (HPF)-based feedforward control, which is expressed as follows:

$$G_{ff1}(s) = \frac{k_a s}{s + \omega_a}. \quad (8)$$

The HPF is chosen because it can be equivalently treated as a virtual parallel resistor at the PCC within the corner-frequency of HPF [30], which helps to improve the stability of the system.

With the digital control, the computation and pulsewidth modulation (PWM) will introduce the control delay, which can be expressed as follows:

$$G_d(s) = e^{-sT_d} \quad (9)$$

where T_d is the delay time, which is typically 1.5 times of sampling period T_s , i.e., $T_d = 1.5T_s$. To get the adequate state-space model of the control delay, the third-order Pade approximation is applied to make the model sufficiently accurate within the Nyquist frequency, i.e., half of the sampling frequency, and meanwhile minimize the complexity, as shown in Fig. 4, which is expressed as

$$G_d(s) = e^{-sT_d} \approx \frac{120 - 60T_d s + 12(T_d s)^2 - (T_d s)^3}{120 + 60T_d s + 12(T_d s)^2 + (T_d s)^3}. \quad (10)$$

The admittance of L filter in the converter dq -frame can be given as

$$Y_p(s) = \frac{1}{(s + j\omega_1)L_1 + R_1} \quad (11)$$

where ω_1 is the nominal angular frequency of the grid, and R_1 is the equivalent series resistor (ESR).

Since all the components in ACC are linear, their state-space models can be directly obtained according to their transfer

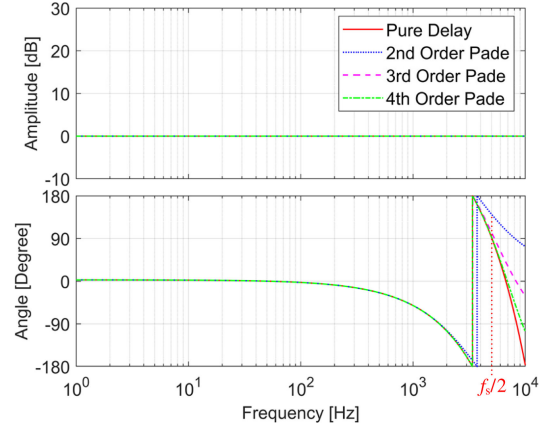


Fig. 4. Comparison of Pade approximations with different orders.

functions, where the details are presented in Appendix. With these substate-space models denoted by subscript 1 to 4, the composite model of ACC can be obtained by rearranging these matrices in a diagonal form, which is expressed as

$$\underbrace{\begin{bmatrix} \dot{\vec{x}}_1 \\ \dot{\vec{x}}_2 \\ \dot{\vec{x}}_3 \\ \dot{\vec{x}}_4 \end{bmatrix}}_{\dot{\vec{x}}_{acc}} = \underbrace{\begin{bmatrix} F_1 & & & \\ & F_2 & & \\ & & F_3 & \\ & & & F_4 \end{bmatrix}}_{F_{acc}} \underbrace{\begin{bmatrix} \vec{x}_1 \\ \vec{x}_2 \\ \vec{x}_3 \\ \vec{x}_4 \end{bmatrix}}_{\vec{x}_{acc}} + \underbrace{\begin{bmatrix} H_1 & & & \\ & H_2 & & \\ & & H_3 & \\ & & & H_4 \end{bmatrix}}_{H_{acc}} \underbrace{\begin{bmatrix} \vec{a}_1 \\ \vec{a}_2 \\ \vec{a}_3 \\ \vec{a}_4 \end{bmatrix}}_{\vec{a}_{acc}} \quad (12a)$$

$$\underbrace{\begin{bmatrix} \vec{b}_1 \\ \vec{b}_2 \\ \vec{b}_3 \\ \vec{b}_4 \end{bmatrix}}_{\vec{b}_{acc}} = \underbrace{\begin{bmatrix} J_1 & & & \\ & J_2 & & \\ & & J_3 & \\ & & & J_4 \end{bmatrix}}_{J_{acc}} \underbrace{\begin{bmatrix} \vec{x}_1 \\ \vec{x}_2 \\ \vec{x}_3 \\ \vec{x}_4 \end{bmatrix}}_{\vec{x}_{acc}} + \underbrace{\begin{bmatrix} K_1 & & & \\ & K_2 & & \\ & & K_3 & \\ & & & K_4 \end{bmatrix}}_{K_{acc}} \underbrace{\begin{bmatrix} \vec{a}_1 \\ \vec{a}_2 \\ \vec{a}_3 \\ \vec{a}_4 \end{bmatrix}}_{\vec{a}_{acc}} \quad (12b)$$

where the expressions of matrices F_1 , H_1 , J_1 , and K_1 are defined in (A1); F_2 , H_2 , J_2 , and K_2 in (A2); F_3 , H_3 , J_3 , K_3 in (A3); and F_4 , H_4 , J_4 , and K_4 in (A6).

According to Fig. 3, the input vector \vec{a}_{acc} and output vector \vec{b}_{acc} in (12) can be expanded as follows:

$$\vec{a}_{acc} = \begin{bmatrix} \vec{a}_1 \\ \vec{a}_2 \\ \vec{a}_3 \\ \vec{a}_4 \end{bmatrix} = \begin{bmatrix} i_{d_err} \\ i_{q_err} \\ v_d^c \\ v_q^c \\ v_{md} \\ v_{mq} \\ v_{Ld} \\ v_{Lq} \end{bmatrix}, \quad \vec{b}_{acc} = \begin{bmatrix} \vec{b}_1 \\ \vec{b}_2 \\ \vec{b}_3 \\ \vec{b}_4 \end{bmatrix} = \begin{bmatrix} v_{m1d} \\ v_{m1q} \\ v_{m2d} \\ v_{m2q} \\ v_{od} \\ v_{oq} \\ i_d^c \\ i_q^c \end{bmatrix}. \quad (13)$$

The input vector \vec{u}_{acc} and output vector \vec{y}_{acc} of overall ACC are expressed as

$$\vec{u}_{acc} = \begin{bmatrix} i_{d_ref} \\ i_{q_ref} \\ v_d^c \\ v_q^c \end{bmatrix} \quad \vec{y}_{acc} = \begin{bmatrix} i_d^c \\ i_q^c \end{bmatrix}. \quad (14)$$

Consequently, the physical interconnection among different components, shown in Fig. 3, can be depicted as

$$\underbrace{\begin{bmatrix} i_{d_err} \\ i_{q_err} \\ v_d^c \\ v_q^c \\ v_{md} \\ v_{mq} \\ v_{Ld} \\ v_{Lq} \end{bmatrix}}_{\vec{a}_{acc}} = \underbrace{\begin{bmatrix} 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 & 0 & -1 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix}}_{L_{acc1}} \underbrace{\begin{bmatrix} v_{m1d} \\ v_{m1q} \\ v_{m2d} \\ v_{m2q} \\ v_{od} \\ v_{oq} \\ i_d^c \\ i_q^c \end{bmatrix}}_{\vec{b}_{acc}} + \underbrace{\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{bmatrix}}_{L_{acc2}} \underbrace{\begin{bmatrix} i_{d_ref} \\ i_{q_ref} \\ v_d^c \\ v_q^c \end{bmatrix}}_{\vec{u}_{acc}} \quad (15a)$$

$$\underbrace{\begin{bmatrix} i_d^c \\ i_q^c \end{bmatrix}}_{\vec{y}_{acc}} = \underbrace{\begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}}_{L_{acc3}} \underbrace{\begin{bmatrix} v_{m1d} \\ v_{m1q} \\ v_{m2d} \\ v_{m2q} \\ v_{od} \\ v_{oq} \\ i_d^c \\ i_q^c \end{bmatrix}}_{\vec{b}_{acc}} + \underbrace{\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}}_{L_{acc4}} \underbrace{\begin{bmatrix} i_{d_ref} \\ i_{q_ref} \\ v_d^c \\ v_q^c \end{bmatrix}}_{\vec{u}_{acc}} \quad (15b)$$

where the prefixes Δ in (15) are disregarded for simplification.

Accordingly, the state-space model of overall ACC can be established as

$$\dot{\vec{x}}_{acc} = A_{acc}\vec{x}_{acc} + B_{acc}\vec{u}_{acc} \quad (16a)$$

$$\vec{y}_{acc} = C_{acc}\vec{x}_{acc} + D_{acc}\vec{u}_{acc} \quad (16b)$$

where A_{acc} , B_{acc} , C_{acc} , and D_{acc} are the matrices of the state-space model of ACC, which can be formulated according to the

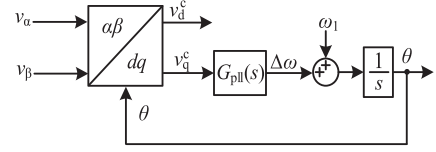


Fig. 5. Block diagram of the SRF-PLL.

rule defined in (6) and using matrices F_{acc} , H_{acc} , J_{acc} , and K_{acc} in (12), and L_{acc1} , L_{acc2} , L_{acc3} , and L_{acc4} in (15).

B. Phase-Locked Loop

Two dq -frames are defined in this article to include the dynamics of the PLL [8]. One is the grid dq -frame that defined by the phase angle of fundamental positive-sequence PCC voltage \mathbf{v} , denoted as θ_1 . The other is the converter dq -frame, which is defined by the phase angle obtained from conventional synchronous rotating frame (SRF)-PLL, denoted as θ . The input and output variables of the state-space model in the converter dq -frame will be denoted with the superscript c .

The control scheme of the SRF-PLL is shown in Fig. 5, where v_α and v_β are the PCC voltages in the $\alpha\beta$ -frame; and $G_{pll}(s)$ is the PLL controller.

