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Plug-and-Play Voltage/Current Stabilization DC Microgrid Clusters with Grid-Forming/Feeding Converters

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Abstract—In this paper, we propose a new decentralized control scheme for Microgrid (MG) clusters, given by the interconnection of atomic dc MGs, each composed by grid-forming and grid-feeding converters. In particular, we develop a new Plug-and-Play (PnP) voltage/current controller for each MG in order to achieve simultaneous voltage support and current feeding function with local references. The coefficients of each stabilizing controller are characterized by explicit inequalities, which are related only to local electrical parameters of the MG. With the proposed controller, each MG can plug-in/out of the clusters seamlessly irrespectively of the power line parameters and models of other MGs. A profound proof of closed-loop stability of MG clusters is provided. Moreover, theoretical results are validated by hardware-in-loop (HiL) tests.

I. INTRODUCTION

During the past decades, dc MGs have been recognized more and more attractive compared with ac MG [1], as they provide a higher efficiency, more natural interface. Grid-forming converters are used as the interface between energy storage system (ESSes) and the system to provide voltage support in dc MGs. To achieve simultaneous voltage support and communication-less current sharing among ESSes, voltage-current (V-I) or I-V droop control [2], [3] is widely adopted by imposing virtual impedance for output voltages. However, voltage deviations and current sharing errors cannot be eliminated due to different line impedances. Another key challenge is that the stability of connected ESSes is sensitive to the chosen virtual impedances which should be designed taking into account the specific MG topologies [4], [5], [6]. Recently, an alternative class of decentralized primary controllers, called PnP controller according to the terminology used in [7], has been proposed in [8], [9], [10]. In [10], to achieve PnP robust voltage control, information about line impedances need be known to form the upper and lower boundary for system model. On the other hand, PnP controllers in [8], [9] form a decentralized control architecture where each regulator can be synthesized using information about the corresponding ESSes only [9] or, at most, specific parameters of the power lines connected to the ESSes [8]. The latter pieces of information are not required in the design procedure of [9], which is therefore termed line-independent method.

However, for the PnP methods mentioned above, the synthesis of a PnP controller requires to solve a convex optimization problem, and if it is unfeasible, the plug-in/out of corresponding ESS must be denied. Moreover, they are only suited for grid-forming converters, as they provide only voltage support in the system. However, one complete MG must be composed of renewable energy source (RESes), ESSes and loads to achieve the power generation, storage and consumption. When RESes such as PV sources are added in dc MGs, grid-feeding converters should be used as the interface to achieve current feeding for the system according to the reference given by e.g. maximum power point tracking algorithm [11]. Furthermore, the current stabilization should be guaranteed. In [12], a current-based PI primary droop control is proposed considering the constant current load. Then, a current-based PnP controller is proposed for grid-feeding converters [13]. The joint utilization of grid-feeding and grid-forming converters has been considered for studying energy management problems [14], [15], [16]. However, from the stability point of view, if the grid-forming and grid-feeding converters are considered simultaneously, the controller and its stability should be redesigned. To authors’ knowledge, the stabilization of MG clusters including both types of converters has never been considered before, independently of the number of MGs and the topologies.

In this paper, considering a MG cluster, a PnP voltage/current controller is proposed to achieve voltage support and current feeding functions simultaneously. The set of coefficients of each local controller is explicitly characterized through a set of inequalities which only depends on the local parameters. In particular, we show that controller design is always feasible and does not require to solve an optimization problem. Global closed-loop stability is formally proven.

The paper is structured as follows. In Section II and III-A, the model of a MG cluster and the proposed controller are introduced. In Section III-B, the global closed-loop stability is proven. Finally, the HiL tests are shown in Section IV.

