Identification Design for Dynamic Voltage Restorer to Mitigate Voltage Sag Based on the Elliptical Transformation

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Abstract—In this paper, a new identification tool for dynamic voltage restorer (DVR) is proposed to achieve flexible active and reactive power dispatch during voltage sags. The presented tool entirely relies on the theoretical analysis of the elliptical transformation, and identification marks are determined for different power injections by using one set of digital codes. Besides, two parameters are presented in the accurate mathematical description of the current references, which guarantee continuous power delivery by selecting the proper values. The chief advantages include the smooth transition state during changes in different power deliveries as well as the elimination of active and reactive power oscillations. Then, the characteristics of the identification tool corresponding to the different power dispatch are analyzed to reveal the feasibility of the given current references. Finally, experimental tests utilizing a laboratory prototype are used to verify the flexibility of the proposed control schemes.

Index Terms—Voltage sags, elliptical transformation, identification tool, power dispatch, dynamic voltage restorer, power quality

I. INTRODUCTION

The widespread use of renewable energy sources has a significant impact on the stability of the distribution system, and puts forward higher requirements for improving power quality during voltage sags [1], [2]. In addition, the industrial production has always acted in compliance with the strict international standards [3], [4], or different national grid codes [5], [6]. As a result, a voltage sag study is essential to predict the effect of the event on sensitive loads and industrial processes. In other words, timely mitigation of voltage sag is understood as the most attractive solution to improve power quality in the distribution system. The preservation of the rated magnitude and the removal of the phase jump should be identified as the criteria when the improvement of power quality is adopted in [7]. At the same time, the introduction of custom power instruments, particularly the use of dynamic voltage restorer (DVR) at the realm of disturbance suppression, has dramatically improved the load power quality to satisfy the industrial production activities. It is also a very economical solution of eliminating voltage sags [8], [9]. Fig.1 shows the diagram of the DVR connected to the sensitive load through the secondary winding of the transformer. In this configuration, the three-phase converter is connected to the primary of the transformer via an LC filter. The required energy can be taken from an energy storage device that is connected to the dc link, which balances the power flow from the DVR to the ac source.

In recent studies, the development of compensation strategy for DVR based on the instantaneous reactive power theory [10]–[12] is applied to improve the relevant power quality indicators significantly. An attractive solution, named pre-phase compensation [13], [14], has been proposed where the different voltage sags can be eliminated at the cost of a large number of active power requirements. Other solutions, including in-phase strategy and energy-optimized strategy, have been presented in [15], [16], but the main drawback with these approaches is a failure to eliminate phase jump.

Concerning the control strategies for the mentioned compensation methods, the positive-negative sequence component (PNSC) is an excellent base for the flexible power quality regulation to enhance the DVR’s behavior [17]–[19]. Similarly, different control objectives have been presented when alleviating the symptoms of current harmonics [20], [21], dc-
In addition, the power oscillation significantly affects the continuity of the power supply from DVR with exceeding the maximum allowable power capability. Furthermore, advanced controllers for PNSC presented in [28]–[34] can achieve an insightful control objective related to the removal of power oscillations. In [28], the controller only provides active power delivery without the corresponding oscillation term while maintaining the injected voltage safely controlled to a predefined value. In [29], the injection of the peak current can be achieved by delivering only reactive power, and the oscillation elimination of reactive power is a priority objective. Studies [30], [31] deal with the oscillation elimination of active power focused on dc-link voltage optimization, active power exchange maximization, and a combination of the two. Meanwhile, the control strategy in [32] is carried out in order to achieve the oscillation eliminations of active and reactive power simultaneously providing priority to active power delivery to maintain the maximum current injection. Nevertheless, the reference generators of the controller [32] may exceed the current capability of the converter and then lead to the disconnection of the converter due to overcurrent. On the contrary, the control strategy in [33] can restore the dropped voltage magnitudes to the rated values confined within the maximum voltage limit, guaranteeing oscillation elimination of power terms. Specifically, study [34] is conceived to completely avoid power oscillations considering certain specific techniques (e.g. power-characteristic-oriented or voltage-support-oriented) when injecting active and reactive power through sophisticated reference generators. As a drawback, it is unable to maximize power delivery capability. However, control strategies should be optimized according to the load requirements, taking into account not only the maximum power capability of DVR but also the gradual transition process from one power injection level to another. In this sense, the interesting methods based on the elliptical transformation have been presented to maximize the volt-ampere sizing in [35], [36], but they are only the preliminary studies. Therefore, the simple and effective mechanism satisfying the aforementioned gradual transition process needs further investigation.

In this paper, the mentioned elliptical transformation has been used to build a new identification tool that can show the change in the joining regions of different power injection levels. This new property can reflect realistically the dynamic response of DVR by an adjustable active and reactive power dispatch. In detail, this dynamic process is defined as a triplet of the digital codes. Three digits form an identification tool, where the first digit denotes the flexible selection of individual power control strategy, and the last two digits denote the criteria to continuous power delivery based on two control parameters. The values of two parameters change continuously in the fixed numerical ranges and describe the different applications embedded in the elliptical trajectory. In other words, this advantage can prioritize between active and reactive power regulation according to the first digital code, and an easy mechanism of tuning the last two digital codes permits to different operation modes. Thence, there is the unrestricted possibility to reflect the power delivery trend of DVR response during voltage sags. It allows a gradual transition from one power injection level to another with the continuous regulation of two parameters. The properties of the proposed identification tool obtained by the set of three digits can represent the flexible power dispatch.