According to Fig. 5, the open-loop transfer function between the input q -axis voltage perturbation Δv_q^c and the output synchronization angle variation $\Delta\theta$ is given as

$$\Delta\theta = \underbrace{\left(k_{pp} + k_{ip} \frac{1}{s} \right)}_{G_{pll}(s)} \cdot \frac{1}{s} \cdot \Delta v_q^c. \quad (17)$$

In the time domain, (17) can be expressed by two differential equations

$$\frac{d\phi_q}{dt} = \Delta v_q^c \quad (18a)$$

$$\frac{d\Delta\theta}{dt} = k_{pp}\Delta v_q^c + k_{ip}\phi_q. \quad (18b)$$

Therefore, the state-space model for the SRF-PLL can be given as

$$\underbrace{\begin{bmatrix} \dot{\phi}_q \\ \dot{\Delta\theta} \end{bmatrix}}_{\dot{\vec{x}}_{pll}} = \underbrace{\begin{bmatrix} 0 & 0 \\ k_{ip} & 0 \end{bmatrix}}_{F_{pll}} \underbrace{\begin{bmatrix} \phi_q \\ \Delta\theta \end{bmatrix}}_{\vec{x}_{pll}} + \underbrace{\begin{bmatrix} 1 \\ k_{pp} \end{bmatrix}}_{H_{pll}} \underbrace{\begin{bmatrix} \Delta v_q^c \end{bmatrix}}_{\vec{a}_{pll}} \quad (19a)$$

$$\underbrace{\begin{bmatrix} \Delta\theta \end{bmatrix}}_{\vec{b}_{pll}} = \underbrace{\begin{bmatrix} 0 & 1 \end{bmatrix}}_{J_{pll}} \underbrace{\begin{bmatrix} \phi_q \\ \Delta\theta \end{bmatrix}}_{\vec{x}_{pll}} + \underbrace{\begin{bmatrix} 0 \end{bmatrix}}_{K_{pll}} \underbrace{\begin{bmatrix} \Delta v_q^c \end{bmatrix}}_{\vec{a}_{pll}}. \quad (19b)$$

C. DC-Link Voltage Control

The block scheme of the DVC is shown in Fig. 6. To avoid the operating-point-dependent control dynamics, the voltage-square control scheme is employed [31], i.e., using the error $(v_{dc_ref}^2 - v_{dc}^2)/2$ to calculate the power reference P_{ref} , and then generate the d -axis current reference.

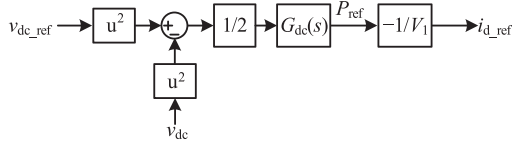


Fig. 6. Block diagram of DVC.

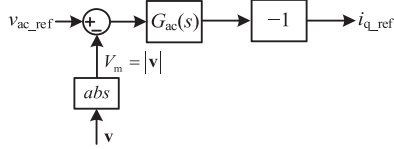


Fig. 7. Block diagram of the AVC.

The active power reference in the frequency domain can be given as

$$P_{\text{ref}} = \underbrace{\left(k_{\text{pd}} + \frac{k_{\text{id}}}{s} \right)}_{G_{\text{dc}}(s)} \frac{v_{\text{dc_ref}}^2 - v_{\text{dc}}^2}{2}. \quad (20)$$

Therefore, the small-signal variation of the active power reference ΔP_{ref} resulted from dc-link voltage perturbation Δv_{dc} can be expressed as

$$\Delta P_{\text{ref}} = -G_{\text{dc}}(s) V_{\text{dc}0} \Delta v_{\text{dc}} \quad (21)$$

where $V_{\text{dc}0}$ is the rated dc-link voltage.

The d -axis current reference is generated by

$$i_{d_ref} = -\frac{P_{\text{ref}}}{V_1} \Rightarrow \Delta i_{d_ref} = -\frac{\Delta P_{\text{ref}}}{V_1} = \frac{G_{\text{dc}}(s) V_{\text{dc}0}}{V_1} \Delta v_{\text{dc}} \quad (22)$$

where V_1 is the rated voltage at the PCC point.

In the time domain, (22) can be expressed as

$$\frac{d\gamma_{\text{dc}}}{dt} = \Delta v_{\text{dc}} \quad (23a)$$

$$\Delta i_{d_ref} = \frac{k_{\text{pd}} V_{\text{dc}0}}{V_1} \Delta v_{\text{dc}} + \frac{k_{\text{id}} V_{\text{dc}0}}{V_1} \gamma_{\text{dc}}. \quad (23b)$$

According to (23), the state-space model of the DVC can be derived as follows:

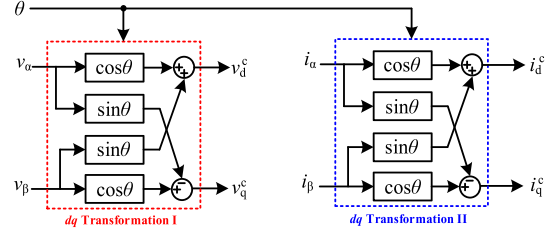
$$\underbrace{\begin{bmatrix} \dot{\gamma}_{\text{dc}} \\ \ddot{x}_{\text{dvc}} \end{bmatrix}}_{\dot{\mathbf{x}}_{\text{dvc}}} = \underbrace{\begin{bmatrix} 0 \\ \gamma_{\text{dc}} \end{bmatrix}}_{F_{\text{dvc}}} + \underbrace{\begin{bmatrix} 1 \\ \ddot{x}_{\text{dvc}} \end{bmatrix}}_{H_{\text{dvc}}} \underbrace{\begin{bmatrix} \Delta v_{\text{dc}} \\ \ddot{a}_{\text{dvc}} \end{bmatrix}}_{\ddot{\mathbf{a}}_{\text{dvc}}} \quad (24a)$$

$$\underbrace{\begin{bmatrix} \Delta i_{d_ref} \\ \ddot{b}_{\text{dvc}} \end{bmatrix}}_{\ddot{\mathbf{b}}_{\text{dvc}}} = \underbrace{\begin{bmatrix} k_{\text{id}} V_{\text{dc}0} \\ V_1 \end{bmatrix}}_{J_{\text{dvc}}} \underbrace{\begin{bmatrix} \gamma_{\text{dc}} \\ \ddot{x}_{\text{dvc}} \end{bmatrix}}_{\mathbf{x}_{\text{dvc}}} + \underbrace{\begin{bmatrix} k_{\text{pd}} V_{\text{dc}0} \\ V_1 \end{bmatrix}}_{K_{\text{dvc}}} \underbrace{\begin{bmatrix} \Delta v_{\text{dc}} \\ \ddot{a}_{\text{dvc}} \end{bmatrix}}_{\ddot{\mathbf{a}}_{\text{dvc}}}. \quad (24b)$$

D. AC Voltage Magnitude Control

The block diagram of the AVC is shown in Fig. 7.

Assuming that the ac voltage is regulated using the droop control method, then the expression of the q -axis current reference


 Fig. 8. Block diagram of dq transformations.

can be given as

$$i_{q_ref} = -\underbrace{\frac{k_{\text{pa}} \omega_{\text{ac}}}{s + \omega_{\text{ac}}}}_{G_{\text{ac}}(s)} (v_{\text{ac_ref}} - V_m) \quad (25)$$

where $V_m = |v| = \sqrt{v_d^2 + v_q^2}$. The small-signal variation of voltage magnitude ΔV_m resulting from the Δv_d and Δv_q can be derived as follows:

$$(V_m + \Delta V_m)^2 = (V_1 + \Delta v_d)^2 + \Delta v_q^2 \Rightarrow \Delta V_m \approx \Delta v_d. \quad (26)$$

According to (25) and (26), the following can be obtained

$$\Delta i_{q_ref} = \frac{k_{\text{pa}} \omega_{\text{ac}}}{s + \omega_{\text{ac}}} \Delta v_d. \quad (27)$$

In the time domain, (27) can be expressed by

$$\frac{dx_{\text{ac}}}{dt} = -\omega_{\text{ac}} x_{\text{ac}} + k_{\text{pa}} \omega_{\text{ac}} \Delta v_d \quad (28a)$$

$$x_{\text{ac}} = \Delta i_{q_ref}. \quad (28b)$$

Then, the state-space model of AVC can be derived as

$$\underbrace{\begin{bmatrix} \dot{x}_{\text{ac}} \\ \ddot{x}_{\text{avc}} \end{bmatrix}}_{\dot{\mathbf{x}}_{\text{avc}}} = \underbrace{\begin{bmatrix} -\omega_{\text{ac}} \\ F_{\text{avc}} \end{bmatrix}}_{F_{\text{avc}}} \underbrace{\begin{bmatrix} x_{\text{ac}} \\ \ddot{x}_{\text{avc}} \end{bmatrix}}_{\mathbf{x}_{\text{avc}}} + \underbrace{\begin{bmatrix} k_{\text{pa}} \omega_{\text{ac}} \\ H_{\text{avc}} \end{bmatrix}}_{H_{\text{avc}}} \underbrace{\begin{bmatrix} \Delta v_d \\ \ddot{a}_{\text{avc}} \end{bmatrix}}_{\ddot{\mathbf{a}}_{\text{avc}}} \quad (29a)$$

$$\underbrace{\begin{bmatrix} \Delta i_{q_ref} \\ \ddot{b}_{\text{avc}} \end{bmatrix}}_{\ddot{\mathbf{b}}_{\text{avc}}} = \underbrace{\begin{bmatrix} 1 \\ J_{\text{avc}} \end{bmatrix}}_{J_{\text{avc}}} \underbrace{\begin{bmatrix} x_{\text{ac}} \\ \ddot{x}_{\text{avc}} \end{bmatrix}}_{\mathbf{x}_{\text{avc}}} + \underbrace{\begin{bmatrix} 0 \\ K_{\text{avc}} \end{bmatrix}}_{K_{\text{avc}}} \underbrace{\begin{bmatrix} \Delta v_d \\ \ddot{a}_{\text{avc}} \end{bmatrix}}_{\ddot{\mathbf{a}}_{\text{avc}}}. \quad (29b)$$

IV. IMPLICIT SUBSTATE-SPACE MODELS AND INTERCONNECTIONS

The major challenge of CCM-based modeling in the converter level lies in the representation of the implicit substate-space modes and implicit connections caused by the control couplings. The implicit connections between ACC and PLL can be established by linearizing the dq transformations. Moreover, the implicit connections and substate-space models between DVC control loop and voltages and currents at PCC can be obtained according to the active power balance principle.

