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Analysis and Suppression for Frequency Oscillation in a Wind-Diesel System

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ABSTRACT In a wind-diesel system with weak network architecture, many techniques are utilized to enhance its stability. However, the frequency oscillation between the grid-side converter and the diesel generator may be caused by their interactions, and there are only a few studies considering this issue, which is a major challenge for the stability. To tackle this challenge, the cause of frequency oscillation is studied, and an adaptive fuzzy PI controller based on the variable universe is proposed to suppress oscillation in this paper. The control parameter of the wind turbine generator (WTG) converter’s dc-link voltage loop and wind speed has an important influence on the oscillation. Our main idea is to suppress frequency oscillation by the optimizing control parameter. In order to analyze the interaction between WTG and diesel generator, we develop the small-signal models of the wind-diesel generator. Subsequently, the adaptive fuzzy PI controller based on the variable universe is proposed in the dc-link voltage loop to optimize control parameter instead of gain-scheduled PI controller, and its key feature is the innovative use of an extension factor with d-axis current in the output universe. The function of the extension factor is to adapt WTG to different wind speeds. The experimental results demonstrate that the proposed controller can significantly suppress frequency oscillation. The oscillation amplitude of isolated grid frequency is also significantly reduced by up to 0.175 Hz.

INDEX TERMS Frequency oscillation, fuzzy PI controller, wind turbine generator (WTG), variable universe, wind-diesel system.

I. INTRODUCTION

With the rapid development of renewable energy, a large number of power electronic devices are connected to the power system. The increasing of installed capacity of wind power brings power system new challenges of operation and control. Especially in a wind-diesel system, the capacity of power electronic devices accounts for a large proportion. Due to poor adaptability of the device controllers and the interactions between the devices and the wind-diesel system, frequency oscillations are easily caused, which need to be improved [1]–[3].

At present, some studies on wind turbine generator (WTG) oscillation can be broadly categorized into various classes. a) Oscillations caused by self-characteristic of WTG. Reference [4] considered wind shear and tower shadow effects in WTGs. Such oscillation is called a 3p oscillation, which can cause shaft torsion load aggravation and shaft torque oscillation, and inevitably leads to electromagnetic torque and power fluctuations in the generator [5]. b) Sub-synchronous resonance (SSR) oscillations. SSR oscillations in nearby wind turbine-generators connected to series capacitive compensated transmission systems were studied [6]–[8]. Furthermore, references [9], [10] pointed out some rules of SSR problems in wind farm. c) Inter-area oscillations. Inter-area oscillations of WTGs and interconnected system were researched [11], [12]. The level of oscillation was related to the output power of WTGs [13]. In this paper, a new oscillation problem caused by the interactions between WTGs and the weak grid is one of the major challenges for system stability, which is less studied.

Currently, there are many analysis methods for frequency oscillation. a) Modal identification method was applied to discriminate and analyze the real-time monitoring waveform
Section III uses the small-signal model to analyze the contributions with respect to the proposed control algorithms. This paper optimizes control parameter based on fuzzy control optimizing PI control parameter [25], [26]. Therefore, this disadvantage of the GSPI controller. However, wind speed is not considered. This paper tackles the oscillations between DC-link capacitor of the gridside converter (GSC) of permanent magnet synchronous generator (PMSG)-based wind turbine and the diesel generator in an isolated grid, as the above strategies are inappropriate. Generally, gain scheduled PI (GSPI) controller is one of the most popular methods in the DC-link voltage control loop of GSC [22]–[24]. In this paper, the frequency oscillation is caused by the interaction between WTG and the diesel generator. DC-link voltage and wind speed are two factors that influence the oscillation. DC-link voltage is applied in the GSPI controller. However, wind speed is not considered. Moreover, the fuzzy control theory has the advantage of optimizing PI control parameter [25], [26]. Therefore, this paper optimizes control parameter based on fuzzy control theory to mitigate the oscillation in a wind-diesel system. The contributions with respect to the proposed control algorithms are as follows.

- To suppress frequency oscillation, this paper develops an adaptive fuzzy PI controller based on the variable universe, which proposes an extension factor with d-axis current in the output universe. The function of the extension factor is to add wind speed to the optimization of the control parameter.
- Based on oscillation phenomena and eigenvalue analysis of a small-signal model of the wind-diesel system, it is found that the control parameter has an influence on the oscillation. With the increasing of wind speed, the amplitude of oscillation decreases.
- Comparing with the state-of-the-art GSPI control, the oscillation amplitude of isolated grid frequency and DC-link voltage with the proposed method are significantly reduced by up to 0.175 Hz and nearly 10 V respectively.

