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He, Li; Li, Yong; Shuai, Zhikang; Guerrero, Josep M.; Cao, Yijia; Wen, Ming; Wang, Weiyu; Shi, Jingrong

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A Flexible Power Control Strategy for Hybrid AC/DC Zones of Shipboard Power System with Distributed Energy Storages

Li He, Student Member, IEEE, Yong Li, Senior Member, IEEE, Zhikang Shuai, Senior Member, IEEE, Josep M. Guerrero, Fellow, IEEE, Yijia Cao, Senior Member, IEEE, Ming Wen, Weiyu Wang, Student Member, IEEE, and Jingrong Shi

Abstract—The use of integrated shipboard power system (SPS) has greatly contributed to the next-generation vessels development. In this sense, how to realize the reasonable power distribution between hybrid zones in SPS is becoming one of the key problems to ensure system robustness and reliability. In this paper, a flexible power control strategy is proposed for the coordinated operation of the hybrid AC/DC zones in SPS. First, the interactive relationship of the AC/DC interface is analyzed, and the virtual inertia and capacitance are defined to reveal the interactive influence of the AC and the DC sub-grids, which leads to a new V-f droop principle. Then, the flexible control strategy is designed based on the droop principle as well as the characteristics of the analogous virtual synchronous generator (VSG), and the key parameters’ determination are discussed in detail, which can realize a proper assignment of cross-zone supportive power and improve the system dynamic response. In addition, the coordinated control loops are designed with the distributed energy storages (DESs) and interlinking converters (ICs) for the implementation of the strategy. Finally, the proposed strategy is validated by the simulation, which leads to a new V-f droop principle. Then, the flexible control strategy is designed based on the droop principle which leads to a new V-f droop principle. Then, the flexible control strategy is designed based on the droop principle which leads to a new V-f droop principle. Then, the flexible control strategy is designed based on the droop principle which leads to a new V-f droop principle. Then, the flexible control strategy is designed based on the droop principle which leads to a new V-f droop principle.

Index Terms—Flexible power control; hybrid AC/DC zones; virtual synchronous machine (VSG); distributed energy storages (DESs); shipboard power system (SPS)

NOMENCLATURE

SPS
Shipboard power system.
ES
Energy storage.
DES
Distributed energy storage.

ICs
Interlinking converters.
MTGs
Main turbine generators.
MVAC
Medium-voltage AC.
MVDC
Medium-voltage DC.
VSG
Virtual synchronous generator.
H
Inertial constant.
f
Reference frequency.
P_{INV}
Equivalent input mechanical power.
P_{REF}
Output electromagnetic power.
S_{IC}
Power rating of the inverter.
C_{DC}
Capacitance of the DC side capacitor.
V_{DC}
Voltage of the DC bus.
P_{REC}
Input power of DC side.
P_{REF,AC}
Output power to AC side.
f
Stable value of frequency.
\Delta f
Frequency variation.
V_{REF}
Rated value of the DC voltage.
\Delta V_{DC}
Voltage variation.
M
Correlation coefficient of the AC frequency and the DC voltage.
H_{VSG}
Virtual inertia constant.
\kappa_{DC}
Droop coefficient of DC zone.
P_0
Initial output power of AC source.
P_{REF,DC}
Reference output power of DC source.
\Delta V_{DC}
Virtual voltage variation.
D_{VSG}
Virtual damping coefficient of AC grid.
P_{REF,ES,DC}
Reference power of ES unit in DC zone.
\kappa_{AC}
Droop coefficient of AC zone.
P_0
Initial output power of AC source.
P_{REF,AC}
Reference output power of AC source.
\Delta f_{VR}
Virtual frequency variation.
D_{VDC}
Virtual damping coefficient of DC grid.
P_{REF,DC}
Reference power of IC.
Q
Reactive power.
\theta_{REF}
Reference reactive power.
I_{ES}
Output current of ES unit.
I_{d,REF}
Reference current of d-axis.
I_{q,REF}
Reference current of q-axis.
SoC
State of charge.
G_{vi}
Global variation index.

I. INTRODUCTION

With the development of the shipboard power system (SPS), the electric-power based loads are widely used in SPS [1]-[3], and renewable sources, such as photovoltaic system and wind generation, are drawing the industrial at-
tention to be implemented in SPS, which can improve the fuel efficiency and alleviate the increasing pressure of environmental protection and demand of cost saving [4]-[6]. Due to the limited space and requirement of high reliability, regionalization is adopted to design SPS, which means various generators and loads are deployed and managed in different zones according to their functions and the format of current, so there are hybrid AC/DC zones operating in SPS, which are equipped with individual generators and energy storage (ES) units, and each zone can serve as a power reserve [7], [8]. Therefore, a feasible strategy is necessary to enable the hybrid zones to work in a coordinated way, which helps to better utilize the capability of mutual power support between hybrid zones and improves the stability of SPS.

At present, the energy management for SPS is mainly concerned from the regard of making a balance between the power generation and the highly impulse power load. In [9] and [10], the typical multi-agent control principle is introduced to the shipboard system for the real-time load management, which can realize optimal regulation of the power generation and consumption in SPS, and this method is also friendly to the newly implemented equipment. Based on the principle of demand-side management, a method of optimal demand-side management and power generation scheduling is proposed in [11], which can improve ship energy efficiency, and contribute to the optimal operation of SPS. The above method can effectively improve the SPS performance. However, these methods are highly dependent on the communication system and require the support of complex algorithms, which means the system reliability might be threatened during severe maritime conditions. Considering the advantages of ES, there are other literatures focusing on utilizing the ESs in power management of SPS. [12]-[15] utilize the heuristic algorithms, such as fuzzy logic method and predictive control method, to design the control strategies of ESs and effectively relieve the negative impact brought by high-power ramp rate loads. However, the reported methods also require high-functioning center controller and the characteristics of zonal structure are not fully considered.