A. dq -Transformation I

As shown in Fig. 8, the inputs of dq -transformation I are PCC voltages in the stationary frame, i.e., v_{α} and v_{β} , and the synchronization angle θ obtained from the PLL; the outputs are PCC voltages in the converter dq -frame v_d^c and v_q^c . The input

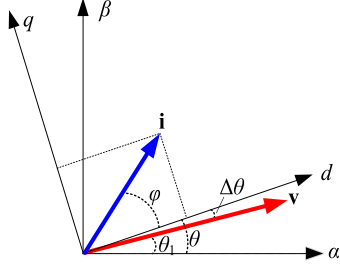


Fig. 9. Relationships of different phase angles.

and output voltages can be represented in the complex space vector form, i.e.

$$\mathbf{v}^s = v_\alpha + jv_\beta \quad \mathbf{v}^c = v_d^c + jv_q^c. \quad (30)$$

The relationship between the PCC voltage vector \mathbf{v}^s and converter dq -frame defined by synchronization angle θ is shown in Fig. 9. Accordingly, the dq -transformation can be expressed as

$$\mathbf{v}^s = \mathbf{v}^c \cdot e^{-j\theta}. \quad (31)$$

Assuming that both inputs, including PCC voltages and synchronization angle, contain the small-signal perturbations, the PCC voltage in the stationary $\alpha\beta$ -frame can be expressed as follows:

$$\mathbf{v}^s = (\mathbf{V}_1 + \Delta\mathbf{v}) e^{j\theta_1} \quad (32)$$

where $\mathbf{V}_1 = V_1 + j0$ is the steady-state PCC voltage vector in the grid dq -frame, and $\Delta\mathbf{v} = \Delta v_d + j\Delta v_q$ is the corresponding small-signal perturbation.

Similarly, the PLL output synchronization angle with the small-signal perturbation can be expressed as

$$\theta = \theta_1 + \Delta\theta. \quad (33)$$

Substituting (33) and (32) into (31) yields

$$\begin{aligned} \mathbf{v}^c &= \mathbf{v}^s \cdot e^{-j\theta} = (V_1 + \Delta\mathbf{v}) e^{j\theta_1} e^{-j(\theta_1 + \Delta\theta)} \\ &= (V_1 + \Delta\mathbf{v}) e^{-j\Delta\theta}. \end{aligned} \quad (34)$$

Considering the small-signal perturbation $\Delta\theta$ and applying the first-order Taylor expansion, (34) can be approximated as follows:

$$\begin{aligned} \mathbf{v}^c &\approx (V_1 + \Delta\mathbf{v})(1 - j\Delta\theta) \\ &= \underbrace{V_1}_{\mathbf{v}_1^c} + \underbrace{\Delta\mathbf{v} - jV_1\Delta\theta - j\Delta\mathbf{v}\Delta\theta}_{\Delta\mathbf{v}^c}. \end{aligned} \quad (35)$$

By neglecting the second-order small-signal variation term $\Delta\mathbf{v}\Delta\theta$, the small-signal variation of PCC voltage in the converter dq -frame $\Delta\mathbf{v}^c$ can be obtained as

$$\Delta\mathbf{v}^c \approx \Delta\mathbf{v} - jV_1\Delta\theta = \Delta v_d^c + j\Delta v_q^c. \quad (36)$$

Therefore, the relationship between the PCC voltages in converter dq -frame and grid dq -frame can be given as

$$\Delta v_d^c = \Delta v_d \quad (37a)$$

$$\Delta v_q^c = \Delta v_q - V_1\Delta\theta. \quad (37b)$$

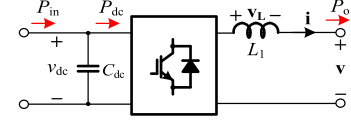


Fig. 10. Active power flow of VSC.

B. dq -Transformation II

As shown in Fig. 8, the inputs of dq -transformation I are the PCC currents in the stationary frame, i.e., i_α and i_β , and the synchronization angle θ obtained from PLL; the outputs are the PCC currents in the converter dq -frame i_d^c and i_q^c . The input and output currents can be represented in the complex space vector form, i.e.

$$\mathbf{i}^s = i_\alpha + j i_\beta \quad \mathbf{i}^c = i_d^c + j i_q^c. \quad (38)$$

The relationship between the PCC current vector \mathbf{i}^s and converter dq -frame defined by synchronization angle θ is shown in Fig. 9. Accordingly, the dq -transformation can be expressed as

$$\mathbf{i}^c = \mathbf{i}^s \cdot e^{-j\theta}. \quad (39)$$

Assuming that PCC current vector contains the small-signal perturbations, i.e.

$$\mathbf{i}^s = (\mathbf{I}_1 + \Delta\mathbf{i}) e^{j\theta_1} \quad (40)$$

where $\mathbf{I}_1 = I_{d1} + jI_{q1}$ is the steady-state PCC current vector in the grid dq -frame and thereby $\varphi = \arctan(I_{q1}/I_{d1})$; $\Delta\mathbf{i} = \Delta i_d + j\Delta i_q$ is the corresponding small-signal perturbation.

Substituting (33) and (40) into (39) yields

$$\begin{aligned} \mathbf{i}^c &= \mathbf{i}^s e^{-j\theta} = (\mathbf{I}_1 + \Delta\mathbf{i}) e^{-j\Delta\theta} \approx (\mathbf{I}_1 + \Delta\mathbf{i})(1 - j\Delta\theta) \\ &= \mathbf{I}_1 + \underbrace{\Delta\mathbf{i} - j\mathbf{I}_1\Delta\theta - j\Delta\mathbf{i}\Delta\theta}_{\Delta\mathbf{i}^c}. \end{aligned} \quad (41)$$

By neglecting the second-order small-signal variation term $\Delta\mathbf{i}\Delta\theta$, the following can be obtained:

$$\Delta\mathbf{i}^c \approx \Delta\mathbf{i} - j\mathbf{I}_1\Delta\theta = \Delta i_d^c + j\Delta i_q^c. \quad (42)$$

Therefore, the relationship between the PCC currents in grid dq -frame and converter dq -frame can be given by

$$\Delta i_d = \Delta i_d^c - I_{q1}\Delta\theta \quad (43a)$$

$$\Delta i_q = \Delta i_q^c + I_{d1}\Delta\theta. \quad (43b)$$

C. Active Power Balance

As shown in Fig. 10, the dynamic equation for the dc-link capacitor can be given by

$$\frac{1}{2} C_{dc} \frac{d(v_{dc}^2)}{dt} = P_{in} - P_{dc}. \quad (44)$$

Applying the small-signal perturbation yields

$$C_{dc} V_{dc0} \frac{d\Delta v_{dc}}{dt} = \Delta P_{in} - \Delta P_{dc}. \quad (45)$$

Assuming that input power fluctuation is negligible, i.e., $\Delta P_{in} \approx 0$ and the power switches are ideal with no loss,

the input active power injected into the dc side of VSC is equal to the output active power at the ac side, i.e., $\Delta P_{dc} \approx dE_L/dt + \Delta P_o$, where E_L is the energy storage in the inductor L_1 .

The energy stored in the inductor L_1 can be given by

$$E_L = \frac{1}{2} L_1 \mathbf{i}^2 = \frac{1}{2} L_1 (i_d^2 + i_q^2). \quad (46)$$

Applying the small-signal perturbation yields

$$\frac{dE_L}{dt} = L_1 \left(I_{d1} \cdot \frac{d\Delta i_d}{dt} + I_{q1} \cdot \frac{d\Delta i_q}{dt} \right). \quad (47)$$

The output instantaneous complex power at the PCC is expressed as

$$\begin{aligned} \mathbf{S}_o &= \mathbf{v} \mathbf{i}^* \approx V_1 \mathbf{i}_1^* + V_1 \cdot \Delta \mathbf{i}^* + \Delta \mathbf{v} \cdot \mathbf{i}_1^* \\ &= \underbrace{V_1 I_{d1}}_{P_{o1}} + \underbrace{I_{d1} \Delta v_d + I_{q1} \Delta v_e + V_1 \Delta i_d}_{\Delta P_o} \\ &\quad + j \underbrace{(-V_1 I_{q1})}_{Q_{o1}} + j \underbrace{(I_{d1} \Delta v_q - I_{q1} \Delta v_d - V_1 \Delta i_q)}_{\Delta Q_o} \\ &\Rightarrow \Delta P_o = I_{d1} \Delta v_d + I_{q1} \Delta v_q + V_1 \Delta i_d. \end{aligned} \quad (48)$$

Considering $\Delta P_{dc} \approx dE_L/dt + \Delta P_o$, and substituting (47) and (48) into (45) yields

$$\begin{aligned} C_{dc} V_{dc0} \frac{d\Delta v_{dc}}{dt} &= - \left(L_1 I_{d1} \cdot \frac{d\Delta i_d}{dt} + L_1 I_{q1} \cdot \frac{d\Delta i_q}{dt} \right. \\ &\quad \left. + I_{d1} \Delta v_d + I_{q1} \Delta v_q + V_1 \Delta i_d \right) \end{aligned} \quad (49)$$

which can be further rewritten as

$$\frac{dx_{dc}}{dt} = \frac{I_{d1}}{C_{dc} V_{dc0}} \Delta v_d + \frac{I_{q1}}{C_{dc} V_{dc0}} \Delta v_q + \frac{V_1}{C_{dc} V_{dc0}} \Delta i_d \quad (50a)$$

$$\Delta v_{dc} = - \left(\frac{L_1 I_{d1} \Delta i_d + L_1 I_{q1} \Delta i_q}{C_{dc} V_{dc0}} + x_{dc} \right). \quad (50b)$$

Consequently, an additional state-space model of active power balance can be established to represent the implicit connections between the dc-link voltage dynamics and the PCC voltages and currents, which is expressed as

$$\begin{aligned} \begin{bmatrix} \dot{x}_{dc} \\ \dot{x}_{apb} \end{bmatrix} &= \underbrace{\begin{bmatrix} 0 \\ \mathbf{F}_{apb} \end{bmatrix}}_{\mathbf{F}_{apb}} \begin{bmatrix} x_{dc} \\ \mathbf{x}_{apb} \end{bmatrix} + \underbrace{\begin{bmatrix} \frac{I_{d1}}{C_{dc} V_{dc0}} & \frac{I_{q1}}{C_{dc} V_{dc0}} & \frac{V_1}{C_{dc} V_{dc0}} & 0 \end{bmatrix}}_{\mathbf{H}_{apb}} \begin{bmatrix} \Delta v_d \\ \Delta v_q \\ \Delta i_d \\ \Delta i_q \end{bmatrix} \\ &\quad \underbrace{\begin{bmatrix} \Delta v_d \\ \Delta v_q \\ \Delta i_d \\ \Delta i_q \end{bmatrix}}_{\mathbf{a}_{apb}} \end{aligned} \quad (51a)$$

$$\begin{aligned} \begin{bmatrix} \Delta v_{dc} \\ \mathbf{b}_{apb} \end{bmatrix} &= \underbrace{\begin{bmatrix} -1 \\ \mathbf{J}_{apb} \end{bmatrix}}_{\mathbf{J}_{apb}} \begin{bmatrix} x_{dc} \\ \mathbf{x}_{apb} \end{bmatrix} + \underbrace{\begin{bmatrix} 0 & 0 & -\frac{L_1 I_{d1}}{C_{dc} V_{dc0}} & -\frac{L_1 I_{q1}}{C_{dc} V_{dc0}} \end{bmatrix}}_{\mathbf{K}_{apb}} \begin{bmatrix} \Delta v_d \\ \Delta v_q \\ \Delta i_d \\ \Delta i_q \end{bmatrix} \\ &\quad \underbrace{\begin{bmatrix} \Delta v_d \\ \Delta v_q \\ \Delta i_d \\ \Delta i_q \end{bmatrix}}_{\mathbf{a}_{apb}} \end{aligned} \quad (51b)$$