This paper is organized as follows. Section II describes the oscillation phenomena in an isolated wind-diesel grid. Section III uses the small-signal model to analyze the wind-diesel system. The proposed fuzzy PI controller is designed in section IV. The experiment results are shown in section V. Finally, the conclusion is drawn in section VI.

II. MOTIVATION

A. ISOLATED WIND-DIESEL GRID FRAMEWORK

The isolated grid includes a diesel generator, a PMSG-based wind turbine, and load. The isolated grid framework is shown in Fig. 1. The role of a diesel generator is to support isolated grid voltage and frequency. The PMSG-based wind turbine is simulated by an indoor WTG. The indoor WTG consists of operating cabinet, grid-connected cabinet, main control cabinet, induction motor (IM) and PMSG. The driving system of wind turbine simulation is composed of inverter and IM. The output of IM is adjusted by the inverter. IM drags PMSG running. The output power of PMSG is fed to the isolated grid through the converter. The maximum power point tracking (MPPT) is achieved by stator-side converter (SSC). DC-link voltage is stabilized by GSC. The wind turbine simulation algorithm is applied to PLC. According to wind speed, pitch angle and generator speed, wind turbine mechanical power are calculated by (1).

\[
P_m = 0.5 \rho C_p(\lambda, \beta) A_r V_w^3,
\]

\[
C_p(\lambda, \beta) = c_1(c_2 \lambda_i - c_3 \beta - c_4) e^{-c_5 \lambda_i} + c_6 \lambda,
\]

\[
\lambda_i = \frac{1}{\omega_r V_w^3}
\]

\[
\lambda = \frac{1}{\lambda} + 0.08 \beta - \frac{0.035}{\beta^3 + 1}
\]

where \( P_m \) is mechanical power, \( \rho \) is air density, \( C_p \) is the power coefficient, \( \lambda \) is the tip speed ratio, \( \beta \) is the pitch angle, \( A_r \) is the effective area covered by turbine blades, \( V_w \) is wind speed, \( c_1, c_2, c_3, c_4, c_5 \) and \( c_6 \) are coefficients. \( \omega_r \) is the generator-angular speed. Wind speed is obtained by a look-up table or I external input. The pitch angle control system is also simulated in PLC.

The overall control block diagrams of the isolated wind-diesel grid are shown in Fig. 2. \( P_e \) is output power of PMSG-based wind turbine, \( P_d \) is output power of diesel generator and \( P_l \) is load power. Power deviation \( P_{dev} \) is the sum of \( P_e \), \( P_d \), and \( P_l \). Then frequency deviation \( f_{dev} \) is obtained by frequency dynamic model \( H_\delta(s) \), while \( M \) is inertia coefficient and \( D \) is damping coefficient. The diesel generator is controlled to balance grid power flow. The governor and engine
TABLE 1. Parameters of isolated grid.

<table>
<thead>
<tr>
<th>Systems</th>
<th>Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Diesel engine</td>
<td>Rated power</td>
<td>13.5 kW</td>
</tr>
<tr>
<td>Diesel generator</td>
<td>Rated power</td>
<td>10 kW</td>
</tr>
<tr>
<td></td>
<td>Rated frequency</td>
<td>50 Hz</td>
</tr>
<tr>
<td></td>
<td>( T_d )</td>
<td>0.005 s</td>
</tr>
<tr>
<td></td>
<td>( T_g )</td>
<td>0.1 s</td>
</tr>
<tr>
<td>Constant load</td>
<td>Rated power</td>
<td>4.5 kW</td>
</tr>
<tr>
<td>Electronic load</td>
<td>Rated power</td>
<td>10 kW</td>
</tr>
<tr>
<td>Wind turbine</td>
<td>Rated wind speed</td>
<td>12 m/s</td>
</tr>
<tr>
<td></td>
<td>Blade radius</td>
<td>2.53 m</td>
</tr>
<tr>
<td>PMSG</td>
<td>Rated power</td>
<td>9 kW</td>
</tr>
<tr>
<td></td>
<td>Rated angular speed</td>
<td>38.4 rad/s</td>
</tr>
<tr>
<td></td>
<td>( L_f )</td>
<td>5 mF</td>
</tr>
<tr>
<td></td>
<td>( C_f )</td>
<td>31.4 ( \mu )F</td>
</tr>
<tr>
<td></td>
<td>( J )</td>
<td>0.00375 kg·m²</td>
</tr>
<tr>
<td>Wind-diesel system</td>
<td>( M )</td>
<td>0.5</td>
</tr>
<tr>
<td></td>
<td>( D )</td>
<td>0.01</td>
</tr>
</tbody>
</table>

The grid parameters are shown in Table 1.

