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Online Detection and Estimation of Grid Impedance Variation for Distributed Power Generation

Manel Jebali-Ben Ghorbal*, Walid Ghziat†, Ilhem Slama-Belkhodja‡ and Josep M. Guerrero§

*†‡University of Tunis El Manar, ENIT-L.S.E, BP 37-1002, Tunis le Belvédère, Tunisie
* Email: maneljebali2001@yahoo.fr, † Email: ghziaiwalid@gmail.com, ‡ Email: ilhem.slama@enit.rnu.tn
§ Dept. Energy Technology, Aalborg University, 9220 Aalborg, Denmark
Technical University of Catalonia, 08036 Barcelona, Spain, Email: joz@et.aau.dk

Abstract—A better knowledge of the grid impedance is essential in order to improve power quality and control of the Distributed Power Generation Systems (DPGS) and also for a safe connection or reconnection to the utility grid. An LCL-filter associated to a Voltage Source Inverter (VSI) is usually used in DPGS based on renewable energy. The VSI controller is used to determine the grid impedance in both healthy operation and faulty modes. When grid faults occurrence, the grid impedance variations have a considerable influence on the control and the stability of the system, even on the decision to disconnect the DPGS systems of the network. This work presents a rapid and simple technique to detect the grid impedance variation and to determine the grid impedance before and after grid faults occurs. Implementation on FPGA control board, simulations and experimental results are presented to validate the described method.

I. INTRODUCTION

The Distributed Power Generation Systems (DPGS) are gaining popularity due to their contribution to feed the grid with renewable energy. They need smart interfaces between the operator and the network to improve power quality and to satisfy the costumers need in energy. This is the reason why grid information is of primer importance when connecting the DG system to the utility network. Indeed, a grid impedance variation has an effect on the stability of the system [1], and on the current control loop of a Voltage Source Inverter (VSI) [2]. The grid impedance information can also detect a grid failure and be useful to prevent the DG from other complications such as the islanding operation. In the litterature, several methods were discussed, for grid impedance variation detection or grid impedance estimation [3], [4], [5]. These methods can be classified into three categories:

- Methods using control loop variations to estimate resistive and inductive parts of the grid impedance to include them into the control to improve its performances [6].
- Methods using harmonic injection signal into the system, then use mathematical methods to analyse the output signal in order to determine the grid impedance [7], [9], [12], and [13].
- Methods using extra devices for the grid impedance estimation purpose [8].

In previous studies focusing on grid impedance calculation methods using inter-harmonic injection signal, the grid parameters are extracted from current and voltage responses at the point of common coupling (PCC). These methods complied with hardware limitations and have the real advantage to be embedded in a PV-inverter platform. However, to obtain a good accuracy, the best knowledge of the background environment is required, in order to subtract background voltage noises from the obtained voltage response. For this purpose, dedicated A/D hardware devices and sensible sensors are required [14]. Another work in the same field investigated an inter-harmonic voltage injection within the digital processor instead of the grid voltage [2]. The main drawback of this method is that the disturbance, repetitive or not, should be carefully chosen in terms of amplitude, duration and frequency to avoid negative effect on the THD of the grid. Another method described in [15] discussed the variation of the inductive part of the grid impedance $L_g$ on the current controller, and proposed an $L_g$ estimator by exciting the LCL-filter. However, this method did not take into consideration the resistive part of the grid $R_g$.

The method presented in this paper is from the first group of classification methods. Its principle consists on detecting fault occurrence using temporal redundancies of current measurements, and then estimating the impedance variation by leading the system to resonance. To avoid resonance and its negative effect, the algorithm is stopped as soon as the resonance is reached from one hand, and from the other hand a passive damping is used to achieve the stability of system and to reduce the effect of resonance phenomenon. Note that there are two damping methods: passive damping consisting on adding a resistor in series with the LCL-filter capacitance and active damping which is carried out by implementing a virtual resistor in the control strategy in order to avoid reducing the efficiency of system.