The rest of the paper is organized as follows. A brief review of the equivalent concept of elliptical trajectory is presented in Section II. In addition, the chosen voltage support scheme and the algorithm of the proposed strategy can also be provided. Mathematical analysis and all necessary vector relationships are presented to demonstrate the strategy for the individual active and reactive power injections in Section III. Section IV verifies the feasibility of the proposed method through selected experimental results. Finally, Section V presents the conclusions of this paper.

II. SYSTEM DESCRIPTION AND MODELING
ELLIPTICAL TRANSFORMATION

In order to facilitate all subsequent analysis, this section gives a brief description of the elliptical transformation. Note that there is no consideration for harmonic distortion under voltage sags in this paper.

A. Quantitative Analysis of Elliptical Transformation

Fig.2 shows a typical vector diagram for the elliptical transformation in this paper, as also discussed in [36]. The magnitudes of load voltage and current (\(\vec{V}_L\) and \(\vec{I}_L\)) are constant at rated percentages during all the operating conditions. Based on this principle, the phase difference between the load voltage \(\vec{V}_L\) and the instantaneous voltage source \(\vec{V}_{sag}\) will happen once a voltage sag occurs. As a result, the injected voltage \(\vec{V}_{inj}\) exists a phase shift \(\beta\) with respect to the current reference phasor \(\vec{I}_L\). The provision of voltage support will be essential, and it has become a prime target to meet sag-ride through. For better visualization, the graphical representation of the compensation voltage vectors is shown in Fig.3, which is able to describe the individual active and reactive power control. At first, draw one line \(l_p\) perpendicular to the horizontal axis, and the given line passes through the top locus of the voltage vector (\(\vec{V}_L\)) so that the injected active power can remain the specific mapping. Thus, the horizontal injected power \(P_{inj}\) is always fixed, and it is aligned with the current vector. There is a new relationship that the top locus of the injected power vector is still located at a particular point of a line segment, which is also a portion of the trajectory (line \(l_p\)). At the same time, this injected power is the sum of a constant amount of \(P_{inj}\) and arbitrary values of \(Q_{inj}\). Thus, the drawn line \(l_p\) can be defined as the equi-active power line. A typical perpendicular injected power component associated with the constant length of \(P_{inj}\) holds the same direction of vertical current vector \(\vec{I}_p\) and is also proportional to the arbitrary values \(Q_{inj}\). As shown in Fig.3, the vector \(\vec{V}_c\) tracing the elliptical trajectory, which begins with point D to any point of the equi-active line \(l_p\) as an example at point E, represents one specific compensated voltage. It should be noted that the
The total amount of power injection is the combination of constant $P_{inj}$ and arbitrary values of $Q_{inj}$.

Again, construct a line $l_q$ parallel to the horizontal axis but at a specific mapping distance equal to the power quantity $Q_{inj}$. Still, the drawn line $l_q$ can be designed as the equi-reactive power line, as depicted in Fig.4. This line $l_q$ can also be denoted the terminal point locus of injected voltage, and it is the tradeoff between arbitrary amount $P_{inj}$ and constant values $Q_{inj}$. An adjustable horizontal injected power component associated with the constant value of $Q_{inj}$ maintains the same direction of the current reference, and it is also proportional to the arbitrary values $P_{inj}$. As depicted in Fig.4, the vector $\vec{V}_e$, which also begins with point D to any point of the equi-reactive line $l_q$, for example, at point R, describes the voltage that should be compensated. It should also be seen that the maximum value of output power is the sum of a constant amount of $Q_{inj}$ and an arbitrary amount of $P_{inj}$.

In sum, by superimposing the vector diagram of the equi-reactive power line $l_q$ onto the equi-active power line $l_p$, the terminal point locus of the injected voltage can depict particular system condition that satisfies the elliptical trajectory. On the one hand, the arbitrary injected power can be obtained by utilizing the individual controllable active and reactive power components. On the other hand, the strategies based on the power dispatch are realized for two situations as follows:

1) The controllable reactive power: based on the horizontal constant active power, one orthogonal power generator is required to increase the output voltage dramatically. This perpendicular power vector is the key to the control algorithm since the instantaneous injected reactive power can be regulated by selecting an adjustable scalar parameter.

2) The controllable active power: based on a similar analysis, one injected active power generator that satisfies a constant reactive power component can be achieved by choosing a proper scalar parameter. Then, the injected voltage is determined with a combination of both transferred active and reactive powers.

B. New Forms of Adjustable Current Reference Generator

The main purpose of this subsection is to describe the current reference generators by utilizing the elliptical transformation. Since the three double-winding transformers with a neutral of the secondary connected to ungrounded are used to interface the load to the grid in this paper, the zero sequence component is not present. To understand the nature of the compensation strategy, the mathematical models in the stationary reference frame (SRF) can be described (\(\vec{v}_\alpha = \vec{v}_\alpha^+ + \vec{v}_\alpha^-\) and \(\vec{v}_\beta = \vec{v}_\beta^+ + \vec{v}_\beta^-\)) as a function of times.

\[
\begin{align*}
\vec{v}_\alpha &= V^+ \sin(\omega t + \varphi_+) + V^- \sin(\omega t - \varphi_-) \\
\vec{v}_\beta &= -V^+ \cos(\omega t + \varphi_+) + V^- \cos(\omega t - \varphi_-)
\end{align*}
\]

(1)

where \(\vec{v}_\alpha^+, \vec{v}_\alpha^-, \vec{v}_\beta^+, \vec{v}_\beta^-\) are the positive and negative voltage sequences, respectively. \(V^+\) and \(V^-\) are their magnitudes. The pair \(\varphi_+\) and \(\varphi_-\) are the initial phase angles of positive and negative sequence. Then, the computation of output power can be given

\[
p = p^+ + p^- \\
q = q^+ + q^-
\]