\( \omega \) reference classical PI controller is to stabilize the WTG speed at the reference value. The control strategy of GSC is shown in Fig. 3. \( \tau \) is the mechanical time constant of pitch servo, and \( J \) is a moment of inertia. Isolated wind-diesel dynamics of diesel generator are modeled as in [27]. \( T_d \) and \( T_g \) are time constants of engine and governor respectively. \( k_{po} \) and \( k_{idc} \) are controller parameters of diesel generator. In the pitch system of WTG, \( \beta_{ref} \) is a reference value of pitch angle, \( \tau_p \) is the mechanical time constant of pitch servo, and the classical PI controller is to stabilize the WTG speed at the reference value. \( \omega_r \) is obtained by rotor motion equation. \( T_m \) is mechanical torque, and \( J \) is a moment of inertia. Isolated grid parameters are shown in Table 1.

The control strategy of GSC is shown in Fig. 3. \( C \) is the DC-link capacitance, \( L_f \) and \( C_f \) are inductance and capacitance of filter respectively. \( i_{abc} \) is the output current, \( u_{abc} \) is the grid voltage, \( i_{dq} \) and \( u_{dq} \) are the current and voltage in \( dq \) coordinate system respectively, \( \theta_g \) is the phase angle obtained by phase-locked loop (PLL), \( \omega \) is the grid angle frequency. In the inner loop, \( i_{d,ref} \) and \( i_{q,ref} \) are the d-axis and q-axis current references respectively. In the outer loop, \( u_{dc,ref} \) and \( u_{dc} \) are the reference value and actual value of DC-link voltage respectively. \( v_{d,ref} \) and \( v_{q,ref} \) are output voltage references of GSC, and can be calculated by (2).

\[
\begin{align*}
\begin{cases}
    v_{d,ref} &= H(s)(i_{d,ref} - i_d) + u_d - \omega \Delta T \omega_f i_q \\
    v_{q,ref} &= H(s)(i_{q,ref} - i_q) + u_q + \omega \Delta T \omega_f i_{gd}
\end{cases}
\end{align*}
\] (2)

where \( H(s) \) is the transfer function of current loop. When reactive power is not required, \( i_{q,ref} \) is set to zero. Then \( i_{d,ref} \) is obtained by the state-of-the-art GSPI control. The GSPI controller can be expressed by (3).

\[
\begin{align*}
i_{d,ref} &= G_k (u_{dc,ref} - u_{dc})(k_{po} + k_{idc} + \frac{k_{dc}}{s})
\end{align*}
\] (3)

where \( G_k \) is the gain based on DC-link voltage deviation.

B. MOTIVATIONAL EXPERIMENTS

In experiments, when \( V_w \) is 0 m/s, 8 m/s and 12 m/s, WTG is connected to the large power grid and isolated wind-diesel grid respectively. Experimental results under each case are shown in Fig. 4 and Fig. 5. When \( V_w \) is 0 m/s, there is no output power from SSC, and GSC control signals are enabled to stabilize the DC-link voltage at its reference value. When \( V_w \) is 8 m/s and 12 m/s, the output power of WTG is fed to the large power grid or isolated grid. When WTG is connected to the large power grid, experimental results are shown in Fig. 4. When WTG is connected to the isolated wind-diesel grid, the experimental results are shown in Fig. 5.

