Enhancing the Frequency Adaptability of Periodic Current Controllers for Grid-Connected Power Converters

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Abstract—It is mandatory for grid-connected power converters to synchronize the feed-in currents with the grid. Moreover, the power converters should produce feed-in currents with low total harmonic distortions according to the demands, by employing advanced current controllers, e.g., Proportional Resonant (PR) and Repetitive Controllers (RC). The synchronization is actually to detect the instantaneous grid information (e.g., frequency and phase of the grid voltage) for the current control, which is commonly performed by a Phase-Locked-Loop (PLL) system. As a consequence, harmonics and deviations in the estimated frequency by the PLL could lead to current tracking performance degradation, especially for the periodic signal controllers (e.g., PR and RC) of high frequency-dependency. In this paper, the impacts of frequency deviations induced by the PLL and/or the grid disturbances on the selected current controllers are investigated by analyzing the frequency adaptability of these current controllers. Subsequently, strategies to enhance the frequency-variation-immunity for the current controllers are proposed for the power converters to produce high quality feed-in currents even in the presence of frequency deviations. Experiments on a single-phase grid-connected inverter system are presented, which have verified the proposals and also the effectiveness of the frequency adaptive current controllers.

I. INTRODUCTION

Power electronics converters have been widely used in grid-connected renewable energy systems like wind turbine systems and PhotoVoltaic (PV) systems [1], [2]. However, due to their non-linearity and also the intermittency, harmonic challenges are also associated with the power electronics interfaced renewable energy systems, which have to be dealt with by employing advanced control strategies according to the demands [3]. Commonly, a two-cascaded control system is adopted in the grid-connected power converters [4]. Since the inner current controller of the cascaded loops is responsible for shaping the current (i.e., power quality issues), great efforts have been devoted to the control of the feed-in grid current, which is also required to be synchronized with the grid voltage. Phase Locked Loop (PLL) systems are widely used in the grid-connected inverters for synchronization [5]–[8]. Hence, the information (especially the grid frequency) provided by a PLL system is of importance for the current controllers, and it is extensively used at different levels of the entire control system (e.g., reference transformation).

The current control can be implemented in the rotating reference frame ($dq$), the stationary reference frame ($\alpha\beta$), or the three-phase natural reference frame ($abc$) [4], [9], [10]. Taking the control in the $dq$-frame for an example, Park and/or Clarke transforms enable the employment of Proportional Integrator (PI) controllers, where the PLL estimated grid frequency is a must for the transforms. Consequently, either frequency variations in the grid or the frequency estimation error by a PLL system will result in control degradations when using PI controllers. On the other hand, in order to simplify the control, periodic signal controllers like Repetitive Controller (RC) [11]–[15] and Proportional Resonant (PR) controller with parallel RESonant (RES) based harmonic compensators [4], [14], [16]–[18] are developed in either the $\alpha\beta$- or the $abc$-frame. In that case, the control accuracy of both the PR with RES or RC controllers is strongly affected by the designed center frequency of the resonant controller [12], [16]. Basically, the center frequency (e.g., the fundamental frequency – 50 Hz) should be placed at which the control gain can approach infinite, and a constant value is selected for simplicity. Thus, the frequency deviations will result in a finite control gain at the resonant frequencies.

Additionally, an online update of the center frequency is enabled by feeding back the PLL estimated frequency to the current controller in order to enhance the control performance. However, the grid voltage as the input of the PLL systems cannot always be maintained as “constant” in terms of amplitude, frequency, and/or phase, due to multiple eventualities like continuous connection and disconnection of loads and fault to ground because of lightning strikes [19], [20]. That is why the grid codes also demand that the power converters should be able to operate within a specified frequency range or even regulate the frequency [21]. Together with background distortions, a large obstacle has been posed for the PLL systems. As a result, the current controllers in the $\alpha\beta$- or the $abc$-frame will inevitably suffer from frequency deviations.
advanced synchronizations (e.g., PLL systems) are desirable, resulting in a possibility for the feed-in current to either due to the PLL errors or the grid disturbances [11], [12], [22], in order to ensure a reliable and satisfactory control of the grid current, and also it is essential to enhance the frequency adaptability of the periodic current controllers [13], [23]–[28].