II. DC MGs with Grid-Forming/Feeding Converters

A. Electrical model of MGs

A MG composed of one grid-forming converter and one grid-feeding converter connected to a single point of common
A MG cluster is obtained by interconnecting $N$ MGs, induced by the set $D = \{1, \ldots, N\}$. Two MGs are neighbors if there is a power line connecting them and denote with $N_i \subset D$ the subset of neighbors of MG $i$. The neighboring relation is symmetric which means $j \in N_i$ implies $i \in N_j$. Furthermore, let $\mathcal{E} = \{(i, j) : i \in D, j \in N_i\}$ collect unordered pairs of indices associated to lines. The topology of the MG cluster is then described by the undirected graph $G_{\mathcal{E}}$, with nodes $D$ and edges $\mathcal{E}$. The electrical scheme of the $i$-th MG is illustrated in left block of Fig. 1.

\[
\begin{align*}
\text{MG } i & : \\
\frac{dV_i}{dt} &= \frac{1}{C_{ti}} \bar{i}^C_{ti} + \frac{1}{C_{ti}} V_i + \sum_{j \in N_i} \left( \frac{V_j}{C_{tij}} R_{tij} - \frac{V_i}{C_{tij}} R_{tij} \right) \\
\frac{dI^C_{ti}}{dt} &= \frac{1}{L_{ti}} \bar{V}_i - \frac{R_{ti}}{T_{ti}} I^C_{ti} + \frac{1}{T_{ti}} V^C_{ti} \\
\frac{dV^C_{ti}}{dt} &= \frac{1}{L_{ti}} V_i - \frac{R_{ti}}{T_{ti}} V^C_{ti} + \frac{1}{T_{ti}} V^V_{ti} \\
\end{align*}
\]

where variables $V_i$, $I^C_{ti}$, $I^V_{ti}$ are the $i$-th PCC voltage, filter current from RES and filter current from ESS, respectively. For the grid-feeding converter, $V^C_i$ represents the command and $R^C_{ti}$, $L^C_{ti}$ are the electrical parameters. For the grid-forming converter, $V^V_i$ represents the command and $R^V_{ti}$, $L^V_{ti}$ are the electrical parameters; $C_{ti}$ is the capacitor at the PCC bus. Moreover, $V_i$ is the voltage at the PCC of each neighboring MGs $j \in N_i$ and $R_{tij}$ and $L_{tij}$ are the resistance and inductance of the dc power line connecting MGs $i$ and $j$. In general, the RL parameters are different for grid-feeding and grid-forming converters.

**Fig. 1:** Electrical Scheme of MG $i$ with PnP Voltage/Current Controller.

**B. State-space model of MG Clusters**

Dynamics (1) provides the state-space model:

\[
\begin{align*}
\Sigma^{MG}_{[i]} : \\
\hat{x}^{[i]}(t) &= A_{[i]} x^{[i]}(t) + B_i u^{[i]}(t) + M_i d^{[i]}(t) \\
&\quad + \xi^{[i]}(t) + \Lambda_{\text{load},i} x^{[i]}(t) \\
\hat{z}^{[i]}(t) &= H_i x^{[i]}(t) \\
\end{align*}
\]

where $x^{[i]} = [V_i, I^C_{ti}, I^V_{ti}]^T$ is the state of the system, $u^{[i]} = [V^C_{ti}, V^V_{ti}]$ is the control input, $d^{[i]} = I_{ti}$ is the exogenous input and $\hat{x}^{[i]} = [I^C_{ti}, V^C_{ti}]$ is the controlled variable. The term $\xi^{[i]} = \sum_{j \in N_i} A_{ij} (x^{[j]} - x^{[i]})$ accounts for the coupling with each MG $j \in N_i$. The matrices of $\Sigma^{MG}_{[i]}$ are obtained from (1). The details about matrices can be found in [17].

The overall model for a MG cluster is given by

\[
\begin{align*}
\hat{x}(t) &= Ax(t) + Bu(t) + Md(t) \\
\hat{z}(t) &= Hx(t)
\end{align*}
\]

where $x = (x^{[1]}, \ldots, x^{[N]}) \in \mathbb{R}^{3N}$, $u = (u^{[1]}, \ldots, u^{[N]}) \in \mathbb{R}^{2N}$, $d^C = (d^{[1],C}, \ldots, d^{[N],C}) \in \mathbb{R}^{N}$, $z = (z^{[1]}, \ldots, z^{[N]}) \in \mathbb{R}^{2N}$. Matrices $A$, $B$, $M$ and $H$ are reported in Appendix A in [17].

