

Aalborg Universitet

Level-Set Interface Description Approach for Thermal Phase Change of Nanofluids

Yahyaee, Ali; Bahman, Amir Sajjad; Olesen, Klaus; Sørensen, Henrik

Published in: Nanomaterials

DOI (link to publication from Publisher): 10.3390/nano12132228

Creative Commons License CC BY 4.0

Publication date: 2022

Document Version Publisher's PDF, also known as Version of record

Link to publication from Aalborg University

Citation for published version (APA):

Yahyaee, A., Bahman, A. S., Olesen, K., & Sørensen, H. (2022). Level-Set Interface Description Approach for Thermal Phase Change of Nanofluids. *Nanomaterials*, 12(13), Article 2228. https://doi.org/10.3390/nano12132228

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
 You may freely distribute the URL identifying the publication in the public portal -

Take down policy

If you believe that this document breaches copyright please contact us at vbn@aub.aau.dk providing details, and we will remove access to the work immediately and investigate your claim.

Downloaded from vbn.aau.dk on: December 06, 2025



MDPI

Article

Level-Set Interface Description Approach for Thermal Phase Change of Nanofluids

Ali Yahyaee ^{1,*}, Amir Sajjad Bahman ^{1,*}, Klaus Olesen ² and Henrik Sørensen ¹

- Department of Energy, Aalborg University, 9220 Aalborg, Denmark; hs@energy.aau.dk
- ² Danfoss Silicon Power, 24941 Flensburg, Germany; klaus_olesen@danfoss.com
- * Correspondence: ayn@energy.aau.dk (A.Y.); amir@energy.aau.dk (A.S.B.)

Abstract: Simulations of thermally driven phase change phenomena of nanofluids are still in their infancy. Locating the gas-liquid interface location as precisely as possible is one of the primary problems in simulating such flows. The VOF method is the most applied interface description method in commercial and open-source CFD software to simulate nanofluids' thermal phase change. Using the VOF method directs to inaccurate curvature calculation, which drives artificial flows (numerical non-physical velocities), especially in the vicinity of the gas-liquid interface. To recover accuracy in simulation results by VOF, a solver coupling VOF with the level-set interface description method can be used, in which the VOF is employed to capture the interface since it is a mass conserving method and the level-set is employed to calculate the curvature and physical quantities near the interface. We implemented the aforementioned coupled level-set and VOF (CLSVOF) method within the open-source OpenFOAM® framework and conducted a comparative analysis between CLSVOF and VOF (the default interface capturing method) to demonstrate the CLSVOF method's advantages and disadvantages in various phase change scenarios. Using experimental mathematical correlations from the literature, we consider the effect of nanoparticles on the base fluid. Results shows that the new inferred technique provides more precise curvature calculation and greater agreement between simulated and analytical/benchmark solutions, but at the expense of processing time.

Keywords: thermal phase change; nanofluids; interface curvature; level-set; volume of fluid; benchmark study



Citation: Yahyaee, A.; Bahman, A.S.; Olesen, K.; Sørensen, H. Level-Set Interface Description Approach for Thermal Phase Change of Nanofluids. *Nanomaterials* **2022**, *12*, 2228. https://doi.org/10.3390/nano12132228

Academic Editors: Mikhail Sheremet and Malik Zaka Ullah

Received: 6 May 2022 Accepted: 23 June 2022 Published: 29 June 2022

Publisher's Note: MDPI stays neutral with regard to jurisdictional claims in published maps and institutional affiliations.



Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https://creativecommons.org/licenses/by/4.0/).

1. Introduction

Recently, there has been a rising interest in the application of thermal phase change processes to nanofluids, particularly flow boiling of nanofluids [1–3]. Flow boiling is an efficient cooling technique because it removes latent heat of vaporization while pushing the flow owing to the density difference. Furthermore, nanofluids can be used to improve heat transfer in industrial applications, which was proved to be a very successful technique by Choi and Eastman [4] for the first time. Following that, several researchers began to investigate various aspects of employing nanofluids in cooling applications both experimentally [5–11] and numerically [12–19].

Phase change research was generally experimental; however, experiments in this field are restricted, and even a little mistake might result in a huge error [20]. As a result, it is necessary to numerically model phase change processes in order to fully comprehend the available experimental data and to accurately characterize the underlying physics. The ability to examine complex geometries and various conditions is one of the most important benefits of numerical simulation [21,22].

While phase transition has been researched for more than half a century, its complicated physical nature, which involves simultaneous heat, mass, and momentum transfer,

Nanomaterials **2022**, 12, 2228 2 of 21

makes numerical predictions difficult. Locating the interface position is a significant difficulty in CFD modeling of two-phase flows. The issue is how to construct a sharp interface by analyzing the curvature of the interface and forecasting physical parameters that change dramatically across the interface. As seen in Figure 1, the gas–liquid interface can be represented using interface tracking and capturing techniques. The interface tracking techniques are primarily divided into three categories: front tracking methods, marker methods, and arbitrary Lagrangian–Eulerian methods. The primary advantage of this technique is its ability to appropriately analyze the interface profile; however, since the computational domain requires meshing updates when the interface deforms, it will be prohibitively difficult to precisely monitor the interface while maintaining a reasonable degree of re-meshing repetition. This is related to the production of an overwhelming mesh, which renders interface tracking approaches outdated.

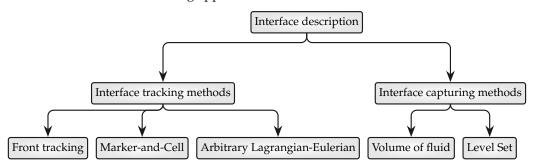


Figure 1. An overview of the numerical approaches and their branches that have been introduced and implemented for the description of the dispersed phase topology or for the localization of the interface between two phases.

As an alternative to interface tracking techniques, interface capturing techniques can be discussed, which specify the interface location using a scalar function. The volume-of-fluid (VOF) and level-set (LS) functions are the most well-known scalar functions for describing the gas–liquid interface. The VOF method, which was pioneered by [23], has evolved into a norm for both open-source and commercial CFD software. A volume fraction (α) is employed in the VOF technique to distinguish between the fluid 1 and fluid 2 inside the domain. The cell is filled with fluid 1 when $\alpha=1$, and with fluid 2 when $\alpha=0$. Each phase's volume fraction is tracked across the domain in this model, which uses a single momentum equation to address the fluids.

OpenFOAM's phase change solvers mostly employ VOF to describe interfaces, as well as research into simulating flow boiling of nanofluids, and it has been applied in a broad variety of phase change circumstances, some of which are listed in the Table 1. The volume fraction gradient is used as the normal vector field perpendicular to the gas—liquid interface in the VOF technique. Because the volume fraction is not a smooth function, the direction of the normal vector is chaotic. The curvature of the unit normal vector is equal to its divergence. Additionally, due to the smeared interface, a finite gradient of curvature develops in the normal direction. These impacts lead to an incorrect curvature calculation, which results in a larger numerical error for phase change calculations [24].

Nanomaterials **2022**, 12, 2228 3 of 21

Table 1. An overview of some of the studies that have used VOF as their interface capture technique is shown in the next section. The scope of these simulations is restricted to thermally induced phase transitions or flow boiling of nanofluids simulations.

Publication	Remarks
Soleimani et al. [25]	The VOF method is used to model subcooled flow boiling of HFE-7100 in a microchannel heat sink with variable concentrations of alumina nanoparticles.
Zhang et al. [26]	In a tiny tube, the VOF approach is used to quantitatively investigate the heat transfer and pressure drop properties of gas–liquid Taylor flows. CuO/water nanofluid was the liquid, while nitrogen was the gas.
Rabiee et al. [27]	flow condensation inside a smooth horizontal tube was simulated. Moreover, the effect of some parameters such as mass flux, tube hydraulic diameter, vapor quality and difference between the wall and saturation temperature on the heat transfer coefficient were investigated.
Yahyaee et al. [28]	This article simulates the development of bubbles and their escape from a superheated horizontal surface. A cylindrical hollow initiates the bubble nucleation process. The simulation will be carried out utilizing VOF using a new OpenFOAM-based two-phase solver.
Abedini et al. [29]	The VOF method are used to explore the subcooled boiling of Alumina-water nanofluid in both vertical concentric annulus and vertical tube. There is a comparison of the inlet vapor volume fraction fluctuation at various nanoparticles concentrations.