In view of the above issues, in this paper, the frequency adaptability of the selected periodic current controllers (i.e., PR, RES, and RC) is explored in the consideration of the PLL estimated frequency variations owing to either the PLL inherent errors or the grid disturbances. In § II, a brief description of the dual-loop control method for single-phase grid-connected inverters is presented. Then, the frequency adaptability of the periodic current controllers is focused on. More important, solutions to enhance the frequency adaptability of these current controllers are also proposed, being the frequency adaptive current controllers. The discussions and the effectiveness of the frequency adaptive current controllers are verified by experiments in § IV before the conclusion.

II. FREQUENCY ADAPTABILITY ANALYSIS

A. Control of Single-Phase Grid-Connected Converters

Fig. 1 shows a typical configuration of a single-phase grid-connected system and its overall cascaded dual-loop control structure, where an LCL-filter is used considering the power quality issues [4]. It is shown in Fig. 1 that the PLL estimated grid frequency (ω pll) is feeding back to the current controller as aforementioned in order to improve the control performance. Especially, the frequency ω pll is used to transform AC quantities (i.e., the grid current i g and voltage v g) to DC quantities (i.e., i dq and v dq) for PI controllers in the dq-frame or reversely (dq → αβ). Yet for simplicity in the case of the current control in either the αβ- or the abc-frame, a fixed constant frequency (i.e., the nominal grid frequency ω g0) is designed for the periodic current harmonic controllers in practice (especially, when implemented in a digital signal processor), as it is shown in Fig. 2. In both cases, the current controller performance will be affected by the PLL estimated frequency, which is used to generate the grid current reference according to Fig. 1. Notably, other current controllers like the Dead-Beat (DB) control can also be used as the fundamental-frequency current controller [29], [30].

B. Frequency Sensitivity Analysis of the Current Controllers

In practice, it is difficult to attain an acceptable feed-in current even with high-order grid filters (e.g., an LCL-filter) because of the always existing background distortions in the grid voltage. Thus, harmonic compensators are typically incorporated in the current control loop, as it is shown in Fig. 2, where the fundamental-frequency current controller (i.e., G PR(s)) can be given as

\[
G_{PR}(s) = k_p + \frac{k_i s}{s^2 + \omega_0^2}
\]

in which \(k_p\) and \(k_i\) are the control gains. It can be seen in Fig. 2 that the harmonic compensator embraces either a paralleled multi-resonant controller \(G_{RES}(s)\) or a repetitive controller \(G_{RC}(s)\), which is effective only in the αβ-frame. Accordingly, the harmonic compensators can be expressed as

\[
G_{RES}(s) = \sum_{h=3,5,7,\ldots} G_{h RES}(s)
\]

\[
G_{RC}(s) = k_{rc} e^{-2\pi s / \omega g0} \frac{1}{1 - e^{-2\pi s / \omega g0}}
\]

where \(G_{h RES}(s)\) is the \(h\)th-order resonant controller with \(h\) being the harmonic order and \(k_{rc}\) is the control gain of the RC harmonic compensator. Furthermore, the individual resonant controller can be given as

\[
G_{h RES}(s) = \frac{k^h s}{s^2 + (h\omega g0)^2}
\]

in which \(k^h\) is the control gain of the corresponding \(h\)th-order resonant controller. In addition, the RC based harmonic controller can further be expanded into [30]

\[
G_{RC}(s) = k_{rc} \left[ \frac{\omega_0}{2\pi s} + \frac{\omega_0}{\pi} \sum_{k} \frac{s}{s^2 + (k\omega_0)^2} \right]
\]

with \(k = 1, 2, 3, \ldots\). Eq. (5) indicates the inherent resonant characteristic of the RC controller with an identical resonant
increases

frequency not be completely eliminated. In general, the PLL estimated with an advanced PLL system, the frequency deviations can be expressed as