When wind speed is 0 m/s in Fig. 4, it can be seen that the relevant variables of WTG are stable when WTG is connected to the large power grid. Comparing \( i_q \) and \( i_{q,ref} \) in Fig. 4(a) with those in Fig. 5(a), there is no significant difference. However, oscillation amplitudes of the other variables increase gradually in Fig. 5(d)(g)(j). The fluctuation of \( i_{d,ref} \) and \( i_d \) in Fig. 5(d) is more obvious than those in Fig. 4(d). Compared with \( u_{dc} \) in Fig. 4(g), \( u_{dc} \) in Fig. 5(g) fluctuates severely. Meanwhile, compared with Fig. 4(j), \( u_q \) in Fig. 4(j) fluctuates violently. When wind speed is 8 m/s, the reference of d-axis current \( i_{d,ref} \) is increased to regulate output power. In Fig. 4(h)(k), the relevant variables of WTG are stable when WTG is connected to the large power grid. However, when WTG is connected to the isolated wind-diesel grid, oscillation phenomena of \( i_{d,ref} \) and \( u_{dc} \) are also generated as shown in Fig. 5(e)(h)(k).

At the wind speeds of 0 and 8 m/s, when WTG is connected to the isolated grid, it causes the severe oscillation phenomena. In the inner loop, due to the PI controller as shown in Fig. 3, current responses are rapid. It can be seen that \( i_q \) is stable at \( i_{q,ref} \) which is zero. \( i_d \) is changed with its reference \( i_{d,ref} \). The fluctuation of \( i_{d,ref} \) is caused by the deviation between \( u_{dc,ref} \) and \( u_{dc} \), which leads to the variation...
of output power. Furthermore, the rapid change of output power of WTG has an important influence on the voltage and frequency of the isolated grid. Thus, the fluctuation of $u_q$ is caused which is obtained by PLL. As we know, $u_q$ is normally zero. According to the control algorithm shown in Fig. 3, the variation of $u_q$ affects the output voltage of GSC and aggravates the oscillation.

When $V_w$ is 12 m/s, WTG runs at the rated power, and the experimental results are shown in Fig. 4(c)(f)(i)(l) and Fig. 5(c)(f)(i)(l). In Fig. 4(c)(f)(i)(l), WTG is connected to the
large power grid, and the operation of WTG is also stable. Compared with case 1 and case 2 in Fig. 5, the oscillation amplitudes of relevant variables of case 3 in Fig. 5 are reduced. Though \( u_{dc} \) has a certain fluctuation, \( \Delta u_{dc} \) is very close to \( u_{dc,ref} \). As a result, \( \Delta i_d, \Delta i_q, \Delta u_d \) and \( \Delta u_q \) have little variations. In case 3, WTG operation remains relatively stable. \( u_{dc} \) and \( u_q \) are calculated by the Clark and Park transforms based on the measured grid three-phase voltage. In large power grid, the grid voltage and frequency are generally constant regardless of wind speed changes. Thus, \( u_d \) and \( u_q \) are also constant. However, in isolated grid, when wind power changes, the voltage and frequency of the wind-diesel system are influenced, then \( u_d \) and \( u_q \) are changed. At the rated wind speed, wind power is almost constant, then \( u_d \) and \( u_q \) are essentially unchanged.

In Fig. 6, frequency deviation \( \Delta f \) and output power \( P_e \) and \( u_{dc} \) are compared at different cases. Fig. 6(a) and (b) show the experimental results when wind speed \( V_w \) is 0 m/s. The variation of \( \Delta f \) is severe. Oscillation frequency and amplitude of \( \Delta f \) are 2 Hz and 0.3 Hz respectively. \( u_{dc} \) fluctuation amplitude is up to 10 V, and \( P_e \) fluctuates severely around zero. The DC-link capacitances are rapidly charging or discharging. When \( V_w \) is 8 m/s, the experimental results are shown in Fig. 6(c) and (d). Oscillation frequency and amplitude of \( \Delta f \) are 2.9 Hz and 0.2 Hz respectively. \( P_e \) is about 3 kW, and fluctuation amplitude of \( u_{dc} \) is less than that when \( V_w \) is 0 m/s. The oscillation amplitude of \( \Delta f \) in Fig. 6(c) is smaller than that in Fig. 6(a). When \( V_w \) is 12 m/s, the results are shown in Fig. 6(e) and (f). Oscillation frequency and amplitude of \( \Delta f \) are 2 Hz and 0.11 Hz respectively. \( \Delta f \) is significantly better than Fig. 6(a) and (c). \( P_e \) is about 9 kW, and \( u_{dc} \) in Fig. 6(f) is of small fluctuation. The relationship between oscillation amplitude of \( \Delta f \) and \( \Delta i_d, \Delta i_q \) is obtained as shown in Fig. 7. It can be seen that the oscillation amplitude of \( \Delta f \) is decreased with increasing absolute value of \( \Delta i_d, \Delta i_q \), which keeps a linear relationship.

