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Huang, Liang; Wu, Chao; Zhou, Dao; Blaabjerg, Frede

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Article

Impact of Grid Strength and Impedance Characteristics on the Maximum Power Transfer Capability of Grid-Connected Inverters [†]

Liang Huang , Chao Wu * , Dao Zhou and Frede Blaabjerg

Department of Energy Technology, Aalborg University, 9220 Aalborg Øst, Denmark; lihu@et.aau.dk (L.H.); zda@et.aau.dk (D.Z.); fbl@et.aau.dk (F.B.)

- * Correspondence: cwu@et.aau.dk
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Abstract: Continuously expanding deployments of distributed power generation systems are transforming conventional centralized power grids into mixed distributed electrical networks. The higher penetration and longer distance from the renewable energy source to the main power grid result in lower grid strength, which stimulates the power limitation problem. Aimed at this problem, case studies of inductive and resistive grid impedance with different grid strengths have been carried out to evaluate the maximum power transfer capability of grid-connected inverters. It is revealed that power grids with a higher short circuit ratio (SCR) or lower resistance-inductance ratio (R/X) provide higher power transfer capability. Moreover, under the resistive grid conditions, a higher voltage at the point of common coupling (PCC) is beneficial to increase the power transfer capability. Based on mathematical analysis, the maximum power curves in the inductive and resistive grids can be found. Moreover, a performance index is proposed in this paper to quantify the performance of the system with different parameter values. Finally, the effectiveness of the analysis is verified by simulation.

Keywords: grid-connected inverter; short circuit ratio; grid impedance; maximum power transfer capability



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1. Introduction

In the past decades, due to a foreseen exhaustion of conventional fossil-based energies and their climate impact, traditional centralized power generation using fossil fuels has been increasingly considered unsustainable in the long term. Consequently, many global efforts have been devoted to developing more renewable energy sources, such as wind and solar photovoltaics (PVs) [1]. Thus, the proportion of distributed power generation systems has increased quite fast, especially in Europe [2]. Moreover, due to the fact that the best locations to get wind and solar energy are often far from the main grid, the long-distance transmission-line impedance makes the grid weaker than before, which brings a significant challenge to effective power transmission [3]. Although a high voltage direct current (HVDC) system can replace the alternating current (AC) system for long-distance power transmission [4,5], the grid-side converter of the HVDC system still faces the challenge of connecting to a weak grid in some cases [6,7]. Therefore, it is necessary to study the maximum power transfer capability of grid-connected inverters.

The strength of the grid is defined by the short circuit ratio (SCR), which is the ratio of the short circuit power at the point of common coupling (PCC) and the rated power of the inverter. When the SCR is below 6–10, the grid is weak. In the case that the SCR is above 20, the grid is strong [8]. According to the definition of the SCR, the increase of the rated inverter power or the transmission impedance will reduce the SCR and make the grid weaker. The PCC voltage varies easily when a large amount of active power is injected into a weak grid. Thus, the reactive power control has to be used to keep the PCC voltage

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around its rated value [9]. Since the total rated power of the inverter is constant, the more the output reactive power, the less the output active power, which will limit the power transfer capability of the grid-connected inverter. Therefore, the SCR is an important factor that influences the maximum power transfer capability of the grid-connected inverter.

Most previous works have focused on improving the control strategies of inverters to increase the power transfer capability limited by control stability, such as improved grid-following control methods [10–12] and newly developed grid-forming control methods [13–16]. A gain-scheduling controller with the H-infinity method is presented in [10] to extend the stability range of classical grid-following inverters. Similarly, a current errorbased voltage angle and magnitude compensation method is proposed in [11] to improve system stability. Moreover, a power-synchronization-based grid-forming control method is proposed in [13], which has better stability performance than grid-following inverters. Differently, the natural maximum power transfer capability of grid-connected inverters mainly depends on the physical parameters of the system, which is constant for an existing system [17,18]. Hence, it is a key property for engineering design and analysis.

Recently, it was reported in [19] that not only the SCR but also the resistance-inductance ratio (R/X) of grid impedance affects the maximum power transfer capability of grid-connected inverters. However, [19] mainly discusses the inductive grid case, while the resistive grid case is not analyzed. In fact, both the inductive and resistive grids exist in real applications. Generally, high-voltage lines are inductive, while low-voltage lines are resistive [20,21]. Therefore, the resistive grid case should also be analyzed. This paper attempts to fill this research gap and provides a full map of both cases. Since both current and voltage limitations are considered, this research is closer to reality.

Furthermore, our early work in [22] mainly analyzes the impact of the SCR and the R/X ratio on the maximum power transfer capability in the constant PCC voltage case, where the impact of the PCC voltage is not considered. Based on our early work, this paper reveals that the PCC voltage amplitude is also a key factor affecting the maximum power transfer capability of the system, especially in the resistive grid case. It was found that a higher PCC voltage than the rated value in a resistive grid is beneficial to increase the power transfer capability of grid-connected inverters.

The rest of this paper is organized as follows. Section 2 introduces the study system and its simplified model. Then, the maximum power transfer capability of the system at the rated PCC voltage is analyzed. Section 3 analyzes the maximum power transfer capability of the system at varying PCC voltage. After that, optimal parameters for maximum power operation in the inductive and resistive grids are illustrated in Section 4. The simulation results are illustrated in Section 5. Finally, concluding remarks are drawn in Section 6.