Using other interface capture techniques, most notably the level-set approach, results in a more accurate estimation of interface curvature. The level-set approach, presented by [30], calculates a distance function for the entire computational domain's cells. The zero distance denotes the interface between gases and liquids. The cells with a positive distance are believed to be in the continuous phase (liquid), whereas those with a negative distance are thought to be in the scattered phase (gas). Dhir's group has extensively employed the level-set technique [31–34] to investigate a variety of phase change events, including nucleate boiling, film boiling from a horizontal cylinder, and subcooled pool boiling. Apart from Dhir's group, ref. [35] investigated film boiling using the level-set approach, and [36] simulated the evaporation of a moving and deforming droplet. The level-set technique, on the other hand, is a non-conservative methodology that does not ensure mass conservation in phase transition calculations [37]. The primary drawback of the level-set approach is the fluid mass loss. Ref. [38] presented a combination approach of level-set and VOF termed CLSVOF, which was extensively adopted by others [39-42]. It generates a precise, sharp interface and compensates for the level-set method's drawback. The volume fractions of liquid and gas are calculated using VOF, and level-set determines geometrical interface properties such as the curvature and normal vector in each cell.

According to the best knowledge of the writers, prior research on nanofluid flow boiling has used VOF to capture the interface; however, this technique produces less accurate gas—liquid curvature calculations, which in turn yields in less accurate results. Due to the fact that numerous studies in the literature have identified level-set as an interface description method for calculating curvature, level-set is used for the first time in this paper for nanofluids' thermally driven phase change modeling, and the obtained results are compared to VOF's utilizing benchmark scenarios to demonstrate their respective strengths and limitations in different thermal phase change circumstances. Benchmark instances are

- Evaporation by heat conduction,
- Condensation by heat conduction,
- Film condensation on a vertical plate,
- 2D film boiling.

We picked these four benchmark cases because of their relevance in a wide range of processes: one-dimensional boiling, one-dimensional condensation, two-dimensional condensation, and two-dimensional boiling. To ensure the solver's accuracy, simulation results were validated using analytical solutions.

Nanomaterials **2022**, 12, 2228 4 of 21

2. Numerical Formulation

The mass, momentum, and energy conservation equations as well as the advection interface description equations are expressed as follows for two incompressible and immersible fluids

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{U}) = 0, \tag{1}$$

$$\frac{\partial(\rho \mathbf{U})}{\partial t} + \nabla \cdot (\rho \mathbf{U} \mathbf{U}) = -\nabla p + \nabla \cdot \boldsymbol{\tau} + \rho \mathbf{g} + \mathbf{F},\tag{2}$$

$$\frac{\partial \alpha}{\partial t} + \mathbf{U} \cdot \nabla \alpha = -m'' \left[\frac{1}{\rho_1} - \alpha \left(\frac{1}{\rho_1} - \frac{1}{\rho_V} \right) \right],\tag{3}$$

$$\frac{\partial(\rho c_p T)}{\partial t} + \nabla \cdot (\rho c_p \mathbf{U} T) = \nabla \cdot (k \nabla T) - m'''(h_v - h_l), \tag{4}$$

where m''' represents the rate of exchanged volumetric mass flux, which was determined by applying the Tanasawa model ([43]). In this model, the interface superheat temperature (ΔT sat) is used to determine the interface mass flux:

$$m''' = \frac{2\gamma}{2 - \gamma} \left(\frac{M_{\rm l}}{2\text{BR}}\right)^{1/2} \frac{\rho_{\rm v}(h_{\rm v} - h_{\rm l})\Delta T_{\rm sat}|\nabla\alpha|}{T_{\rm sat}^{3/2}},\tag{5}$$

where γ is the evaporation coefficient (here ir is equal to 1), M_1 is the fluid's molecular weight, and R the universal gas constant.

The domain is created for a mixture, using the α function to differentiate the liquid and gas. In this study, the interface description is provided via the use of two separate techniques for interface capture, VOF and CLSVOF. The VOF approach represents the interface and separate phases using a liquid (nanofluid) volume fraction function (α).

$$\alpha = \frac{V_{\text{nf}}}{V} = \begin{cases} 1 & \text{nanofluid} \\ 0 < \alpha < 1 & \text{Interface} \end{cases} , \tag{6}$$

where α denotes the nanofluid's volume fraction, $V_{\rm nf}$ denotes the volume of nanofluid contained inside a cell, and V is the total cell volume. The volume fraction function of liquid (α) is also used to determine the density of a mixture ($\rho_{\rm m}$), the viscosity of a mixture ($\mu_{\rm m}$), the constant pressure specific heat of a mixture ($c_{p,\rm m}$), and the thermal conductivity of a mixture ($k_{\rm m}$).

$$\rho_{\rm m} = \alpha \rho_{\rm nf} + (1 - \alpha) \rho_{\rm v},\tag{7}$$

$$\mu_{\rm m} = \alpha \mu_{\rm nf} + (1 - \alpha) \mu_{\rm v},\tag{8}$$

$$c_{\nu,m} = \alpha c_{\nu,nf} + (1 - \alpha)c_{\nu,\nu}, \tag{9}$$

$$k_{\rm m} = \alpha k_{\rm nf} + (1 - \alpha) k_{\rm v}. \tag{10}$$

We integrated the CLSVOF technique with VOF into an OpenFOAM solver for thermally induced phase changes. The CLSVOF method makes use of the VOF method's mass conservatism and the LS method's interface sharpness. A new scalar field termed level-set function (ψ) is defined in the CLSVOF method instead of α , which is used in VOF method. The reader is directed to Omar et al's [24] paper for more thorough details on the CLSVOF method's implementation and governing equations.

Nanomaterials **2022**, 12, 2228 5 of 21

2.1. Governing Equations Used to Calculate Nanofluids Thermophysical Properties

This paper investigates nanofluids thermally driven phase change cases. Nanofluids are assumed to be homogeneous, and their properties can be determined experimentally or theoretically. The density, specific heat capacity, viscosity, thermal conductivity, and surface tension of a nanofluid are calculated using [44–47]:

$$\rho_{\rm nf} = \phi_{\rm np}\rho_{\rm np} + (1 - \phi_{\rm np})\rho_{\rm bf},\tag{11}$$

$$\mu_{\rm nf} = (1 + 2.5\phi_{\rm np})\mu_{\rm bf},$$
 (12)

$$c_{p,\text{nf}} = \frac{\phi_{\text{np}}\rho_{\text{np}}c_{p,\text{np}} + (1 - \phi_{\text{np}})\rho_{\text{bf}}c_{p,\text{bf}}}{\rho_{\text{nf}}},$$
(13)

$$k_{\rm nf} = \frac{k_{\rm np} + (n-1)k_{\rm bf} - (n-1)\phi_{\rm np}(k_{\rm bf} - k_{\rm np})}{k_{\rm np} + (n-1)k_{\rm bf} + \phi_{\rm np}(k_{\rm bf} - k_{\rm np})},$$
(14)

$$\frac{\sigma_{\rm bf} - \sigma_{\rm nf}}{\sigma_{\rm bf}} = b \ln \left(\frac{\phi_{\rm np}}{a} + 1 \right),\tag{15}$$

where ϕ_{np} is the volumetric concentration of nanoparticles. The number n specifies the empirical shape factor, which is equal to three for spherical nanoparticles. The np, bf, and nf, respectively, indicate the characteristics of nanoparticles, base fluid, and obtained nanofluid. The experimental values (a and b) are 7.673×10^{-7} and -7.773×10^{-3} [47]. Spherical Al_2O_3 nanoparticles with $\phi_{np}=0.01$ are added to the base fluid.

2.2. Discretization Schemes for Solution Algorithm

OpenFOAM has a number of built-in numerical schemes for discretizing the terms in each conservation equation. As seen in Table 2, second-order schemes are used in different cases for all OpenFOAM calculations in this study.

