Regenerator heat exchanger – calculation of heat recovery efficiency and pressure loss

Different configuration sensitivity analysis

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Theoretical background


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Regenerator effectiveness

The parameters as: geometry, sensitivity study of regenerator heat exchanger performance, taking into account, such
decentralized pressure loss in the regenerator heat exchanger with

In this report is presented analytical calculation method to calculate efficiency and

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These two parameters are cont

surfaces.

Performance of heat exchangers is determined based on two main parameters: efficiency
to exchange / recover heat and pressure loss due to friction between fluid and exchanger

These two parameters are contradicting each other which mean that the higher is

efficiency the higher becomes pressure loss. The aim of the optimized design of heat

exchanger is to reach the highest or the required heat efficiency and at the same time to

keep pressure losses as low as possible keeping total exchanger size within acceptable

size.

In this report is presented analytical calculation method to calculate efficiency and

pressure loss in the regenerator heat exchanger with a fixed matrix that will be used in the
decentralized ventilation unit combined in the roof window. Moreover, this study presents

sensitivity study of regenerator heat exchanger performance, taking into account, such

parameters as: geometry, matrix material, surface geometry, shifting time, air flow.

Theoretical background

Regenerator effectiveness

Theoretical background presented in this report is also broader elaborated in [1].
Regenerator effectiveness is a function of four dimensionless numbers as presented below:

\[ \varepsilon = \phi[NTU_0, C^*, C_{r}^*, (hA)^*] \]

Where dimensionless numbers can be presented as follows:

\[ NTU_0 = \frac{1}{C_{\text{min}}} \left[ \frac{1}{\frac{1}{(hA)_k} + \frac{1}{(hA)_c}} \right] \]

\[ C^* = \frac{C_{\text{min}}}{C_{\text{max}}} \]

\[ C_{r}^* = \frac{C_r}{C_{\text{min}}} \]

\[ (hA)^* = \left( \frac{hA}{(hA)_{\text{on the } C_{\text{min}} \text{ side}}} \right) / \left( \frac{hA}{(hA)_{\text{on the } C_{\text{max}} \text{ side}}} \right) \]

Matrix wall heat capacity rate \( C_r \) for a fixed-matrix or rotary regenerator is defined as follows:

\[ C_r = \begin{cases} \frac{M_w C_w N}{P_t} = \frac{C_r N}{P_t} & \text{rotary regenerator} \\ \frac{M_w C_w}{P_t} = \frac{C_r}{P_t} & \text{fixed-matrix regenerator} \end{cases} \]

In this study case both fluid flows have equal capacity ratio (inlet and outlet air volume flow and type of gas is the same).

Knowing \( C^* \) and \( NTU_0 \) the counter-flow regenerator effectiveness \( \varepsilon_{cf} \) can be determined from:

\[ \varepsilon_{cf} = \frac{1 - \exp[-NTU_0(1-C^*)]}{1 - C^* \exp[-NTU_0(1-C^*)]} \frac{NTU_0}{1 + NTU_0} \]

Knowing \( C_{r}^* \) and \( \varepsilon_{cf} \), the regenerator effectiveness \( \varepsilon \) can be calculated from (valid for \( \varepsilon<0.9 \)):

\[ \varepsilon = \varepsilon_{cf}[1 - \frac{1}{9(C_{r}^*)^{1.93}}] \]

**Longitudinal wall heat conduction effect on regenerator effectiveness**

This parameter might be not negligible, particularly for a high effectiveness regenerators having short flow length \( L \). Longitudinal wall conduction reduces the exchanger
effectiveness. One side of regenerator is always hotter than the other. Hence, longitudinal heat conduction in the matrix wall occurs in the same direction through both periods. Effect of longitudinal wall heat conductivity adds to the governing differential equation dimensionless number $\lambda$, where:

$$\lambda = \frac{k_{w}A_{k,t}}{LC_{\text{min}}}$$

And $k_{w}$ - is matrix thermal conductivity, $A_{k,t}$ – is section area of the matrix, $L$ is matrix depth.
Including longitudinal wall heat conduction in efficiency calculation is obtained by using following expression:

$$\varepsilon = \varepsilon_{cf} \left[ 1 - \frac{1}{9(C_{r}^{*})^{1.93}} \right] \left( 1 - \frac{C_{\lambda}}{2 - C} \right)$$

where

$$C_{\lambda} = \frac{1}{1 + NTU_{0}(1 + \lambda \Phi)/(1 + \lambda NTU_{0})} - \frac{1}{1 + NTU_{0}}$$