**III. DESIGN OF STABILIZING VOLTAGE/CURRENT CONTROLLERS**

**A. Structure of PnP Voltage/Current controllers**

In order to track constant references $z_{\text{ref},i}(t)$, when $d(t)$ is constant as well, the MG model is augmented with integrators [18]. A necessary condition for making error $e(t) = z_{\text{ref},i}(t) - z_i(t)$ equal to zero as $t \to \infty$, is that, for arbitrary $\bar{d}$ and $\bar{z}_{\text{ref}}$, there are equilibrium states and inputs $\hat{x}$ and $\hat{u}$ verifying (2). The existence of these equilibrium points can be shown as in the proof of Proposition 1 in [8].

Let $I_{\text{cap},i}^u > 0$ define the maximal output current capability provided by MG $i$. According to the block on the bottom right of Fig. 1, the dynamics of integrators are given by

\[
\begin{align*}
\hat{V}^{C}_{[i]}(t) &= \hat{V}^{C}_{[i]}(t) + \hat{C}_{ti} \frac{\bar{d}^{[i]}(t)}{\hat{C}_{ti}} \\
\hat{V}^{V}_{[i]}(t) &= \hat{V}^{V}_{[i]}(t) - \hat{C}_{ti} \frac{(\bar{d}^{[i]}(t) - \bar{d}^{[i]}(t))}{\hat{C}_{ti}}
\end{align*}
\]

where $\hat{V}^{C}_{[i]} = [V^{C}_{[1]}, \ldots, V^{C}_{[N]}] \in \mathbb{R}^{N}$ is the state, $\hat{V}^{V}_{[i]} = [V^{V}_{[1]}, \ldots, V^{V}_{[N]}] \in \mathbb{R}^{N}$ is the command, $\hat{C}_{ti}$, $\hat{C}_{tij}$ are the capacitance and resistance of the dc power line connecting MGs $i$ and $j$. The overall augmented system is obtained from (4) as

\[
\begin{align*}
\dot{\hat{x}}^{[i]}(t) &= \hat{A}_{[i]} x^{[i]}(t) + \hat{B}_i u^{[i]}(t) + \hat{M}_i d^{[i]}(t) \\
\hat{z}^{[i]}(t) &= \hat{H}_i x^{[i]}(t)
\end{align*}
\]
B. Conditions for stability of the closed-loop MG Cluster

For showing stability, we will use local Lyapunov functions

\[ V_i(\hat{x}_{i|1}) = [\hat{x}_{i|1}]^T P_i \hat{x}_{i|1}. \] (7)

**Assumption 1.** The positive definite matrix \( P_i \in \mathbb{R}^{5 \times 5} \) in (7) fulfills

\[ P_i = \begin{bmatrix} \eta_i & 0_{1 \times 2} & 0_{1 \times 2} \\ 0_{2 \times 1} & P_{22,i}^C & 0_{2 \times 2} \\ 0_{2 \times 1} & 0_{2 \times 2} & P_{44,i}^V \end{bmatrix}, \] (8)

where

\[ P_{22,i}^C = \begin{bmatrix} p_{22,i}^C & p_{23,i}^C \\ p_{23,i}^C & p_{33,i}^C \end{bmatrix}, \quad P_{44,i}^V = \begin{bmatrix} p_{44,i}^V & p_{45,i}^V \\ p_{45,i}^V & p_{55,i}^V \end{bmatrix}. \] (9)

And \( \eta_i > 0 \) is a local parameter satisfying \( \eta_i = \hat{\sigma} C_{ti}, \ i \in \mathcal{D} \) where \( \hat{\sigma} > 0 \) is a constant parameter, common to all MGs.