Table 2. The techniques for discretizing the solution algorithm for benchmark instances are listed in the following table. All of the schemes are standard second-order approaches that can be found in OpenFOAM solvers and are implemented as such.

Terms	Schemes
Temporal term	Backward
Convective term in momentum equation	vanLeerV
Convective term in energy equation	vanLeer
Compression velocity term in momentum equation	interfaceCompression
Diffusion term in momentum equation	Gauss Linear corrected
Viscous term in momentum equation	Gauss Linear

3. Benchmark Study

The VOF and CLSVOF methods in thermal phase change cases are compared in this section. Experimental correlations and analytical solutions serve as the fundamental comparison ground for quantifying the results of different benchmark situations. To quantify the outcomes for various benchmark scenarios, analytical solutions and experimental correlations were employed as the basic comparison ground. The Latex routines were used to generate schematics of benchmark cases and graphs illustrating the findings. It is critical to note that when we refer to liquids in the following benchmark situations, we are referring to nanofluidic liquids.

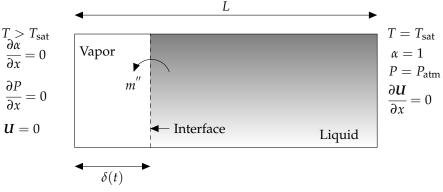
The study was conducted using different benchmark cases and a systematic grid refinement. All the benchmark cases were created using simple rectangular blocks. These blocks are divided into N_k grids. For example, $N_k = [30, 80, 130, 180]$ are the number of grids in the first two benchmark cases. If e_k is the error generated by dividing the domain into N_k grids, convergence rate (R_k) is defined as

Nanomaterials **2022**, 12, 2228 6 of 21

$$R_{k} = \frac{\log(e_{k}/e_{k-1})}{\log(N_{k}/N_{k-1})}.$$
(16)

3.1. Evaporation by Heat Conduction

The Stefan problem, also known as evaporation by heat conduction, is a 1D benchmark example that is generally utilized to test thermally driven phase change mass transfer in a new solver. Figure 2 illustrates the 1D evaporation by heat conduction problem schematically. Without convection, the left wall's greater temperature induces evaporation at the interface, resulting in interface motion to the right. Evaporation is entirely controlled by conduction heat transfer. Table 3 contains the thermophysical characteristics utilized to solve this test case.



Initial condition: $P = P_{atm}$, $T = T_{sat}$, U = 0

Figure 2. The graphic depicts the 1D Evaporation by heat conduction problem (also known as the Stefan problem) and the boundary conditions associated with it. Gray denotes liquid, while white denotes a part of geometry that is filled with vapor at a saturated temperature. The phase change occurs at the gas–liquid interface, shown by the dashed line. Phase change is induced when the wall in contact with the vapor reaches a temperature greater than superheat. As a result of the evaporation phase change previously described, the interface, which also serves as a measure for the vapor layer thickness, is shifting to the right.

Table 3. Base fluid, nanoparticles, and gas properties used in the evaporation by heat conduction (also known as Stefan problem) and condensation by heat conduction (also known as Horizontal film condensation problem) benchmark cases. These two benchmark cases are presented and solved in Sections 3.1 and 3.2.

	Dimension	Base Fluid	Nanoparticles	Vapor
Thermal conductivity, k	$\mathrm{W}\mathrm{m}^2\mathrm{K}^{-1}$	0.648	36	0.03643
Density, ρ	$ m kgm^{-3}$	645	3600	5.1450
Viscosity, μ	Pa s	1.48×10^{-4}		1.502×10^{-5}
Specific heat capacity c_p	${ m kJ}{ m kg}^{-1}{ m K}^{-1}$	2.794	0.765	2.687
Latent Heat, h	$kJ kg^{-1}$	762.52		2777.1
Surface tension, σ	$N \mathrm{m}^{-1}$	0.045417		

The analytical solutions [48] for the temperature distribution (T(x,t)) and the thickness of vapor film (δ) are as follows

$$T(x,t) = T\Big|_{x=0} - \frac{\Delta T_{\sup}}{\operatorname{erf}(\epsilon)} \operatorname{erf}\left(\frac{x}{2\sqrt{\frac{k_{v}t}{\rho_{v}c_{n,v}}}}\right),\tag{17}$$

Nanomaterials **2022**, 12, 2228 7 of 21

$$\delta(t) = 2\epsilon \sqrt{\frac{k_{\rm v}t}{\rho_{\rm v}c_{p,\rm v}}},\tag{18}$$

where ϵ is a constant given by

$$\epsilon \exp(\epsilon^2) \operatorname{erf}(\epsilon) = \frac{c_{p,v} \Delta T_{\sup}}{(h_v - h_1) \sqrt{g}}.$$
(19)

Evaporation by heat conduction benchmark case is solved for $N_{\rm k} = [30, 80, 130, 180]$ number of nodes and results for three implemented interface description methods are presented in Figure 3 as

- The dimensionless location of the interface (δ^*) through dimensionless time (t^*), and
- Jakob number distribution (Ja) within the 1D domain to study temperature distribution.

The interface location and time are normalized by scaling with the domain length (L) and the Capillary time scale (t_{σ}) which itself is

$$t_{\sigma} = \sqrt{\frac{\rho_{\rm v} L^3}{\sigma}}. (20)$$

The Jakob number, here, is introduced to present a dimensionless display of temperature profile and is presented as

$$Ja = \frac{c_{p,v}(T - T_{sat})}{(h_v - h_1)}.$$
 (21)

As shown in Figure 3a,c, when we use the coarsest grid structure ($N_k = 30$) the dimensionless vapor film thickness (δ^*) graph has a zigzag path. When we use more refined grid structures, this zigzag path is gradually turned into curved lines (noises are dumped), and results become closer the analytical solution.

The Jakob number along domain at t=20 s is shown in Figure 3b,d. As can be seen, the Jakob number close to the gas–liquid interface shows higher values than the analytical solution, in particular when coarser grid structures ($N_k = [30, 80]$) are used for the simulation. This is due to the fact that a source term implicitly sets the interface temperature to saturation [49,50].

By looking at Figure 3b,d, we cannot uncover how different implemented interface description methods are functioning compared to each other. So to reach this goal, we study the logarithmic error graph for different methods. The L2 error norm is used to quantify the aforementioned difference between simulation and analysis. The following equation can be used to obtain the L2 norm of the temperature distribution error (e_T) for various grid sizes as

$$e_T = \sqrt{\frac{\sum_{i=1}^{N_k} \left(\frac{T_{\text{num,i}} - T_{\text{ana,i}}}{T_{\text{ana,i}}}\right)^2}{N_k}}.$$
 (22)

The L2 norm error of the temperature profile is shown in Figure 4. The convergence with using finer grid structure is seen for all VOF and CLSVOF. CLSVOF has a somewhat lower error rate than VOF, as can be observed. According to results in Figure 4, the rate of convergence (calculated using Equation (16)) for two grid structures with finest mesh size ($N_k = [130, 180]$) are calculated and states that CLSVOF with the convergence rate of 0.125 has a better performance than VOF with convergence rate of 0.085.

A dashed line shows the analyzed calculation time for the various number of grids in Figure 4, the VOF approach is proved to be quicker for all grid sizes.

Nanomaterials **2022**, 12, 2228 8 of 21

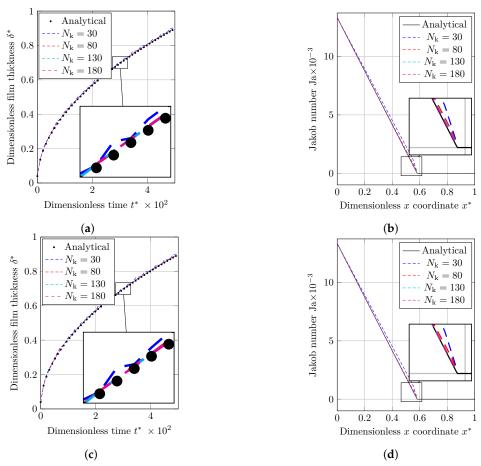


Figure 3. A comparison between the numerical data achieved using the VOF and CLSVOF techniques with the numerical solutions to the evaporation by heat conduction problem. (a) The thickening of the vapor film's dimensionless thickness with respect to time as calculated using the VOF technique is shown. (b) The Jakob number profile throughout the dimensionless length as determined using the VOF approach is shown. (c) The thickening of the vapor film's dimensionless thickness with respect to time, as determined using the CLSVOF technique. (d) CLSVOF technique was used to obtain Jakob number distribution throughout the dimensionless length.