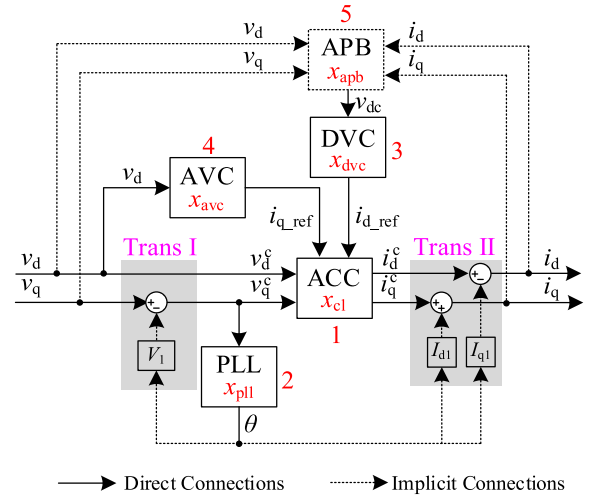


Fig. 11. Interconnection relationships among different control loops.

According to physical connections shown in Fig. 1 and implicit connections in (37), (43), and (51), the overall connections among different control loops are depicted in Fig. 11, where the prefixes Δ are disregarded for simplification.

V. SYSTEM STATE-SPACE MODEL IN THE dq -FRAME

A. State-Space Model of VSC

Considering the state-space models of ACC, PLL, DVC, AVC, and APB, the composite system model of VSC can be given as follows:

$$\begin{bmatrix} \dot{\vec{x}}_{acc} \\ \dot{\vec{x}}_{pll} \\ \dot{\vec{x}}_{dvc} \\ \dot{\vec{x}}_{avc} \\ \dot{\vec{x}}_{apb} \end{bmatrix} = \mathbf{F}_{vsc} \cdot \begin{bmatrix} \vec{x}_{acc} \\ \vec{x}_{pll} \\ \vec{x}_{dvc} \\ \vec{x}_{avc} \\ \vec{x}_{apb} \end{bmatrix} + \mathbf{H}_{vsc} \cdot \begin{bmatrix} \vec{u}_{acc} \\ \vec{a}_{pll} \\ \vec{a}_{dvc} \\ \vec{a}_{avc} \\ \vec{a}_{apb} \end{bmatrix} \quad (52a)$$

$$\begin{bmatrix} \vec{y}_{acc} \\ \vec{b}_{pll} \\ \vec{b}_{dvc} \\ \vec{b}_{avc} \\ \vec{b}_{apb} \end{bmatrix} = \mathbf{J}_{vsc} \cdot \begin{bmatrix} \vec{x}_{acc} \\ \vec{x}_{pll} \\ \vec{x}_{dvc} \\ \vec{x}_{avc} \\ \vec{x}_{apb} \end{bmatrix} + \mathbf{K}_{vsc} \cdot \begin{bmatrix} \vec{u}_{acc} \\ \vec{a}_{pll} \\ \vec{a}_{dvc} \\ \vec{a}_{avc} \\ \vec{a}_{apb} \end{bmatrix} \quad (52b)$$

where $\mathbf{F}_{vsc} = \text{diag}(A_{acc}, F_{pll}, F_{dvc}, F_{avc}, F_{apb})$, $\mathbf{H}_{vsc} = \text{diag}(B_{acc}, H_{pll}, H_{dvc}, H_{avc}, H_{apb})$, $\mathbf{J}_{vsc} = \text{diag}(C_{acc}, J_{pll}, J_{dvc}, J_{avc}, J_{apb})$, and $\mathbf{K}_{vsc} = \text{diag}(D_{acc}, K_{pll}, K_{dvc}, K_{avc}, K_{apb})$, with the matrices A_{acc} , B_{acc} , C_{acc} , and D_{acc} defined in (16), the matrices F_{pll} , H_{pll} , J_{pll} , and K_{pll} defined in (19), the matrices F_{dvc} , H_{dvc} , J_{dvc} , and K_{dvc} defined in (24), the matrices F_{avc} , H_{avc} , J_{avc} , and K_{avc} defined in (29), and the matrices F_{apb} , H_{apb} , J_{apb} , and K_{apb} defined in (51).

According to Fig. 11, the input vector \vec{u}_{VSC} and output vector \vec{y}_{VSC} of overall VSC are expressed as

$$\vec{u}_{\text{VSC}} = \begin{bmatrix} v_d \\ v_q \end{bmatrix} \quad \vec{y}_{\text{VSC}} = \begin{bmatrix} i_d \\ i_q \end{bmatrix}. \quad (53)$$

The interconnection relationship can be described as

$$\begin{array}{c} \text{ACC} \\ \text{PLL} \\ \text{DVC} \\ \text{AVC} \\ \text{APB} \end{array} \begin{bmatrix} i_{d_ref} \\ i_{q_ref} \\ v_d^c \\ v_q^c \\ v_{dc} \\ v_d \\ v_q \\ i_d \\ i_q \end{bmatrix} = \underbrace{\begin{bmatrix} 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -V_1 & 0 & 0 & 0 \\ 0 & 0 & -V_1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & -I_{q1} & 0 & 0 & 0 \\ 0 & 1 & I_{d1} & 0 & 0 & 0 \end{bmatrix}}_{L_{\text{VSC}1}} \underbrace{\begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 1 & 0 \\ 0 & 1 \\ 0 & 1 \\ 0 & 0 \\ 1 & 0 \\ 0 & 1 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}}_{L_{\text{VSC}2}} \underbrace{\begin{bmatrix} i_d^c \\ i_q^c \\ \theta \\ i_{d_ref} \\ i_{q_ref} \\ v_{dc} \end{bmatrix}}_{\vec{b}_{\text{VSC}}} + \underbrace{\begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 1 & 0 \\ 0 & 1 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}}_{L_{\text{VSC}3}} \underbrace{\begin{bmatrix} i_d \\ i_q \end{bmatrix}}_{\vec{y}_{\text{VSC}}} + \underbrace{\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}}_{L_{\text{VSC}4}} \underbrace{\begin{bmatrix} v_d \\ v_q \end{bmatrix}}_{\vec{u}_{\text{VSC}}}. \quad (54a)$$

$$\vec{y}_{\text{VSC}} = \underbrace{\begin{bmatrix} 1 & 0 & -I_{q1} & 0 & 0 & 0 \\ 0 & 1 & I_{d1} & 0 & 0 & 0 \end{bmatrix}}_{L_{\text{VSC}3}} \underbrace{\begin{bmatrix} i_d^c \\ i_q^c \\ \theta \\ i_{d_ref} \\ i_{q_ref} \\ v_{dc} \end{bmatrix}}_{\vec{b}_{\text{VSC}}} + \underbrace{\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}}_{L_{\text{VSC}4}} \underbrace{\begin{bmatrix} v_d \\ v_q \end{bmatrix}}_{\vec{u}_{\text{VSC}}}. \quad (54b)$$

Therefore the state-space model of VSC can be derived as

$$\dot{\vec{x}}_{\text{VSC}} = A_{\text{VSC}} \vec{x}_{\text{VSC}} + B_{\text{VSC}} \vec{u}_{\text{VSC}} \quad (55a)$$

$$\vec{y}_{\text{VSC}} = C_{\text{VSC}} \vec{x}_{\text{VSC}} + D_{\text{VSC}} \vec{u}_{\text{VSC}} \quad (55b)$$

where A_{VSC} , B_{VSC} , C_{VSC} , and D_{VSC} are the matrices of the state-space model of ACC, which can be formulated according to the rule defined in (6) and using matrices F_{VSC} , H_{VSC} , J_{VSC} , and K_{VSC} in (52) and $L_{\text{VSC}1}$, $L_{\text{VSC}2}$, $L_{\text{VSC}3}$, and $L_{\text{VSC}4}$ in (54).

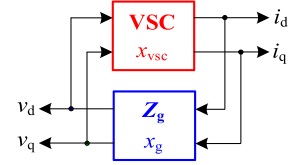


Fig. 12. Block diagram of VSC and grid impedance.

B. State-Space Model of the Grid-Side Impedance

As for the equivalent grid impedance shown in Fig. 1, its dynamic equations can be derived as

$$C_g \left(\frac{dv_{Cgd}}{dt} - \omega_1 v_{Cgd} \right) = i_d - i_{Lgd} \quad (56a)$$

$$L_g \left(\frac{di_{Lgd}}{dt} - \omega_1 i_{Lgd} \right) + R_{Lg} i_{Lgd} = v_{Cgd} + R_{Cg} (i_d - i_{Lgd}) \quad (56b)$$

$$C_g \left(\frac{dv_{Cgq}}{dt} + \omega_1 v_{Cgq} \right) = i_q - i_{Lgq} \quad (56c)$$

$$L_g \left(\frac{di_{Lgq}}{dt} + \omega_1 i_{Lgq} \right) + R_{Lg} i_{Lgq} = v_{Cgq} + R_{Cg} (i_q - i_{Lgq}) \quad (56d)$$

where $v_{Cgd/q}$ and $i_{Lgd/q}$ are the grid capacitor voltage and grid inductor current, respectively; and R_{Lg} and R_{Cg} are the ESRs of L_g and C_g , respectively.