2. Maximum Power Transfer Capability of Grid-Connected Systems at the Rated PCC Voltage

2.1. System Configuration and Mathematical Model

Figure 1 shows the typical configuration of grid-connected wind and PV generation systems. Generally, a wind generation unit contains an AC/DC converter for maximum power point tracking (MPPT) control and a DC/AC inverter for grid connection. Similarly, a PV generation unit mainly contains a DC/DC converter for MPPT control and a DC/AC inverter for grid connection. In the entire wind or PV power plant, all these generation units are connected at the PCC. The total output power of inverters at the PCC is injected into the high-voltage transmission network connected to the main grid. To simplify the analysis, the transmission network is represented by a transmission line, as shown in Figure 1. In the following sections, this paper will mainly focus on the impact of transmission-line impedance on the maximum power transfer capability of the system.

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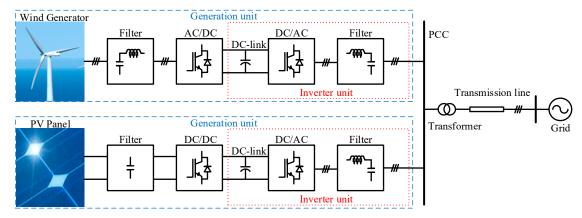


Figure 1. Typical configuration of grid-connected wind and PV generation systems.

Grid-connected inverters usually operate in current-controlled mode, so the whole generation power plant can be treated as an ideal current source. Moreover, the grid can be represented by its Thevenin's equivalent circuit; the equivalent circuit of the grid-connected generation system is shown in Figure 2. Assuming the PCC voltage vector is aligned to the d-axis, $V_{pcc} \angle 0$ is the vector of the PCC voltage, $I_{inv} \angle \varphi_i$ is the vector of the inverter current, $V_g \angle \varphi_v$ is the vector of the grid voltage, and Z_g is the grid impedance. It is noted that series-connected resistor R_g and inductor X_g are used to represent grid impedance Z_g .

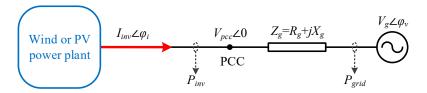


Figure 2. Equivalent circuit of the grid-connected generation system.

The stiffness of the grid at the PCC can be described by the SCR, which is expressed as:

$$SCR = \frac{S_{SC}}{S_N} = \frac{3/2 \cdot V_g^2 / |Z_g|}{3/2 \cdot V_{pcc(rated)} \cdot I_{inv(rated)}}$$
(1)

where S_{SC} is the short-circuit apparent power at the PCC, S_N is the total rated apparent power of inverters, V_g is the amplitude of grid voltage, $V_{pcc(rated)}$ and $I_{inv(rated)}$ are the amplitude of the rated PCC voltage and rated inverter current.

Generally, the rated PCC voltage should be equal to the grid voltage, namely, " $V_{pcc(rated)}$ = V_g ", and the rated current $I_{inv(rated)}$ is the same as the maximum inverter current $I_{inv(max)}$, which is determined by the endurable current of the power semiconductor. Thus, the grid impedance can be represented by the SCR according to Equation (1), which is expressed as:

$$|Z_g| = \sqrt{R_g^2 + X_g^2} = \frac{V_g}{I_{inv(max)} \cdot SCR}$$
 (2)

According to the equivalent circuit in Figure 2, the relationship between the grid voltage and the inverter current can be derived as:

$$V_{pcc} \angle 0 = V_g \angle \varphi_v + (R_g + jX_g) \cdot I_{inv} \angle \varphi_i \tag{3}$$

To simplify the vector expression in Equation (3), the current vector $I_{inv} \angle \varphi_i$ can be expressed by the d-axis component " $i_d = I_{inv} \cdot \cos(\varphi_i)$ " and the q-axis component " $i_q = I_{inv} \cdot \cos(\varphi_i)$ "

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 $I_{inv} \cdot \sin(\varphi_i)$ ". Thus, the relationship between the two current components and the PCC voltage can be derived as:

$$(R_g^2 + X_g^2)(i_d^2 + i_q^2) + 2V_{pcc}(X_g i_q - R_g i_d) + V_{pcc}^2 - V_g^2 = 0$$
(4)

2.2. Ideal Maximum Power without Current Limitation

Firstly, an ideal case without current limitation is analyzed as follows. Substituting " $V_{pcc} = V_g$ " and Equation (2) into Equation (4), the per-unit values of i_d and i_q can be derived as:

$$i_{q(pu)}^{2} + \frac{2 \cdot SCR}{\sqrt{(R_{g}/X_{g})^{2} + 1}} \cdot i_{q(pu)} + \left[i_{d(pu)}^{2} - \frac{2 \cdot SCR \cdot (R_{g}/X_{g})}{\sqrt{(R_{g}/X_{g})^{2} + 1}} \cdot i_{d(pu)}\right] = 0$$
 (5)

Considering Equation (5) as a quadratic equation of $i_{q(pu)}$, thus, only when Equation (6) is satisfied, does Equation (5) have solutions.