**Pressure drop calculation**

Total pressure loss on the heat exchanger is described by following equation:

$$\frac{\Delta p}{p_{t}} = \frac{G^{2}}{2g_{c}\rho_{t}p_{t}} \left[ 1 - \sigma^{2} + K_{c} \right] \frac{1}{\text{entrance effect}} + \frac{2 \left( \frac{\rho_{t}}{\rho_{0}} - 1 \right)}{\rho_{t}^{2}} \frac{L}{r_{k} \rho_{t}} \left( \frac{1}{\rho_{m}} - (1 - \sigma^{2} - K_{e}) \frac{\rho_{t}}{\rho_{0}} \right) \frac{1}{\text{momentum effect}}$$

Normally core frictional pressure is dominating term. Normally the core pressure drop represents 90% or more of total pressure drop for gas flows in many compact heat exchangers. The entrance effect represents the pressure loss, and the exit effect represents in many cases a pressure rise.

**Prototype regenerator heat exchanger**

Prototype regenerator heat exchanger is presented in Fig. 1, however also other configurations and geometries are considered in this study. The prototype is a flat plate regenerator made of high density polystyrene (HDP), see the prototype in Fig. 1.
Following parameters are considered in the initial study of the prototype exchanger:

**GEOMETRY**
- Length: 18 cm
- Width: 2 x 12 = 24 cm
- Height: 8 cm
- Plate thickness: 1 mm
- Number of plates 70

**AIR FLOWS:**
- Volume flow (filter G3): 20.5 [m³/h]
- Volume flow (filter G2): 22 [m³/h]
- Volume flow (no filter): 25.2 [m³/h]

**HEAT EXCHANGER MATERIAL PROPERTIES:**
- Density: 930 [kg/m³]
- Thermal conductivity: 0.5 [W/mK]
- Specific heat capacity: 1900 [J/kgK]

**OTHER:**
- Shifting time (total shifting time): 70 [s]

**Results – prototype heat exchanger**
Using analytical effectiveness and pressure loss calculation method presented in [1] and in the first chapter of this report following results are obtained as presented in Fig. 2.
Pressure loss fraction for regenerator pressure entrance, core and exit effect for 25.2 m³/h are calculated, see Table 1.

<table>
<thead>
<tr>
<th>Entrance effect</th>
<th>Core friction</th>
<th>Exit effect</th>
</tr>
</thead>
<tbody>
<tr>
<td>[%]</td>
<td>[%]</td>
<td>[%]</td>
</tr>
<tr>
<td>15</td>
<td>94</td>
<td>-9</td>
</tr>
</tbody>
</table>

Table 1. Pressure loss distribution in prototype regenerator.

It can be observed that the core friction is dominating term, entrance effect contributes to pressure loss and exit effect contradict pressure loss. Results are with good agreement with expectations.

**Sensitivity analysis**

In this chapter is presented sensitivity analysis of regenerator heat exchanger taking into account several parameters: exchanger geometry (total), matrix shape, material properties, air flow, shifting time, area density. Parameters investigated are efficiency to regenerate heat and pressure drop on the exchanger. In the sensitivity analysis it is assumed that only the one parameter varies at the time. Typical surface geometries of the exchanger were investigated. The inspiration was taken from [2] and the potential candidates are presented in Fig. 3. From Fig. 3 following geometries were investigated: square, pentagon, tube (with wall) and rectangular (called flat plate in this study). For the comparison purpose, area density parameter was kept the same for all types of investigated regenerators (but porosity was not kept the same).
In the sensitivity study presented in this report, 5 different typical materials used to manufacture heat exchangers were studied. Their thermal properties, density (ρ), thermal conductivity (λ) and specific heat capacity (C_p) are collected and presented in Table 2.

<table>
<thead>
<tr>
<th>HEAT EXCHANGER MATERIALS</th>
<th>ρ</th>
<th>λ</th>
<th>C_p</th>
</tr>
</thead>
<tbody>
<tr>
<td>HDP (Polyethylene)</td>
<td>930</td>
<td>0,5</td>
<td>1,9</td>
</tr>
<tr>
<td>Ceramics (low thermal conductivity)</td>
<td>2000</td>
<td>5</td>
<td>0,9</td>
</tr>
<tr>
<td>Ceramics (high thermal conductivity)</td>
<td>7850</td>
<td>50</td>
<td>0,9</td>
</tr>
<tr>
<td>Aluminum</td>
<td>2730</td>
<td>155</td>
<td>0,893</td>
</tr>
<tr>
<td>Copper</td>
<td>8960</td>
<td>400</td>
<td>0,385</td>
</tr>
</tbody>
</table>

Table 2. Thermal properties of materials investigated as potential candidates to manufacture regenerator.
Sensitivity 1.1

GEOMETRY:
Length: 6 /step 2/ 24 cm
Width: 24 cm
Height: 8 cm
Plate thickness: 1 mm
Area density: 577

AIR FLOW:
Volume flow: 25,2 [m³/h]

OTHER:
Shifting time (total shifting time): 70 [s]

MATERIAL:
HDP, Ceramic – low λ, Ceramic – high λ, Aluminum, Copper.