According to (56), the state-space model of the grid impedance can be derived as

$$\underbrace{\begin{bmatrix} \dot{v}_{Cgd} \\ \dot{i}_{Lgd} \\ \dot{v}_{Cgq} \\ \dot{i}_{Lgq} \end{bmatrix}}_{\dot{\vec{x}}_g} = \underbrace{\begin{bmatrix} 0 & -\frac{1}{C_g} & \omega_1 & 0 \\ \frac{1}{L_g} & \frac{-R_{Lg}-R_{Cg}}{L_g} & 0 & \omega_1 \\ -\omega_1 & 0 & 0 & -\frac{1}{C_g} \\ 0 & -\omega_1 & \frac{1}{L_g} & \frac{-R_{Lg}-R_{Cg}}{L_g} \end{bmatrix}}_{F_g} \underbrace{\begin{bmatrix} v_{Cgd} \\ i_{Lgd} \\ v_{Cgq} \\ i_{Lgq} \end{bmatrix}}_{\vec{x}_g} + \underbrace{\begin{bmatrix} \frac{1}{C_g} & 0 \\ \frac{R_{Cg}}{L_g} & 0 \\ 0 & \frac{1}{C_g} \\ 0 & \frac{R_{Cg}}{L_g} \end{bmatrix}}_{H_g} \underbrace{\begin{bmatrix} i_d \\ i_q \end{bmatrix}}_{\vec{a}_g} \quad (57a)$$

$$\underbrace{\begin{bmatrix} v_d \\ v_q \end{bmatrix}}_{\vec{b}_g} = \underbrace{\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}}_{J_g} \underbrace{\begin{bmatrix} v_{Cgd} \\ i_{Lgd} \\ v_{Cgq} \\ i_{Lgq} \end{bmatrix}}_{\vec{x}_g} + \underbrace{\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}}_{K_g} \underbrace{\begin{bmatrix} i_d \\ i_q \end{bmatrix}}_{\vec{a}_g}. \quad (57b)$$

C. State-Space Model of Overall System

The block diagram of single VSC and grid impedance is given in Fig. 12. The composite system model of VSC and grid

impedance can be given by

$$\underbrace{\begin{bmatrix} \dot{\vec{x}}_{\text{vsc}} \\ \dot{\vec{x}}_g \end{bmatrix}}_{\dot{\vec{x}}_{\text{all}}} = \underbrace{\begin{bmatrix} A_{\text{vsc}} & \\ & F_g \end{bmatrix}}_{F_{\text{all}}} \underbrace{\begin{bmatrix} \vec{x}_{\text{vsc}} \\ \vec{x}_g \end{bmatrix}}_{\vec{x}_{\text{all}}} + \underbrace{\begin{bmatrix} B_{\text{vsc}} & \\ & H_g \end{bmatrix}}_{H_{\text{all}}} \underbrace{\begin{bmatrix} \vec{u}_{\text{vsc}} \\ \vec{a}_g \end{bmatrix}}_{\vec{a}_{\text{all}}} \quad (58a)$$

$$\underbrace{\begin{bmatrix} \vec{y}_{\text{vsc}} \\ \vec{b}_g \end{bmatrix}}_{\vec{b}_{\text{all}}} = \underbrace{\begin{bmatrix} C_{\text{vsc}} & \\ & J_g \end{bmatrix}}_{J_{\text{all}}} \underbrace{\begin{bmatrix} \vec{x}_{\text{vsc}} \\ \vec{x}_g \end{bmatrix}}_{\vec{x}_{\text{all}}} + \underbrace{\begin{bmatrix} D_{\text{vsc}} & \\ & K_g \end{bmatrix}}_{K_{\text{all}}} \underbrace{\begin{bmatrix} \vec{u}_{\text{vsc}} \\ \vec{a}_g \end{bmatrix}}_{\vec{a}_{\text{all}}} \quad (58b)$$

where the matrices A_{vsc} , B_{vsc} , C_{vsc} , and D_{vsc} are defined in (55), and the matrices F_g , H_g , J_g , and K_g are defined in (57).

According to Fig. 12, the interconnections between the VSC and grid impedance can be explained by the following equations:

$$\text{VSC} \underbrace{\begin{bmatrix} v_d \\ v_q \\ i_d \\ i_q \end{bmatrix}}_{\vec{a}_{\text{all}}} = \underbrace{\begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}}_{L_{\text{all}11}} \underbrace{\begin{bmatrix} i_d \\ i_q \\ v_d \\ v_q \end{bmatrix}}_{\vec{b}_{\text{all}}} + \underbrace{\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}}_{L_{\text{all}12}} \underbrace{\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}}_{\vec{u}_{\text{all}}} \quad (59a)$$

$$\underbrace{\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}}_{\vec{y}_{\text{all}}} = \underbrace{\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}}_{L_{\text{all}13}} \underbrace{\begin{bmatrix} i_d \\ i_q \\ v_d \\ v_q \end{bmatrix}}_{\vec{b}_{\text{all}}} + \underbrace{\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}}_{L_{\text{all}14}} \underbrace{\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}}_{\vec{u}_{\text{all}}} \quad (59b)$$

Thus, the whole system state-space model can be obtained as

$$\dot{\vec{x}}_{\text{all}} = A_{\text{all}} \vec{x}_{\text{all}} + B_{\text{all}} \vec{u}_{\text{all}} \quad (60a)$$

$$\vec{y}_{\text{all}} = C_{\text{all}} \vec{x}_{\text{all}} + D_{\text{all}} \vec{u}_{\text{all}} \quad (60b)$$

where A_{all} , B_{all} , C_{all} , and D_{all} are obtained using (58) and (59) and are expressed as

$$A_{\text{all}} = F_{\text{all}} + H_{\text{all}} L_{\text{all}1} (I - K_{\text{all}} L_{\text{all}1})^{-1} J_{\text{all}} \quad (61a)$$

$$B_{\text{all}} = C_{\text{all}} = D_{\text{all}} = 0 \quad (61b)$$

and \vec{x}_{all} can be expanded as (61c), shown at the bottom of this page.

VI. MATHEMATICAL RELATIONSHIP BETWEEN STATE-SPACE MODELS IN DIFFERENT FRAMES

In order to bridge the state-space models of VSC in the dq -frame and the $\alpha\beta$ -frame, the relationships between the variables in the two frames have to be established.

Assumed that the state-space model of the subsystem or the whole system in the dq -frame is denoted by

$$\dot{\vec{x}}_{dq} = A_{dq} \vec{x}_{dq} + B_{dq} \vec{u}_{dq} \quad (62a)$$

$$\vec{y}_{dq} = C_{dq} \vec{x}_{dq} + D_{dq} \vec{u}_{dq} \quad (62b)$$

which can represent the state-space models of components or the whole system.

The variables in the state vector \vec{x}_{dq} , input vector \vec{u}_{dq} , and the output vector \vec{y}_{dq} can be categorized into two types. One type is the variable that appeared in dq pairs, such as i_d and i_q . The other type is the variable that does not have their d or q counterparts, such as v_{dc} and θ .

As for the dq pairs, taking x_d and x_q as the example, the complex space vector and its conjugation can be defined as

$$\mathbf{x}_{dq} = x_d + jx_q \quad (63a)$$

$$\mathbf{x}_{dq}^* = x_d - jx_q \quad (63b)$$

Then, the transformation between dq pairs and complex space vectors can be obtained as

$$\begin{bmatrix} x_d \\ x_q \end{bmatrix} = \frac{1}{2} \begin{bmatrix} 1 & 1 \\ -j & j \end{bmatrix} \cdot \begin{bmatrix} \mathbf{x}_{dq} \\ \mathbf{x}_{dq}^* \end{bmatrix} \quad (64)$$

As for the single variable, take x_s as an example, it can be treated as the real part of a virtual complex space vector $\tilde{\mathbf{x}}_{dq}$ [32], which can be expressed as

$$\tilde{\mathbf{x}}_{dq} = x_s + jx_v \quad (65)$$

where x_v is the virtual imaginary part. Since x_v is the virtual variable with no physical meaning, it can be set to zero for simplification and thereby $x_s = \tilde{\mathbf{x}}_{dq}$.

Consequently, the transformation rule from the real state vector \vec{x}_{dq} to the complex space state vector $\vec{\mathbf{X}}_{dq}$ can be obtained as

$$\underbrace{\begin{bmatrix} \vdots \\ x_d \\ x_q \\ \vdots \\ x_s \\ \vdots \end{bmatrix}}_{\vec{x}_{dq}} = \frac{1}{2} \underbrace{\begin{bmatrix} \ddots & & & & & \\ & 1 & 1 & & & \\ & -j & j & & & \\ & & & \ddots & & \\ & & & & 2 & \\ & & & & & \ddots \end{bmatrix}}_{T_x} \cdot \underbrace{\begin{bmatrix} \vdots \\ \mathbf{x}_{dq} \\ \mathbf{x}_{dq}^* \\ \vdots \\ \tilde{\mathbf{x}}_{dq} \\ \vdots \end{bmatrix}}_{\vec{\mathbf{X}}_{dq}} \quad (66)$$

The state complex space vector $\vec{\mathbf{X}}_{dq}$ in (66) can be further translated to the stationary frame, which can be expressed as

$$\underbrace{\begin{bmatrix} \vdots \\ \mathbf{x}_{dq} \\ \mathbf{x}_{dq}^* \\ \vdots \\ \tilde{\mathbf{x}}_{dq} \\ \vdots \end{bmatrix}}_{\vec{\mathbf{X}}_{dq}} = \underbrace{\begin{bmatrix} \vdots \\ \mathbf{x}_{\alpha\beta} e^{-j\theta_1} \\ \mathbf{x}_{\alpha\beta}^* e^{j\theta_1} \\ \vdots \\ \tilde{\mathbf{x}}_{\alpha\beta} e^{-j\theta_1} \\ \vdots \end{bmatrix}}_{\vec{\mathbf{X}}_{\alpha\beta}} = e^{-j\theta_1} \underbrace{\begin{bmatrix} \vdots \\ \mathbf{x}_{\alpha\beta} \\ \mathbf{x}_{\alpha\beta}^* e^{j2\theta_1} \\ \vdots \\ \tilde{\mathbf{x}}_{\alpha\beta} \\ \vdots \end{bmatrix}}_{\vec{\mathbf{X}}_{\alpha\beta}} \quad (67)$$