Nowadays, there are few energy management strategies designed for the hybrid zonal SPS. The power control approaches in territorial power systems can be used for the reference of SPS. In general, the coordinated control strategy between AC and DC grids can be classified into two categories: distributed control and master-slave control. The distributed control mainly adopts the principle of droop method, and determines the exchanged power between zones with the droop coefficient [16]-[19]. However, either \( V(f)\)-P droop or \( V^2(f)\)-P droop features hard to calculate the proper droop coefficient and has a mediocre dynamic performance while the severe power disturbance occurs. By comparison, the master-slave control strategy can realize a reasonable power allocation based on the global information [20]-[22]. However, this strategy highly depends on the fast communication network thus the reliability is threatened. In addition, the ES units in SPS are generally installed near the loads and utilized to suppress the local power variation. The potential of cross-zone power supporting of distributed energy storage (DES) is not fully exploited, which indirectly leads to the waste of ES capacity.

In this paper, a flexible power control strategy is proposed for the coordinated operation of the hybrid AC/DC zones in SPS. With the strategy, different zones can provide flexible power support for each other with good dynamic performance. Thus, the stability and reliability of SPS can be enhanced and the DESs are efficiently utilized. The advantages of the strategy and the main contributions of this paper are summarized as follows:

1) A linearized power coupling relationship between the AC and the DC zones is expressed, which is based on the virtual inertia and the virtual capacitance and features a physical meaning.

2) A flexible power control strategy for hybrid zones is proposed, of which the detailed design is derived from the operating characteristics of AC and DC grids, as well as the principle of droop control. Thus, it is feasible to be implemented in practice and improve the dynamic performance of SPS.

3) Compared with global optimization methods, the proposed control strategy is free of high-bandwidth communication network, which features high reliability and efficiently utilizes the DESs’ power supporting capability.

The main structure and content of this paper are summarized as follows. Section II introduces the configuration of the typical hybrid zones of SPS. The interactive power balance analysis is conducted in Section III, which can serve as the basis of the proposed strategy. Section IV discusses the flexible power control strategy from the principle to the control loop’s design, and the main parameter features are also included. The comparative simulation results and discussions verify the theoretical analysis and are presented in Section V. Finally, the conclusions are given in Section VI.

II. CONFIGURATION OF THE HYBRID AC/DC ZONES IN SPS

Fig. 1 shows a developed notional configuration of the hybrid AC/DC zones in SPS, which consists of three parts: AC zone, DC zone and interlinking converters (ICs) [23], [24]. As can be seen from Fig. 1, the AC zone contains main turbine generators (MTGs), high-power propulsion motor, ES units, and other general AC loads. The utility grid access is available in AC zone for the connection of SPS and onshore power grid. The DC zone also contains the power sources and typical DC loads. The high-power DC loads like pre-charging weapons and radars are implemented in DC zone to reduce power step transition. The data and command center is connected to DC bus due to the high reliability of DC grid. The hybrid zones are interlinked by ICs, which serve for the exchange of power flow between zones.

![Fig. 1. One-line diagram of a notional hybrid AC/DC zones in SPS](image-url)
The structure of hybrid AC/DC zone increases the power efficiency since it reduces the power transfer stages. Considering that there are high-power loads (e.g., propulsion load and electromagnetic weapon) installed in both zones, which may cause serious power variation compared with that of terrestrial microgrids, the global power sharing can be rather important to maintain the operating stability. Therefore, it is urgent to enable the hybrid zones to work in a coordinated way, which can exploit the power support ability of DES units.

It is worth noting that, there are two important types of all-electric SPSs, i.e., the medium-voltage AC (MVAC) system and the medium-voltage DC (MVDC) system [9], [24]. The main power generators and propulsion loads can be connected to AC or DC buses due to the different choice of system type. Therefore, the hybrid AC/DC topology with more detailed characteristics will vary according to different systems which SPS adopts. The studied method should have generality for different types of SPS. Thus, considering that key technologies can be cross-fertilized between terrestrial microgrids and SPS [5], without losing generality, we developed the notional structure of hybrid zones in SPS derived from well-accepted microgrid structure, aiming at showing clear and intelligible concept of hybrid AC/DC grid for discussion.

In this paper, the proposed strategy is based on the universal and intelligible concept of hybrid AC/DC grid for discussion.

III. INTERACTIVE POWER BALANCE ANALYSIS BETWEEN AC/DC INTERFACE

The bidirectional converters, which are operating as the ICs between the hybrid zones, can transmit active power between different grids as required. When the power is transferred from the DC side to AC side, the IC can be regarded as a virtual synchronous generator (VSG) [25], and the dynamic power balance of the AC side will vary accordingly, which can be described by the swing motion equation as,

$$\frac{2H}{f_0} \frac{df}{dt} = P_{INV}^0 - P_{INV}^{REF} = \Delta P_{AC}$$  \hspace{1cm} (1)$$

where $H$ is the inertial constant of synchronous generator; $f_0$ is the reference frequency; $P_{INV}^0$ and $P_{INV}^{REF}$ are the equivalent input mechanical power and the output electromagnetic power, respectively.

Similarly, when the active power is transferred from AC side to DC side, the IC can be treated as a virtual DC capacitor to provide voltage support, of which the characteristics can be expressed by

$$\frac{C_{DC}V_{DC}}{S_{IC}} \frac{dV_{DC}}{dt} = P_{REC}^0 - P_{REC}^{REF} = \Delta P_{DC}$$  \hspace{1cm} (2)$$

where $S_{IC}$ is the power rating of the inverter; $C_{DC}$ is the capacitance of the DC side capacitor; $V_{DC}$ is the voltage of the DC bus; $P_{REC}^0$ and $P_{REC}^{REF}$ are the input power of DC side and the output power to AC side, respectively.