Fig 4. Sensitivity 1.1 – Flat plate regenerator.

Fig 5. Sensitivity 1.1 – Square regenerator.
Fig 6. Sensitivity 1.1 – Pentagon regenerator.

Fig 7. Sensitivity 1.1 – Tube regenerator.

Summary

Fig 8. Sensitivity 1.1 – Efficiency summary.
Fig 9. Sensitivity 1.1 – Pressure loss summary.

Sensitivity 1.2

GEOMETRY:
Length: 18 cm
Width: 24 cm
Height: 8 cm
Plate thickness: 1 mm
*Area density 577 – 728*

AIR FLOW:
Volume flow: 25.2 [m³/h]

OTHER:
Shifting time (total shifting time): 70 [s]

MATERIAL:
HDP, Ceramic – low λ, Ceramic – high λ, Aluminum, Copper.

Fig 10. Sensitivity 1.2 – Flat plate regenerator.
Fig 11. Sensitivity 1.2 – Square regenerator.

Fig 12. Sensitivity 1.2 – Pentagon regenerator.

Fig 13. Sensitivity 1.2 – Tube regenerator.
Summary

Fig 15. Sensitivity 1.1 – Efficiency summary.

Fig 14. Sensitivity 1.2 – Pressure loss summary.

Sensitivity 1.3
GEOMETRY:
Length: 18 cm
Width: 24 cm
Height: 8 cm
Plate thickness: 1 mm
Area density 577

AIR FLOW:
Volume flow: 16/step 2/34 [m³/h]

OTHER:
Shifting time (total shifting time): 70 [s]

MATERIAL:
HDP, Ceramic – low $\lambda$, Ceramic – high $\lambda$, Aluminum, Copper.

Fig 16. Sensitivity 1.3 – Flat plate regenerator.

Fig 17. Sensitivity 1.3 – Square regenerator.

Fig 18. Sensitivity 1.3 – Pentagon regenerator.
Fig 19. Sensitivity 1.3 – Tube regenerator.

Summary

Fig 20. Sensitivity 1.3 – Efficiency summary.

Fig 21. Sensitivity 1.3 – Pressure loss summary.
Sensitivity 1.4

GEOMETRY:
Length: 18 cm  
Width: 24 cm  
Height: 8 cm  
Plate thickness: 1 mm  
Area density 577

AIR FLOW:
Volume flow: 25.2 m³/h

OTHER:
Shifting time (total shifting time): 60/step 20/ 240 [s]

MATERIAL:
HDP, Ceramic – low λ, Ceramic – high λ, Aluminum, Copper.

Fig 22. Sensitivity 1.4 – Flat plate regenerator.

Fig 23. Sensitivity 1.4 – Square regenerator.
Conclusions

Presented sensitivity study indicates that HDP and ceramics with low thermal conductivity are good material candidates to manufacture regenerator heat exchangers. The reason why efficiency is one of the highest for these materials is due to not so high thermal conductivity that decreases longitudinal heat loss. For ceramics with high thermal conductivity, aluminum or copper the high thermal conductivity contributes to high longitudinal heat losses and as a result to a lower heat regeneration efficiency. What is more, based on presented analytical calculations, regenerator with flat plate geometry, obtains highest efficiency and at the same time lowest pressure drop. The first round of sensitivity analysis indicates that to reach efficiency higher than 85% for considered air flow rate of 25.2 m³/h, regenerator must have larger surface area than presented prototype model. The higher efficiency can be obtained in 2 manners. The first manner will increase pressure loss through regenerator and to this method accounts: increase of length in airflow direction, increase of number of plates with unchanged thickness. The second manner increases efficiency and keeps pressure drop unchanged or even lower, and this can be obtained by increasing regenerator height and/or width or increase of number of plates and at the same time decrease their thickness. There is also third manner, that requires reduction of volume air flow through regenerator, but this one is not considered as indoor climate, would suffer due to that change. Lastly, it can be observed that shifting time up to 100 s does not have significant influence on efficiency (it should be stated that this is valid for plate thickness of 1mm and can vary with plate thickness).