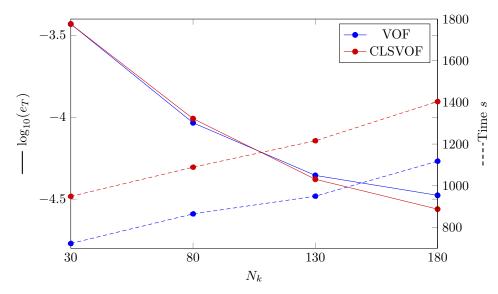


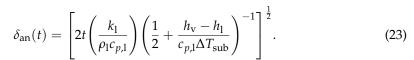
Figure 4. (Solid lines) The error's logarithmic representation where e_T is the L2 norm error computed by Equation (22). (Dashed lines) VOF and CLSVOF computation times for the Stefan problem at various grid sizes.

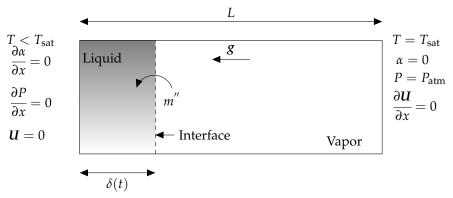
Nanomaterials **2022**, 12, 2228 9 of 21

3.2. Condensation by Conduction

Condensation by conduction, also called Horizontal film condensation problem, is a 1D benchmark case, whose computation results are confirmed with Nusselt's film theory [51]. The benchmark case schematic with its boundary conditions is shown in Figure 5. In the absence of convection, the lower temperature of left wall causes condensation on this wall, increasing liquid film thickness and causing rightward interface motion. Table 3 contains the thermophysical characteristics utilized in this test scenario.

The analytical solution [48] to calculate the liquid film thickness ($\delta_{an}(t)$) is given as





Initial condition: $P = P_{atm}$, $T = T_{sat}$, U = 0

Figure 5. The graphic depicts the 1D condensation by heat conduction problem (also known as the Horizontal film condensation problem) and the accompanying boundary conditions. Gray signifies liquid, whereas white suggests a vapor-filled region of geometry. Both vapor and base liquid are at their saturation temperature. The phase transition takes place at the gas—liquid interface, as shown by the dashed line. Phase change occurs when the wall in contact with the nanofluid cools below superheat. As a consequence of the condensation phase change explained above, the interface, which also acts as a measure for the thickness of the condensed water layer, is moving to the right.

In this investigation, four grid configurations with $N_{\rm k}$ equal to [30, 80, 130, 180] grids in x direction were used. The results will be liquid film thickness (δ) versus time (t), which are made dimensionless by normalizing by L and $t_{\rm c}$ (Equation (20)), respectively. Changes in the dimensionless thickness of a condensed liquid layer (δ^*) versus dimensionless time (t^*), obtained using the VOF and CLSVOF methods, are given in Figure 6. As shown, the results match to the analytical results for all mesh sizes except the coarsest one, which is associated with some distances from the analytical solution.

As with the previous benchmark example, the L2 error is calculated for the VOF and CLSVOF techniques (Figure 7). The L2 error for the condensed film thickness is defined as

$$e_{\delta} = \sqrt{\frac{\sum_{i=1}^{N_{\delta t}} \left(\frac{\delta_{\text{num,i}} - \delta_{\text{ana,i}}}{\delta_{\text{ana,i}}}\right)^{2}}{N_{\delta t}}},$$
(24)

where $N_{\delta t}$ is the number of time intervals. As shown in Figure 7, with grid structures of $N_{\rm k} = [30, 80, 130]$ all methods provide similarly precise results. At the finest grid structure ($N_{\rm k} = 180$) VOF cannot keep up with CLSVOF and deliver higher error. The rate of convergence (Equation (16)) for the grid structures with finest mesh size ($N_{\rm k} = [130, 180]$)

Nanomaterials **2022**, 12, 2228 10 of 21

for two methods are calculated and states that CLSVOF with the convergence rate of 0.04 perform better than VOF with convergence rate of 4.8×10^{-5} .

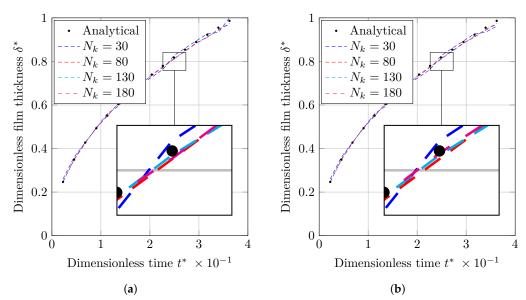


Figure 6. Variation of dimensionless liquid film thickness with dimensionless time achieved by **(a)** VOF and **(b)** CLSVOF for condensation by heat conduction study case.

In Figure 7, the investigation on computational time study is demonstrated as dashed lines. As shown in this figure, VOF delivers faster computation compared to CLSVOF.

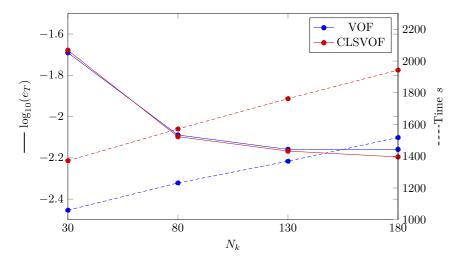


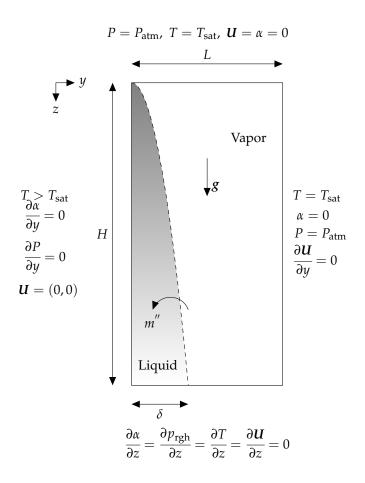
Figure 7. (Solid lines) The error's logarithmic representation where e_{δ} is the L2 norm error computed by Equation (24). (Dashed lines) VOF and CLSVOF computation times for the condensation by heat conduction case problem at various grid sizes. The number of nodes along the x axis is represented by the horizontal axis (N_k).

3.3. Film Condensation on a Vertical Plate

Film condensation on a vertical plate is modeled as a benchmark case and compared with analytical solution. As shown in Figure 8 simulation domain consists of a $L \times H$ rectangle in the y (normal to the wall) and z (along with film flow) directions, which has a nanofluid liquid film with δ_0 thickness on its left wall. The left wall temperature is sub-cooled with $\Delta T_{\rm sub} = 20$ K while rest of the domain is filled with saturated vapor ($T_{\rm sat} = 646$ K). Zero gradient condition is used as boundary conditions for α , T, U, and P at the top and bottom boundaries. The material properties can be seen in Table 4.

To achieve an analytical solution, following assumptions are made [51,52]:

Nanomaterials **2022**, 12, 2228 11 of 21



Initial condition: $P = P_{atm}$, $T = T_{sat}$, U = 0

Figure 8. The condensation of a laminar film on a vertical plate is shown schematically, together with the associated boundary conditions. Gray denotes liquid, but white denotes a geometric area filled with vapor. As seen by the dashed line, the phase change occurs at the gas—liquid interface. When the vertical wall cools below superheat, phase change occurs. The condensation phase change described above results in the formation of a layer of condensed liquid in the shape of a parabola on the left wall.

- The temperature profile across the film is linear,
- Effects of forces caused by inertia and interface shearing stress are neglected.

Table 4. Base fluid, nanoparticles, and gas properties used in the laminar film condensation and 2D film boiling benchmark instances. These two benchmark cases are presented and solved in Sections 3.3 and 3.4.