C. ANALYSIS OF THE OSCILLATION

It can be seen that when WTG is connected to the large power grid, there is no oscillation under the three cases. When WTG is connected to the isolated grid, oscillation phenomenon is caused. Due to constant wind speed, the output power of SSC is constant. Thus, the causation of oscillation in the wind-diesel isolated grid is not the power fluctuation of the wind turbine. It can be seen from Fig. 4, and 5, \( i_q \) is relatively stable, not the major influencing factor of oscillation. \( i_q \) also responds rapidly. The deviation of \( u_{dc} \) and \( u_{dc,ref} \) is large. Thus, in the wind-diesel isolated grid, the immediate cause of oscillation is the variation of \( u_{dc} \). GSPI parameter of the DC-link voltage control loop is inadequate at different wind speeds. At low wind speed, GSPI controller leads to \( \Delta i_d, \Delta i_q \) fluctuation, and \( P_e \) is influenced. The change of isolated grid frequency makes a contribution to variations of \( u_d \) and \( u_q \) in PLL. At the same time, frequency fluctuation also has a corresponding impact in the inner loop, further exacerbates the oscillation. In the vicinity of rated power, the GSPI controller is in a saturated state, and the output power of WTG is relatively stable.

The impedance of the large power grid is very small and can be ignored, but the impedance of the diesel generator is relatively large. Thus, the impedance characteristic of the wind-diesel system is analyzed. We represent the WTG by a Norton equivalent circuit, in the form of a current source \( (i_s) \) in parallel with an impedance \( (Z_{gsc}) \). The load is represented by its impedance \( (Z_{load}) \). \( Z_{par} \) is the parallel impedance of \( Z_{gsc} \) and \( Z_{load} \). The diesel generator is represented by
a Thevenin equivalent circuit, in the form of a voltage source \(u_g\) in series with an impedance \(Z_g\) [28], [29]. The representation of the wind-diesel system is shown in Fig. 8.

In Fig. 8, \(i_g\) is output current of WTG, \(u_g\) is grid output voltage. According to the equivalent circuit, equation (4) is derived.

\[
i_g(s) = \frac{1}{Z_{par}(s) + Z_g(s)}u_g(s) - \frac{Z_{par}(s)}{Z_{par}(s) + Z_g(s)}i_d(s).
\]

In order to suppress the influence of grid voltage on the grid-connected current, it is necessary to increase the modulus of \(Z_{par}(s) + Z_g(s)\). Furthermore, when\(Z_g(s)\) and \(Z_{load}(s)\) are constant, improving \(Z_{par}(s)\) has an important effect on enhancing the anti-disturbance performance of GSC. Generally, under the unity power factor operation assumption, the impedance matrix \(Z_{gsc}(s)\) can be diagonalized. The gain variations of GSPI and PLL would result in a variation of impedance matrix \(Z_{gsc}(s)\). This paper, the synchronous reference frame PLL (SRF-PLL) is adopted, which is one of the most basic and popular PLLs for grid synchronization. Thus, the key point is to change control parameters of GSPI to optimize the impedance characteristics of GSC.

Further physical analysis of the oscillation is made. The major energy storage elements of GSC and diesel generator are capacitors and inductors respectively. WTG is equivalent to capacitor \(C\) and negative resistor \((R < 0)\) at the oscillation frequency. The diesel generator is equivalent to inductor \(L\). Therefore, the wind-diesel isolated grid could be regarded as an \(L-C-R\) second-order negative damping oscillation circuit. Due to the negative resistance effect, power is generated by the negative resistor, and power oscillation begins to diverge. When it diffuses to the limit, equal amplitude oscillation is generated. If the capacitor voltage exceeds its reference value, the capacitor releases energy, the inductor absorbs energy, and the rotor speed of diesel generator increases. If the capacitor voltage goes below its reference value, the capacitor absorbs energy, the inductor releases energy, and the rotor speed of diesel generator speed decreases.