Second round of sensitivity analysis

The aim of the project is to develop regenerator unit that could ensure entire decentralized ventilation unit to deliver minimum heat regeneration efficiency of 85%. The decentralized ventilation unit is mounted in the roof just above roof window and therefore it is in direct contact with outdoor air. This will cause some heat losses that are estimated to reduce entire unit heat regeneration efficiency at approximately 5%. Therefore, regenerator heat efficiency is estimated to have to be around 90%. 

Fig 24. Sensitivity 1.4 – Tube regenerator.
The second round of sensitivity analysis is focused on investigation – how to reach very high thermal efficiency, up to 90%, and not increase pressure loss on regenerator heat exchanger?

In the second round sensitivity analysis is conducted for two air flows: 16 and 25.2 [m³/h]. In the second round sensitivity analysis is conducted only for HDP material and plate geometry.

**Sensitivity 2.1**

**GEOMETRY:**
Length: 18/ step 1/ 26 cm  
Width: 24 cm  
Height: 8 cm  
Plate thickness: 1 mm  
Number of plates: 70  
Area density 577

**AIR FLOW:**  
Volume flow: 16 and 25.2 [m³/h]

**OTHER:**  
Shifting time 70 s.

**MATERIAL:**  
HDP

Fig. 25. Regeneration heat efficiency vs. regenerator length
### Table 3. Regeneration heat efficiency and pressure loss vs. regenerator length

<table>
<thead>
<tr>
<th>L depth [m]</th>
<th>Depth ε</th>
<th>Pressure drop [Pa]</th>
<th>Pressure drop [Pa]</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.18</td>
<td>0.89</td>
<td>1.64</td>
<td>0.83</td>
</tr>
<tr>
<td>0.19</td>
<td>0.89</td>
<td>1.73</td>
<td>0.84</td>
</tr>
<tr>
<td>0.2</td>
<td>0.90</td>
<td>1.82</td>
<td>0.85</td>
</tr>
<tr>
<td>0.21</td>
<td>0.90</td>
<td>1.91</td>
<td>0.85</td>
</tr>
<tr>
<td>0.2</td>
<td>0.90</td>
<td>1.82</td>
<td>0.85</td>
</tr>
<tr>
<td>0.22</td>
<td>0.91</td>
<td>1.99</td>
<td>0.86</td>
</tr>
<tr>
<td>0.23</td>
<td>0.91</td>
<td>2.08</td>
<td>0.86</td>
</tr>
<tr>
<td>0.24</td>
<td>0.91</td>
<td>2.17</td>
<td>0.87</td>
</tr>
<tr>
<td>0.25</td>
<td>0.92</td>
<td>2.26</td>
<td>0.87</td>
</tr>
<tr>
<td>0.26</td>
<td>0.92</td>
<td>2.35</td>
<td>0.88</td>
</tr>
</tbody>
</table>

**Sensitivity 2.2**

**GEOMETRY:**
Length: 18
Width: 24 cm
**Height: 8 – 10 cm**
Plate thickness: 1 mm
Number of plates: 70
Area density 577

**AIR FLOW:**
Volume flow: 16 and 25.2 [m³/h]

**OTHER:**
Shifting time 70 s.

**MATERIAL:** HDP

![Fig. 26. Regeneration heat efficiency vs. regenerator height.](image)
### Table 4. Regeneration heat efficiency and pressure loss vs. regenerator height.

<table>
<thead>
<tr>
<th>H (height) [m]</th>
<th>ε [-]</th>
<th>Pressure drop [Pa]</th>
<th>ε [-]</th>
<th>Pressure drop [Pa]</th>
</tr>
</thead>
<tbody>
<tr>
<td>0,08</td>
<td>0,89</td>
<td>1,64</td>
<td>0,83</td>
<td>2,59</td>
</tr>
<tr>
<td>0,084</td>
<td>0,89</td>
<td>1,55</td>
<td>0,84</td>
<td>2,46</td>
</tr>
<tr>
<td>0,086</td>
<td>0,89</td>
<td>1,51</td>
<td>0,84</td>
<td>2,39</td>
</tr>
<tr>
<td>0,088</td>
<td>0,90</td>
<td>1,48</td>
<td>0,84</td>
<td>2,33</td>
</tr>
<tr>
<td>0,09</td>
<td>0,90</td>
<td>1,44</td>
<td>0,85</td>
<td>2,28</td>
</tr>
<tr>
<td>0,092</td>
<td>0,90</td>
<td>1,41</td>
<td>0,85</td>
<td>2,22</td>
</tr>
<tr>
<td>0,094</td>
<td>0,90</td>
<td>1,38</td>
<td>0,85</td>
<td>2,17</td>
</tr>
<tr>
<td>0,096</td>
<td>0,90</td>
<td>1,34</td>
<td>0,86</td>
<td>2,12</td>
</tr>
<tr>
<td>0,098</td>
<td>0,90</td>
<td>1,32</td>
<td>0,86</td>
<td>2,07</td>
</tr>
<tr>
<td>0,1</td>
<td>0,91</td>
<td>1,29</td>
<td>0,86</td>
<td>2,03</td>
</tr>
</tbody>
</table>