$$\Delta = \frac{4 \cdot SCR^2}{(R_g/X_g)^2 + 1} + \frac{8 \cdot SCR \cdot (R_g/X_g)}{\sqrt{(R_g/X_g)^2 + 1}} \cdot i_{d(pu)} - 4 \cdot i_{d(pu)}^2 \ge 0 \tag{6}$$

According to Equation (6), the maximum value of $i_{d(pu)}$ can be calculated, as given in Equation (7). Because the PCC voltage is considered a constant in this section, the per-unit value of the current i_d is equal to the per-unit value of the inverter active power P_{inv} . Hence, the ideal maximum power of the inverter can be represented by Equation (7).

$$P_{inv(pu)max} = i_{d(pu)max} = SCR \cdot \left[\frac{(R_g/X_g)}{\sqrt{(R_g/X_g)^2 + 1}} + 1 \right]$$
 (7)

According to Equation (7), the relationship between the ideal maximum inverter power $P_{inv(pu)max}$ and the SCR with different R_g/X_g ratios is shown in Figure 3. It can be seen that the relationship between $P_{inv(pu)max}$ and the SCR is linear. In the purely inductive (R/X = 0) case, SCR = 1 is a critical point because when the SCR is lower than 1, the maximum power $P_{inv(pu)max}$ is lower than 1, namely, the maximum output power of the inverter is limited naturally under weak grid conditions. Hence, this natural characteristic between $P_{inv(pu)max}$ and the SCR can be considered a standard to be compared with the maximum power operating point at the stability boundary of different control strategies.

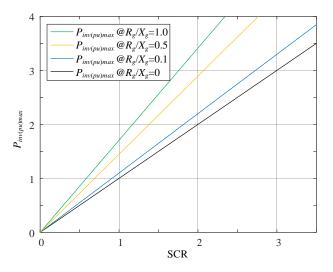


Figure 3. Relationship between ideal maximum inverter power $P_{inv(pu)max}$ and SCRs with different R_g/X_g .

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2.3. Realistic Maximum Power with Current Limitation

In real applications, the maximum inverter current $I_{inv(max)}$ is determined by the endurable current of the power semiconductor. Thus, considering the current limitation of the inverter, the d-axis inverter current should be limited by the expression in Equation (8). To analyze the maximum transferred power of a grid-connected inverter, the d-axis inverter current should be equal to the limiting value in Equation (8). It is worth mentioning that since the active power is transferred from the wind or PV power plant to the grid under normal circumstances, the active power P_{inv} should be positive. Thus, the current i_d should also be positive; hence, a negative i_d is not considered in this paper.

$$i_d \le \sqrt{I_{inv(max)}^2 - i_q^2} \tag{8}$$

It is worth noting that this paper investigates the system without reactive power compensation devices; thus, all the reactive power is provided by the inverter itself. Due to the flexible control ability of inverters, the suitable reactive power from the inverter can be controlled to make sure the PCC voltage operates near its rated value [23,24]. To be easily understandable, the analysis starts with the case where the PCC voltage equals its rated value.

By substituting " $V_{pcc} = V_g$ " and Equation (8) into Equation (4), a standard quadratic equation for the q-axis inverter current i_q can be derived as:

$$\frac{1}{R_g^2 + X_g^2} \cdot i_q^2 + \frac{X_g I_{inv(max)}^2}{(R_g^2 + X_g^2)V_g} \cdot i_q + \left[\frac{I_{inv(max)}^4}{4V_g^2} - \frac{R_g^2 I_{inv(max)}^2}{(R_g^2 + X_g^2)^2}\right] = 0$$
 (9)

Based on Equation (9), positive and negative solutions of the q-axis inverter current can be obtained. As the control law in the voltage PI controller is only suitable for the positive solution, the negative solution is unattainable. Hence, it is disregarded. The positive solution is given by Equation (10).

$$i_q = R_g I_{inv(max)} \cdot \sqrt{\frac{1}{R_g^2 + X_g^2} - \frac{I_{inv(max)}^2}{4V_g^2}} - \frac{X_g I_{inv(max)}^2}{2V_g}$$
(10)

If the solution listed in Equation (10) exists, Equation (11) must be satisfied.

$$\frac{1}{R_g^2 + X_g^2} - \frac{I_{inv(max)}^2}{4V_g^2} \ge 0 \tag{11}$$

Substituting Equation (2) into Equation (11), the range of the SCR is derived as:

$$SCR \ge \frac{1}{2} \tag{12}$$

The expression in Equation (12) shows that the PCC voltage cannot be maintained at the rated value if the SCR is lower than 0.5.

Moreover, when Equations (2) and (10) are substituted into Equation (8), the expression of the d-axis inverter current i_d is derived as:

$$i_{d(pu)} = \frac{i_d}{I_{inv(max)}} = \frac{\sqrt{SCR^2 - \frac{1}{4} + \frac{R_g}{2X_g}}}{SCR \cdot \sqrt{1 + \frac{R_g^2}{X_g^2}}}$$
(13)

In order to visualize the aforementioned analytical analysis, the voltage and current vector diagrams of the grid-connected system at the d-q plane are shown in Figure 4. The purely inductive, purely resistive, and hybrid impedance cases are shown in Figure 4a–c, respectively. The vector amplitudes I_{inv} and V_g are invariable, while the phase angles φ_i

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and φ_v are adjusted to match different values of Z_g . It can be seen from Equation (13) that the d-axis current i_d is always positive because only the inverter mode is considered in this paper. Moreover, according to Equation (10), the q-axis current i_q is negative in the purely inductive case, which is shown in Figure 4a. However, the q-axis current i_q is positive in the purely resistive case, which is shown in Figure 4b. Then, in the hybrid case, the current vector should be in the middle area between these two extreme cases, which is shown in Figure 4c.