Therefore, the IC is a converter that can change the operating state and power direction according to the requirements, of which the interactive power supporting balance is shown in Fig.2. Based on the power balance when the power is transferred between different zones, combining (1) and (2) yields,

$$\frac{2H}{f_0} \frac{df}{dt} = \frac{C_{DC}V_{DC}}{S_{IC}} \frac{dV_{DC}}{dt} = \frac{P_{INV}^0}{P_{INV}^{REF}} = \Delta P_{AC}$$  \hspace{1cm} (3)$$

where $P_{INV}^0$ and $P_{INV}^{REF}$ are the input power of different zones, respectively.

$$V_{DC} = \sqrt{M(f - f_0) + V_{REF}^2}$$  \hspace{1cm} (4)$$

where $f$ represents the stable value of frequency after power disturbance in AC/DC interface; $V_{REF}$ is the rated value of the DC voltage; $M$ is defined as the correlation coefficient of the AC frequency and the DC voltage.

Integrating both sides of (3) and assuming that the frequency and DC voltage are both in reference value at the initial time, then the following equations can be obtained

$$V_{DC} = \sqrt{M(f - f_0) + V_{REF}^2}$$  \hspace{1cm} (5)$$

where $\Delta V_{DC} = V_{DC} - V_{REF} = \Delta V_{DC}$ into (5) yields

$$\Delta V_{DC}^2 + 2V_{REF}\Delta V_{DC} = \frac{4H}{f_0C_{DC}}\Delta f$$  \hspace{1cm} (6)$$

The equation (8) indicates that voltage deviation and frequency change are coupled in a nonlinear way, and the coupling degree is significantly influenced by $H_{VSG}$ and $C_{DC}$. Virtual inertia constant $H_{VSG}$ is used to quantitatively describe equivalent inertia provided by converters as well as illustrate the coupling relationship of AC frequency and DC voltage. More specifically, it can be deduced from Fig. 3 that, with larger value of virtual inertial constant $H_{VSG}$ and fixed $C_{DC}$, the increase of $\Delta f$ leads to larger $\Delta V_{DC}$ with the same changing direction, vice versa, which implies that more active power should be released (larger $\Delta V_{DC}$ in DC side) to provide more inertia support for AC side and this coincides with the physical characteristics of the hybrid system. In contrast, the increase of $C_{DC}$ will impose a negative impact on the coupling relationship. Taking the point A ($C_{DC} = 1$ mF) and B ($C_{DC} = 9$ mF) as examples, it can be observed that when the frequency is increased by 4Hz, the difference of corresponding DC voltage deviations can be as large as 0.692kV, and the smaller $C_{DC}$ corresponds to larger $\Delta V_{DC}$. The analysis above can be served as the reference of the determination of key parameters in the following control system.

Expanding equation (8) using Taylor series, we can obtain (9) below. Further, considering that AC frequency is varied in
a relatively small range (generally restricted within ±0.005p.u.), the terms equal to or higher than second order can be neglected. Therefore, a linearized relationship between AC frequency and DC voltage can be obtained for the AC/DC interface, as shown in (10) and (11):

\[
\Delta V_{DC} = \frac{M}{2V_{REF}} \Delta f - \frac{M^2}{8V_{REF}^2} \Delta f^2 + \cdots \tag{9}
\]

\[
V_{DC} = V_{REF} + \frac{M}{2V_{REF}} (f - f_0) \tag{10}
\]

\[
\Delta V_{DC} = \frac{2H_{VSG} S_{DC}^2}{V_{REF} C_{DC} f_0} \Delta f = M' \cdot \Delta f \tag{11}
\]

\[
M' = \frac{M}{2V_{REF}} \tag{12}
\]

Fig. 4 gives the comparison between the nonlinear and linearized descriptions discussed above. The slope of \(\Delta V'\) is acquired by taking the difference between (8) and (11). It can be observed that, the operation of linearizing by Taylor equation (shown in violet slope) just brings about little mismatch from the original value (shown in blue slope). With the increase of the frequency deviation, the mismatch, shown by \(\Delta V'\), will become larger but restricted as large as 0.039kV, which means the coupling relationship of \(\Delta f'\) and \(\Delta f\) can be presented using the linearized equation (10) in the normal operation condition.

For the sake of clarity, it is worth pointing out the difference between the conventional modeling linearization and the linearized coupling relationship in this paper. Generally, the modeling linearization of AC and DC networks with multiple converters can be rather more complex, due to that parameters variation (i.e., X/R ration) and different operating scenarios should be carefully considered. However, different from the abovementioned conventional model linearization, we develop the linearized coupling relationship from the regard of power balance for the hybrid-grid interface. Therefore, the conventional model linearization aims to build an order-reduced matrix to describe the inner operational features of AC or DC system, and the proposed method is aiming to describe the power coupling relationship at the interface between AC and DC system. The mentioned two-linearization operations are considered for different purposes and objectives.

IV. PROPOSED FLEXIBLE POWER CONTROL STRATEGY

In this Section, the flexible power control strategy will be introduced systematically. Firstly, the DESs power response in AC and DC zones are designed carefully in subsections A and B, respectively, where the output power is divided to local response and cross-zone response, and the parameters features are visualized discussed for determining proper values. Then, the IC reference power is accordingly designed to transmit the mutual support power for achieving flexible power sharing between hybrid zones, which also includes the control loops illustration for the practical implementation.

A. Power Response of DES in DC zone

When there appears power shortage in the DC zone, which might be caused by the operation of high-power apparatus, the DES unit located in the DC zone will be immediately activated to compensate the power imbalance. Assuming the general droop principle is adopted for the DES, which can be described as

\[
P_{DC}^{REF} = k_{DC} (V_{REF} - V_{DC}) + P^0_{DC} \tag{12}
\]

where \(k_{DC}\) is the droop coefficient of DC zone; \(P^0_{DC}\) and \(P_{DC}^{REF}\) represent the initial output power and the reference output power of DC source, respectively.