(2)

Based on [36], one set of existing current references is defined

\[
\begin{align*}
\vec{i}_p^+ &= k^+(k_1 p^+ - k_2 q^+) \\
\vec{i}_q^+ &= k^+(k_3 p^+ - k_4 q^+) \\
\vec{i}_p^- &= k^-(k_5 p^- - k_6 q^-) \\
\vec{i}_q^- &= k^-(k_7 p^- - k_8 q^-)
\end{align*}
\]

(3)
Obviously, the defined four parameters in (3) can be rewritten as follows:

\[
\begin{align*}
\hat{k}_1 &= -(V^+)^2 - \frac{V^+ V^+ \cos(\theta) - V^+ V^- \sin(\theta)}{\hat{S}_{2c}} \\
\hat{k}_2 &= -V^+ V^- \cos(\theta) - V^+ V^- \sin(\theta) \\
\hat{k}_3 &= -V^+ V^- \cos(\theta) + V^+ V^- \sin(\theta) \\
\hat{k}_4 &= -(V^-)^2 - \frac{V^+ V^- \cos(\theta) + V^+ V^- \sin(\theta)}{\hat{S}_{2s}}
\end{align*}
\]

(5)

where \( \theta = 2\omega t + \varphi_+ - \varphi_- \). The \( \hat{S}_{2c} \) and \( \hat{S}_{2s} \) denote the forged power introduced by positive and negative components, respectively. It can be found that the two forged power are orthogonal oscillating terms at twice the fundamental frequency. On the other hand, these oscillating terms also cause power losses and operating current rise, and therefore, this is the main reason why forged power terms \( \hat{S}_{2c} \) and \( \hat{S}_{2s} \) must disappear. As the first approximation, (5) should be expressed without forged power terms as

\[
\begin{align*}
\hat{k}_1 &= -(V^+)^2 \quad k_2 = 0 \quad k_3 = 0 \quad k_4 = -(V^-)^2
\end{align*}
\]

(6)

Again, the defined four parameters in (4) will be rewritten as follows:

\[
\begin{align*}
\hat{k}_5 &= -(V^-)^2 - \frac{V^+ V^- \cos(\theta) + V^+ V^- \sin(\theta)}{\hat{S}_{2c}} \\
\hat{k}_6 &= -V^+ V^- \cos(\theta) + V^+ V^- \sin(\theta) \\
\hat{k}_7 &= -V^+ V^- \cos(\theta) - V^+ V^- \sin(\theta) \\
\hat{k}_8 &= -(V^-)^2 - \frac{V^+ V^- \cos(\theta) - V^+ V^- \sin(\theta)}{\hat{S}_{2s}}
\end{align*}
\]

(7)

Obviously similar to (6), (7) should also be expressed without forged power terms as

\[
\begin{align*}
\hat{k}_5 &= -(V^-)^2 \quad k_6 = 0 \quad k_7 = 0 \quad k_8 = -(V^-)^2
\end{align*}
\]

(8)

Inserting (6) and (8) into (3)-(4), a new set of reference generators can be also defined as follows:

\[
\begin{align*}
\tilde{i}_p^+ &= \hat{\alpha} + \hat{\beta} = \frac{(k_p p - q)(\hat{\alpha}^2 + \hat{\beta}^2)}{(V^+)^2} + \frac{(V^-)^2}{(V^-)^2} \\
\tilde{i}_q^+ &= \hat{\alpha} + \hat{\beta} = \frac{(k_p p - q)(\hat{\alpha}^2 + \hat{\beta}^2)}{(V^+)^2} + \frac{(V^-)^2}{(V^-)^2} \\
\tilde{i}_p^- &= \hat{\alpha} + \hat{\beta} = \frac{-(p + k_p q)(\hat{\alpha}^2 + \hat{\beta}^2)}{(V^+)^2} + \frac{(V^-)^2}{(V^-)^2} \\
\tilde{i}_q^- &= \hat{\alpha} + \hat{\beta} = \frac{-(p + k_p q)(\hat{\alpha}^2 + \hat{\beta}^2)}{(V^+)^2} + \frac{(V^-)^2}{(V^-)^2}
\end{align*}
\]

(9)

(10)

(11)

(12)

where \( k_p \) and \( k_q \) are the control parameters, respectively. These parameters can take any values from -1 to 1, and also give rise to multiple injection strategies. Next, the selection of control parameters and the complete mathematical analysis will be presented in Section III.

III. THEORETICAL APPROACH TO THE CONTROL STRATEGY

The best way to accomplish the proposed reference generators is a smart selection of \( k_p \) and \( k_q \). Obviously, there are infinite combinations with these double parameters (\( k_p \) and \( k_q \)) in (9)-(12).

A. Targets for the Positive and Negative Sequence Currents

To distinguish clearly between the symbol \( k_p \) and \( k_q \), the parameter utilized to control the active and reactive power separately in the following is defined as \( k_{pq} \). The reference injected power \( p^* \) and \( q^* \) can be displayed in the pq space vector plane. In such a plane, the injected active and reactive powers coincide with the p axis [real axis (Re)] and q axis [imaginary axis (Im)], respectively. Hence, the reference injected power, named apparent power \( s^* \), can be derived by adding (2)

\[
s^* = k_{pq} (p^* m + j q^* n^*)
\]

(13)

where \( j = \sqrt{-1} \), \( m = a, b, \) or c. Therefore, there are infinite combinations with the changeable parameter of \( k_{pq} \) in (13). It can also be seen that the linear controllability benefiting from previous individual power control schemes can not exist. Therefore, two joint strategies are proposed to simplify (13) by utilizing the reference active and reactive powers.