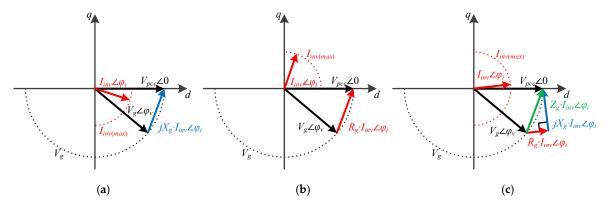


Figure 4. Voltage and current vector diagrams of the grid-connected system with various impedance characteristics of the power grid. (a) Purely inductive impedance; (b) purely resistive impedance; (c) hybrid impedance.

As seen in Figure 4, because the amplitude of the inverter current is invariable, the larger the d-axis current component, the smaller the q-axis current component, and vice versa. Thus, as the output reactive power increases, the output active power decreases. This characteristic is more obvious in a weaker grid, where the amplitude of Z_g is higher.

The output active power of the inverter P_{inv} shown in Figure 2 can be calculated as:

$$P_{inv} = \frac{3}{2} V_{pcc} i_d \tag{14}$$

Thus, according to Equations (13) and (14), the output active power of the inverter (per unit) can be derived as:

$$P_{inv(pu)} = \frac{P_{inv}}{S_N} = \frac{3/2 \cdot V_g \cdot i_d}{3/2 \cdot V_g \cdot I_{inv(max)}} = i_{d(pu)} = \frac{\sqrt{SCR^2 - \frac{1}{4} + \frac{R_g}{2X_g}}}{SCR \cdot \sqrt{1 + \frac{R_g^2}{X_g^2}}}$$
(15)

Moreover, according to Equations (1) and (2), the power loss introduced by the transmission line (per unit) is derived as:

$$P_{loss(pu)} = \frac{P_{loss}}{S_N} = \frac{3/2 \cdot I_{inv(max)}^2 \cdot R_g}{3/2 \cdot V_g \cdot I_{inv(max)}} = \frac{\frac{R_g}{X_g}}{SCR \cdot \sqrt{1 + \frac{R_g^2}{X_g^2}}}$$
(16)

Thus, according to Equations (15) and (16), the transferred active power to the grid (per unit) can be derived as:

$$P_{grid(pu)} = P_{inv(pu)} - P_{loss(pu)} = \frac{\sqrt{SCR^2 - \frac{1}{4}} - \frac{R_g}{2X_g}}{SCR \cdot \sqrt{1 + \frac{R_g^2}{X_g^2}}}$$
(17)

Based on Equations (15) and (17), Figure 5 presents the relationship between the inverter power $P_{inv(pu)}$, grid power $P_{grid(pu)}$, and R_g/X_g ratio with different SCRs at the

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rated PCC voltage. Since the SCR is usually higher than 1 in practice, the situation where SCR is lower than 1 is omitted. It can be seen that a higher SCR leads to higher grid power, $P_{grid(pu)}$. However, a higher R/X ratio causes lower grid power, $P_{grid(pu)}$. Therefore, inductive grids with a high SCR have a high power transfer capability, while resistive grids with a low SCR have a limited power transfer capability.

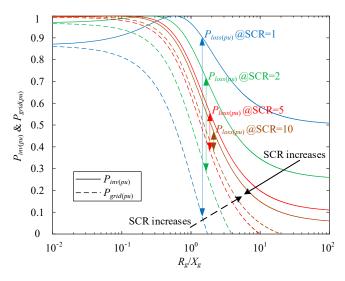


Figure 5. Relationship between inverter power $P_{inv(pu)}$, grid power $P_{grid(pu)}$, and R_g/X_g ratio with different SCRs at the rated PCC voltage.

Moreover, in the resistive grid ($R_g/X_g > 1$) case, the higher the SCR, the lower the output power of the inverter, $P_{inv(pu)}$. It seems counterintuitive. This is because more reactive power has to be supplied to maintain the PCC voltage so that the output active power of the inverter is limited. This indicates that it is uneconomical to use reactive power to compensate the PCC voltage in resistive grids because much of the potential active power capacity is sacrificed. Aiming at this problem, tuning the PCC voltage within a small range can reduce reactive power consumption and increase the power transfer capability in resistive grids, which will be analyzed in the next section.

3. Maximum Power Transfer Capability of Grid-Connected Systems at Varying PCC Voltages

In the previous section, the situation where the PCC voltage equals the rated value was evaluated. A more general situation where the PCC voltage varies within a small range around the rated value will be analyzed in this section.