Except for the response to the local power deviation, the DES in DC zone should also be responsible for the power demand of the opposite zone, i.e., the AC zone. More specifically, the power demand mismatch in AC zone can be reflected by the frequency deviation, i.e., \(\Delta f\), which leads to the corresponding change of \(\Delta V_{DC}\) according to (11), and is re-denoted as \(\Delta V_{VIR}^{DC}\) to be distinguished from the real voltage change, since it is not a real detected voltage change. Then the droop equation (12) can be adjusted to consider the virtual voltage change derived from \(\Delta f\) and expressed by

\[
P_{DC}^{REF} = k_{DC} (V_{REF} - \Delta V_{VIR}^{DC} - V_{DC}) + P^0_{DC} \tag{13}
\]

In practice, it is often desirable to include a component of damping torque by adding a term proportional to frequency deviation to describe the effect of damping torque, which can contribute to smoothing the frequency change when power imbalance occurs [26]. Thus the characteristic equation (1) is accordingly developed as

\[
P_{INV}^{REF} = P_{INV}^0 - \frac{2H_{VSG}}{f_0} \cdot \frac{d\Delta f}{dt} - D_{VSG} (f - f_0) \tag{14}
\]

where \(D_{VSG}\) is the virtual damping coefficient of AC grid.

Equation (14) gives a more detailed external characteristic description of the active power for SG. Substituting (10) and (11) into (14) leads to

\[
\frac{2H_{VSG}}{M'} \frac{d\Delta V_{VIR}^{DC}}{dt} = P_{INV}^0 - P_{INV}^{REF} - \frac{D_{VSG}}{M'} \Delta V_{VIR}^{DC} \tag{15}
\]

With the help of (15), the frequency inertial response in AC
zone is correspondingly transferred into the response of virtual voltage deviation in DC zone, which makes the DC grid acquire the dynamic response capability for AC grid. Besides, since the response equation is derived from the characteristics of practical SG, the power dynamic performance of DC grid can be frequency-friendly while serving for the AC grid. In other words, since equation (15) is derived from the swing equation of SG, the output power of DC zone is accordance with the characteristics of synchronous machine, and better power support effects can be obtained through this virtual SG (i.e., the DC zone).

Assuming that there is a power demand vacancy in AC zone, the frequency variation will be reflected by $\Delta V_{\text{AC}}^\text{IR}$, and such virtual delta voltage is accordingly added to the common voltage droop equation, which is the process of deducing (13) from (12) and enables DC zone respond to AC power events. Besides, we have designed the additional output power based on the characteristics of SG, which is denoted as $P^\text{INV}$ in equation (15). Thus we can obtain a flexible output power of ES unit in DC zone, denoted as $P^\text{REF,DC,ES}$, by combining $P^\text{PES,DC}$ in (13) and $P^\text{INV}$ in (15), which leads to the following power reference.

$$P^\text{REF,DC,ES} = P^\text{PES,DC} + k_{\text{DC}}(V_{\text{REF}} - \Delta V_{\text{VIR}} - V_{\text{DC}}) - \frac{2H_{\text{VSG}}}{M^'} \frac{dV_{\text{IR}}}{dt} - \frac{D_{\text{VSG}}}{M^'} \Delta V_{\text{VIR}}$$

or

$$P^\text{REF,DC,ES} = P^\text{PES,DC} + k_{\text{DC}}(V_{\text{REF}} - \Delta V_{\text{VIR}} - V_{\text{DC}}) - \frac{D_{\text{VSG}}}{M^'} \Delta V_{\text{VIR}} - \frac{2H_{\text{VSG}}}{M^'} \frac{dV_{\text{IR}}}{dt}$$

(16)

When the power imbalance occurs in the AC zone, $\Delta f$ will be no longer equal to zero, which leads to the corresponding change of $\Delta V_{\text{AC}}^\text{IR}$. Then the variation is reflected in the DC grid by changing the DC reference voltage, which is shown by the droop adjustment term in (16) and activates the DES in DC zone to increase output power. Besides, the virtual inertia response term is added to improve the dynamic of frequency response, which is derived from the characteristics of VSG. Furthermore, equation (17) gives another view of illustration for the proposed flexible strategy, in which the output power of the DES can be divided into two decoupled parts. The local voltage response term represents the power dispatch to respond to the local voltage variation, and the dynamic frequency response is realized by the cross-zone flexible term.

Fig. 5 shows the influences on output power of DES exerted by the change of different parameters. It can be observed from Fig. 5(a) that, with the increase of correlation coefficient $M$, the ES power $P^\text{REF,DC,ES}$ decreases since the frequency variation has less coupling influence with DC voltage according to (11), whereas $D_{\text{VSG}}$ brings about the significantly positive correlation with $P^\text{PES,DC}$. It means $H$ should not be too small since it is proportional to $M'$ according to equation (6), and output power of DES may beyond the limit with small inertia coefficient. Therefore, considering the fact that $H$ directly influences the output power of DESs and the transmitted power through IC, the power characteristics which are shown in Figs. 5 should be regarded as major factors while determining $H_{\text{VSG}}$. Additionally, it is shown in Fig. 5(b) that, compared with that of Fig. 5(a), the changes of $k_{\text{DC}}$ and $d\Delta V_{\text{VIR}}/dt$ bring about smoother impact on the output power of DES, which implies that the proposed strategy is less influenced by the local preset parameters, i.e., $k_{\text{DC}}$, and at the initial moment of frequency deviation (corresponding to a large absolute value of $d\Delta V_{\text{VIR}}/dt$), the ramp rate of $P^\text{REF,DC,ES}$ is gentle and no active power impulse will be brought to the system.