\[ \omega_{\text{PLL}} = \omega_g + \Delta \omega \]

in which \( \Delta \omega = \Delta \omega_g + \Delta \omega_{\text{PLL}} \) represents the estimated angular frequency deviations. It consists of the grid frequency disturbances \( \Delta \omega_g = \omega_g - \omega_i \) with \( \omega_g \) being the instantaneous grid frequency and/or the PLL tracking errors \( \Delta \omega_{\text{PLL}} \). As discussed above, (1)-(5) and (7) imply that a small frequency variation (i.e., \( \Delta \omega \)) induced by the grid frequency changes and/or PLL estimation errors can contribute to a degradation of the error rejection capability for those current controllers, which are supposed to approach to infinite at the targeted frequencies (i.e., \( k \omega_{\text{PLL}} \)). This impact is referred to as the frequency adaptability, which is illustrated as the following.

According to (4) and (7), the magnitude response (i.e., \( s = j h \omega_{\text{PLL}} \)) of an individual resonant controller \( G^h_{\text{RES}}(s) \) at the corresponding frequency \( (h \omega_{\text{PLL}}) \) can be obtained as

\[ |G^h_{\text{RES}}(j h \omega_{\text{PLL}})| = \left| \frac{j k^h_{\text{RES}} h \omega_{\text{PLL}}}{-h^2 \omega_{\text{PLL}}^2 + h^2 \omega_0^2} \right| = \frac{k^h_{\text{RES}}}{h \omega_0} \frac{\delta + 1}{\delta^2 + 2 \delta} \]  

with \( \delta = \Delta \omega / \omega_0 \), and Eq. (8) indicates that the gain will not be infinite unless \( \delta = 0 \) (i.e., \( \Delta \omega = 0 \)). The control gain reduction of the resonant controllers due to the frequency variations \( \Delta \omega \) is illustrated in Fig. 4, where it can be observed that even a small frequency variation of \( \pm 0.2 \% \) can result in a significant performance degradation of the resonant controllers (e.g., the magnitude decreases from \( \infty \) dB to 48.5 dB). It demonstrates that the RES based harmonic compensator and also the PR controller with \( h = 1 \) is sensitive to frequency variations. In other words, the RES controller in (4) has a poor frequency-variation-immunity.

In the same manner, substituting \( s = j h \omega_{\text{PLL}} \) into (3) gives the magnitude response of the RC controller \( G_{\text{RC}} \) as

\[ |G_{\text{RC}}(j h \omega_{\text{PLL}})| = \left| \frac{k_{\text{RC}} e^{-j 2 \pi h (1 + \delta)}}{1 - e^{-j 2 \pi h (1 + \delta)}} \right| \]  

According to the Euler’s formula, the following is obtained

\[ |G_{\text{RC}}(j h \omega_{\text{PLL}})| = \frac{k_{\text{RC}}}{\sqrt{2 - 2 \cos(2 \pi h \delta)}} \]  

which implies that the RC controller no longer can approach infinite control gain when there is a frequency tracking error from the PLL system (and/or grid frequency changes), i.e., \( \delta \neq 0 \) and \( \Delta \omega \neq 0 \). Fig. 5 further illustrates the effect of a frequency deviation on the current control error rejection ability of the RC harmonic compensator. As it can be observed in Fig. 5, a remarkable gain drop (e.g., the magnitude decreases from \( \infty \) dB to 28.5 dB) occurs due to a frequency change of
normally implemented in a digital signal processor of a fixed back the PLL estimated frequency, since the RC controller is the case of a varying grid frequency. Tracking error), the current controllers have to be frequency good current control in terms of a zero-error elimination of and 5 is that the frequency sensitivity of the periodic current controllers (i.e., the PR, RES, and RC controllers) is poor, and thus enhancing the frequency adaptability is necessary in order to produce high-quality currents.