### Sensitivity 2.3

**GEOMETRY:**
- Length: 18
- Width: 24 cm
- Height: 8 cm
- Plate thickness: 1 mm
- **Number of plates: 70/step 2/88**
- **Area density 577 - 728**

**AIR FLOW:**
- Volume flow: 16 and 25,2 [m³/h]

**OTHER:**
- Shifting time 70 s.

**MATERIAL:** HDP

---

![Number of plates (1mm)](image)

**Fig. 27.** Regeneration heat efficiency vs. number of 1 mm thick plates.
Table 5. Regeneration heat efficiency and pressure loss vs. number of 1mm thick plates.

**Sensitivity 2.4**

**GEOMETRY:**
- Length: 18
- Width: 24 cm
- Height: 8 cm
- Plate thickness: 0.5 mm
  - **Number of plates:** 70/step 5/115
  - **Area density:** 577 - 954

**AIR FLOW:**
- Volume flow: 16 and 25.2 [m$^3$/h]

**OTHER:**
- Shifting time 70 s.

**MATERIAL:** HDP

![Graph](image.png)

Fig. 28. Regeneration heat efficiency vs. number of 0.5 mm thick plates.
Table 6. Regeneration heat efficiency and pressure loss vs. number of 0.5 mm thick plates.

Sensitivity 2.5

GEOMETRY:
Length: 18
Width: 24 cm
Height: 8 cm
Plate thickness: 0.5 mm
Number of plates: 70/step 5/115
Area density 577 - 954

AIR FLOW:
Volume flow: 16 and 25.2 [m³/h]

OTHER:
Shifting time 70 and 140 s.

MATERIAL: HDP

Table 7. Regeneration heat efficiency and plate thickness of 1 mm and 0.5 mm.
Configurations reaching 90% heat recovery efficiency

Chosen regenerator configurations that result in 90% heat efficiency are presented in Table X.

Volume flow: 25,2 [m³/h]
Shifting time 70 s.
Material: HDP

<table>
<thead>
<tr>
<th>L depth [m]</th>
<th>W width [m]</th>
<th>H height [m]</th>
<th>N number of plates</th>
<th>ε</th>
<th>Pressure drop [Pa]</th>
</tr>
</thead>
<tbody>
<tr>
<td>0,18</td>
<td>0,24</td>
<td>0,14</td>
<td>70</td>
<td>0,90</td>
<td>1,43</td>
</tr>
<tr>
<td>0,18</td>
<td>0,24</td>
<td>0,13</td>
<td>75</td>
<td>0,90</td>
<td>1,93</td>
</tr>
<tr>
<td>0,18</td>
<td>0,24</td>
<td>0,12</td>
<td>78</td>
<td>0,90</td>
<td>2,39</td>
</tr>
<tr>
<td>0,18</td>
<td>0,24</td>
<td>0,11</td>
<td>80</td>
<td>0,90</td>
<td>2,86</td>
</tr>
<tr>
<td>0,18</td>
<td>0,24</td>
<td>0,09</td>
<td>85</td>
<td>0,90</td>
<td>3,45</td>
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<tr>
<td>0,18</td>
<td>0,24</td>
<td>0,08</td>
<td>90</td>
<td>0,90</td>
<td>4,38</td>
</tr>
</tbody>
</table>

Table 8. Selected configurations reaching 90% heat recovery efficiency.

Conclusions

- It can be observed that increase of height and/or width of the regenerator is a win-win scenario. Efficiency increases and pressure drop decreases.
- It can be observed from the graphs in this report that at least two dimensions would have to be increased to reach efficiency of around 90% for air flow at 25,2 m³/h. If only one dimension is manipulated then this dimension would probably become too large and regenerator would not fit to ventilation unit.
- To reach high efficiency and keep geometry unchanged or increased insignificantly number of plates would have to be increased.
- Increase of number of plates increases efficiency but at the same time increases also pressure loss. This can be counteracted by making plates thinner, however, if plates become thinner then regenerator becomes more sensitive to switching time. The longer switching time the lower efficiency becomes!

References