![Fig. 5 Relationship of $P^\text{REF,DC,ES}$ with different parameters’ change. (a) Variation of $P^\text{REF,DC,ES}$ when $M$ and $D_{\text{VSG}}$ change. (b) Variation of $P^\text{REF,DC,ES}$ when $k_{\text{DC}}$ and $\Delta V_{\text{VIR}}$ change.](image)

**B. Power Response of DES in AC zone**

Similarly, when there appears net power variation due to the change of load demand in the AC zone, the local DES unit will be activated to compensate the power mismatch. Assuming the frequency droop control is implemented, which is given by

$$P^\text{REF} = k_{\text{AC}}(f_0 - f) + P^\text{PAC}$$

(18)

where $k_{\text{AC}}$ is the droop coefficient of AC zone; $P^\text{PAC}$ and $P^\text{REF}$ represent the initial output power and the reference output power of AC source, respectively.

By the help of equation (11), the variation of DC voltage in DC zone, i.e., $\Delta V_{\text{DC}}$, can be transferred into a corresponding frequency change, denoted as $\Delta V_{\text{VIR}}$, which enables the DES unit in AC zone to respond to the power variation of DC zone. Accordingly, the updated droop equation can be described as

$$P^\text{REF} = k_{\text{AC}}(f_0 - f) + P^\text{PAC}$$

(19)

Comparing the power dynamic characteristics of both the AC grid and DC grid, which are shown in (1) and (2), the voltage performances of DC side can be further defined as

$$P^\text{REC} = \frac{C_{\text{DC}}V_{\text{DC}}}{S_{\text{IC}}} \frac{dV_{\text{DC}}}{dt} - D_{\text{VDC}}(V_{\text{DC}} - V_{\text{REF}})$$

(20)

where $D_{\text{VDC}}$ is the virtual damping coefficient of DC grid. The virtual damping coefficient in AC system is utilized to describe the damping torque which contributes to smoothing the variation of AC frequency. Similarly, $D_{\text{VDC}}$ of the DC grid is
introduced here to describe the effect of damping the variation of DC voltage.

Substituting the coupling relationship of \( f \) and \( V_{DC} \) into equation (20) leads to
\[
\frac{M'^2 C_{DC} f_\phi}{S_{IC}} \frac{d\Delta f_{\text{VIR}}}{dt} = P^{\text{ref}}_{\text{AC,ES}} - P^{\text{REF,DC}} - D_{\text{VDC}} M' \Delta f_{\text{VIR}} \tag{21}
\]

Equation (21) helps the DES unit in AC zone acquire the dynamic response ability for DC zone. Additionally, since the response equation is derived from the characteristics of the real capacitor, the power dynamic performance of AC grid can be voltage-friendly while supporting DC grid.

Combining equations (19) and (21), one can obtain
\[
P^{\text{ref,AC,ES}} = P^{\text{ref,AC}} + \underbrace{k_{AC} (f_\phi - f)}_{\text{local frequency response}} - (C_{\text{VIR}} M'^2 f_\phi \frac{d\Delta f_{VIR}}{dt} + D_{\text{VDC}} M' \Delta f_{\text{VIR}}) \tag{22}
\]

or
\[
P^{\text{ref,AC,ES}} = P^{\text{ref,AC}} + k_{AC} (f_\phi - f) - (k_{AC} + D_{\text{VDC}} M') \Delta f_{\text{VIR}} - C_{\text{VIR}} M'^2 f_\phi \frac{d\Delta f_{\text{VIR}}}{dt} \tag{23}
\]

When the power imbalance occurs in the DC zone, \( \Delta V_{\text{DC}} \) will be no longer equal to zero, which leads to the corresponding change of \( \Delta f_{\text{VIR}} \). Then the variation is reflected in the AC grid by changing the reference frequency, which is shown by the droop adjustment term in (22) and activates the DES in AC zone to change output power. Besides, the virtual inertia response term is added to improve the dynamic of voltage response which is derived from the operating characteristics of capacitor.

Fig. 6 shows the influences on output power of DES exerted by the change of different parameters. It can be observed from Fig. 6(a) that, with the increase of correlation coefficient \( M \), the ES power \( P^{\text{ref,AC,ES}} \) increases since the DC voltage variation has more coupling influence with frequency according to (11), which is inverse of that in equation (16) and Fig. 5 (a). And \( D_{\text{VDC}} \) also brings about the positive correlation with \( P^{\text{ref,AC,ES}} \).

Furthermore, it is shown in Fig. 6(b) that, the changes of \( k_{AC} \) and \( d\Delta f_{\text{VIR}}/dt \) exert smooth impact on \( P^{\text{ref,AC,ES}} \) which implies that, for the AC zone, the proposed strategy is the same less influenced by the local preset parameters, i.e., \( k_{AC} \). Besides, with a wide range of \( d\Delta f_{\text{VIR}}/dt \) (e.g., from 0 to -10 Hz/s), the output power of ES, i.e., \( P^{\text{ref,ES,AC}} \), is varying with a smooth linear track, thus no active power impulse will be brought to the system.

\[
\text{Output power of DES in AC zone (p.u.)}
\]
\[
\text{Correlation coefficient: } M' \quad \text{Virtual damping constant: } D_{\text{VDC}}
\]

\[\text{(a)}\]

\[\text{Fig. 6 Relationship of } P^{\text{ref,AC,ES}} \text{ with different parameters' change. (a) Variation of } P^{\text{ref,AC,ES}} \text{ when } M' \text{ and } D_{\text{VDC}} \text{ change. (b) Variation of } P^{\text{ref,AC,ES}} \text{ when } k_{AC} \text{ and } \Delta f_{\text{VIR}} \text{ change.}\]

C. Cross-zone Power Compensation with IC

From the discussion above, we can see that when there occurs the net power deficiency in DC side, the DES unit in AC side can obtain the power reference to transfer to DC side, and contribute to DC voltage stability. Therefore, the DC voltage is supported by DESs in both AC and DC sides, which will significantly improve the voltage dynamic performance. Similarly, when there occurs the net power deficiency in AC side, the DES unit in DC side can possess the power reference to transfer to AC side, and contribute to AC frequency. Thus, the frequency dynamics of AC sub-grid can be enhanced compared with the situation in which only one-side DES is activated.