III. ENHANCING THE FREQUENCY ADAPTABILITY

As discussed in the last paragraph, in order to achieve a good current control in terms of a zero-error elimination of the harmonics even under a variable grid frequency (or a PLL tracking error), the current controllers have to be frequency adaptive. It means that the control gain should be infinite when $s = jh\omega_{\text{pp}}$. Thus, feeding back the frequency estimated by an advanced PLL system to the current controllers is a possibility to decrease the frequency sensitivity. This is much convenient for the resonant controllers [23]–[25], which is given as

$$G_{\text{RES}}^h(s) = \frac{k^h_i s}{s^2 + (h\omega_{\text{pp}})^2} = \frac{k^h_i s}{s^2 + [h(\omega_0 + \Delta\omega)]^2} \quad (11)$$

Fig. 6(a) shows the implementation of a frequency adaptive resonant controller. It can be observed in Fig. 6(a) and (11) that, by feeding in the PLL estimated frequency, the resonant frequencies of the harmonic controllers $G_{\text{RES}}^h(s)$ will automatically be adjusted to the instantaneous grid frequency. As a result, infinite gains of the resonant controllers are attained in the case of a varying grid frequency.

However, in respect to the RC controller, enhancing the frequency adaptability cannot be reached by simply feeding back the PLL estimated frequency, since the RC controller is normally implemented in a digital signal processor of a fixed sampling rate. In that case, the RC controller shown in (3) can be given as

$$G_{\text{RC}}(z) = \frac{k^i_{\text{RC}} z^{-(N+F)}}{1 - z^{-(N+F)}} \quad (12)$$

in which $N = \lfloor f_s/f \rfloor$ is an integer, $F = f_s/f - N$ is the order of a fractional delay (i.e., $z^{-F}$) with $f = \omega_{\text{pp}}/(2\pi)$, and $f_s$ is the sampling frequency. Therefore, to enhance the

frequency adaptability of the RC controller, one possibility is that the fractional delay $z^{-F}$ induced by the frequency variations should be appropriately approximated. A cost-effective approach to approximate the fractional delay is using Finite-Impulse-Response (FIR) filters as discussed in [12], [32]. It should be noted that, the frequency adaptability of the RC harmonic compensator can be enhanced alternatively by varying the sampling frequency [13], which should ensure an integer of $f_s/f$ (i.e., $F = 0$) in practical applications, but it will increase the cost and the overall complexity.

The most popular but simple and effective solution to the FIR fractional delay $z^{-F}$ is based on the Lagrange interpolating polynomial, which can be expressed as

$$z^{-F} \approx \sum_{l=0}^{L} \left( z^{-l} H_l \right) = \sum_{l=0}^{L} \left( z^{-l} \prod_{i=0}^{L} \frac{F-i}{l-i} \right) \quad (13)$$

where $H_l$ is the Lagrange interpolating polynomial coefficient, $l, i = 0, 1, 2, \ldots, L$, and $L$ is the length of the Lagrange interpolation based fractional delay filter. For convenience, the coefficients of the Lagrange based fractional delay filter $z^{-F}$ are given in Table I. If $L = 1$, Eq. (13) corresponds to a linear interpolation between two samples, i.e., $z^{-F} \approx H_0 + H_1 z^{-1}$. While in the case of $L = 3$, a cubic interpolating polynomial is formulated, i.e., $z^{-F} \approx H_0 + H_1 z^{-1} + H_2 z^{-2} + H_3 z^{-3}$, which has been proved in [12], [30], [32] as a relatively good and accurate approximation of the fractional delay $z^{-F}$ in terms of the bandwidth and also the resultant phase delay. Thus, it can be employed to enhance the frequency-variation-immunity of the RC controller. Following, the general block diagram of a frequency adaptive RC harmonic compensator can be constructed as shown in Fig. 6(b).
Although the Lagrange-interpolation-polynomial based fractional delay filter has several advantages like easy formulas for the coefficients and good response at the low frequencies [32], it may still consume certain memory space if not efficiently implemented in the digital control systems. Moreover, when comparing the frequency adaptive schemes for the RES and RC controllers in Fig. 6, the frequency delay order \( F \) has an indirect mapping relationship with the frequency variations \( \Delta \omega \), requiring an online calculation of the Lagrange coefficients according to the PLL estimated angular frequency \( \omega_{\text{PLL}} \) and the system sampling frequency \( f_s \).