By substituting Equations (2) and (8) into Equation (4), a standard quadratic equation for the q-axis inverter current i_q can be obtained. Then, the positive solution of the quadratic equation is derived as Equation (18). Because the control law in the voltage PI controller is only suitable for the positive solution, the negative solution does not exist in the actual control system. Hence, it is disregarded here.

$$\begin{cases} i_{q(pu)} = \frac{i_q}{I_{inv(max)}} = \frac{1}{V_{pcc(pu)}\sqrt{R_g^2/X_g^2+1}} \left(\sqrt{\frac{V_{pcc(pu)}^2+1}{2} - \frac{K_1}{4}} \cdot \frac{R_g}{X_g} - \frac{K_2}{2}\right) \\ K_1 = SCR^2 \cdot \left(V_{pcc(pu)}^2 - 1\right)^2 + \frac{1}{SCR^2}, K_2 = SCR \cdot \left(V_{pcc(pu)}^2 - 1\right) + \frac{1}{SCR} \end{cases}$$
(18)

where $V_{pcc(pu)}$ is the per-unit value of the PCC voltage, expressed as " $V_{pcc(pu)} = V_{pcc}/V_g$ "; K_1 and K_2 are two intermediate variables.

If the solution listed in Equation (18) exists, the expression in Equation (19) must be satisfied.

$$\frac{1}{\left|V_{pcc(pu)} + 1\right|} \le SCR \le \frac{1}{\left|V_{pcc(pu)} - 1\right|} \tag{19}$$

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According to Equation (19), when the SCR is equal to 1, the range of $V_{pcc(pu)}$ is [0, 2]. When the SCR is equal to 10, the range of $V_{pcc(pu)}$ is [0.9, 1.1]. Hence, it is noted that the PCC voltage is naturally close to its rated value under strong grid conditions, where reactive power compensation may not be necessary. However, the PCC voltage varies easily under weak grid conditions. Thus, reactive power compensation is necessary to keep the PCC voltage close to its rated value.

When Equation (18) is substituted into Equation (8), the expression of the d-axis inverter current i_d can be derived as:

$$i_{d(pu)} = \frac{i_d}{I_{inv(max)}} = \frac{1}{V_{pcc(pu)}} \sqrt{\frac{V_{pcc(pu)}^2 - 1}{2} + \frac{K_1}{4} + (1 - \frac{K_1}{2} + \sqrt{\frac{V_{pcc(pu)}^2 + 1}{2} - \frac{K_1}{4}} \cdot K_2 \cdot \frac{R_g}{X_g}) \frac{1}{R_g^2 / X_g^2 + 1}}$$
(20)

where the expressions of K_1 and K_2 are shown in Equation (18).

According to Equations (14) and (20), the output active power of the inverter (per unit) can be derived as:

$$P_{inv(pu)} = \frac{P_{inv}}{S_N} = V_{pcc(pu)} i_{d(pu)} = \sqrt{\frac{V_{pcc(pu)}^2 - 1}{2} + \frac{K_1}{4} + (1 - \frac{K_1}{2} + \sqrt{\frac{V_{pcc(pu)}^2 + 1}{2} - \frac{K_1}{4}} \cdot K_2 \cdot \frac{R_g}{X_g}) \frac{1}{R_g^2 / X_g^2 + 1}}$$
(21)

According to Equations (16) and (21), the transferred active power to the grid (per unit) can be derived as:

$$P_{grid(pu)} = \sqrt{\frac{V_{pcc(pu)}^2 - 1}{2} + \frac{K_1}{4} + (1 - \frac{K_1}{2} + \sqrt{\frac{V_{pcc(pu)}^2 + 1}{2} - \frac{K_1}{4}} \cdot K_2 \cdot \frac{R_g}{X_g}) \frac{1}{R_g^2 / X_g^2 + 1}} - \frac{\frac{1}{SCR} \cdot \frac{R_g}{X_g}}{\sqrt{R_g^2 / X_g^2 + 1}}$$
(22)

According to Equations (21) and (22), Figure 6 presents the relationship between inverter power $P_{inv(pu)}$, grid power $P_{grid(pu)}$, and PCC voltage $V_{pcc(pu)}$ with different R_g/X_g ratios and SCRs. Moreover, the points (A_1, A_2, A_3) , (B_1, B_2, B_3) , (C_1, C_2, C_3) , and (D_1, D_2, D_3) in Figure 6 are the maximum value points of $P_{grid(pu)}$.

As shown in Figure 6a,b, when the SCR is low, the grid power $P_{grid(pu)}$ drops significantly as the R/X ratio increases. For example, the maximum value of $P_{grid(pu)}$ decreases from point A_1 to A_2 and A_3 as the R/X ratio increases. However, as presented in Figure 6c,d, when the SCR is high, the maximum value of $P_{grid(pu)}$ can stay at a high level, such as points D_1 , D_2 , and D_3 . Therefore, a larger SCR is beneficial for power transmission.

Comparing the maximum power points (A_1, A_2, A_3) , (B_1, B_2, B_3) , (C_1, C_2, C_3) , and (D_1, D_2, D_3) in Figure 6, the rated PCC voltage in the inductive grid $(R_g/X_g=0.1)$ is appropriate for power transmission. In contrast, a higher PCC voltage than the rated value in the resistive grid $(R_g/X_g=10)$ is beneficial for power transmission. Furthermore, as shown in Figure 6a, the value of $P_{grid(pu)}$ in the resistive grid $(R_g/X_g=10)$ is lower than 0 whatever the PCC voltage is, which means that the resistive weak grid cannot be used for power transmission. Hence, a required minimum SCR should be known in the resistive grid.