1) Joint strategy with the positive-sequence control

By setting \( k_p = k_q = k_{pq} \), reference apparent power is simplified and rewritten as follows:

\[
s^* = (k_{pq} p^* m + j q^* n^*)
\]

(14)

As shown in Fig.5a, when \( k_p \) changes from 0 to 1, the length of apparent power vector changes within the first quadrant of a Cartesian coordinate. The apparent power trajectory is directed to the sliding line (denoted by the parameter \( k_p \)). It slides along the sliding line toward the origin, which determines the boundaries of the existing regions. On the other hand, apparent power also varies with the change if \(-1 \leq k_p \leq 0 \), and it is entered the second quadrant of a Cartesian coordinate. The parameter \( k_p \) divides the apparent power into two regions. The sliding action occurs on the areas between the blue line and the p axis.

2) Joint strategy with the negative-sequence control

By setting \( k_p = -k_q = k_{pq} \), reference apparent power is, again, rewritten as follows

\[
s^* = (p^* m + j k_{pq} q^* n^*)
\]

(15)

Illustrative plots are drawn in Fig.5b. It can be seen from (15) that this joint strategy also splits the apparent power into two areas. The existing region is determined by two red lines and the p axis. To observe the controllability, a simple analysis reveals that merging strategies 1) and 2) can be put together, and the proposed reference generators are also normalized as follows:

\[
\begin{align*}
\tilde{i}_{\alpha}^{+*} &= \hat{i}_{\alpha}(p) + \hat{i}_{\alpha}(q) = \frac{(k_{pq} p^* - q^*) (\hat{\alpha}^2 + \hat{\beta}^2)}{(V^+)^2} + \frac{(V^-)^2}{(V^-)^2} \\
\tilde{i}_{\alpha}^{-*} &= \hat{i}_{\alpha}(p) + \hat{i}_{\alpha}(q) = \frac{-(p^* + k_{pq} q^*) (\hat{\alpha}^2 + \hat{\beta}^2)}{(V^+)^2} + \frac{(V^-)^2}{(V^-)^2} \\
\tilde{i}_{\beta}^{+*} &= \hat{i}_{\beta}(p) + \hat{i}_{\beta}(q) = \frac{(k_{pq} p^* - q^*) (\hat{\alpha}^2 + \hat{\beta}^2)}{(V^+)^2} + \frac{(V^-)^2}{(V^-)^2}
\end{align*}
\]

(16)

(17)

(18)
The different active and reactive power dispatches can be achieved by selecting $k_{pq}$ ($k_p$ or $k_q$) inside the range of $-1 < k_{pq} < 1$. From (16)-(19), the output currents depend on the control parameter, voltage characteristics, and the references active and reactive powers. For instance, the resulting p-component current can be regulated by $k_{pq}$, and the graphical diagram is plotted under the given phase angle $\phi = \varphi_+ - \varphi_-$ (for example, $30^\circ$). $I_p$ current trajectories shown in Fig.6a are obtained by setting $k_{pq}$ from 0 to 0.5, and the results are also demonstrated in Fig.6b from 0.5 to 1. As shown in Fig.7, $I_p$ current trajectories can be obtained when $k_{pq}$ is adjusted from -1 to 0. It can also be seen that the length of the p-component current reference can decrease to the minimum value when $k_{pq}$ moves towards -0.5.

B. Modeling and Analysis of Identification Design

The main aspects of the two joint strategies are tabulated in Table I. Strategy 1) can only describe one changeable requirement of the active power, whereas strategy 2) allows more flexible controllability of the reactive power. In summary, the adaptive controllability of individual power control is preserved in the presented joint approaches. It enables the DVR system to be optimized under voltage sags and makes it flexible to satisfy the load requirements. During voltage sags, the apparent power rotates around the geometric center (i.e., point 0 in Fig.5) depending on which the adjustable parameters $k_p$ or $k_q$ have been chosen. The main axis occupies a leading
position compared to the abscissa axis. This angle is used as the mark that identifies the compensation strategies. Hence, the representative variables of the terminal point locus have been codified. This digital code indicated in the last two columns of Table I allows a fast procedure to identify the type of chosen parameter. The first digit represents the orientation state based on the horizontal axis (joint strategy with active power control = '1'; joint strategy with reactive power control = '0'). The second and third digits are associated with the presence of compensation strategies ($k_p = k_q = k_{pq} \in [0, 1] = '00'$; $k_p = k_q = k_{pq} \in [-1, 0] = '11'$; $k_p = -k_q = k_{pq} \in [0, 1] = '01'$; $k_p = -k_q = k_{pq} \in [-1, 0] = '10'$).

Considering the distribution areas of the parameter ($k_{pq}$), the light blue triangles as depicted in Fig.8a, corresponding to the joint strategy with active power control, describe the portion of $[0, 1]$, in which this existing region is controlled with the code selection of '00'. However, the dark counterpart represents the situation of $[-1, 0]$, in which the proposed region is controlled with the code selection of '11'. At the same time, the representative variables with reactive power control have also been codified similarly in Fig.8b. The light blue triangles provide information in which the given region can be guaranteed using code '01' if $k_p = -k_q = k_{pq}$ is set to $[0, 1]$. Also, it can be observed that the dark blue triangles can be codified by utilizing '10' when $k_p = -k_q = k_{pq}$ is regulated within the range of $[-1, 0]$. Therefore, the flexible identification tool created by the digit codes is obtained by selecting two parameters ($k_p$ and $k_q$).