With the power demands appearing in both zones, there may be clash among control signals. In other words, both zones will be requiring power support from the opposite zone and the power transmitted through ICs should be properly determined, or the power transferred to the opposite zone may oscillate or fluctuate during the cross-zone support, since the frequency and voltage in both zones are not stable in the transient process. To avoid this situation and transmit the flexible support power of DESs in different zones, the reference power of IC between the DC and AC zones are defined in (24), as the difference of the flexible terms from equations (17) and (23), which can reduce the possible power oscillation during the mutual power support.

\[
P^{\text{IC}} = (P^{\text{ref,AC,ES}} - P^{\text{ref,AC}}) - (P^{\text{ref,DC,ES}} - P^{\text{ref,DC}}) \tag{24}
\]

It is worth noting that equation (24) is obtained by finding the difference of the flexible terms of equations (16) and (22), and the process and more essentially detailed expression is given as follows.

\[
P^{\text{IC}} = (k_{DC} + D_{V_{SG}, DC}) \Delta f_{\text{VIR}} - (k_{AC} + D_{\text{VDC}} M') \Delta f_{\text{VIR}} + \frac{2 H_{V_{SG}, DC}}{M'} \frac{d\Delta f_{\text{VIR}}}{dt} - C_{\text{VIR}} M'^2 f_\phi \frac{d\Delta f_{\text{VIR}}}{dt} \tag{25}
\]

It can be seen from the above equation that, the IC reference power can be calculated from the virtual AC frequency and DC voltage variation. Since \( \Delta f_{\text{VIR}} \) and \( \Delta V_{\text{DC}} \) are derived from the real frequency and voltage change according to equation (11), the IC power can be conveniently obtained by collecting and processing frequency and DC voltage values of IC’s con-
nnecting points at both DC and AC sides. Therefore, there is no need to know the real-time active power of every DESs’ converters.

Therefore, the proposed strategy does not need central controller, which features high reliability and response speed. More specifically, the proposed method is based on the improved droop principle, and the IC and DES need only signals of frequency and DC voltage. Then, the value of power reference can be obtained by the local controller embedded in DESs and IC, of which the process is free of high-bandwidth communication and feasible to be implemented in practice.

Fig. 7 gives the illustration of four different power states of IC, in which the response power of DESs in DC and AC zones are also depicted respectively with blue and purple surfaces. Besides, the relationship between virtual variable changes (i.e., Δ\text{VIR} and Δ\text{VDC}) and the corresponding voltage and frequency variation are clearly shown at the ground coordinate. Assuming the power flowing from AC side to DC side is positive, the operational states are discussed in detail as follows:

1) State I: In this state, Δ\text{VIR}>0, Δ\text{VDC}<0, which indicates that the power generation is beyond the power demand in AC zone and there appears net power vacancy in DC zone. Therefore, there are surplus power supply in AC zone raising the frequency and the power deficiency in DC zone deteriorating the voltage, and the power flow of IC is supposed to be transferred from AC side to DC side, which can properly dispatch and utilize the redundant power.

2) State II: In this state, Δ\text{VIR}<0, Δ\text{VDC}<0, which indicates that there is net power deficiency in both the AC zone and DC zone and the additional power demands are required in both sides. Therefore, on the premise of ensuring local power quality, the direction of IC power is determined according to (24) and is not always unified in this situation, which means the supportive power will be shared accordingly to improve the global power quality of both zones. It should be noted that, the IC will be blocked when there is a risk that the power quality is down below the normal variation threshold in both zones (determined by the operator), and the emergency measures such as load shedding are supposed to be taken.

3) State III: In this state, Δ\text{VIR}<0, Δ\text{VDC}>0, which indicates that the power generation is beyond the power demand in DC zone and there appears net power vacancy in AC zone. Therefore, there are surplus power supply in DC zone raising the voltage and the power deficiency in AC zone deteriorating the frequency, and the power flow of IC is supposed to be transferred from DC side to AC side.

4) State IV: In this state, Δ\text{VIR}>0, Δ\text{VDC}>0, which indicates that there appears power generation surplus in both zones. The generation units in SPS will reduce the output power in this situation. Besides, by accordingly changing the power flow and activating the DESs of the whole system, the proposed strategy can provide another power balancing channel and help the absorption of excessive power generation.

It is worth noting that, during long-term operation, the DESs in SPS will be charged to keep its reasonable state of charge (SoC) level when the SPS is working in the stable condition and no impulse power demand is expected. Besides, since the power variation is shared by all the DESs in hybrid zones, the proposed strategy can indirectly contribute to maintaining the balance of SoC.

D. Design of the Flexible Power Control Loop

The proposed power control strategy is realized through the coordination of the IC and the DESs in hybrid zones, as shown in Fig. 8. By collecting the variation of local electrical variable (i.e., \(V_{\text{DC}}\) of DC zone and \(f\) of AC zone), the ES unit can respond to the local power variation according the preset droop coefficient. Besides, the change of local electrical variable will be transferred to the opposite zone according to (17) and (23), so that an inter-zone flexible response is realized by generating the additional power signal to the ES controller in the opposite zone. The difference between \(P_{\text{REF}}^{\text{EFF}}\) and \(P_{\text{REC}}^{\text{REF}}\) is set as the power reference of IC, which can reduce the possible power fluctuation during operation. The detailed feature analysis with different parameters (e.g., Figs. 5 and 6 and relevant contents) can serve for the guidance of parameter determination. Based on the visualized analysis in the previous section, we can choose the reasonable values of the parameters when employ the strategy in practice.