II. PRINCIPLE OF THE PROPOSED METHOD

A. Studied system

The studied system topology is shown in Fig. 1. The grid is connected to a pulsewidth-modulation (PWM) Voltage-Source Inverter (VSI) with a low-pass LCL-filter and the grid is presented by a single phase sinusoidal voltage source with an impedance $Z_g$. The impedance of the grid incorporates a resistive part $R_g$ and an inductive part $L_g$. The LCL-filter is choosen especially due to its ability to operate as well in islanded mode as in grid connected mode which is a significant advantage for DPGS applications. Besides, as with L-filter, high frequency current harmonics can be limited with the use...
of the LCL-filter. The main issue to be taken into account when adopting the LCL-filter solution is its resonance. It’s worth to say that the grid background disturbances has a great impact on the LCL resonance frequency. Indeed, this point was investigated in the proposed method to calculate the grid inductive part of the impedance.

**B. Grid Impedance model and principle of the method**

Several grid models have been proposed in the literature [10], [11]. Each model was trying to describe the grid harmonic behavior with a different level of complexity. For example, the authors in [9] considered the grid as a cascaded Z-blocks. Each block involves a resistive and inductive parts, a capacitive part which presents the consumer side of the grid and an ideal source supply denote $V_s$. In this work, we consider the simplest grid model, a series inductive-resistive branch as shown in Fig. 2. The total grid impedance is then $Z_g = R_g + j\omega L_g$ and $V_g$ is an ideal source supply. The output VSI-voltage is denoted $V_o$.

The principle of the method of detection and estimation of grid impedance is depicted in Fig. 3. As it is detailed in the subsection (C), the LCL-filter excitation allows the determination of the grid inductance parameter $L_g$, then, a residual based of current measurement is continuously calculated. When its value becomes higher than a predefined threshold, so when a grid fault is detected, the system is driven near the resonance to perform a new calculation of $L_g$ parameter value. The knowledge of $L_g$ value and residual measurements, before and after fault occurrence, allow to calculate grid resistance value $R_g$.

**C. PR-controller design and grid impedance estimation method**

First, the influence of the inductive part of the grid on the LCL filter is discussed. Fig. 4 shows the block diagram of the PR regulator where $s$ is the Laplace operator, $K_{PWM}$ the gain of the inverter and $T_{PWM}$ the control delay. For calculation simplifications consideration, the resistive part is neglected. The transfer function of the VSI closed loop output voltage $V_o$ to the grid current $I_g$ can be expressed as

$$
\frac{I_g}{V_o} = \frac{1}{L_f s} \left( \frac{R_d}{L_2 + L_0} + \frac{s^2 + \omega_{res}^2 R_d s + \omega_{res}^2}{C_f} \right)
$$

being

$$
Z_j^2 = \frac{1}{C_f(L_2 + L_0)}
$$

$$
\omega_{res} = \sqrt{\frac{L_f + (L_2 + L_0)}{L_f C_f (L_2 + L_0)}}
$$

From (2), the expression of the resonance frequency of the LCL filter is deduced. Hence, an increase in the inductive grid part impedance leads to a decrease in the resonance frequency of the LCL-filter as is shown in Fig. 5. The resonance frequency should be of the following range

$$
10\omega_g < \omega_{res} < \frac{\omega_{PWM}}{2}
$$
being $\omega_g$ the grid frequency and $\omega_{PWM}$ the switching frequency which is usually chosen between 1Khz and 20Khz. The bode plot of the transfer function from inverter output voltage $V_o$ to the grid current $i_g$ (1) of Fig. 6 is drawn for two different values of $L_g$. A first spike is shown for $L_g = 1.5mH$ and a second one for $L_g = 4.5mH$.

\[ \hat{L}_g = \frac{(L_2 + L_f) - (4\pi^2 L_f C f_s L_2 f_{res}^2)}{(4\pi^2 L_f C f_s f_{res}^2 - 1)} \]

being $\hat{L}_g$ the estimated grid inductance.

![Fig. 5. Influence of $L_g$ variations on the resonance frequency $f_{res}$.](image)

![Fig. 6. Bode diagram of the transfer function of $V_o$ to $i_g$.](image)

The grid impedance value is then derived from the resonance frequency of the LCL-filter expressed in (2). Several methods have been proposed for the excitation of the LCL-filter [2], [12], [15], and various types of approach are mentioned to reach the resonance. In our case, the method increases the proportional gain of the PR regulator $K_p$ until the roots move close to the right-half plane that’s to say the instability region. Fig. 7 shows the migration of these resonant poles with the increase of $K_p$.

As the proportional gain is incremented, the system stability margin is progressively reduced to zero. It is noticeable that every stage needs a speacial period, denoted $T_{FFT}$, to make it possible to calculate the Fourier Transform of the obtained current signal. Having the resonant frequency of the system, the grid inductance can be consequently deduced as follows.