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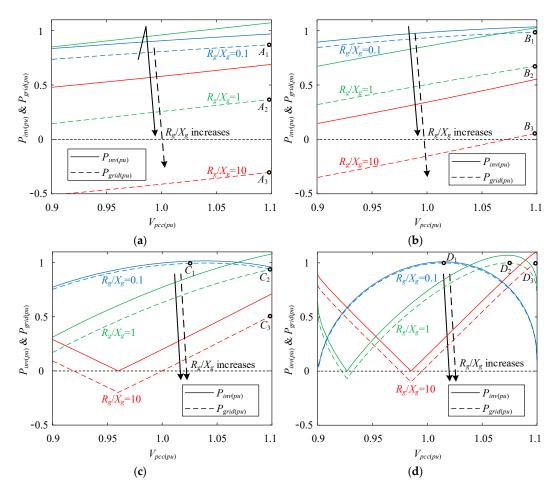


Figure 6. Relationship between inverter power $P_{inv(pu)}$, grid power $P_{grid(pu)}$, and PCC voltage $V_{pcc(pu)}$ with different R_g/X_g ratios and SCRs. (a) SCR = 1; (b) SCR = 2; (c) SCR = 5; (d) SCR = 10.

4. Optimal Parameters for Maximum Power Operation in Inductive and Resistive Grids

Based on the aforementioned analysis, the maximum power transfer capability of the grid-connected system is jointly determined by the SCR and the R/X ratio as well as the PCC voltage. Therefore, the optimal values of these parameters for effective power transmission need to be investigated in a mathematical manner.

According to Equation (17), when the PCC voltage is at the rated value, the partial derivatives of $P_{grid(pu)}$ can be derived as:

$$\frac{\partial P_{grid(pu)}}{\partial \frac{R_g}{X_g}} = -\frac{\frac{1}{2} + \frac{R_g}{X_g} \sqrt{SCR^2 - \frac{1}{4}}}{SCR \cdot \sqrt{\left(1 + \frac{R_g^2}{X_g^2}\right)^3}} < 0$$
 (23)

$$\frac{\partial P_{grid(pu)}}{\partial SCR} = \frac{\frac{1}{2} + \frac{R_g}{X_g} \sqrt{SCR^2 - \frac{1}{4}}}{2 \cdot SCR^2 \cdot \sqrt{1 + \frac{R_g^2}{X_g^2}} \cdot \sqrt{SCR^2 - \frac{1}{4}}} > 0$$
 (24)

It can be seen from Equation (23), the partial derivative from $P_{grid(pu)}$ to the R/X ratio is smaller than 0, which means that as the R/X ratio decreases, $P_{grid(pu)}$ increases. Namely, R/X = 0 is the theoretically optimal value for power transmission. Moreover, it can be seen from Equation (24), the partial derivative from $P_{grid(pu)}$ to the SCR is larger than 0, which means that as the SCR increases, $P_{grid(pu)}$ increases. Namely, SCR = ∞ is the theoretically optimal value for power transmission. Obviously, these two optimal values, in theory,

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cannot be obtained in real applications. Nevertheless, a higher SCR or a lower R/X ratio is beneficial to increase the power transfer capability of the system.

Aside from the SCR and the R/X ratio, the PCC voltage is another key parameter affecting the maximum power transfer capability of the system. As aforementioned, the rated PCC voltage in an inductive grid is appropriate for power transmission, while a higher PCC voltage than the rated value in a resistive grid is beneficial for power transmission. Thus, according to Equation (22), the curves for maximum $P_{grid(pu)}$ with different R_g/X_g ratios, SCRs, and PCC voltages are shown in Figure 7. Figure 7a presents the inductive grid impedance case, where the rated PCC voltage is preferable to be used. Figure 7b shows the resistive grid impedance case, where the power curves at two PCC voltages are compared. Obviously, a higher PCC voltage is better than the rated PCC voltage.

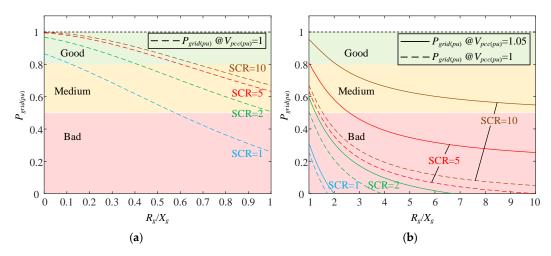


Figure 7. Curves for maximum $P_{grid(pu)}$ with different R_g/X_g ratios, SCRs, and PCC voltages. (a) Inductive grid impedance case; (b) resistive grid impedance case.

Based on the above analysis, $P_{grid(pu)}$ in Equation (22) can be considered a key performance index to quantify the performance of the system at different V_{pcc} , SCRs, and R/X values. Namely, if $P_{grid(pu)}$ is within [0.8, 1], the performance of the system is good. If $P_{grid(pu)}$ is within [0.5, 0.8], the performance is medium. If $P_{grid(pu)}$ is lower than 0.5, the performance of the system is bad. Hence, the suitable V_{pcc} , SCRs, and R/X values can be found according to this definition of performance.