Fig. 9 shows the detailed design of the dual loop controllers based on Fig. 8. It can be seen that, the controllers for DESs and IC are developed from the common control structure of converters [27], [28], which means the controllers are easily incorporated into the engineering application. Besides, the hysteresis controller is adopted to avoid the frequent activation of the converter when the DC voltage or frequency changes near the boundaries of dead band, which is utilized well in engineering practice and can protect the DES unit during the cross-zone power compensation. More specifically, when the frequency or voltage variation is less than the specific threshold, the proposed strategy should have no response and there may be no power support from the ES unit, which can prevent activation caused by interfering signals and small power disturbances. It should be noted that, the threshold is usually set as a small value and will not influence the effectiveness of the strategy.
The parameters of the simulation model are listed in Table I. In this strategy, the IC is blocked and will not transfer any power between hybrid sides, so the two sides are islanded from each other. Since the DC and AC side should only be responsible for local power variation in this situation, the voltage and frequency quality would be the worst when local net power changes, and nearly have no fluctuation when the power disturbance occurs in the other side. Therefore, the key parameters used in this strategy are the respective local droop coefficients described in equations (12) and (18), which are \( k_{DC} \) and \( k_{AC} \).

2) Proposed flexible strategy: In this strategy, the IC is utilized flexibly for power sharing between AC and DC sides, transferring active power according to the proposed equations. In this situation, not only the local droop response will be activated (i.e., the conventional droop control for local power disturbance), but also the mutual power support between zones will be employed [i.e., the cross-zone flexible power response defined in equations (17) and (23)]. Thus, the hybrid sides are connected with each other, and the power of DESs in two sides can be dispatched for the opposite sides. Therefore, the key parameters used in this strategy include \( k_{DC}, k_{AC}, H_{VSG}, C_{DC}, D_{VSG}, D_{VDC} \).

3) Only droop strategy: In this strategy, the voltage and frequency variation can be mutually transformed according to the sampling period time constant, and thus the virtual frequency and virtual voltage changes are obtained. Then, adding the
virtual terms to the conventional droop equations and so-called “ac-dc droop” method, which is defined as only droop strategy, can be obtained. This method is well accepted for the coordinated control of hybrid AC/DC microgrids and can be found in [18]. Compared with the proposed strategy, this mutual transformation of AC frequency and DC voltage has no clear physical meaning. Besides, the key parameters of the strategy are \( k_{DC} \) and \( k_{AC} \), which makes it less adjustable when determining power reference.

As can be seen from the illustration above that, the proposed strategy has the additional parts concerning the physical operational characteristics, i.e. inertia, capacitance and damping effects, which enable our strategy to provide more flexible power support ability. Therefore, in the simulation cases, the parameters \( k_{DC} \) and \( k_{AC} \), used in all three methods will be set as the same value for each strategy for fairness. As for the parameters utilized only in the proposed strategy, we will determine their values according to the theoretical analysis.

In the simulation cases of this paper, the normal variation range of power quality in this paper are defined as ±0.5% of frequency (±0.25 Hz) for AC zone and ±5% of voltage (±0.35 kV) for DC zone. In order to reflect overall variation and stability level of the hybrid system, a global variation index is defined here and described as,

\[
G_v = \frac{\Delta f}{f_{\text{max}} - f_{\text{min}}} + \frac{\Delta V_{\text{DC}}}{V_{\text{max}} - V_{\text{min}}} \quad (26)
\]

where \( f_{\text{max}} \) and \( V_{\text{max}} \) are the maximum value of the normal variation of \( f \) and \( V_{\text{DC}} \), respectively; \( f_{\text{min}} \) and \( V_{\text{min}} \) are the minimum value of the normal variation, respectively.

The global variation index is essentially the normalization of the variation of both frequency and DC voltage. The more this index approaches to zero, the more stable the whole system is, which can be used to directly reflect the stability level of the hybrid grid.

A. Case 1: Step Power Change in AC Zone

Figs. 10-13, Table II and Table III show the simulation results of case 1. When the net power increment of 5 MW is activated at 4 s, the frequency of AC zone drops immediately down below 49.75 Hz. As can be seen from Fig. 10 (a), the proposed strategy features fewer decrease of frequency compared with other two strategies.

Besides, the frequency converges to the higher stable value of 49.88 Hz at 8.5 s, and the overshoot is less than that of other methods after the load power decreases at 16 s, which illustrates the flexible control strategy has good dynamic response characteristics. Moreover, Fig. 12(a) gives the output power increment of the local generation including DES units. The sudden power increment can be observed in all three scenarios at 4 s, which is provided by the inertial response of synchronous generator. However, with the proposed strategy, due to the smoother frequency deviation, the output power of local generations in AC zone is lower when the system is stable, meaning that fewer power burden is added.

The output power of IC is shown in Fig. 11, in which the power flowing from DC side to AC side is assumed to be positive. It can be observed that the IC properly responds to the frequency deviation in AC zone according to (16) and (24). In addition, the voltage of DC zone is depicted in Fig. 10 (b). Due to more supportive power is distracted and transferred from the DC zone, the fluctuation of DC voltage is a little more obvious than that of other strategies, which, however, is negligible compared to the threshold of power quality (i.e., ±5%) and means that the stability will not be deteriorated for the DC zone while supporting the AC grid.

The stability of the hybrid system is reflected by the global variation index which is depicted and listed in Fig. 13 and Table III. As can be seen, even the change of DC voltage is taken into consideration, the comprehensive normalized variation of the proposed strategy is the smallest among three scenarios, which illustrates the effectiveness of the strategy when AC power variation occurs.