Fig. 7 gives two possibilities to implement digitally the fractional delay filter of (13) in low-cost digital signal processors. It can be observed that the Farrow structure [32] has less delay units and thus consumes less memory space compared to the direct structure that has been employed in [12]. Thus, the Farrow structure is a more efficient implementation of the fractional delay filter. Table II further summarizes the computational burden (complexity) of the two fractional delay filter structures. It can be seen that, in terms of implementation, the frequency adaptive scheme for the RC harmonic compensator is more complicated than that for the RES controller. Nevertheless, the above discussions have revealed that an advanced PLL system in terms of accuracy and dynamics is crucial for the enhancement of the controller frequency adaptability, especially for single-phase grid-interfaced converters.

**IV. EXPERIMENTAL VERIFICATIONS**

**A. Test-Rig Description**

In order to verify the above analysis and also to test the effectiveness of the enhanced frequency adaptability of the current controllers, experiments have been carried out on a single-phase grid-connected inverter system referring to Fig. 1, where an AC programmable power source has been used in order to change the frequency. The system parameters are listed in Table III. For comparison, a DB controller and the PR controller are adopted as the fundamental-frequency current controller, and the RES and RC controllers are used to compensate the harmonics. As for the synchronization, a second order generalized integrator based PLL algorithm [4], [5] has been adopted due to its robust immunity to background distortions and fast dynamics. In the experiments, a commercial DC power supply has been used, and thus the current amplitude reference has been set directly as shown in Table III.

**B. Discrete Current Controllers**

Since the control systems were done in a dSPACE DS 1103 system, the resonant controller can easily be implemented in a discrete form using one Forward Euler method and one Backward Euler method [5], [24]. Then, the frequency adaptive RES harmonic compensator can be obtained in its discrete form as

\[
G_{\text{RES}}^h(z) = \frac{(z^{-1} - z^{-2})T_s}{1 + (h^2 \omega_{\text{PLL}}^2 T_s^2 - 2)z^{-1} + z^{-2}}
\]

with \( T_s = 1/f_s \) being the sampling period. Notably, other discretization methods like the Tustin with pre-warping, the impulse invariant, and the Trapezoidal method can be employed to discretize the resonant controller of (4) at the cost of increased complexity [5]. While for the DB controller, it can be expressed as

\[
G_{\text{DB}}(z) = \frac{z^{-1}}{(1 - z^{-1})G_f(z)}
\]
where $G_f(z)$ is the filter model. In practice, a low pass filter is incorporated into the RC controller in order to improve the controller robustness [30]. Then, the RC harmonic compensator of (3) is modified as given by

$$G_{RC}(z) = \frac{k_{rc}z^{-(N+F)}Q(z)}{1-z^{-(N+F)}Q(z)} \cdot C(z) \quad (16)$$

in which $Q(z) = \alpha_1 z + \alpha_0 + \alpha_1 z^{-1}$ is the low pass filter with $\alpha_0 + 2\alpha_1 = 1$ and $\alpha_0, \alpha_1 > 0$, and $C(z) = e^{zm}$ is a phase-lead compensator. The phase-lead number $m$ is determined by experiments. All the parameters of these controllers are shown in Table IV, where it can be seen that only the 3rd, 5th, and 7th RES controllers were incorporated with the fundamental-frequency controller (i.e., the PR controller).

### C. Experimental Results

The frequency adaptability of the discussed current controllers in the case of a varying grid frequency has firstly been tested, and the results are shown in Fig. 8, where the grid frequency was programmed within a range of 49.5 Hz to 50.5 Hz (i.e., ±1%). It can be observed in Fig. 8 that the DB controller is immune to frequency deviations due to its model-dependent characteristic, while the PR controller is significantly affected by the frequency changes. Specifically, when the grid frequency increases, the performance of the PR controller is significantly degraded, thus resulting in a poor current THD that may exceed the limitation (e.g., THD < 5%) [3]. In addition, it is also shown in Fig. 8 that both the RES and the RC periodic signal controllers present poor frequency adaptability, since they are highly frequency-dependent controllers. The test results are in a close agreement with the analysis presented in § II.B (Fig. 4).