	Dimension	Base Fluid	Nanoparticles	Vapor
Thermal conductivity, λ	${ m W}{ m m}^2{ m K}^{-1}$	0.531	36	0.538
Density, ρ	$\mathrm{kg}\mathrm{m}^{-3}$	370.4	3600	242.7
Viscosity, μ	Pa s	4.53×10^{-5}		3.23×10^{-6}
Specific heat capacity C_p	${ m kJkg^{-1}K^{-1}}$	239	0.765	352
Latent Heat, h	$kJ kg^{-1}$	1963.5		2240
Surface tension, σ	$N m^{-1}$	7.55×10^{-5}		

Nanomaterials **2022**, 12, 2228 12 of 21

Based on the aforementioned assumptions, the analytical solution [48] for the liquid film thickness (δ) is

$$\delta = \left[\frac{4\mu_1 k_1 \Delta T_{\text{sub}} z}{g(h_{\text{v}} - h_1)\rho_1(\rho_1 - \rho_{\text{v}})} \right]^{\frac{1}{4}}.$$
 (25)

Four grid structures of $N_k = [120 \times 240, 140 \times 280, 160 \times 320, 180 \times 360]$ are picked for studying this case. A factor of 10 is applied to the grid structure in the y and z axis to achieve fine mesh distribution in the liquid film region. Scaling with L and H normalizes the liquid film thickness (δ) and the z coordinate, whereas scaling with L normalizes the y coordinate. Table 5 displays the geometric parameter values for a case study of film condensation on a vertical plate.

Table 5. The geometric parameters utilized in the vertical condensation benchmark are shown in the table below. All of the dimensions are shown as functions of the length of the domain. The reader will refer to Figure 8 in order to have a better understanding of this table.

L	Length of domain	0.5 L
Н	Height of domain	3 L
$\delta(0)$	Thickness of condensed film at $t = 0$	0.01 L

The dimensionless results for the condensed film thickness using VOF and CLSVOF methods are presented in Figure 9. The results of the VOF simulation are shown to be different from those of the analysis and cannot predict the shape of condensed film correctly, whereas CLSVOF provides more accurate condensed film shape. By refining the grids, the results converge to the analytical solution.

To examine the difference between VOF and CLSVOF methods performance, the L2 error calculation is provided in Figure 10. In this case, the L2 error for the condensed nanofluid film thickness is defined by equation

$$e_{\delta} = \sqrt{\frac{\sum_{i=1}^{N_{k}} \left(\frac{\delta_{\text{num,i}} - \delta_{\text{ana,i}}}{\delta_{\text{ana,i}}}\right)^{2}}{N_{k}}},$$
(26)

where N_k is the grid's number in the y axis. As it can be seen in Figure 10, the error generated by CLSVOF is significantly lower than VOF. The rate of convergence (Equation (16)) between the finest mesh structures ($N_k = [160 \times 320, 180 \times 360]$) for CLSVOF method is equal to 0.005, while for VOF has a better convergence with value of 0.17.

In Figure 10 the computational time study is presented too (dashed lines). As shown and unlike previous benchmark cases, CLSVOF method delivers faster computation compared to VOF. This is because VOF struggle to reach the convergence criteria in each time step in this benchmark case.

Nanomaterials **2022**, 12, 2228

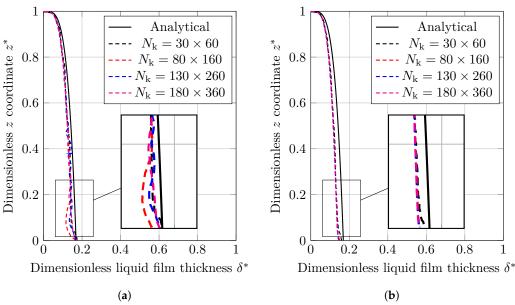


Figure 9. Analytical and numerical results for the normalized thickness of condensed film on a vertical plate predicated using (a) VOF and (b) CLSVOF.

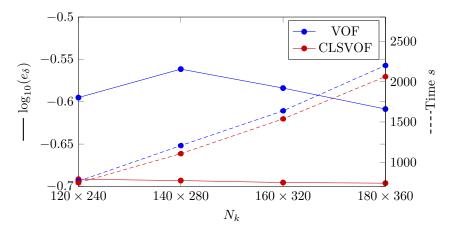


Figure 10. (Solid lines) Logarithmic representation of the error, where e_{δ} denotes the L2 norm of the error as determined by Equation (24). (Dashed lines) Time required to simulate the vertical film condensation scenario using the VOF and CLSVOF techniques at different grid structures.

3.4. 2D Film Boiling

The study case is a 2D film boiling problem. As seen in Figure 11, between the surface and the liquid exists a vapor layer in the form of sinusoidal. The liquid is at its saturation temperature ($T_{\rm sat}=646$ K), but the surface temperature is above it ($\Delta T_{\rm sup}=5$ K). The phase change happens at the liquid–vapor interface, and the produced vapor is subsequently released as bubbles. The computational domain is defined by the rectangle with the dimension of $L=\lambda/2$ and $H=\lambda$. In this situation, λ is defined as

$$\lambda = \sqrt{\frac{\sigma}{(\rho_1 - \rho_v)g}}. (27)$$

According to Figure 11, the numerical domain exhibits horizontal symmetry. As a result, just a portion of the domain is simulated. Vertical borders are said to have a symmetric boundary condition. The higher border is given the pressure outlet condition, whereas the vertical gradient for other variables is equal to zero.

Nanomaterials **2022**, 12, 2228 14 of 21

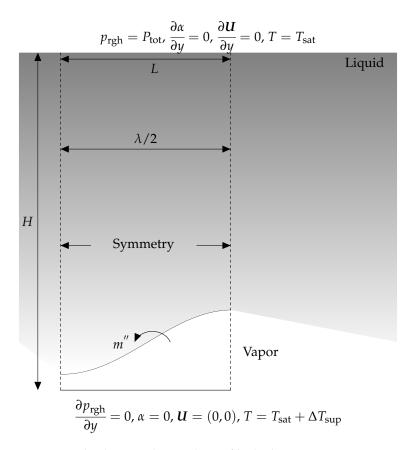


Figure 11. The diagram depicts the 2D film boiling scenario's geometry and boundary conditions. Between the liquid's surface and the vapor is a sinusoidal vapor layer. The liquid is at its saturation temperature, but the surface temperature is greater than it. The phase change happens at the liquid-vapor interface, and the bubbles of generated vapor depart the vapor film layer.

The thickness of the vapor film is initiated by the following equation,

$$\delta = \frac{\lambda_0}{64} \left(4 + \cos\left(\frac{2\beta x}{\lambda_0}\right) \right),\tag{28}$$

where λ_0 is the critical wavelength of Taylor equation, obtained by

$$\lambda_0 = 26\sqrt{\frac{3\sigma}{(\rho_1 - \rho_v)g}}. (29)$$

The Nusselt number in this case is calculated by

$$Nu = \frac{\int_0^L \left(\frac{\lambda}{\Delta T} \frac{\partial T}{\partial y}\Big|_{y=0}\right) dx}{I}.$$
 (30)

The outcomes of 2D film boiling scenario can be predicted using a number of empirical relationships. We use the experimental correlation offered by [53]. This correlation define Nusselt number of 2D film boiling as

Nu = 0.425
$$\left[\frac{\rho_{\rm v}(\rho_{\rm l} - \rho_{\rm v})g (h_{\rm v} - h_{\rm l})}{k_{\rm v}\mu_{\rm v}\Delta T} \right]$$
. (31)

Four grid structures of $N_{\rm k} = [160 \times 320, 220 \times 440, 260 \times 520, 280 \times 560]$ are used to analyze these benchmark scenarios. The material properties used to simulate the 2D film boiling benchmark are shown in Table 4. To have the dimensionless numbers as results, x

Nanomaterials **2022**, 12, 2228 15 of 21

and y coordinate are normalized by scaling with λ (calculated by Equation (27)) and t is become dimensionless by scaling with t_{σ} (calculated by Equation (20)).