It was reported in [21] that the R/X ratio of the high voltage line is around 0.3, while the R/X ratio of the low voltage line is around 7 in real applications. Thus, as shown in Figure 7a, when the R/X ratio is 0.3, an SCR higher than 2 is required in order to make P_{grid} higher than 0.8 pu (good performance). Moreover, as shown in Figure 7b, when the R/X ratio is 7, an SCR higher than 10 and a PCC voltage higher than 1.05 pu are required in order to make P_{grid} higher than 0.5 pu (medium performance).

In order to apply the above research to practical projects, a case study on wind generation is discussed, as follows. Question: How to increase the penetration level from 20% to 40% for wind generation connected to an inductive grid with $R_g/X_g=0.3$ and SCR = 3? If the penetration level is increased from 20% to 40%, the rated power S_N will be doubled, and the SCR will become 3/2. As shown in Figure 7a, when the R_g/X_g is 0.3, an SCR higher than 2 is preferable. Thus, the grid impedance $|Z_g|$ should be reduced to 3/4. For example, increasing the voltage level can reduce grid impedance. Moreover, since the low inertia in wind generation systems may cause frequency instability issues, grid-forming control techniques on inverters are recommended to support the grid frequency. Moreover, energy storage systems (ESSs) can also be used to smooth the wind energy and realize an uninterrupted supply of power.

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5. Simulation Verification

In order to verify the effectiveness of the theoretical analysis, a 30 kW grid-connected inverter simulation model with classical vector current control was established in Matlab/Simulink. The control method is shown in Figure 8. To avoid the influence of high-frequency harmonics, the average model of the inverter was used. Firstly, an inductive grid case ($R_g/X_g=0.3$) with low SCRs was carried out. Then, a resistive grid case ($R_g/X_g=7$) with SCR = 10 was performed. The key parameters of the grid-connected inverter are listed in Table 1. Moreover, the parameters of grid impedance in the inductive grid and resistive grid cases are summarized in Table 2.

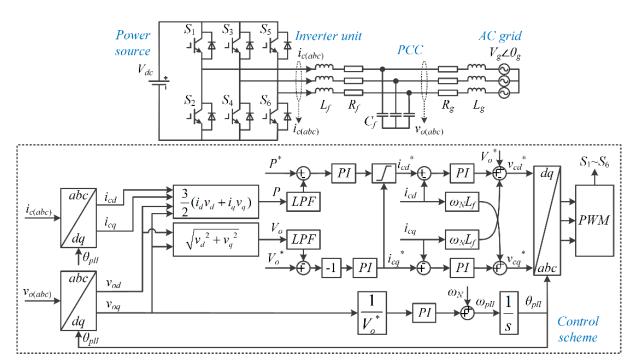


Figure 8. Classical grid-following vector current control method.

Table 1. Parameters of grid-connected systems.

	Parameters	Values
V_g	Grid phase voltage (peak value)	311 V
f_g	Grid frequency	50 Hz
S_N	Rated apparent power of inverter	30 kVA
I _{max}	Maximum current of inverter (peak value)	64.3 A
$\overline{V_{dc}}$	DC-link voltage	700 V
L_f	Output filter inductor	5 mH
C_f	Output filter capacitor	5 μF

Table 2. Parameters of grid impedances.

Parameters	Values (Inductive Case)	Values (Resistive Case)
R/X ratio of grid impedance	0.3	7
Short circuit ratio	1/2	10
Grid inductor	14.7 mH/7.3 mH	0.22 mH
Grid resistor	$1.38 \Omega/0.69 \Omega$	0.48 Ω
	R/X ratio of grid impedance Short circuit ratio Grid inductor	Parameters (Inductive Case) R/X ratio of grid impedance 0.3 Short circuit ratio 1/2 Grid inductor 14.7 mH/7.3 mH

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The simulation results of the inductive grid case are shown in Figure 9, where the power reference P_{ref} , the output active power of inverter P_{inv} , and the transferred active power to the grid P_{grid} are presented, respectively. Moreover, I_{inv} is the amplitude of the inverter current, and i_d and i_q are the d-axis and q-axis components of the inverter current. It can be seen that as the power reference increases, the current amplitude I_{inv} increases. When I_{inv} reaches 1 pu, i_d is limited; thus, P_{inv} is also limited. In the steady state, the maximum value of P_{grid} represents the maximum power transfer capability of the grid-connected inverter. As shown in Figure 9a, when the SCR is equal to 1, the maximum value of P_{grid} is around 0.70 pu. Moreover, as shown in Figure 9b, when the SCR is equal to 2, the maximum value of P_{grid} is around 0.85 pu. These simulation results agree well with the maximum power operating points for $R_g/X_g = 0.3$, as shown in Figure 7a.