Substituting (67) into (66) yields

$$\vec{x}_{dq} = T_x \cdot \vec{\mathbf{X}}_{dq} = T_x \cdot e^{-j\theta_1} \cdot \vec{\mathbf{X}}_{\alpha\beta} \quad (68)$$

$$\vec{x}_{\text{all}} = [\gamma_{id} \ \gamma_{iq} \ x_{ff_d} \ x_{ff_q} \ x_{del_1d} \ x_{del_2d} \ x_{del_3d} \ x_{del_1q} \ x_{del_2q} \ x_{del_3q} \ i_d^c \ i_q^c \ \phi_q \ \theta \ \gamma_{dc} \ x_{ac} \ x_{dc} \ v_{Cgd} \ i_{Lgd} \ v_{Cgq} \ i_{Lgq}]^T \quad (61c)$$

Similar transformation rule can be derived for the input vector \vec{u}_{dq} and the output vector \vec{y}_{dq} , which are defined as

$$\vec{u}_{dq} = T_u \cdot \vec{U}_{dq} = T_u \cdot e^{-j\theta_1} \cdot \vec{U}_{\alpha\beta} \quad (69a)$$

$$\vec{y}_{dq} = T_y \cdot \vec{Y}_{dq} = T_y \cdot e^{-j\theta_1} \cdot \vec{Y}_{\alpha\beta}. \quad (69b)$$

Substituting (68) and (69) into (62) yields

$$\begin{aligned} & \frac{d \left(T_x \cdot e^{-j\theta_1} \cdot \vec{X}_{\alpha\beta} \right)}{dt} \\ &= A_{dq} \cdot \left(T_x \cdot e^{-j\theta_1} \cdot \vec{X}_{\alpha\beta} \right) + B_{dq} \cdot \left(T_u \cdot e^{-j\theta_1} \cdot \vec{U}_{\alpha\beta} \right) \end{aligned} \quad (70a)$$

$$\begin{aligned} & T_y \cdot e^{-j\theta_1} \cdot \vec{Y}_{\alpha\beta} \\ &= C_{dq} \cdot \left(T_x \cdot e^{-j\theta_1} \cdot \vec{X}_{\alpha\beta} \right) + D_{dq} \cdot \left(T_u \cdot e^{-j\theta_1} \cdot \vec{U}_{\alpha\beta} \right). \end{aligned} \quad (70b)$$

The derivative term in the left side of (70a) can be expanded as follows:

$$\frac{d \left(T_x \cdot e^{-j\theta_1} \cdot \vec{X}_{\alpha\beta} \right)}{dt} = T_x e^{-j\theta_1} \cdot \frac{d\vec{X}_{\alpha\beta}}{dt} - j\omega_1 T_x e^{-j\theta_1} \cdot \vec{X}_{\alpha\beta} \quad (71)$$

where $\omega_1 = d\theta_1/dt$. By substituting (71) into (70a) and eliminating $e^{-j\theta_1}$ from both sides of (70), the state-space model in stationary $\alpha\beta$ -frame can be obtained as

$$\dot{\vec{X}}_{\alpha\beta} = T_x^{-1} (A_{dq} + j\omega_1 I) T_x \cdot \vec{X}_{\alpha\beta} + T_x^{-1} B_{dq} T_u \cdot \vec{U}_{\alpha\beta} \quad (72a)$$

$$\vec{Y}_{\alpha\beta} = T_y^{-1} C_{dq} T_x \cdot \vec{X}_{\alpha\beta} + T_y^{-1} D_{dq} T_u \cdot \vec{U}_{\alpha\beta}. \quad (72b)$$

As a conclusion, the transformation between the matrices of the state-space model in the dq - and $\alpha\beta$ -frame can be expressed as follows:

$$A_{\alpha\beta} = T_x^{-1} (A_{dq} + j\omega_1 I) T_x \quad (73a)$$

$$B_{\alpha\beta} = T_x^{-1} B_{dq} T_u \quad (73b)$$

$$C_{\alpha\beta} = T_y^{-1} C_{dq} T_x \quad (73c)$$

$$D_{\alpha\beta} = T_y^{-1} D_{dq} T_u. \quad (73d)$$

VII. MODAL ANALYSIS USING UNIFIED STATE-SPACE MODEL

The modal analysis is a common practice for the small-signal stability of power grids, which is mainly about how to interpret the dynamic modes of system by analyzing the eigenvalues, eigenvectors, participation factor, and sensitivity of the state matrix in the state-space models. Since the modal analysis procedures are the same for the dq state matrix A_{dq} and $\alpha\beta$ state matrix $A_{\alpha\beta}$, therefore the notation $A_{dq/\alpha\beta}$ is used to stand for either A_{dq} or $A_{\alpha\beta}$ for the following analysis.

The eigenvalues of state-matrix $A_{dq/\alpha\beta}$ can be derived by:

$$\det(\lambda I - A_{dq/\alpha\beta}) = 0. \quad (74)$$

Assuming that $A_{dq/\alpha\beta}$ is n by n matrix, n eigenvalues can be obtained by solving (74).

Suppose that h th eigenvalue of $A_{dq/\alpha\beta}$, λ_h , is expressed as

$$\lambda_h = \sigma_h + j\omega_h. \quad (75)$$

Then, corresponding frequency f_h and damping ratio ζ_h of h th dynamic mode can be obtained as

$$f_h = \frac{\omega_h}{2\pi} \quad (76a)$$

$$\zeta_h = -\frac{\sigma_h}{\sqrt{\sigma_h^2 + \omega_h^2}}. \quad (76b)$$

The stability of the h th dynamic mode can be assessed by the value of ζ_h : when $\zeta_h > 0$, the mode is stable; when $\zeta_h = 0$, the mode is marginally stable; and when $\zeta_h < 0$, the mode is unstable.

The right eigenvector \vec{R}_h of λ_h is defined as

$$A_{dq/\alpha\beta} \cdot \vec{R}_h = \lambda_h \cdot \vec{R}_h \quad (77)$$

which contains n elements, indicating the magnitudes and phase angles of n state variables of $x_{dq}/\vec{X}_{\alpha\beta}$, respectively, in the h th dynamic mode [33], i.e.

$$\vec{R}_h = \begin{bmatrix} M_1 e^{j\varphi_1} \\ \vdots \\ M_i e^{j\varphi_i} \\ \vdots \\ M_n e^{j\varphi_n} \end{bmatrix} \rightarrow \begin{bmatrix} x_1 \\ \vdots \\ x_i \\ \vdots \\ x_n \end{bmatrix} = \vec{x}_{dq}/\vec{X}_{\alpha\beta}. \quad (78)$$

To provide a good insight into tuning the control parameters to damp the critical dynamic modes, the sensitivity of the damping ratio with respect to the specific control parameter can be also calculated. The damping ratio ζ_h with respect to the control parameter p can be obtained as

$$\frac{\partial \zeta_h}{\partial p} \approx \frac{\zeta_h (p_0 + \Delta p) - \zeta_h (p_0)}{\Delta p} \quad (79)$$

where p_0 is the original control parameter, and $\Delta p = 5\% - 10\%$ p_0 is the parameter perturbation.

It should be noted that since the elements of $A_{\alpha\beta}$ are complex numbers, the eigenvalues of complex matrix $A_{\alpha\beta}$ are not paired with their conjugations, which can directly reveal the coupled oscillation frequencies in the $\alpha\beta$ -frame caused by the asymmetrical dynamics of the control system.

VIII. EXPERIMENTAL VERIFICATION

In order to verify the correctness of the unified modular state-space model and modal analysis, a downscaled experimental setup is built in the lab, as shown in Fig. 13, where two converters are operated back-to-back. The converter 1# draws the constant magnitude of current at ac side, which can be treated as a constant power source given that both the power loss and ac voltage magnitude of converter 1# are constant. The converter 2# is the grid-connected VSC, which contains ACC, PLL, DVC, and AVC control loops. All the control algorithms are implemented in the dSPACE 1007. The capacitor C_g and inductor L_g are connected with grid simulator Chroma 61845 to emulate the weak grid. The main circuit parameters of the grid-connected VSC are shown in Table I. The control parameters and steady-state values are

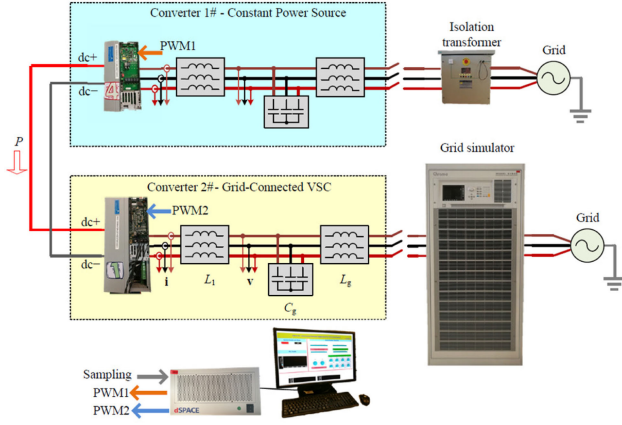


Fig. 13. Photograph of the experimental setup.

 TABLE I
 MAIN CIRCUIT PARAMETERS OF GRID-CONNECTED VSC

Parameters	Values	
V_{dc}	Input dc-link voltage	600 V
V_1	Rated line to line grid voltage, RMS	126 V
f_1	Grid fundamental frequency	50 Hz
f_{sw}	Inverter switching frequency	10 kHz
f_s	Inverter control sampling frequency	10 kHz
P_n	Rated power	3050 W
C_{dc}	Dc-link capacitance	1500 μ F
L_1	Inverter-side inductance	1 mH
R_1	ESR of the inverter-side inductor	0.3 m Ω
C_g	Equivalent grid-side capacitance	20 μ F
R_{Cg}	ESR of the grid-side capacitor	0.5 m Ω
L_g	Equivalent grid-side inductance	11 mH
R_{Lg}	ESR of the grid-side inductor	3.3 m Ω

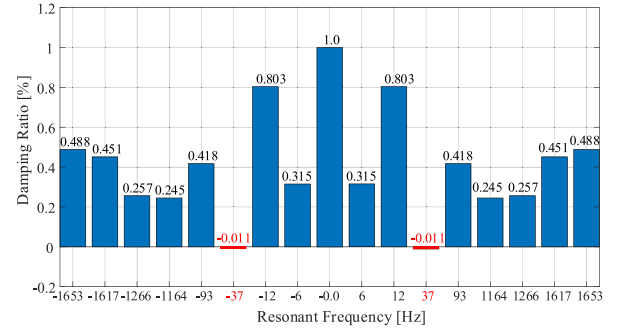
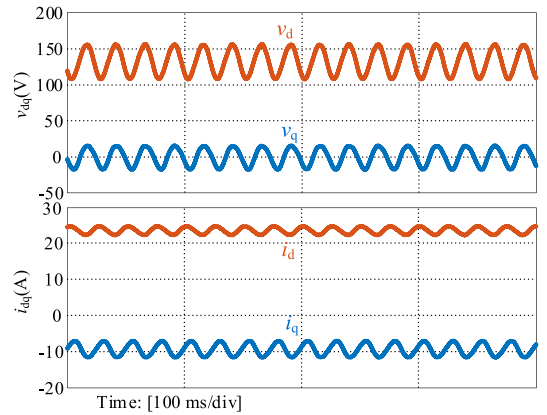
presented in Table II. In real-life applications, the dc source with variable input power may be used, such as a PV generator, where the steady-state values of the system will be changed by the input power fluctuations. In this case, the stability analysis may need to be performed at different operating points.