In Figure 12, the first detached bubble form for VOF and CLSVOF is compared at a given height. The first striking result in Figure 12b is the bubble shape predicted by CLSVOF when the two coarsest grid structures are used ($N_k = [160 \times 320, 220 \times 440]$). The interface is connected to the bottom wall, as can be seen in the magnified image of this graph. This behavior is inconsistent with the benchmark scenario and has not been seen with the VOF and various grid density shown in Figure 12b. This demonstrates that the CLSVOF technique is ineffective when the grid structure is coarse and the interface is close and parallel to the wall. Thus, in the discussion provided for the Nusselt number, the CLSVOF findings for the grid structure $N_k = [160 \times 320, 220 \times 440]$ will be omitted.

VOF and CLSVOF anticipate bubble sizes that are almost identical, but the forms of the bubbles and the curvatures of the bottoms vary. A low-pressure region is formed in the wake of the rising bubbles as a result of the separation and rise of the bubbles. It generates vorticities at the sharp corners of bubbles and affects the bottom curvature.

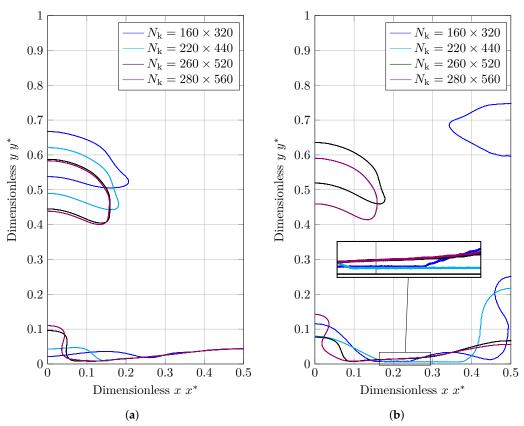


Figure 12. Bubble shape in 2D film boiling benchmark case at a specific height for different grid structures of $N_k = [160 \times 320, 220 \times 440, 260 \times 520, 280 \times 560]$). (a) VOF; (b) CLSVOF.

The space-averaged Nusselt number over dimensionless time is shown in Figure 13a,b. The thickness of the film has a significant impact on the Nusselt number. When the vapor layer is thin, the heat flux is larger, and when the film is thick, the heat flux is lower. As the vapor pushes to fill the bubble, the residual layer thins, increasing the average heat flux and Nusselt number; however, following detachment, the vapor returns to the superheated wall and the film thickness increases, leading to a lower Nusselt number.

Nanomaterials **2022**, 12, 2228 16 of 21

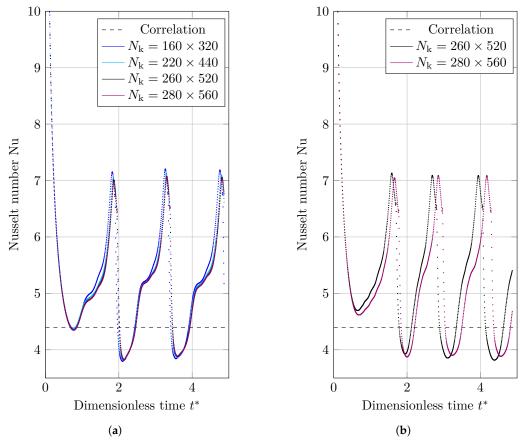


Figure 13. Nusselt number data for the 2D film boiling benchmark scenario that are spatially averaged. The horizontal dashed line is showing the Berenson correlation Nusselt number. (a) VOF; (b) CLSVOF.

In order to perform an individual investigation on the Nusselt number results, the difference between the mean Nusselt number calculated by Berenson correlation (Equation (31)) and time-averaged Nusselt number is presented for VOF and CLSVOF in different studied grid structures (Figure 14). In this case, the error for the time-averaged Nusselt number ($e_{\rm Nu}$) is defined by equation

$$e_{\text{Nu}} = \frac{\sum_{i=1}^{N_{\delta t}} \frac{\text{Nu}_{\text{num},i} - \text{Nu}_{\text{cor}}}{\text{Nu}_{\text{cor}}}}{N_{\delta t}},$$
(32)

where $N_{\delta t}$ is the number of time intervals, Nu_{num,i} mean Nusselt number in the *ith* time step and Nu_{cor} is the Nusselt number calculated by Berenson correlation. As demonstrated in Figure 14, the error generated by CLSVOF is less than VOF. The rate of convergence (Equation (16)) between the finest grid structures ($N_{\rm k} = [260 \times 520, 280 \times 560]$) are 0.05 and 0.4 for VOF and CLSVOF, respectively, showing a better convergence for CLSVOF method.

We evaluated the computing time for a bubble separation duration in order to examine the computational time. The bubble detachment period is defined as the time between the detachment of two consecutive bubbles from the vapor film. The computational time study is shown by dashed lines in Figure 10. As can be seen, the VOF method delivers faster computation than CLSVOF for the detachment of one bubble.

Nanomaterials **2022**, 12, 2228 17 of 21

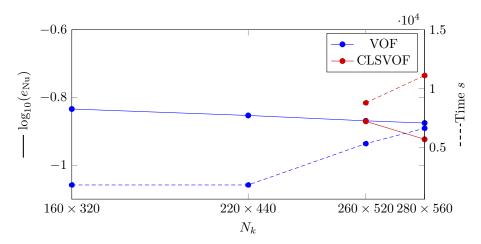


Figure 14. (Solid lines) Logarithmic representation of the error in which e_{Nu} is the L2 norm of error for Nusselt number calculation. (Dashed lines) Computation time study for 2D film boiling using VOF and CLSVOF techniques at various grid sizes.

4. Conclusions

Both OpenFOAM's default thermally induced phase change solver and prior studies on flow boiling of nanofluids employ VOF to capture the interface; however, this technique calculates less precise gas-liquid curvature, resulting in less accurate results. Given that several studies in the literature have identified level-set as a way for precisely calculating curvature, we combined VOF with level-set (called CLSVOF) and attempted to regain accuracy in simulation results. We have presented quantitative validations of the CLSVOF method versus VOF using a self developed solver. The impact of nanoparticles on the base fluid are considered using empirical equations from the literature. Four scenarios were utilized as test cases. The first test case is the evaporation by heat conduction problem (a one-dimensional evaporation problem); the second is the condensation by heat conduction (also a one-dimensional condensation problem); the third is condensation on a vertical plate (a two-dimensional condensation problem); the fourth is film boiling (a 2D boiling problem). These four test cases were chosen to illustrate a variety of thermal phase transition events. To conclude the benchmark study on these cases, we present Figure 15, which illustrates the performance of the VOF and CLSVOF methods in terms of accuracy, computation time, and convergence rate. As seen in Figure 15, the CLSVOF methodology outperforms or is similar to the VOF method in terms of both accuracy and convergence rate, albeit at the expense of computing time. We can observe that there are no accuracy benefits when simulating 1D benchmark situations with CLSVOF. This is because the curvature in these 1D cases is zero and the improved curvature computation is the basis for CLSVOF's superior accuracy performance.

Nanomaterials **2022**, 12, 2228 18 of 21

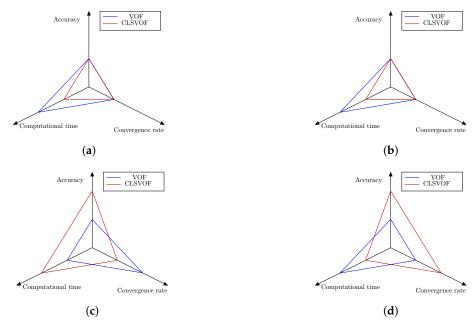


Figure 15. The accuracy, computing time, and convergence rate of the VOF and CLSVOF techniques are shown graphically for four thermally driven phase change benchmark scenarios. Each axis, as indicated, represents a research region and contains two values. If one of the techniques has greater performance in that region, the second value is allocated to that approach, while the first method will receive the first value. (a) Stefan problem; (b) the condensation by heat conduction; (c); 2D vertical film condensation; (d) 2D film boiling.