![Fig. 7. Root locus of the PR-controlled system for two values of $K_p$.](image)

**D. Grid Impedance Variation Detection Method**

The method is based on the dynamic space parity approach, and more precisely on the temporal redundancies of current measurement. Theoretical developments are given in [16], and their application to fault detection and isolation (FDI) of faulty sensor in electrical drives has been experimentally demonstrated. In addition to the mathematical developments, the principle can be simply explained: in healthy conditions, with constant grid impedance, with a very low measurement sampling time, $T_a$, the difference between two consecutive measurements remains lower than a calculated threshold.
When a grid impedance variation occurs, this difference increases and the defined residual becomes higher than the threshold. The residual $Res_{igk}$ is defined by (5) and (6).

$$Res_{igk} = r_k + r_{k-1} + r_{k-2} \quad (5)$$

$$r_k = |i_{g_k} - 2i_{g_{k-1}} + i_{g_{k-2}}| \quad (6)$$

where $i_{g_k}$, $i_{g_{k-1}}$, $i_{g_{k-2}}$ are the measured current at $kT_a$, $(k-1)T_a$ and $(k-2)T_a$ respectively.

As the measured current waveform is sinusoidal, an analytical expression of the maximum value of $Res_{igk}$ is performed [16] and leads to the threshold expressed by (7).

$$\begin{align*}
\varepsilon &= 3\omega^2T_a^2I_m \\
I_m &= \frac{V_{om} - V_{gm}}{|Z_g|}
\end{align*} \quad (7)$$

with $\omega = \frac{2\pi}{T_a}$, $\tau_s$ is the system time constant, $V_{om}$ the maximum VSI output voltage, $V_{gm}$ the maximum grid voltage and $|Z_g|$ is the grid impedance amplitude. As $L_g$ was estimated as explained before, $R_g$ can be deduced using (7) as follows:

$$\hat{R}_g = \sqrt{\frac{9\omega^4T_a^4}{\varepsilon^2} (V_{om} - V_{gm})^2 - (\omega L_g)^2} \quad (8)$$

However, if the grid impedance increases or decreases, the current residual measurement $Res_{igk}$ changes. As the residual value in healthy mode is denoted by $\varepsilon_h$ and by $\varepsilon_f$ in faulty mode, the grid impedance variation is calculated as shown in (10).

$$|\Delta Z| = \frac{k_f}{\varepsilon_f} - \frac{k_h}{\varepsilon_h} \quad (9)$$

$$\begin{align*}
|\Delta Z| &= 3\omega^2T_a^2(E_m - V_{gm})(\frac{1}{\varepsilon_f} - \frac{1}{\varepsilon_h}) \\
|\Delta Z| &= |Z_f| - |Z_h|
\end{align*} \quad (10)$$

III. SIMULATIONS RESULTS

Simulations were carried out using Matlab and PSIM softwares. The method described above for detection and estimation of grid impedance variation is tested on a 2.5kW single phase inverter. The system’s parameters are given in Table I. The grid resistance $R_g$ is set to 0.673Ω and the $L_g$ to 1.5mH. The variation of the grid impedance $Z_g$ is simulated by inserting a variable fault impedance $Z_d = R_d + j\omega L_d$, controlled by a switching gate block. For more clarity, in healthy mode, the grid impedance variation is null ($Z_d = 0$) so the total grid impedance is equal to $Z_{g1}$. Then, as the switch gate is opened, at the fault instant, the grid impedance varies according to (11). Fig. 8 presents the grid current evolution as the incrementation of $k_p$ is proceeding from 17 to 31. The figure shows the tendency of the system to be unstable as the current $i_g$ increased gradually until reaching the resonance. As can be seen, the residual value exceeds its threshold as the resonance phenomena occurs, and presents a peak at the instant of fault, i.e at 0.53s.