Using the state-space model in the dq -frame, it is able to identify the critical oscillation modes and tell the stability margin by checking the corresponding damping ratios. Based on the control parameters presented in Table II, the frequencies and damping ratios of different dynamic modes are shown in Fig. 14; the dynamic mode at ± 37 Hz have negative damping ratios, which is unstable. However, these stability analysis is difficult to be verified in the grid dq -frame directly from the perspectives of both the measurement and the interpretation.

On the one hand, the current and voltage oscillations cannot be measurable directly and the ideal phase angle θ_1 defined by the fundamental positive component of PCC voltage needs to be

 TABLE II
 CONTROL PARAMETERS AND STEADY-STATE VALUES

Parameters	Values	
k_a	Proportional gain of the feedforward controller	1
ω_a	Corner frequency of the feedforward controller	1.256e4
k_{pc}	Proportional gain of the ac current controller	5.236
k_{ic}	Integral gain of the ac current controller	1.827e3
k_{pp}	Proportional gain of the PLL controller	1.392
k_{ip}	Integral gain of the PLL controller	1.223e2
k_{pd}	Proportional gain of the active power controller	0.095
k_{id}	Integral gain of the active power controller	2.998
k_{pa}	Proportional gain of the ac voltage controller	1.519
ω_{ac}	Corner frequency of the ac voltage controller	6.283
I_{d1}	Steady-state value ac current at d -axis	25 A
I_{q1}	Steady-state value ac current at q -axis	-9.6A
V_{d1}	Steady-state value PCC voltage at d -axis	126 V
V_{q1}	Steady-state value PCC voltage at q -axis	0 V


 Fig. 14. Frequencies and damping ratios of dynamic modes in the ideal grid dq -frame.

 Fig. 15. Transformed waveforms in the grid dq -frame estimated by PLL with 20 Hz control bandwidth.

estimated for dq -transformation, which could be easily distorted by oscillation itself. Any algorithm that used to estimate θ_1 may introduce additional errors due to the dynamics of the phase-tracking controller and the filters used for separating the fundamental positive component of PCC voltage from oscillations. Figs. 15 and 16 show the oscillated voltage and current

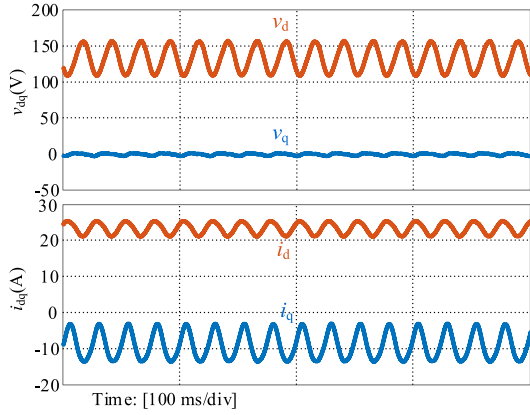


Fig. 16. Transformed waveforms in the grid dq -frame estimated by PLL with 100 Hz control bandwidth.

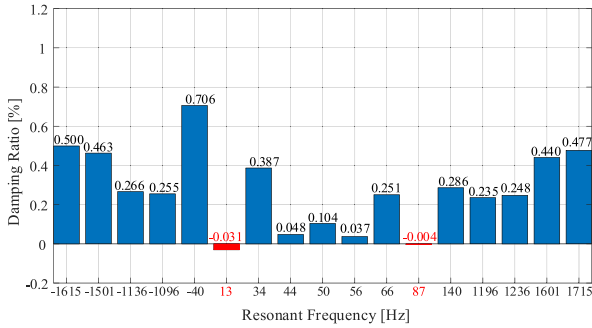


Fig. 17. Frequencies and damping ratios of dynamic modes in the $\alpha\beta$ -frame.

waveforms in the different grid dq -frame estimated by PLL with different control bandwidths. As can be seen, the oscillation magnitudes of voltages and currents are significantly different from each other in different estimated grid dq -frames.

On the other hand, the linkage between oscillation frequencies in the dq -frame and the $\alpha\beta$ -frame is control-structure dependent. Considering the 50 Hz frequency shift effect of the dq transformation, if the control system is symmetrical for d - and q -axis (such as single current control loop), then 37 Hz oscillation in the dq -frame only results in single oscillation at 87 Hz in the $\alpha\beta$ -frame [27]. If the control system is asymmetrical, then 37 Hz oscillation in the dq -frame will result in 13 and 87 Hz in the $\alpha\beta$ -frame. Therefore, it is not straightforward to predict the actual oscillations in the $\alpha\beta$ -frame based on the modal analysis results in the dq -frame.

Using the state-space model in the $\alpha\beta$ -frame, the frequencies and damping ratios of different dynamic modes can be directly obtained, as shown in Fig. 17, the dynamic modes at 13 and 87 Hz have negative damping ratios, and thus they are unstable. Moreover, according to (78), the right eigenvectors of the two critical dynamic modes at 13 and 87 Hz can be obtained, which provides an insight on the oscillations magnitudes of the PCC voltages and currents in the $\alpha\beta$ -frame, as shown in Fig. 18. As can be seen, the oscillations in PCC voltages are dominated at 87 Hz, whereas comparable oscillations at both 13 and 87 Hz

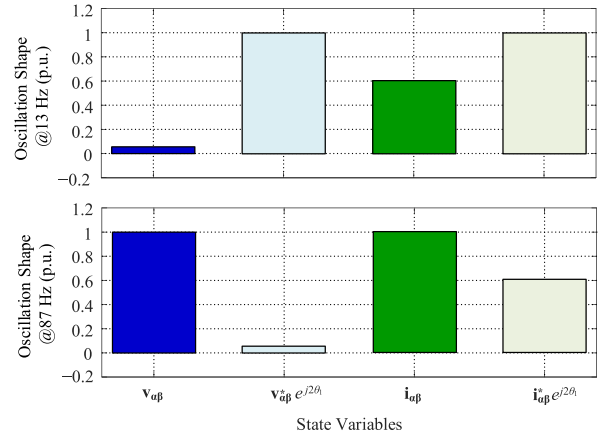


Fig. 18. Oscillations of PCC voltages and currents for unstable modes at 13 and 87 Hz in the $\alpha\beta$ -frame.

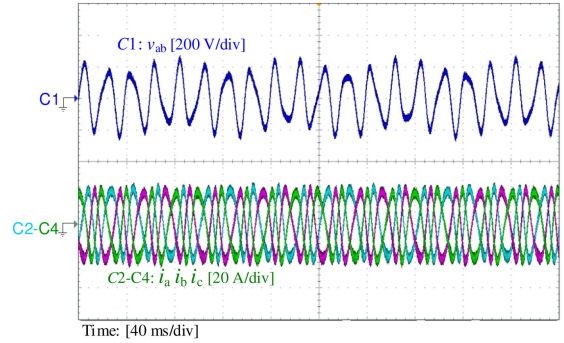


Fig. 19. Oscillated experimental waveforms in the $\alpha\beta$ -frame.

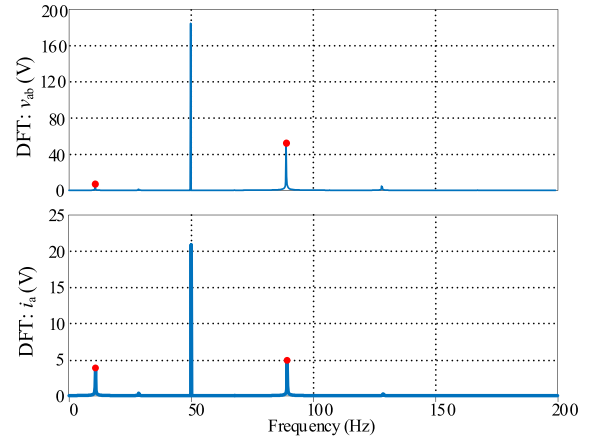


Fig. 20. DFT analysis experimental waveforms in the $\alpha\beta$ -frame.

are observed in the PCC currents. These analysis results can be directly verified in the $\alpha\beta$ -frame.

Fig. 19 shows experimental results, where the sustained low-frequency oscillations can be observed in both the PCC voltages and currents. According to the discrete Fourier transformation (DFT) analysis presented in Fig. 20, the oscillation frequencies can be observed at 13 and 87 Hz, and the normalized magnitudes of the oscillations are matched well with the predictions presented in Fig. 18.

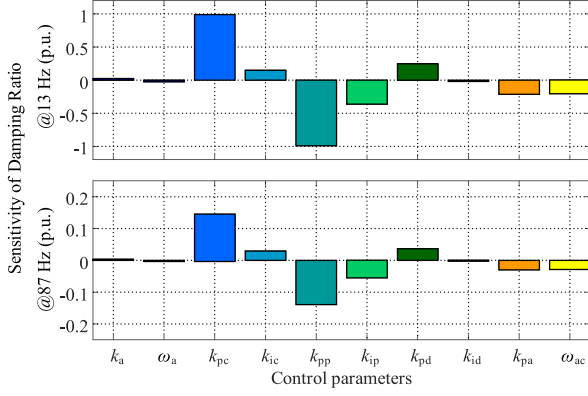


Fig. 21. Damping ratio sensitivity of the unstable modes and critical modes.