Moreover, the poor frequency adaptability is further verified by the steady-state performance of the RES and RC controllers under a severe abnormal grid frequency (i.e., $2\pi \times 49$ rad/s), as it is shown in Fig. 9. It is observed in Fig. 9 that there will be a phase shift between the grid voltage $v_g$ and the feed-in grid current $i_g$ due to the frequency deviation, and thus leading to a poor power factor. That is to say, the grid-connected inverter system is not operating at unity power factor mode, which may violate the integration demands. Those experimental results have demonstrated the frequency-variation-immunity of the selected current controllers.

According to the discussions in § III, the strategies to enhance the frequency adaptability of the periodic current controllers were applied and the single-phase grid-connected inverter system has been tested. Fig. 10 shows the steady-state performances of the enhanced current controllers. It can be observed in Fig. 10 that, when the PLL estimated frequency $\omega_{PLL}$ is fed back to the resonant controller of (14), the tracking performance is improved. As a result, in the case of frequency variations induced by PLL tracking errors and/or the grid disturbances, a unity power factor operation as well as an improved current quality is always achieved. Similarly, when applying the frequency adaptive scheme to the RC harmonic compensator, there is no phase shift between the grid voltage and the injected grid current as shown in Fig. 10(b), and
i.e., the system is operating at a unity power factor to feed in high-quality currents. It should be pointed out that the parallel structure shown in Fig. 7(a) is adopted for adapting the RC harmonic controller to grid frequency changes without considering the implementation efficiency.

In addition, the dynamics of the frequency adaptive schemes were tested in the case of a grid-frequency step change (i.e., from 49.5 Hz to 50.5 Hz). The experimental results are presented in Fig. 11, which has verified the effectiveness of the proposed frequency adaptive schemes in terms of dynamics. Similar conclusions can be drawn: it is convenient to feed back the PLL estimated frequency according to Fig. 6(a) in such a way that the frequency adaptability of the RES controller is effectively improved; while by approximating the fractional order delay according to Fig. 7(a), the frequency adaptability of the RC harmonic controller is also enhanced. Both will contribute to an improved power factor as well as a lower THD of the feed-in currents.

Fig. 12 has further validated the effectiveness of the proposed schemes to enhance the frequency-variation-immunity of the current controllers under a wide range of grid frequency variations. When compared with the THD of shown in Fig. 8, it can be observed in Fig. 12 that the periodic current controllers with the proposed frequency adaptability schemes can maintain an almost constant THD despite the variations of the grid frequency (or the PLL estimated frequency). It is also worth to point out that the RC harmonic controller consists of all the resonant controllers with the corresponding frequency below the Nyquist frequency. As a consequence, for the PR controller with a repetitive controller as the harmonic
compensator, the grid current THD is lower than that in the case when the resonant controllers are paralleled as the harmonic compensator, where only a number of harmonics are compensated.

V. CONCLUSION

The sensitivity to frequency variations of selected current controllers for grid-connected power converters has been explored in this paper. The investigation has revealed that the dead-beat current controller is immune to frequency deviations since it is a model-based predictive controller. In contrast, the resonant (RES) controller and the repetitive controllers (RC) are very sensitive to the frequency variations induced by the PLL control errors and/or the grid disturbances. This is because both periodic current controllers are strongly dependent on the center frequencies, and infinite control gains at the frequencies of interest (e.g., the fundamental frequency) cannot be achieved due to the frequency deviations. In addition, this paper has also introduced means to enhance the frequency adaptability of the discussed current controllers – simply feeding back the PLL estimated frequency to the RES controller or properly approximating the fractional delay for the RC harmonic controller. Experiments performed on a single-phase grid-connected inverter have verified the discussions.

REFERENCES