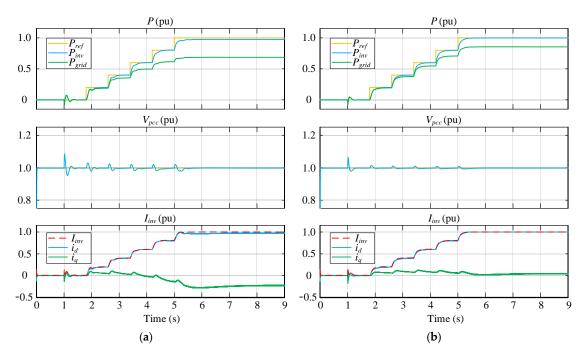


Figure 9. Simulation results of the inductive grid case with $R_g/X_g=0.3$ and low SCRs. (a) SCR = 1; (b) SCR = 2.

The simulation results of the resistive grid case are shown in Figure 10, focusing on the power reference P_{ref} , the output active power of the inverter P_{inv} , and the transferred active power to the grid P_{grid} . Figure 10 shows that as the power reference increases, the current amplitude I_{inv} increases. When I_{inv} reaches 1 pu, i_d is limited and P_{inv} is also limited. In Figure 10a, the PCC voltage is controlled as 1 pu. It can be seen that i_q is quite large but i_d is small, so that the output active power of the inverter P_{inv} is limited (as low as 0.2 pu), and the grid power P_{grid} is only 0.1 pu. In contrast, as shown in Figure 10b, when the PCC voltage is controlled as 1.05 pu, i_d is not so small. Thus, the output active power of the inverter P_{inv} is 0.7 pu and the grid power P_{grid} is only 0.6 pu. These simulation results are in accordance with the maximum power operating points for $R_g/X_g = 7$ and SCR = 10, as shown in Figure 7b.

It can be seen in Figures 9 and 10 that there is a steady-state error on the power P_{inv} when the current reaches the limiting value. In fact, this steady-state error is equal to $(1-P_{inv}(pu))$. According to the expression of $P_{inv}(pu)$ in Equation (21), the steady-state error can be calculated accurately. The power steady-state errors in different cases are compared in Table 3. It can be seen that for the inductive grid case, the rated PCC voltage has a relatively small power steady-state error. As the R/X ratio increases, a higher PCC voltage has a smaller power steady-state error, which can also be observed from Figure 6d. Moreover, when $V_{pcc}(pu)$ is equal to 1, the impact of the R/X ratio and the SCR on $P_{inv}(pu)$ are shown in Figure 5. It can be seen in Figure 5 that there is a maximum power point on

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each constant SCR curve. When R/X ratios are smaller than the R/X ratios at the maximum power points, $P_{inv(pu)}$ increases as SCR increases. However, when R/X ratios are larger than the R/X ratios at the maximum power points, $P_{inv(pu)}$ decreases as SCR increases. Even so, the R/X ratio at each maximum power point is not the optimal one because the optimal R/X ratio should be determined by $P_{grid(pu)}$.

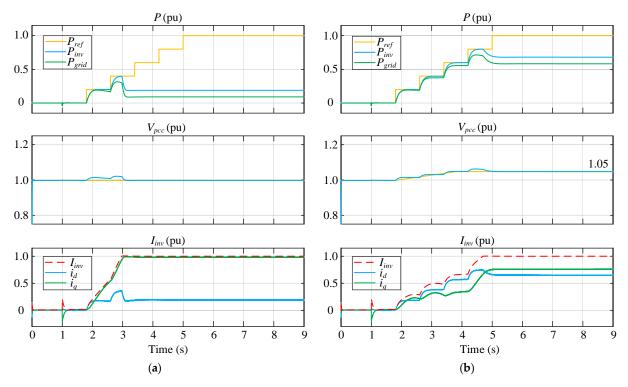


Figure 10. Simulation results of the resistive grid case with $R_g/X_g = 7$ and SCR = 10. (a) $V_{pcc} = 1$ pu; (b) $V_{pcc} = 1.05$ pu.

Table 3. Power steady-state error comparison in different cases.

Steady-State	Error on P_{inv}	$V_{pcc} = 1 \text{ pu}$	V_{pcc} = 1.05 pu	V_{pcc} = 1.1 pu
	SCR = 1	2.68%	0	0
$R_g/X_g = 0.3$	SCR = 2	0.08%	0	0
	SCR = 5	1.82%	0	0
	SCR = 10	2.90%	0	68.39%
$R_g/X_g = 1$	SCR = 5	22.57%	4.97%	0
	SCR = 10	25.84%	0	22.22%
$R_g/X_g = 7$	SCR = 5	76.03%	50.76%	25.33%
	SCR = 10	80.93%	31.78%	0

6. Conclusions

This paper investigates the maximum power transfer capability of grid-connected inverters, which is jointly determined by the SCR, the R/X ratio of grid impedance, and the PCC voltage amplitude. The maximum power curves in the inductive grid and resistive grid cases, with different SCRs and PCC voltages, are illustrated and benchmarked. It is revealed that increasing the SCR or reducing the R/X ratio of grid impedance can increase the maximum power transfer capability of the system. In order to have higher power transfer capability, SCR > 2 and R/X < 1 are recommended to be used. Moreover, under resistive grid conditions, a higher PCC voltage than the rated value is beneficial for power transmission. Based on this research, a suitable SCR can be designed for high-

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penetration renewable generation systems in practice. Finally, simulation results verified the effectiveness of the theoretical analysis.

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