### III. ANALYSIS OF SMALL-SIGNAL STABILITY

Small-signal stability of wind-diesel isolated grid is analyzed. The output power of WTG is the main cause of the oscillation. Since GSC of WTG is often operated with unity power factor, the output power of WTG is reflected in the d-axis current. Within a certain range of the stable operating point, \(G_k\) is almost constant, and (4) can be written as (5).

\[
i_{d,\text{ref}} = \left( u_{dc,\text{ref}} - u_{dc} \right) \left( k_{pdc} + \frac{k_{ide}}{s} \right), \tag{5}
\]

where \(k_{pdc}\) and \(k_{ide}\) are proportional and integral coefficients of GSPI controller respectively. The DC-link power is expressed by (6).

\[
u_{dc} C \frac{dI_{dc}}{dt} = P_s + 1.5(u_{d1}i_d + u_{q1}i_q), \tag{6}
\]

where \(P_s\) is the PMSG output power. In order to simplify the analysis, some realistic assumptions and approximations are made in the models. Due to the rapid response of internal loop of GSC, assuming that \(i_d = i_{d,\text{ref}}, i_q = i_{q,\text{ref}} = 0\), and \(u_d\) is constant within the small-signal fluctuation, equations (5) and (6) are linearized, and the small-signal dynamic models of WTG is obtained by (7) when \(P_s\) is constant.

\[
\begin{align*}
\Delta \dot{i}_{d1} &= k_{ide}(\Delta u_{dc,\text{ref}} - \Delta u_{dc}), \\
\Delta \dot{i}_d &= k_{pdc}(\Delta u_{dc,\text{ref}} - \Delta u_{dc}) + \Delta \dot{i}_d, \\
\Delta \dot{u}_{dc} &= \frac{-\Delta P_s + 1.5(u_{q0}\Delta i_d + i_{q0}\Delta u_{q1} + u_{d0}\Delta i_d + i_{d0}\Delta u_{d1})}{C u_{dc,0}},
\end{align*}
\]

where ‘\(\Delta\)’ indicates a small-signal value around the operating point, subscript ‘0’ indicates steady-state value around the operating point. The role of diesel generator in the isolated grid is to regulate frequency by its output power. Diesel generator’s mechanical power reference \(P_{dm,\text{ref}}\) is obtained by (8).

\[
P_{dm,\text{ref}} = (\omega_{\text{ref}} - \omega)(k_{pdc} + \frac{k_{iwo}}{s}), \tag{8}
\]

where \(H\) is inertia coefficient of diesel generator, and \(P_{dm}\) is mechanical power. To simplify the analysis, assuming \(P_{dm} = P_{dm,\text{ref}}\), the small-signal dynamic models of diesel generator are obtained by (9).

\[
\begin{align*}
\Delta \dot{P}_{dm} &= k_{pdc}(\Delta \omega_{\text{ref}} - \Delta \omega), \\
\Delta P_{dm} &= k_{iwo}(\Delta \omega_{\text{ref}} - \Delta \omega) + \Delta P_{dm}, \\
\Delta \dot{\omega} &= \frac{\Delta P_{dm} - \Delta P_d}{H \omega_0}.
\end{align*}
\]

According to (7) and (9), the state equation of wind-diesel system is obtained by (10).

\[
\begin{pmatrix}
\Delta \dot{i}_{d1} \\
\Delta \dot{i}_{dc} \\
\Delta \dot{P}_{dm} \\
\Delta \dot{\omega}
\end{pmatrix} =
\begin{pmatrix}
0 & 0 & 0 & 0 \\
-1.5u_{d0} & -k_{ide} & 0 & 0 \\
1.5u_{q0} & 0 & 0 & -k_{iwo} \\
H \omega_0 & H \omega_0 & H \omega_0 & H \omega_0
\end{pmatrix}
\begin{pmatrix}
\Delta i_{d1} \\
\Delta u_{dc} \\
\Delta P_{dm} \\
\Delta \omega
\end{pmatrix}.
\]

In this model, different parameters of the DC-link voltage controller are selected, and the eigenvalues are calculated as shown in Table 2 and Table 3. DC-link voltage controller...
parameters have influences on the eigenvalues $\lambda_1$ and $\lambda_2$, $\lambda_3$ and $\lambda_4$ are mainly affected by the parameters of diesel generator controller. Therefore, in order to analyze the influence of DC-link voltage controller parameters, $\lambda_3$ and $\lambda_4$ are ignored.