As Fig.9a shows, the contour color map is presented within the first quadrant of the p-q axis system, where the more affected areas are marked between the dotted line in blue and the p axis, and the areas which are subject to the reactive power control are marked between the red line and the reference abscissa. The blue line and the red line denote the maximum and minimum boundaries of the two control parameters, respectively. In this figure, the smaller the parameter $k_{pq}$, the larger the controllable reactive power. The given variable Q (or -Q) denotes the controllable reactive power which is decided by the parameter $k_{pq}$ inside the ranges from -1 to 0. At the same time, the adjustable active power gradually decreases as the value of the parameter $k_p$ decreases. In Fig.9a, three parameters $k_{p1}$, $k_{p2}$ and $k_{p3}$ denote the indices of the flexible ranges which are less than 1, respectively. The horizontal solid line in green represents the adjustable active power. In this way, the three green solid dots in the p-axis represent the main characteristic of the adjustable active power. Their locations determine the actual amount of active power. In addition, the vertical solid line in green represents the reactive power decided by the parameter $k_q$.

To account for variation in the power requirements during voltage sags, the knee points of the adjustable active power are randomly located by varying p-axis values according to preset parameter distributions (e.g., $k_{p1}$, $k_{p2}$ and $k_{p3}$). The number of knee points corresponding to preset parameter distributions is generated within the value range of the parameter $k_p$.

In reality, these knee points accurately describe the gradual transition from one adjustable active power level to another. The joint regions including two neighboring active power ranges can be easily identified. Also, these preset parameter distributions approximate the adjustable trend of the active power dispatch embedded in the existing control strategy. In a specific application, one single knee point can be selected according to an actual control strategy if the relationship of $k_p = -k_q = k_{pq}$ is satisfied. In this case, the flexible power dispatch with the controllable reactive power and the adjustable active power can be decided by using the digital codes of '001'.

Compared to Fig.9a, it can be seen from Fig.9b that a crisp green line at the joint region including two neighboring active power ranges is obtained in this case once the
corresponding parameter distributions are selected. Given the flexible selection of the knee points, two control parameters $k_p$ and $k_q$ can be adjusted according to specific cases in practical applications. In Fig.9b, one single knee point can also be chosen according to an actual control strategy if the relationship of $k_p = -k_q = k_{pq} \in [-1, 0]$ is satisfied. Then, the flexible power dispatch with the controllable reactive power and the adjustable active power can be decided by using the digital codes of '010'.

Also, the same reasoning holds for another strategy known as the flexible power dispatch with the controllable active power and the adjustable reactive power. The whole digital codes are recorded as '100' once the condition that the $k_p = k_q$ satisfies the rule of $k_{pq} \in [0, 1]$. Then, the corresponding power dispatch can also be designed similar to Fig.9a-Fig.9b.

### C. Proposed Control Scheme

Also, further discussion to illustrate the selection of the control parameters is required. Fig.10 depicts the simplified diagram of the control proposal. Then, it is clear evidence that the reference injected voltages can be increased to a safe predefined value. In the first three blocks, the voltage at the point of common coupling (PCC) is measured and computed based on the elliptical trajectory. Then, the next step is responsible for estimating the voltage vectors using a sequence extractor. The core of the compensation algorithm is the Mux block, and two reference blocks can calculate the new current references using the offline selection of $k_{pq}$ (or $k_p, k_q$). Next, the current loop in the last block is proposed to reduce the error in a steady state. Afterwards, the reference reactive power can also be approximately obtained by multiplying current reference by positive voltage, i.e. $q^* = I_q^* (\bar{v}_a^2 + (\bar{v}_b^2)^2)^{0.5}$. At the same time, the reference active power satisfies the condition of $p^* = P_{dc}$, as shown in Fig.11.

Different types of voltage sag can be programmed: (1) before 0.1s, PCC voltages are steady-state condition; (2) at time $t = 0.1$s, a voltage sag of 0.5 p.u. with a phase jump $\delta$ of $+25^\circ$ occurs (Type A sag [37]). Afterwards, from $t = 0.1$s to 0.4s, the proposed active and reactive power dispatches start by means of (16)-(19). Finally, the control algorithm is disabled when the voltage sags are clear at time $t = 0.4$s. Fig.12 shows this representative case of voltage sag.

The first way, named as Case A, is designed for the mentioned voltage condition. Also, the same reasoning, again, holds for another scheme known as Case B and Case C. In particular, the unique requirements of this strategy for different applications can be shown in the first two columns of Table II. At the same time, the horizontal scale of all figures is marked as the 40 ms/div, which is utilized to display the time range in each experimental result.
The injected voltage curves are shown in Fig.14b. The voltage sag magnitude and the load voltage magnitude are also shown in Fig.14c. The dc-link voltage is shown in Fig. 14d. It can be seen that the control scheme with the controllable active power and constant reactive power can be implemented by selecting two parameters in Case A. Thus, the first digit of the identification tool is ’1’. In addition, the last two digits of the identification tool satisfy the digital codes of ’00’ since the two parameters perform the rule of $k_p = k_q = k_{pq} \in [0, 1]$ inside the time range from 0.1 s to 0.2 s. Then, this proposed identification marks can decide to the flexible power dispatch with the controllable active power and constant reactive power by using the digital codes of ’100’.