In absence of coupling terms \( \hat{\xi}_{i|1}(t) \), and load terms \( \hat{A}_{load,i} \hat{x}_{i|1}(t) \), we would like to guarantee asymptotic stability of the nominal closed-loop MG

\[ \hat{x}_{i|1}(t) = (A_{ni} + \hat{B}_i K_i) \hat{x}_{i|1}(t) + \hat{M}_i \hat{d}_{i|1}(t). \] (10)

By direct calculation, one can show that \( F_i \) has the following structure

\[ F_i = \begin{bmatrix} 0 & f_{12,i} & 0 & f_{14,i} & 0 \\ f_{21,i} & f_{22,i} & f_{23,i} & 0 & 0 \\ f_{41,i} & 0 & 0 & f_{44,i} & f_{45,i} \\ 0 & 0 & 0 & 0 & 0 \\ \end{bmatrix} \]

\[ = \begin{bmatrix} 0 & \frac{1}{1 - e^{-t_i}} & 0 & \frac{1}{1 - e^{-t_i}} & 0 \\ \frac{(k_{1,i}^V - 1)}{t_i} & \frac{(k_{2,i}^V - R_{ti}^V)}{t_i} & \frac{e^{-t_i}}{t_i} & 0 & 0 \\ 0 & -1 & 0 & 0 & 0 \\ \frac{(k_{3,i}^V - 1)}{t_i} & 0 & 0 & \frac{(k_{3,i}^V - R_{ti}^V)}{t_i} & \frac{e^{-t_i}}{t_i} \\ -1 & 0 & 0 & 0 & 0 \\ \end{bmatrix} \] (11)

\[ = \begin{bmatrix} 0 & F_{12,i}^C & F_{14,i}^V \\ F_{21,i}^C & F_{22,i}^C & 0 \\ F_{41,i}^V & 0 & F_{44,i}^V \end{bmatrix}. \]

From Lyapunov theory, asymptotic stability of (10) can be certified by the existence of a Lyapunov function \( V_i(\hat{x}_{i|1}) = [\hat{x}_{i|1}]^T P_i \hat{x}_{i|1} \) where \( P_i = P_i^T > 0 \) and

\[ Q_i = F_i^T P_i + P_i F_i \] (12)

is negative definite. In presence of nonzero coupling terms, we will show that asymptotic stability can be achieved under Assumption 1.

Based on (8) and (11), (12) can be rewritten as (13) shown in the upper part of the next page.

Next, we provide two lemmas and two propositions by which we can analyze the closed-loop system and parametrize explicitly the set of stabilizing controllers.

**Lemma 1.** Under Assumption 1, if \( Q_i \leq 0 \), \( Q_i \in \mathbb{R}^{5 \times 5} \) has the following structure

\[ Q_i = \begin{bmatrix} 0 & 0_{1 \times 2} & 0_{1 \times 2} \\ 0_{2 \times 1} & Q_{22,i}^C & 0_{2 \times 2} \\ 0_{2 \times 1} & 0_{2 \times 2} & Q_{44,i}^V \end{bmatrix} \] (14)

Furthermore, the blocks on the diagonal must verify

\[ \begin{cases} Q_{22,i}^C \leq 0 \\ Q_{44,i}^V \leq 0 \end{cases} \] (15a) (15b)

**Proof.** See the proof of Lemma 2 in [17]. \( \Box \)

**Remark 1.** Since the blocks \( Q_{22,i}^C \) and \( Q_{44,i}^V \) belong to \( \mathbb{R}^{2 \times 2} \), from (15), the determinants of \( Q_{22,i}^C \) and \( Q_{44,i}^V \) are nonnegative.

**Proposition 1.** [9] If \( Q = Q^T \leq 0 \) and an element \( q_{ii} \) on the diagonal are verified \( q_{ii} = 0 \), then

(i) The matrix \( Q \) cannot be negative definite.

(ii) The \( i \)-th row and column of \( Q \) have zero entries.