![Fig. 10 Power quality variations in case 1. (a) Frequency changes. (b) DC voltage changes.](image)

![Fig. 11 Active power of IC in case 1.](image)

![Fig. 12 Active power increment from local source in case 1. (a) Power generation increment in AC zone. (b) Power generation increment in DC zone.](image)
Proposed flexible support

Besides, fluctuation of frequency is mild and can even be negligible, ranging from 49.90 to 50.03 Hz, which means the frequency quality, corresponding to the stability for AC zone, is little influenced. Therefore, the proposed strategy helps improving the robust characteristics from the regard of the whole SPS system.

The global variation index is depicted and listed in Fig. 17 and Table V. As can be seen, even the change of frequency is taken into consideration, the comprehensive normalized variation of the proposed strategy is the smallest among three scenarios (the little larger overshoot during power decrease is of the negligible magnitude), which illustrates the effectiveness of the strategy when DC power variation occurs.

B. Case 2: Step Power Change in DC Zone

Figs. 14-17, Table IV and Table V show the simulation results of case 2. Due to the lack of rotational inertia in DC zone, there occurs a sudden drop of DC voltage when the net power increment of 5 MW is activated at 4s, as shown in Fig. 14(a). However, with the proposed flexible strategy, the fluctuation of DC voltage is mitigated since the dynamic response characteristics of the strategy (more and quicker power transferred shown in Fig. 15) help to gain more response time for the local DC sources.

With the proposed strategy, the DC voltage decreases with a mild trend and reaches the lowest point of 6.87 kV, then the voltage stabilizes at the value of 6.89 kV at t=10s. In comparison, the DC voltage in other two scenarios drops directly from reference value to 6.81 kV and 6.75 kV, respectively. It can be seen that the only-droop strategy provides higher stable point, but also makes the system suffer the sudden impulse of voltage variation, which brings about negative effect on system stability and might shorten the life span of equipment in DC zone. When the load power decrease is activated at 16s, the voltage recovers to 7 kV, and the proposed method offers a smoother transient process with little overshoot. Therefore, we can conclude that the flexible strategy significantly improves the voltage quality when the power variation occurs in DC zone. Besides, the power burden of DGs including DES in DC zone is relieved compared with that of other two scenarios, as shown in Fig. 16(a).

As can be seen from Figs. 15-16, the better performance of the strategy benefits from the quick power transfer of IC from AC zone to DC zone, and the power burden is properly shared by both zones, which exploits the power support ability of the DESs in the whole system. Besides, the fluctuation of frequency is mild and can even be negligible, ranging from 49.90 to 50.03 Hz, which means the frequency quality, corresponding to the stability for AC zone, is little influenced. Therefore, the proposed strategy helps improving the robust characteristics from the regard of the whole SPS system.
C. Case 3: Consecutive Power Changes in AC&DC Zones

Figs. 18-21, Table VI and Table VII show the simulation results of case 3. A series of net power events in hybrid zones are activated in this simulation case. As can be seen in Fig. 18, the power quality (i.e., the variation of frequency and DC voltage) of the hybrid zones when power disturbances occur has been significantly improved with the help of the proposed strategy.

During 4-10 s, the net power increment of 4.5 MW is adopted in DC zone and causes a voltage drop accordingly. The flexible strategy effectively slows down the variation trend of DC voltage, shown in Fig. 18(b), which leaves larger drop margin for the next power variation. During 10-22 s, the net power increment of 5 MW is activated in AC zone and causes a frequency drop accordingly. As shown in Fig. 18(a), though the frequency curve with the flexible strategy is lower at the beginning of 10 s, it reaches to the higher lowest point of 49.78 Hz, and converges to stable value more quickly and thus has better transient response. By comparison, the frequency of other scenarios both drop under the normal variation range, and some emergency measures might be taken to keep the system’s stability. In addition, the DC voltage is also showing higher stable value with 6.84 kV compared with other two scenarios.

The power increments are canceled at 22 s in DC zone and at 32 s in AC zone, respectively. During the recovery process, smoother variations of frequency and voltage can be observed from Fig. 20, which illustrates the good performance of the strategy under the de-loading situation. It is worth noting that, the performance under continuous power variation might have no such significant improvement in stable value compared with that when power disturbance occurs in only single zone, but the transient performance improvement is still clear and contributes to the system robustness.

It can be observed from Fig. 20 that, the better performance is realized by the reasonable power sharing between the hybrid zones and our strategy does not require more power supply from local generations, meaning that no extra power burden is caused with the proposed method, which features high efficiency during operation.

The global variation index is depicted and listed in Fig. 21 and Table VII. As can be seen, when the consecutive power variations occur in both AC and DC zones, the comprehensive normalized variation of the proposed strategy is the smallest among three scenarios, which illustrates the effectiveness of the strategy under complex operational situations.
VI. CONCLUSION

In this paper, a flexible power control strategy for hybrid SPS system is proposed, which fully considers global power support capability of DESs in different zones. The proposed strategy sufficiently utilizes the operational features of both the AC and DC grids, and shows good performances in diminishing the variation of frequency and DC voltage during severe power events. Key findings of this paper can be summarized as:

1) The relationship between the frequency and the DC voltage is discussed based on the principles of VSG and virtual capacitor, which is used to design the flexible power strategy for the DESs and ICs of the hybrid zones in SPS;

2) The proposed strategy is designed according to the operating characteristics of the hybrid system, which enables the DES units to respond to the net power deviation of both the local and the opposite zones, and by the help of ICs between the hybrid grids, a reasonable mutual power support is realized to enhance the power quality and dynamics of the whole SPS while facing short-term high power demand.

In the future works, a multi-level power control strategy will be extended from this study for multiple time scale optimization of SPS’s performance, in which the operational features of variable generations will be considered and hybrid energy storage system will be considered.

VII. REFERENCES