Dynamic waveforms are shown in Fig.15, in comparison with the results depicted in Fig.14. Note that the measured reactive power is increased from 0 to a maximum value of 300Var. Then, this value is reduced to 200Var, and the final amount of the measured value is equal to 90Var shown at the foot curve of Fig.15a when the control parameter is continuously shifted ($k_q = 0.9 \rightarrow 0.6 \rightarrow 0.3$). The measured active power is increased from 0 to a rough value of 185W as depicted at the peak curve in Fig.15a, where the control parameter is $k_p = 0.6$. The load voltage in Fig.15b can be restored to the nominal value with the constant active power injection and adjustable value of the reactive power injection. The first digit of the identification tool is marked as ‘0’ when the two parameters are chosen in Case B. The last two numbers of the identification tool are given as ‘10’ since the Case B within the time range between 0.2 s and 0.3 s satisfies the rule of $k_p = -k_q = k_{pq} \in [-1, 0]$. As a result, one set of digital codes can be noted as ‘010’ in order to achieve the presented control scheme.

Fig.16 depicts the experimental results of the proposed Case C. It is interesting to note that the maximum value of the measured active power is 250W, then this value is decreased to 190W, and the final amount of this active power is equal to 90W, while the measured value of the reactive power is almost 190Var, as displayed in Fig.16a. The load voltages are continuously shifted ($k_p = 0.5 \rightarrow 0.7 \rightarrow 0.9$).

**IV. EXPERIMENTAL ANALYSIS**

This section validates the theoretical contributions of this paper by experimental results. A dSPACE DS1202 hardware has been utilized as the control platform. The sag source has been emulated by using a Chroma programmable ac source 61611. A Chroma programmable ac electronic load 63804 is served as the three-phase sensitive load, and one Danfoss FC 302 converters are used as a three-phase IGBT bridge. The details of the power configuration are shown in Fig.13. Table III provides the main parameters of the experimental test setup.

**A. Tests of the Joint Strategies During Voltage Sag**

A set of experiments is conducted to evaluate the proposed reference generators. Observe that the measured reactive power is nearly 150Var shown in Fig.14a, which tracks the parameter $k_q = 0.5$. However, the measured active power is almost 165W during the period $t = 0.1s$ to 0.2s. Then, this value is increased up to 210W, and the final amount of the measured value is equal to 240W, given in Fig.14a, because the control parameter is continuously shifted ($k_p = 0.5 \rightarrow 0.7 \rightarrow 0.9$).

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**TABLE II: The Measured Active Power (Watts) and Reactive Power (Vars)**

<table>
<thead>
<tr>
<th>Schemes</th>
<th>Adjust parameter</th>
<th>$p^* + p^-$</th>
<th>$q^* + q^-$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Case A</td>
<td>$k_p = 0.5 \rightarrow 0.6 \rightarrow 0.9$</td>
<td>165 → 210 → 240</td>
<td>150</td>
</tr>
<tr>
<td>Case B</td>
<td>$k_p = -0.6 \rightarrow -0.6 \rightarrow -0.6$</td>
<td>185 → 300 → 200 → 90</td>
<td>190</td>
</tr>
<tr>
<td>Case C</td>
<td>$k_p = 0.9 \rightarrow 0.6 \rightarrow 0.3$</td>
<td>250 → 190 → 90</td>
<td>190</td>
</tr>
</tbody>
</table>

**TABLE III: System Parameters for DVR Setup**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>DVR (exclude injected transformer)</td>
<td>$k_p = 0.5$</td>
<td>DVR (include injected transformer)</td>
<td>$k_p = 0.5$</td>
</tr>
<tr>
<td>Grid Frequency</td>
<td>50Hz</td>
<td>Primary Voltage</td>
<td>310W</td>
</tr>
<tr>
<td>Filter Inductance</td>
<td>1.4 mH</td>
<td>Secondary Voltage</td>
<td>310W</td>
</tr>
<tr>
<td>Filter Capacitance</td>
<td>15 µF</td>
<td>Magnetization Resistance</td>
<td>200 p.u.</td>
</tr>
<tr>
<td>Vdc Voltage</td>
<td>180V</td>
<td>load power</td>
<td>3 kW 0.83PF lag</td>
</tr>
<tr>
<td>load power</td>
<td>3 kW</td>
<td>Magnetization Inductance</td>
<td>200 p.u.</td>
</tr>
</tbody>
</table>

---

Fig. 11: The dc-link voltage control

Fig. 12: One representative case of voltage sag with 0.5 p.u.

Fig. 13: Details of the power circuit used in the experiment.
Fig. 14: Experimental results for Case A.

To summarize, Table II includes the main results of the given three strategies. Besides, the three control schemes demonstrate the smooth transition during changes in the control parameters during voltage sags and the elimination of active and reactive power oscillations.

B. Performance With Different Types of Voltage Sag

A complete set of experimental tests has been carried out to reveal the feasibility of the control scheme under different voltage sags. In this situation, two different voltage sags and one type of voltage swell have been programmed to evaluate the behavior of the system. Therefore, a single-phase voltage
sag (a-phase) of 0.4 p.u. is experienced in Test 1 (Type B sag [37]), in which the control parameter is modified ceaselessly ($k_q = -0.2 \rightarrow -0.5 \rightarrow -0.8$) in view of the control parameter ($k_p = 0.5$). Test 2 (Type C sag [37]) suffers a two-phase voltage sag (b- and c-phase) of 0.8 p.u., in which the control parameter is continuously changed ($k_p = 0.2 \rightarrow 0.5 \rightarrow 0.8$) by considering the control parameter ($k_q = 0.5$). Three phases voltage swell of 1.1 p.u., marked as the Test 3, is also occurs when the control parameters are changed during the Case A. Then, this two types of voltage sags and one type of voltage swell are shown in Fig.17.