**Proposition 2.** Under Assumption 1, matrices \( P_i \) and \( Q_i \) have the structure given in (16) (displayed in the upper part of next page), where \( h_i = L_i^V (k_{1,i}^V - (k_{1,i}^V - 1)(k_{2,i}^V - R_{ti}^V)). \)

Moreover, if \( P_i > 0 \), \( Q_i \leq 0 \) and \( Q_i \not= 0 \), one has

\[ \begin{cases} k_{1,i}^V < 1 \\ k_{2,i}^V < R_{ti}^V \\ k_{3,i}^V > 0 \end{cases} \]

\[ \begin{cases} 0 < k_{1,i}^V < \frac{1}{L_i^T} (k_{1,i}^V - 1)(k_{2,i}^V - R_{ti}^V) \end{cases} \] (17)

**Proof.** See proof of Proposition 4 in [17]. \( \Box \)

**Lemma 2.** Let Assumptions 1 and Proposition 2 hold, define \( h_i(v_i) = v_i^T Q_{44,i}^V v_i \), with \( v_i \in \mathbb{R}^2 \). If \( Q_i \leq 0 \), and \( Q_i \not= 0 \), then

\[ h_i(\bar{v}_i) = 0 \iff \bar{v}_i \in \ker(F_{44,i}) \]

**Proof.** See the proof of Proposition 3 in [9]. \( \Box \)

**Proposition 3.** Let \( g_i(w_i) = w_i^T Q_i w_i \), \( \forall i \in \mathcal{D} \) with \( w_i \in \mathbb{R}^5 \). Under Assumption 1, Proposition 2, and Lemma 2, only vectors \( \bar{w}_i \) in the form

\[ \bar{w}_i = [\alpha_i \ 0 \ \gamma_i \ \beta_i \ \delta_i \beta_i] \]

with \( \alpha_i, \gamma_i, \beta_i, \delta_i \in \mathbb{R} \) and \( \delta_i = -\frac{k_{2,i}^V - R_{ti}^V}{k_{3,i}^V} \), fulfill

\[ g_i(\bar{w}_i) = \bar{w}_i^T Q_i \bar{w}_i = 0. \] (18)

**Proof.** See the proof of Proposition 5 in [17]. \( \Box \)

Consider the overall closed-loop MG cluster model

\[ \begin{bmatrix} \dot{x}(t) = (\hat{A} + \hat{B} K) \hat{x}(t) + \hat{M} \hat{d}(t) \\ z(t) = \hat{H} \hat{x}(t) \end{bmatrix} \] (19)
where
\[ \hat{A} = \hat{A}_D + \hat{A}_S + A_L + \hat{A}_C, \]
(23)
where \( \hat{A}_D = \text{diag}(\hat{A}_{11}, \ldots, \hat{A}_{NN}) \) collects the local dynamics only, \( \hat{A}_C \) collects the coupling dynamic representing the off-diagonal items of matrix \( \hat{A} \). Moreover, matrices \( \hat{A}_S = \text{diag}(\hat{A}_{11}, \ldots, \hat{A}_{NN}) \) and \( A_L = \text{diag}(A_{\text{load,1}}, \ldots, A_{\text{load,N}}) \), where
\[ \hat{A}_{\text{load},i} = \begin{bmatrix} \frac{1}{C_{\text{ti}}} \sum_{j \in \mathcal{N}_i} \frac{1}{C_{\text{ji}}} & 0_{4 \times 1} \\ 0_{4 \times 1} & 0_{4 \times 4} \end{bmatrix}, \]
take into account the dependence of each local state on the neighboring MGs and the local resistive load respectively. According to the decomposition (23), the inequality (22) is equivalent to
\[
\left( \hat{A}_D + \hat{B}_C \right) \hat{P} + P(\hat{A}_D + \hat{B}_C) + 2(\hat{A}_S + A_L)P + \hat{A}_C P + P \hat{A}_C \leq 0 \tag{24}
\]
Proposition 4. If gains \( K_i \) are chosen according to (17), then \( Q_i \leq 0 \) for all \( i \in \mathcal{D} \), finally (22) holds.

Proof. See proof of Proposition 6 in [17].