Author Contributions: Conceptualization, A.Y., A.S.B. and H.S.; Data creation, A.Y.; Formal analysis, A.Y.; Investigation, A.Y.; Methodology, A.Y., A.S.B. and H.S.; Software, A.Y.; Supervision, A.S.B., K.O. and H.S.; Validation, A.Y.; Visualization, A.Y.; Writing—original draft, A.Y.; Writing—review editing, A.S.B., K.O. and H.S. All authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by the Department of Energy, in Aalborg University, Aalborg, Denmark.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Not applicable.

Acknowledgments: I would like to thank Jakob Hærvig for all of his helpful suggestions and feedback while I was working on this essay. His generosity in donating his time is much appreciated.

Conflicts of Interest: Authors declares no conflict of interest.

Nomenclature

VOF Volume of Fluid **CSF** Continuum Surface Force Time t U Velocity Pressure р Gravitational acceleration g F Surface tension forces Transferred mass m

T Temperature

c Specific heat

k Thermal conductivity

Nanomaterials **2022**. 12, 2228 19 of 21

- R Universal gas constant
- *h* Latent heat
- M Molecular weight
- V Volume of the cell
- C Compressive factor
- Surface vector
- N Number
- e error
- R convergence rate
- Ca Capillary number
- Ja Jakob number
- Nu Nusselt number
- La Laplace number
- Cp Dimensionless pressure coefficient
- ρ Density
- au Deviatoric viscous stress tensor
- *α* Volume fraction
- γ Evaporation coefficient
- *μ* Dynamic viscosity
- κ Interface curvature
- δ Film thickness
- p constant pressure
- l liquid
- v vapor
- sat saturation
- sup supersaturation
- sub subsaturation
- rgh without the hydrostatic pressure
- tot total
- m mixture
- c compressive
- α volume fraction
- σ capillary
- f cell face
- k nodes in the domain num numerical results
- ana analytical results
- δ film thickness
- T temperature
- Nu nusselt number
- * dimensionless
- " flux rate

References

- 1. Alrbee, K.; Muzychka, Y.S.; Duan, X. Heat Transfer enhancement in laminar Graetz and Taylor Flows using nanofluids. In Proceedings of the International Conference on Nanochannels, Microchannels, and Minichannels, Dubrovnik, Croatia, 10–13 June 2018; Volume 51197, p. V001T02A021.
- 2. Sarafraz, M.M.; Tlili, I.; Tian, Z.; Khan, A.R.; Safaei, M.R. Thermal analysis and thermo-hydraulic characteristics of zirconia–water nanofluid under a convective boiling regime. *J. Therm. Anal. Calorim.* **2020**, *139*, 2413–2422. [CrossRef]
- 3. Sujun, D.; Jiang, H.; Yongqi, X.I.E.; Xiaoming, W.; Zhongliang, H.U.; Jun, W. Experimental investigation on boiling heat transfer characteristics of Al₂O₃-water nanofluids in swirl microchannels subjected to an acceleration force. *Chin. J. Aeronaut.* **2019**, 32, 1136–1144.
- 4. Choi, S.U.S.; Eastman, J.A. *Enhancing Thermal Conductivity of Fluids with Nanoparticles*; Technical Report; Argonne National Lab. (ANL): Argonne, IL, USA, 1995.
- 5. Alarifi, I.M.; Alkouh, A.B.; Ali, V.; Nguyen, H.M.; Asadi, A. On the rheological properties of MWCNT-TiO₂/oil hybrid nanofluid: An experimental investigation on the effects of shear rate, temperature, and solid concentration of nanoparticles. *Powder Technol.* **2019**, 355, 157–162. [CrossRef]

Nanomaterials **2022**, 12, 2228 20 of 21

 Siahmargoi, M.; Rahbar, N.; Kargarsharifabad, H.; Sadati, S.E.; Asadi, A. An Experimental Study on the Performance Evaluation and Thermodynamic Modeling of a Thermoelectric Cooler Combined with Two Heatsinks. Sci. Rep. 2019, 9, 20336. [CrossRef] [PubMed]

- 7. Lyu, Z.; Asadi, A.; Alarifi, I.M.; Ali, V.; Foong, L.K. Thermal and Fluid Dynamics Performance of MWCNT-Water Nanofluid Based on Thermophysical Properties: An Experimental and Theoretical Study. *Sci. Rep.* **2020**, *10*, 5185. [CrossRef]
- 8. Rezaei, A.; Abdollahi, H.; Derikvand, Z.; Hemmati-Sarapardeh, A.; Mosavi, A.; Nabipour, N. Insights into the effects of pore size distribution on the flowing behavior of carbonate rocks: Linking a nano-based enhanced oil recovery method to rock typing. *Nanomaterials* **2020**, *10*, 972. [CrossRef]
- 9. Razavirad, F.; Shahrabadi, A.; Dehkordi, P.B.; Rashidi, A. Experimental pore-scale study of a novel functionalized iron-carbon nanohybrid for enhanced oil recovery (EOR). *Nanomaterials* **2022**, *12*, 103. [CrossRef]
- 10. Ahmadi, A.A.; Arabbeiki, M.; Ali, H.M.; Goodarzi, M.; Safaei, M.R. Configuration and optimization of a minichannel using water–alumina nanofluid by non-dominated sorting genetic algorithm and response surface method. *Nanomaterials* **2020**, *10*, 901. [CrossRef]
- 11. Tirandazi, B.; Yahyaee, A.; Kianpour, M; Shahhosseini, S.; Experimental investigation and modeling of viscosity effect on carbon dioxide absorption using sodium hydroxide. *J. Environ. Chem. Eng.* **2017**, *5*, 2597. [CrossRef]
- 12. Jamei, M.; Olumegbon, I.A.; Karbasi, M.; Ahmadianfar, I.; Asadi, A.; Mosharaf-Dehkordi, M. On the Thermal Conductivity Assessment of Oil-Based Hybrid Nanofluids using Extended Kalman Filter integrated with feed-forward neural network. *Int. J. Heat Mass Transf.* 2021, 172, 121159. [CrossRef]
- Asadi, A.; Bakhtiyari, A.N.; Alarifi, I.M. Predictability evaluation of support vector regression methods for thermophysical properties, heat transfer performance, and pumping power estimation of MWCNT/ZnO-engine oil hybrid nanofluid. *Eng. Comput.* 2021, 37, 3813–3823. [CrossRef]
- Jamei, M.; Karbasi, M.; Mosharaf-Dehkordi, M.; Adewale Olumegbon, I.; Abualigah, L.; Said, Z.; Asadi, A. Estimating the density
 of hybrid nanofluids for thermal energy application: Application of non-parametric and evolutionary polynomial regression
 data-intelligent techniques. Meas. J. Int. Meas. Confed. 2022, 189, 110524. [CrossRef]
- 15. Rashidi, M.M.; Sadri, M.; Sheremet, M.A. Numerical simulation of hybrid nanofluid mixed convection in a lid-driven square cavity with magnetic field using high-order compact scheme. *Nanomaterials* **2021**, *11*, 2250. [CrossRef] [PubMed]
- Sadabadi, H.; Nezhad, A.S. Nanofluids for performance improvement of heavy machinery journal bearings: A simulation study. Nanomaterials 2020, 10, 2120. [CrossRef]
- 17. Al-Yaari, A.; Ching, D.L.C.; Sakidin, H.; Muthuvalu, M.S.; Zafar, M.; Alyousifi, Y.; Saeed, A.A.H.; Bilad, M.R. Thermophysical Properties of Nanofluid in Two-Phase Fluid Flow through a Porous Rectangular Medium for Enhanced Oil Recovery. *Nanomaterials* **2022**, *12*, 1011. [CrossRef]
- 18. Gul, T.; Qadeer, A.; Alghamdi, W.; Saeed, A.; Mukhtar, S.; Jawad, M. Irreversibility analysis of the couple stress hybrid nanofluid flow under the effect of electromagnetic field. *Int. J. Numer. Methods Heat Fluid Flow* **2021**, *32*, 642-659. [CrossRef]
- 19. Yahyaee, A.; Bahman, A. S.; Sørensen, H. A Benchmark Evaluation of the isoAdvection Interface Description Method for Thermally–Driven Phase Change Simulation. *Nanomaterials* **2022**, *12*, 1665. [CrossRef]
- 20. Nujukambari, A.Y.; Bahman, A.S.; Hærvig, J.; Sørensen, H. A Review: New Designs of Heat Sinks for Flow Boiling Cooling. In Proceedings of the 25th International Workshop on Thermal Investigations of ICs and Systems (THERMINIC), Lecco, Italy, 25–27 September 2019; pp. 1–6.
- 21. Hadavand, M.; Yousefzadeh, S.; Akbari, O.A.; Pourfattah, F.; Nguyen, H.M.; Asadi, A. A numerical investigation on the effects of mixed convection of Ag-water nanofluid inside a sim-circular lid-driven cavity on the temperature of an electronic silicon chip. *Appl. Therm. Eng.* **2019**, *162*, 114298. [CrossRef]
- 22. Yahyaee, A.; Bahman, A.S.; Blaabjerg, F. A Modification of Offset Strip Fin Heatsink with High-Performance Cooling for IGBT Modules. *Appl. Sci.* **2020**, *10*, 1112. [CrossRef]
- 23. Hirt, C.W.; Nichols, B.D. Volume of fluid (VOF) method for the dynamics of free boundaries. *J. Comput. Phys.* **1981**, 39, 201–225. [CrossRef]
- 24. Omar, S. Development of a Hyperbolic Equation Solver and the Improvement of the School of Engineering. Ph.D. Thesis, Cardiff University, Cardiff, UK, 2018.
- 25. Soleimani, A.; Sattari, A.; Hanafizadeh, P. Thermal analysis of a microchannel heat sink cooled by two-phase flow boiling of Al2O3 HFE-7100 nanofluid. *Therm. Sci. Eng. Prog.* **2020**, 20, 100693. [CrossRef]
- 26. Zhang, J.; Li, S.; Wang, X.; Sundén, B.; Wu, Z. Numerical studies of gas-liquid Taylor flows in vertical capillaries using CuO/water nanofluids. *Int. Commun. Heat Mass Transf.* **2020**, *116*, 104665. [CrossRef]
- 27. Rabiee, R.; Désilets, M.; Proulx, P.; Ariana, M.; Julien, M. Determination of condensation heat transfer inside a horizontal smooth tube. *Int. J. Heat Mass Transf.* **2018**, 124, 816–828. [CrossRef]
- 28. Yahyaee, A.; Hærvig, J.; Bahman, A.S.; Sørensen, H. Numerical Simulation of Boiling in a Cavity. In Proceedings of the 26th International Workshop on Thermal Investigations of ICs and Systems (THERMINIC), Berlin, Germany, 23–25 September 2020; pp. 1–5.
- 29. Abedini, E.; Zarei, T.; Rajabnia, H.; Kalbasi, R.; Afrand, M. Numerical investigation of vapor volume fraction in subcooled flow boiling of a nanofluid. *J. Mol. Liq.* **2017**, 238, 281–289. [CrossRef]