Fig. 17: Two representative cases of voltage sag with 0.4 p.u. and 0.8 p.u.; one representative case of voltage swell with 1.1 p.u.

Fig.18 shows the experimental result when the PCC voltage is perturbed by Test 1. Note that the measured active power is close to 175W, shown at the high level of Fig.18a. The measured value of the injected reactive power is 80Var at the bottom of the low level in Fig.18a. And then, this value is increased up to 180Var in the middle of the low level in Fig.18a. The maximum value of the measured reactive power is equal to 245Var at the top of the low level in Fig.18a. The injected voltage in Fig.18b can compensate for the load voltage effectively. Fig.18c shows the load voltages and the load currents are shown in Fig.18d. It is important to note that the presented control scheme with the constant active power injection and adjustable reactive power injection is obtained by selecting the condition of $k_p = -k_q = k_{pq} \in [0, 1]$. Therefore, a new set of digital codes (i.e., '001') can be used to determine the identification tool inside the time range from 0.2 s to 0.3 s.

Fig.19 depicts the experimental waveform when the PCC voltage is perturbed by Test 2. Observe that the measured reactive power has been an increase of roughly 165Var represented at the lower curve of Fig.19a. Moreover, the measured value of the injected active power is 55W at the bottom of the upper
Fig. 19: Experimental results for Test 2.

The active power measured is increased up to 150W at the middle of the high curve in Fig.19a, and the maximum amount of the measured active power is equal to 290W at the top of the high curve in Fig.19a. Again, the injected voltage in Fig.19b can also be given based on the elliptical trajectory compensation. Fig.19c shows the load voltages and the load currents are shown in Fig.19d. Also, the flexible active power injection and constant reactive power injection can be fulfilled when the PCC voltage is perturbed by Test 2. Thus, the three digital numbers of the identification tool can be marked as '100' since the condition of $k_p = k_q$ satisfies the rule of $k_{pq} \in [0, 1]$.

Fig. 20: Experimental results for Test 3.

Fig. 21: Experimental results for Test 3.
TABLE IV: Operating States During the Different Sags

<table>
<thead>
<tr>
<th>Sag Depth (p.u.)</th>
<th>Test 1</th>
<th>Test 2</th>
<th>Test 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.4</td>
<td>0.8</td>
<td>1.1 (Swell)</td>
<td></td>
</tr>
<tr>
<td>(q^+ + q^-) (Var)</td>
<td>80 (\rightarrow) 180 (\rightarrow) 245</td>
<td>165</td>
<td>120</td>
</tr>
<tr>
<td>(p^+ + p^-) (W)</td>
<td>175</td>
<td>55 (\rightarrow) 150 (\rightarrow) 200</td>
<td>(-50 \rightarrow) -75 (\rightarrow) -100</td>
</tr>
</tbody>
</table>

TABLE V: Comparison with previous strategies of dynamic response

<table>
<thead>
<tr>
<th>Dynamic Response</th>
<th>Strategy</th>
<th>Proposal</th>
</tr>
</thead>
<tbody>
<tr>
<td>Time (ms)</td>
<td>[28]</td>
<td>[29]</td>
</tr>
<tr>
<td>13</td>
<td>10</td>
<td>20</td>
</tr>
</tbody>
</table>

Fig.20 depicts the experimental waveform when the PCC voltage is perturbed by Test 3. Note that the injected voltage curves are shown in Fig.20a. And then, the load voltage and the load current are also given in Fig.20b-20c. In addition, the voltage phase plots (a-phase an b-phase) between the voltage swell and the load voltage is shown in Fig.21a. Observe that the measured reactive power is close to 120Var, shown at the high level of Fig.21b. Moreover, the measured value of the injected active power is -50W at the top of the lower curve in Fig.21b, then this value is decreased to -75W at the middle of lower curve in Fig.21b, and the minimum amount of the measured active power is equal to -100W at the bottom of the lower curve in Fig.21b.

In sum, these experimental results are validated automatically by the proposed scheme. Table IV presents the significant characteristics of the previous strategies.

C. Discussion on the Benefits of the Identification Tool

Table II and Table IV display a comparison of different power injections when implementing the proposed control schemes. The control strategies considered in this paper can be identified by employing two adjustable parameters according to the mathematical relationship between the horizontal injection power and the vertical injection power in the elliptical trajectory. At the same time, the presented control strategies give priority to the controllable power injection, which matches correctly with the constant power injection. The main advantage of the presented identification tool is to display the digital codes and thus facilitate the multiple available selections of the active and reactive power dispatch during different voltage sags.

However, it is important to see that the load voltage in Fig.15b and Fig.16b are slightly distorted when the voltage sag occurs. IEEE-1159 defines voltage sag as a RMS voltage decrease to between 0.1 p.u. and 0.9 p.u. for duration from 0.5 cycle to 1 minute [38]. The survey of power quality presents that voltage sags with 40%-50% of the nominal value and with the duration from 5 to 30 cycles occurred in about 92% of all power system events [39]. This transient response is within one cycle (e.g., 16ms). There are three reasons that lead to the slight undershoot in two of three voltage phases. The first reason is the abrupt parameter change at \(t = 0.1s\). The second reason is the dead-time influence of the Danfoss FC 302 converter utilized in the experimental test. The last reason is one fixed delay when the sequence extractors are adopted to detect the voltage sequence components. Table V displays a comparison of different dynamic response when implementing the proposed control strategy and conventional control strategies [28]-[32]. By proper changing of two control parameters in (9)-(12), the appropriate strategy is easy to be decided once the equivalent impedance of sag source and the sag depth at the PCC are found.