Theorem 1. If Assumptions 1 is fulfilled, the graph \( \mathcal{G}_{el} \) is connected, control coefficients are chosen according to (17), then the origin of (5) is asymptotically stable.

Proof. See proof of Theorem 2 in [17].

Remark 2. The design of stabilizing controller for each MG can be conducted according to Proposition 2. In particular, differently from the approach in [9], no optimization problem has to be solved for computing a local controller. Indeed, it is enough to choose control coefficient \( k_i^\ell \), \( k_i^{\ell'} \), \( k_i^{\ell''} \), \( k_i^{\ell'''} \), \( k_i^V \), \( k_i^{V'} \), \( k_i^{V''} \), \( k_i^{V'''} \) fulfilling the inequalities in (17). Note that these inequalities are always feasible, implying that a stabilizing controller always exists. Moreover, the inequalities depend only on the parameters \( R_{\text{ti}} \) and \( R_{\text{ti}}^V \) of the MG \( i \). Therefore, the control synthesis is independent of parameters of MGs and power lines, which means that controller design can be executed only once for each converter in a plug-and-play fashion.

IV. HARDWARE-IN-LOOP TEST

In order to verify the correctness of theoretical results, real-time HiL tests have been carried out using dSPACE 1006 platform. The real-time test model comprises four MGs with meshed electrical topology shown in Fig. 2. Meanwhile, the electrical setup information are shown in TABLE I and the transmission lines parameters are shown in TABLE II and the control coefficients are shown in TABLE III.

A. Case 1: PnP Test

In this subsection, the effectiveness of the proposed primary PnP controller is verified. Each MG is started separately. At the beginning, we set different voltage and current references for different MGs. The results are shown in Fig. 3. At \( t = T_1 \), MGs 1–3 are connected together without
changing the control coefficients. As shown in Fig. 3a, after the connection of MGs 1 – 3, only small disturbances appear in the voltage waveform. Moreover, there is no major variation affecting the output currents as shown in Fig. 3b. Then at $t = T2$, MG 4 is connected to the system. Similarly, as shown in Fig. 3, after small disturbance, both the output voltage and current track the respective reference values. Fig. 4 illustrates the current tracking performance by changing the current references for different MGs. At $t = T1$, four MGs are connected together simultaneously. At $t = T2$, the current reference for MG 1 is changed from 1A to 2.5A. At $t = T3$, the current reference for MG 2 is changed from 2A to 3.5A. At $t = T4$, the current reference for MG 3 is changed from 3A to 1.5A. At $t = T5$, the current reference for MG 4 is changed from 4A to 5.5A. As shown in Fig. 4b, whether the current references are increased or decreased, the output currents can track the changed reference. In addition, as shown in Fig. 4a, when the current references are changed, the output voltages are only affected by little oscillations approximately 0.05V.

![Fig. 2: System Configuration of Hardware-in-Loop Test.](image)

![Fig. 3: The Plug-in/out Performance of primary PnP controllers.](image)

![Fig. 4: Voltage and Current Tracking Performance of PnP decentralized controllers.](image)

**B. Case 2: Instability Test**

The correctness and accuracy of coefficient sets in (17) derived from Proposition 2 is verified. According to the system parameters shown in TABLE I, for each MG, the controller coefficients must verify

$$
\begin{align*}
&k_{1,i}^C < 1 \\
&k_{2,i}^C < 0.2 \\
&k_{3,i}^C > 0 \\
&0 < k_{3,i}^C < \frac{1}{L_{Is}}(k_{1,i}^V - 1)(k_{2,i}^V - R_{is}^V)
\end{align*}
$$

(25)

Based on the (25), the value of control coefficients are chosen as shown in Table III. At the beginning, MGs are operated separately and at $t = 0.5s$ MGs are connected together to form the MG cluster. Then at $t = 1s$, the control coefficients are changed in order to violate (25). Fig. 5 including six sub-figures illustrates the system performance when each control coefficient is changed from the stable region to the unstable region. Fig. 5a to 5e show that when control coefficients for the grid-forming converter in MG