Nanomaterials **2022**, 12, 2228 21 of 21

30. Osher, S.; Sethian, J.A. Fronts propagating with curvature-dependent speed: Algorithms based on Hamilton-Jacobi formulations. *J. Comput. Phys.* **1988**, 79, 12–49. [CrossRef]

- 31. Dhir, V.K.; Purohit, G.P. Subcooled film-boiling heat transfer from spheres. Nucl. Eng. Des. 1978, 47, 49–66. [CrossRef]
- 32. Dhir, V.K. Boiling heat transfer. Annu. Rev. Fluid Mech. 1998, 30, 365–401. [CrossRef]
- 33. Dhir, V.K. Numerical simulations of pool-boiling heat transfer. AIChE J. 2001, 47, 813–834. [CrossRef]
- 34. Dhir, V.K.; Warrier, G.R.; Aktinol, E. Numerical Simulation of Pool Boiling: A Review. J. Heat Transf. 2013, 135, 061502. [CrossRef]
- 35. Gibou, F.; Chen, L.; Nguyen, D.; Banerjee, S. A level set based sharp interface method for the multiphase incompressible Navier–Stokes equations with phase change. *J. Comput. Phys.* **2007**, 222, 536–555. [CrossRef]
- 36. Tanguy, S.; Ménard, T.; Berlemont, A. A level set method for vaporizing two-phase flows. *J. Comput. Phys.* **2007**, 221, 837–853. [CrossRef]
- 37. Sato, Y.; Ničeno, B. A sharp-interface phase change model for a mass-conservative interface tracking method. *J. Comput. Phys.* **2013**, 249, 127–161. [CrossRef]
- 38. Sussman, M.; Puckett, E.G. A coupled level set and volume-of-fluid method for computing 3D and axisymmetric incompressible two-phase flows. *J. Comput. Phys.* **2000**, *162*, 301–337. [CrossRef]
- 39. Yu, C.H.; Wen, H.L.; Gu, Z.H.; An, R.D. Numerical simulation of dam-break flow impacting a stationary obstacle by a CLSVOF/IB method. *Commun. Nonlinear Sci. Numer. Simul.* **2019**, 79, 104934. [CrossRef]
- 40. Bahreini, M.; Derakhshandeh, J.F.; Ramiar, A.; Dabirian, E. Numerical study on multiple bubbles condensation in subcooled boiling flow based on CLSVOF method. *Int. J. Therm. Sci.* **2021**, *170*, 107121. [CrossRef]
- 41. Chen, B.; Wang, B.; Mao, F.; Tian, R.; Lu, C. Analysis of liquid droplet impacting on liquid film by CLSVOF. *Ann. Nucl. Energy* **2020**, *143*, 107468. [CrossRef]
- 42. Nemati, H.; Breugem, W.P.; Kwakkel, M.; Jan Boersma, B. Direct numerical simulation of turbulent bubbly down flow using an efficient CLSVOF method. *Int. J. Multiph. Flow* **2021**, *135*, 103500. [CrossRef]
- 43. Tanasawa, I. Advances in condensation heat transfer. In *Advances in Heat Transfer*; Elsevier: Amsterdam, The Netherlands, 1991; Volume 21, pp. 55–139.
- 44. Pak, B.C.; Cho, Y.I. Hydrodynamic and heat transfer study of dispersed fluids with submicron metallic oxide particles. *Exp. Heat Transf. Int. J.* **1998**, *11*, 151–170. [CrossRef]
- 45. Hamilton, R.L.; Crosser, O.K. Thermal conductivity of heterogeneous two-component systems. *Ind. Eng. Chem. Fundam.* **1962**, 1, 187–191. [CrossRef]
- 46. Xuan, Y.; Roetzel, W. Conceptions for heat transfer correlation of nanofluids. *Int. J. Heat Mass Transf.* **2000**, 43, 3701–3707. [CrossRef]
- 47. Zhu, D.S.; Wu, S.Y.; Wang, N. Surface tension and viscosity of aluminum oxide nanofluids. AIP Conf. Proc. 2010, 1207, 460–464.
- 48. Samkhaniani, N.; Ansari, M.R. Numerical simulation of bubble condensation using CF-VOF. *Prog. Nucl. Energy* **2016**, *89*, 120–131. [CrossRef]
- 49. Shin, S.; Choi, B. Numerical simulation of a rising bubble with phase change. Appl. Therm. Eng. 2016, 100, 256–266. [CrossRef]
- 50. Rajkotwala, A.H.; Panda, A.; Peters, E.A.; Baltussen, M.W.; van der Geld, C.W.; Kuerten, J.G.; Kuipers, J.A. A critical comparison of smooth and sharp interface methods for phase transition. *Int. J. Multiph. Flow* **2019**, 120, 103093. [CrossRef]
- 51. Nusselt, W. Die oberflachenkondensation des wasserdamphes. VDI-Zs 1916, 60, 541.
- 52. Samkhaniani, N.; Ansari, M.R. The evaluation of the diffuse interface method for phase change simulations using OpenFOAM. *Heat Transf.—Asian Res.* **2017**, *46*, 1173–1203. [CrossRef]
- 53. Berenson, P.J. Film-boiling heat transfer from a horizontal surface. *J. Heat Transf.* **1961**, *83*, 351–356. [CrossRef]