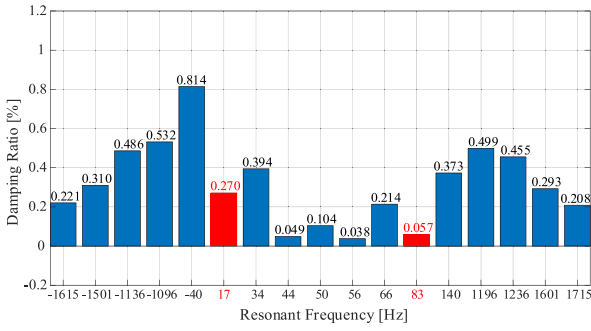
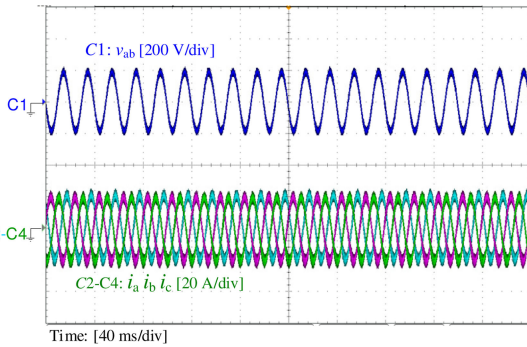

 Fig. 22. Frequencies and damping ratios of dynamic modes in the $\alpha\beta$ -frame after tuning the controllers.


Fig. 23. Stabilized experimental waveforms after tuning controllers.

Fig. 21 shows the damping ratio sensitivity of the critical modes at 13 Hz and 87 Hz with respect to the different controller parameters. It reveals that the tuning of the proportional gains k_{pp} in the PLL controller and k_{pc} in ac current controller is the most effective way to stabilize the unstable modes. As for the case in this article, the control parameters k_{pp} and k_{pc} are set 0.8 and 1.2 of their original values, respectively. Fig. 22 shows the frequencies and damping ratios of dynamic modes in the $\alpha\beta$ -frame after tuning the controllers, where the unstable modes are successfully stabilized.

Fig. 23 shows the experimental results after tuning the controller parameters, and the system is stabilized, which confirms the effectiveness of the control tuning strategy.

IX. CONCLUSION

This article proposed a modular state-space model of grid-connected VSCs, where the cross couplings among various loops are identified and represented by the implicit interconnections, which allows that different control loops can be modeled separately and merged together like building blocks. Moreover, the mathematical relationship between the state-space models in the dq -frame and the $\alpha\beta$ -frame is established. Intuitive interpretations of the modal analysis in the $\alpha\beta$ -frame are also provided, which can directly predict the frequencies and magnitudes of voltage and current oscillations in the $\alpha\beta$ -frame. Experimental results from a 3-kW VSC confirms the accuracy of the established state-space model and the effectiveness of the new modal analysis.

APPENDIX

A. AC Current Controller

The inputs are dq -current errors i_{d_err} and i_{q_err} , and the outputs are part of the PWM references, noted as v_{m1d} and v_{m1q} . Defining the states in integrators of current controllers $G_i(s)$ as γ_{id} and γ_{iq} , the state-space models of the current controllers can be given as

$$\underbrace{\begin{bmatrix} \dot{\gamma}_{id} \\ \dot{\gamma}_{iq} \end{bmatrix}}_{\bar{x}_1} = \underbrace{\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}}_{F_1} \underbrace{\begin{bmatrix} \gamma_{id} \\ \gamma_{iq} \end{bmatrix}}_{\bar{x}_1} + \underbrace{\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}}_{H_1} \underbrace{\begin{bmatrix} i_{d_err} \\ i_{q_err} \end{bmatrix}}_{\bar{a}_1} \quad (A1a)$$

$$\underbrace{\begin{bmatrix} v_{m1d} \\ v_{m1q} \end{bmatrix}}_{\bar{b}_1} = \underbrace{\begin{bmatrix} k_{ic} & 0 \\ 0 & k_{ic} \end{bmatrix}}_{J_1} \underbrace{\begin{bmatrix} \gamma_{id} \\ \gamma_{iq} \end{bmatrix}}_{\bar{x}_1} + \underbrace{\begin{bmatrix} k_{pc} & 0 \\ 0 & k_{pc} \end{bmatrix}}_{K_1} \underbrace{\begin{bmatrix} i_{d_err} \\ i_{q_err} \end{bmatrix}}_{\bar{a}_1}. \quad (A1b)$$

B. Feedforward Controller

The inputs of the feedforward controller are PCC voltages v_d^c and v_q^c , and the outputs are PWM reference noted as v_{m2d} and v_{m2q} . By defining $[x_{ff_d}, x_{ff_q}]^T$ as the state variables, the state-space model of feedforward controllers $G_{ff}(s)$ can be derived as

$$\underbrace{\begin{bmatrix} \dot{x}_{ff_d} \\ \dot{x}_{ff_q} \end{bmatrix}}_{\bar{x}_2} = \underbrace{\begin{bmatrix} -\omega_a & 0 \\ 0 & -\omega_a \end{bmatrix}}_{F_2} \underbrace{\begin{bmatrix} x_{ff_d} \\ x_{ff_q} \end{bmatrix}}_{\bar{x}_2} + \underbrace{\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}}_{H_2} \underbrace{\begin{bmatrix} v_d^c \\ v_q^c \end{bmatrix}}_{\bar{a}_2} \quad (A2a)$$

$$\underbrace{\begin{bmatrix} v_{m2d} \\ v_{m2q} \end{bmatrix}}_{\bar{b}_2} = \underbrace{\begin{bmatrix} -k_a\omega_a & 0 \\ 0 & -k_a\omega_a \end{bmatrix}}_{J_2} \underbrace{\begin{bmatrix} x_{ff_d} \\ x_{ff_q} \end{bmatrix}}_{\bar{x}_2} + \underbrace{\begin{bmatrix} k_a & 0 \\ 0 & k_a \end{bmatrix}}_{K_2} \underbrace{\begin{bmatrix} v_d^c \\ v_q^c \end{bmatrix}}_{\bar{a}_2}. \quad (A2b)$$

C. Digital Control Delay

The inputs of the control delay are PWM references v_{md} and v_{mq} , and the outputs are VSC bridge voltages v_{od} and v_{oq} . By defining $[x_{del_1d}, x_{del_2d}, x_{del_3d}, x_{del_1q}, x_{del_2q}, x_{del_3q}]^T$ as the state variables, the state-space model of the control delay

can be derived as follows:

$$\underbrace{\begin{bmatrix} \dot{x}_{\text{del}_1d} \\ \dot{x}_{\text{del}_2d} \\ \dot{x}_{\text{del}_3d} \\ \dot{x}_{\text{del}_1q} \\ \dot{x}_{\text{del}_2q} \\ \dot{x}_{\text{del}_3q} \end{bmatrix}}_{\dot{\bar{x}}_3} = \underbrace{\begin{bmatrix} F_d & | & 0 \\ \hline 0 & | & F_q \end{bmatrix}}_{F_3} \underbrace{\begin{bmatrix} x_{\text{del}_1d} \\ x_{\text{del}_2d} \\ x_{\text{del}_3d} \\ x_{\text{del}_1q} \\ x_{\text{del}_2q} \\ x_{\text{del}_3q} \end{bmatrix}}_{\bar{x}_3} + \underbrace{\begin{bmatrix} H_d & | & 0 \\ \hline 0 & | & H_q \end{bmatrix}}_{H_3} \underbrace{\begin{bmatrix} v_{md} \\ v_{mq} \end{bmatrix}}_{\bar{a}_3} \quad (\text{A3a})$$

$$\underbrace{\begin{bmatrix} v_{od} \\ \vdots \\ v_{oq} \end{bmatrix}}_{\bar{b}_3} = \underbrace{\begin{bmatrix} J_d & | & 0 \\ \hline 0 & | & J_q \end{bmatrix}}_{J_3} \underbrace{\begin{bmatrix} x_{\text{del}_1d} \\ x_{\text{del}_2d} \\ x_{\text{del}_3d} \\ x_{\text{del}_1q} \\ x_{\text{del}_2q} \\ x_{\text{del}_3q} \end{bmatrix}}_{\bar{x}_3} + \underbrace{\begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}}_{K_3} \underbrace{\begin{bmatrix} v_{md} \\ v_{mq} \end{bmatrix}}_{\bar{a}_3} \quad (\text{A3b})$$

where the matrices F_d , F_q , H_d , H_q , J_d , and J_q are expressed as follows:

$$F_d = F_q = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -120/T_d^3 & -60/T_d^2 & -12/T_d \end{bmatrix} \quad (\text{A4a})$$

$$H_d = H_q = \begin{bmatrix} 0 & 0 & 1 \end{bmatrix}^T \quad (\text{A4b})$$

$$J_d = J_q = \begin{bmatrix} 240/T_d^3 & 0 & 24/T_d \end{bmatrix}. \quad (\text{A4c})$$

D. L Filter

For the L filter, the relationship between the inductor voltages v_{Ld} , v_{Lq} and inductor currents i_d^c , i_q^c in the time domain can be given as

$$\frac{di_d^c}{dt} = \omega_1 i_q^c - \frac{R_1}{L_1} i_d^c + \frac{v_{Ld}}{L_1} \quad (\text{A5a})$$

$$\frac{di_q^c}{dt} = -\omega_1 i_d^c - \frac{R_1}{L_1} i_q^c + \frac{v_{Lq}}{L_1}. \quad (\text{A5b})$$

Therefore, the state-space model of the L filter can be derived as

$$\underbrace{\begin{bmatrix} \dot{i}_d^c \\ \dot{i}_q^c \end{bmatrix}}_{\dot{\bar{x}}_4} = \underbrace{\begin{bmatrix} -\frac{R_1}{L_1} & \omega_1 \\ \omega_1 & -\frac{R_1}{L_1} \end{bmatrix}}_{F_4} \underbrace{\begin{bmatrix} i_d^c \\ i_q^c \end{bmatrix}}_{\bar{x}_4} + \underbrace{\begin{bmatrix} \frac{1}{L_1} & 0 \\ 0 & \frac{1}{L_1} \end{bmatrix}}_{H_4} \underbrace{\begin{bmatrix} v_{Ld} \\ v_{Lq} \end{bmatrix}}_{\bar{a}_4} \quad (\text{A6a})$$

$$\underbrace{\begin{bmatrix} i_d^c \\ i_q^c \end{bmatrix}}_{\bar{b}_4} = \underbrace{\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}}_{J_4} \underbrace{\begin{bmatrix} i_d^c \\ i_q^c \end{bmatrix}}_{\bar{x}_4} + \underbrace{\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}}_{K_4} \underbrace{\begin{bmatrix} v_{Ld} \\ v_{Lq} \end{bmatrix}}_{\bar{a}_4}. \quad (\text{A6b})$$

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