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>DC source voltage</td>
<td>$V_{Pri}$</td>
<td>100 V</td>
</tr>
<tr>
<td>Nominal voltage</td>
<td>$V_{ref,i}$</td>
<td>48 V</td>
</tr>
<tr>
<td>Output capacitance</td>
<td>$C_{is}$</td>
<td>2.2 mF</td>
</tr>
<tr>
<td>Inductance for CDGU</td>
<td>$L_{C,i}^V$</td>
<td>0.018 H</td>
</tr>
<tr>
<td>Inductor + switch loss resistance for CDGU</td>
<td>$R_{C,i}^V$</td>
<td>0.2 Ω</td>
</tr>
<tr>
<td>Inductance for VDGU</td>
<td>$L_{V,i}^V$</td>
<td>0.0018 H</td>
</tr>
<tr>
<td>Inductor + switch loss resistance for VDGU</td>
<td>$R_{V,i}^V$</td>
<td>0.1 Ω</td>
</tr>
<tr>
<td>Switching frequency</td>
<td>$f_{sw}$</td>
<td>10 kHz</td>
</tr>
</tbody>
</table>

**TABLE II: Transmission lines parameters**

<table>
<thead>
<tr>
<th>Connected MGs $(i,j)$</th>
<th>Resistance $R_{i,j}(Ω)$</th>
<th>Inductance $L_{i,j}(mH)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1, 2)</td>
<td>0.3</td>
<td>1.8</td>
</tr>
<tr>
<td>(2, 3)</td>
<td>0.6</td>
<td>5.4</td>
</tr>
<tr>
<td>(3, 4)</td>
<td>0.8</td>
<td>7.2</td>
</tr>
<tr>
<td>(4, 1)</td>
<td>0.7</td>
<td>3.6</td>
</tr>
</tbody>
</table>

**TABLE III: Control Coefficients for MG $i = 1, 2, 3, 4$**

<table>
<thead>
<tr>
<th>Control Coefficients</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>For grid-feeding converters</td>
<td>$k_{1,i}^C$</td>
<td>-0.01</td>
</tr>
<tr>
<td></td>
<td>$k_{2,i}^C$</td>
<td>-2.7015</td>
</tr>
<tr>
<td></td>
<td>$k_{3,i}^C$</td>
<td>40.4018</td>
</tr>
<tr>
<td>For grid-forming converters</td>
<td>$k_{1,i}^V$</td>
<td>-0.480</td>
</tr>
<tr>
<td></td>
<td>$k_{2,i}^V$</td>
<td>-0.108</td>
</tr>
<tr>
<td></td>
<td>$k_{3,i}^V$</td>
<td>30.673</td>
</tr>
</tbody>
</table>
2 go sightly out of the stable region, the system becomes unstable. Fig. 5d to 5f show that the same happens when control coefficients for the grid-feeding converter in MG 2 slightly violate the inequality.

![Diagram](image)

\( k_{V,i} \) changed from -0.48 to 1.1.

\( k_{V,i} \) changed from -0.108 to 0.11.

\( k_{L,i} \) changed from 30.67 to 180.

\( k_{C,i} \) changed from -0.01 to 1.1.

\( k_{C,i} \) changed from -2.7 to 0.3.

\( k_{C,i} \) changed from 40.4 to -1.

Fig. 5: Voltage Profile of Instability Test

V. CONCLUSION

In this paper, a PnP Voltage/Current controller for DC microgrid clusters is proposed. By choosing the control coefficients according to inequalities which are only related to local parameters, the closed-loop stability can be guaranteed for the MG cluster. Under the proposed control structure, each MG can plug in and out without changing the control coefficients and without knowing the electrical topology of the MG cluster. As in [9], the proofs of closed-loop asymptotic stability exploit structured Lyapunov functions, the LaSalle invariance theorem and properties of graph Laplacians. Thus it shows that these tools offer a feasible theoretical framework for analyzing different kinds of MGs equipped with various types PnP decentralized control architectures. Finally, HiL tests prove the effectiveness and accuracy of the theoretical analysis results.

REFERENCES