Based on the aforementioned set of experiments, the main advantage of this identification tool is fully flexible operation that allows to define the behavior of the DVR in different grid scenarios. On the one hand, if the considered scenario deals with a voltage sag in a stiff grid, the adjustable reactive power injection will produce little influence on the voltage at the PCC. Thus, the factor that plays a vital role is in the selection of flexible active power delivery. On the other hand, the process of putting active and reactive power injection together is required to improve the voltage profile at the PCC when the sag-source with high resistive behavior is considered. Under this consideration, the best solution seems to be to raise the voltage in all phases when the parameter \(k_q\) being monotonically changing occurs. Opposite to the mentioned scenario, the choice of adjustable reactive power injection will have a significant effect on the voltage characterization at the PCC if the sag-source is mainly inductive and weak. In this sense, the best solution can be obtained with the smart voltage support service when the parameter \(k_q\) being monotonically tuning occurs.

In other words, the decision on which the suitable power injection is the best for the presented scenarios can be achieved by selecting the first digital code of the identification tool. In the following, four scenarios will be investigated to discuss the possible power dispatches. The first scenario consists of obtaining the maximum active power delivery. When the constant value of \(k_q\) is selected, the maximum active power dispatch can be achieved once the parameter \(k_p\) being monotonically increasing occurs. In this case, the corresponding digital codes of the identification tool is noted as '100'. The second scenario is made up of obtaining the minimum reactive power delivery. By choosing the constant parameter of \(k_p\), the minimum reactive power delivery can be obtained once the parameter \(k_q\) being monotonically decreasing occurs. The corresponding digital codes of the identification tool is remarked as '010'. The third scenario is to be capable of the minimum active power delivery. When setting the constant value of \(k_q\), the minimum active power delivery can be finished once the parameter \(k_p\) being monotonically increasing occurs. The corresponding digital codes of the identification tool is written as '011'. The fourth scenario deals with the maximum reactive power delivery. By selecting the constant value of \(k_q\), the maximum reactive power delivery can be obtained once the parameter \(k_p\) being monotonically decreasing occurs. The corresponding digital codes of the identification tool is written as '001'. Thus, the main contribution of the identification tool is a straightforward manner using the triplet of the digital codes to obtain different power deliveries during voltage sags. The important application is to prioritize the controllable power
injection with this triplet of digital codes to fully explore the capacities of the power dispatch, which corroborates that the presented control strategy is able to comply with the load voltage requirements even in different grid scenarios.

**D. Comparison With the Conventional Strategy**

In the literature, most studies discuss the behavior of eliminating active and reactive power oscillations in different scenarios to increase the immunity against voltage sags. Thus, the mentioned conventional strategies in [28]–[34] have been selected to define the current references (i.e., $\vec{i}_\alpha^+ = \vec{i}_\alpha^+ + \vec{i}_\beta^*$ and $\vec{i}_\beta^* = \vec{i}_\alpha^* + \vec{i}_\beta^*$), where the different forms of control parameter designed in (16)-(19) can be analyzed to obtain the control objectives.

Table VI provides a comparison between the representative strategies and the mentioned strategy in this paper. Obviously, the considered control strategies in the second column of Table VI incorporate the different mechanisms. Furthermore, the first control strategy in [28] provides a remarkable feature of active power injection that permits to mitigate the active power oscillation. Opposite to the first control strategy, the second one in [29] provides a remarkable feature of reactive power injection that permits to mitigate the reactive power oscillation.

The third control strategy in [30] provides a remarkable feature of active and reactive power injection that permits to maximize power delivery capability, while the oscillation terms of the active and reactive power cannot be avoided. The fourth control strategy in [31] provides a remarkable feature of active and reactive power injection that permits to mitigate the active power oscillation. The fifth control strategy in [32] provides a remarkable feature of active and reactive power control that permits to obtain the zero oscillation of active and reactive power injection, while the maximum current limit can exceed the rated current (i.e., $I_{\text{max}} = 10A = 1.4I_{\text{rated}}$).

The sixth control strategy in [33] with the zero power oscillations can be obtained when implementing the maximum voltage limit. Also, the same control objective in [34] can operate at zero power oscillations. In a practical system, however, the capability of maximizing power delivery should be considered depending on both the volt-ampere sizing of DVR and the different grid scenarios.

In addition, the control strategy based on the presented identification tool is the kernel to realize the adjustable power dispatches. The gradual transition from one power delivery level to another is described accurately by these preset parameter distributions, and it allows to show the power dispatch trend embedded in the presented identification tool. Also, this identification tool has been chosen as the operational mechanism to implement all the tests when the current references with the combination of two power deliveries are determined by setting the proper values of two control parameters. It is possible to simultaneously regulate the active power to a preset point and correct the deviation of the reactive power, and vice versa.

**V. CONCLUSION**

The application of elliptical compensation has provided flexible controllability of power support schemes. Also, a new identification tool has been described through the selection of two control parameters. The smooth transition state during changes in different power deliveries and the elimination of active and reactive power oscillations can be realized by setting useful values of control parameters. Meanwhile, the proposed control strategy displays a pretty better dynamic behavior, as can be seen from the identification approach. Detailed theoretical analysis and experimental verification have been achieved. Finally, application examples have been allowed to illustrate the feasibility of the given control algorithm.

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**REFERENCES**


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