$$Z_g = Z_{g1} + Z_d \quad (11)$$

<table>
<thead>
<tr>
<th>TABLE I SYSTEM PARAMETERS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Parameter and designation</td>
</tr>
<tr>
<td>Inverter nominal power $P_N$</td>
</tr>
<tr>
<td>Filter inductance $L_f$</td>
</tr>
<tr>
<td>Filter capacitance $C_f$</td>
</tr>
<tr>
<td>Power width modulation switching frequency $f_{PWM}$</td>
</tr>
<tr>
<td>DC voltage bus $V_{DC}$</td>
</tr>
<tr>
<td>Grid voltage $V_g$</td>
</tr>
<tr>
<td>Inverter gain $K_{PWM}$</td>
</tr>
<tr>
<td>Acquisition Time $T_a$</td>
</tr>
</tbody>
</table>

Fig.9(a) and Fig.9(b) show the grid current residual measurement for two different values of $Z_d$. In these figures, the residual amplitude increases according the the grid impedance variation. Nevertheless, it remains so high comparing with its value in healthy mode. The details in Fig. 10 shows the similarity between theory and simulations. The acquisition time for simulation is chosen equal to 5µs and the residual signal lasts $4T_a = 20\mu s$ as explained in [16]. After detecting a grid fault occurrence, a Fast Fourier Transformation can be be done in order to determine the resonance frequency $f_{res}$. Fig. 11(a) and Fig. 11(b) shows the measured grid current FFT for two grid impedance values. In fact, in Fig. 11(a), there is no grid impedance variation, so the total grid inductance is equal to $Z_{g1}$. However, in Fig. 11(b), the grid impedance increases to $3Z_{g1}$ (11). Table II gives the error of $R_g$ and for $L_g$ for different values of grid impedance with different $\frac{P}{f}$. 

Fig. 8. LCL-Resonance phenomenon of the grid current $i_g$ by the incrementation of $k_p$ (fault instant $T_f = 0.53s$).
TABLE II

<table>
<thead>
<tr>
<th>$\frac{\Delta r}{r}$ ratio</th>
<th>Real $L_g$ value</th>
<th>Estimated $L_g$ value</th>
<th>Error of $L_g$ in %</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.13</td>
<td>1.5 mH</td>
<td>1.44 mH</td>
<td>4</td>
</tr>
<tr>
<td>0.13</td>
<td>4.5 mH</td>
<td>4.40 mH</td>
<td>2.22</td>
</tr>
<tr>
<td>0.7</td>
<td>1.5 mH</td>
<td>1.47 mH</td>
<td>1.33</td>
</tr>
<tr>
<td>0.7</td>
<td>4.5 mH</td>
<td>4.42 mH</td>
<td>1.77</td>
</tr>
<tr>
<td>1.17</td>
<td>1.5 mH</td>
<td>1.47 mH</td>
<td>1.33</td>
</tr>
<tr>
<td>1.17</td>
<td>4.5 mH</td>
<td>4.47 mH</td>
<td>0.66</td>
</tr>
</tbody>
</table>

IV. EXPERIMENTAL RESULTS

The method of a grid impedance variation was tested on a three-phase-1.5kW Induction Machine. The FPGA target device used is Xilinx SPARTAN3 XCS400PQ208. It has 400,000 logical gates and a 50-MHz oscillator (20ns clock period). One of the three phase-current of the IM was measured using hall-effect sensors (LEM 25NA). An interface board (ARCU3I) allows the voltage level adaptation between the LEMs sensors and the ADC interface (2.5V/20A). An Analog-Digital 12-bit-circuit (AD9221) is used for AD conversion of measured stator current, the computation time of the acquisition module is about 2.4$\mu$s. A 10-bits Digital-Analog (DA) converter circuit allowed viewing the current residual
measurement on a scope. In Fig. 12, experimental results of the current residual after a perturbation are shown. The perturbation was set in the FPGA program of the residual calculation. As the variation of the impedance occurs, the level of the residual measurement increases and presents a franc spike. The details in Fig. 13 depict the wave form of the residual that perfectly match with the simulation results. The acquisition time is set to 100µs which is higher than the real acquisition time but it allowed a good residual viewing on the scope. Experimental results are similar to simulations and demonstrate the effectiveness of the proposed method.

V. CONCLUSION

A novel technique for online detection and estimation of grid impedance variation is presented. A PR-controller for a grid-connected LCL-filter inverter is proposed. Simulations demonstrate the reliability of the method, due to the fact that it can be easily implemented and it respects the experimental background limitations. The main features of this method is that it gives accurate values of the impedance of the grid in both safe and faulty modes and can operate without network utility interruption in weak grid system. The error of the estimated inductive part of the grid is low enough to consider the method satisfactory.

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