In Table 2, the control parameter $k_{pdc}$ is set as a constant value. With the increasing $k_{idc}$, the imaginary parts of $\lambda_1$ and $\lambda_2$ are variable and their real parts are constant. In Table 3, the control parameter $k_{idc}$ is set as a constant value. With the increasing $k_{pdc}$, the real parts of $\lambda_1$ and $\lambda_2$ are variable, and the imaginary parts are constant. The real parts of eigenvalues have a major effect on system stability. It can be seen that $k_{pdc}$ has a great impact on system stability. If $k_{pdc}$ is too large, $i_d$ overshooting may be caused. If $k_{pdc}$ is too small, the improper adjustment may lead to increasing oscillation. Therefore, the optimization of the control parameter $k_{pdc}$ has a great influence on the system stability.

$\lambda_3$ and $\lambda_4$ are related to the variation of DC-link voltage deviation based on (3). According to the experimental results in Fig. 5, the DC-link voltage deviation is severe at low wind speeds, $k_{pdc}$ is changed frequently and inappropriately. At high wind speeds, the DC-link voltage deviation is slight. In the small-signal model, unsuitable selection of $k_{pdc}$ will affect the system stability. Thus, besides DC-link voltage deviation, different wind speeds also need to be considered to adjust $k_{pdc}$.

**IV. THE PROPOSED VARIABLE UNIVERSE FUZZY PI CONTROLLER**

In order to improve the system stability, a variable universe fuzzy PI controller is presented to optimize $k_{pdc}$ to suppress the oscillation of $u_{dc}$. The fuzzy PI control algorithm is shown in Fig. 9. $u_{dc, err}$ and $du_{dc, err}/dt$ are input variables of the fuzzy controller. $\alpha$ is a contraction-expansion factor, which is to adapt WTG to the conditions of different wind speeds. The adjustment of proportional coefficient $\Delta k_{pdc}$ is calculated by the variable universe fuzzy PI controller, which includes fuzzifier, fuzzy inference machine and defuzzifier. $k'_{pdc}$ is the initial parameter. Through the modification of $k_{pdc}$, when the grid frequency oscillates, the DC-link voltage of GSC can be more stable and robust.

For simplicity of application, the normal, consistent, and complete fuzzy sets with the triangular membership functions are often considered for input and output variables [30],

### TABLE 2. Wind diesel system eigenvalues when $k_{pdc} = 3.5$.

<table>
<thead>
<tr>
<th>$k_{pdc}$</th>
<th>$\lambda_1$</th>
<th>$\lambda_2$</th>
<th>$\lambda_3$</th>
<th>$\lambda_4$</th>
</tr>
</thead>
<tbody>
<tr>
<td>20</td>
<td>-2.53+j6.569</td>
<td>-2.53+j6.569</td>
<td>-1.971+j0.920</td>
<td>-1.971-j0.920</td>
</tr>
<tr>
<td>50</td>
<td>-2.53+j10.841</td>
<td>-2.53+j10.841</td>
<td>-1.971+j0.920</td>
<td>-1.971-j0.920</td>
</tr>
<tr>
<td>100</td>
<td>-2.53+j15.54</td>
<td>-2.53+j15.54</td>
<td>-1.971+j0.920</td>
<td>-1.971-j0.920</td>
</tr>
<tr>
<td>150</td>
<td>-2.53+j19.115</td>
<td>-2.53+j19.115</td>
<td>-1.971+j0.920</td>
<td>-1.971-j0.920</td>
</tr>
<tr>
<td>180</td>
<td>-2.53+j20.971</td>
<td>-2.53+j20.971</td>
<td>-1.971+j0.920</td>
<td>-1.971-j0.920</td>
</tr>
</tbody>
</table>

### TABLE 3. Wind diesel system eigenvalues when $k_{idc} = 100$.

<table>
<thead>
<tr>
<th>$k_{idc}$</th>
<th>$\lambda_1$</th>
<th>$\lambda_2$</th>
<th>$\lambda_3$</th>
<th>$\lambda_4$</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.5</td>
<td>-0.51+j15.736</td>
<td>-0.51+j15.736</td>
<td>-1.971+j0.920</td>
<td>-1.971-j0.920</td>
</tr>
<tr>
<td>3</td>
<td>-1.52+j15.671</td>
<td>-1.52+j15.671</td>
<td>-1.971+j0.920</td>
<td>-1.971-j0.920</td>
</tr>
<tr>
<td>3.5</td>
<td>-2.53+j15.54</td>
<td>-2.53+j15.54</td>
<td>-1.971+j0.920</td>
<td>-1.971-j0.920</td>
</tr>
<tr>
<td>4</td>
<td>-3.548+j15.34</td>
<td>-3.548+j15.34</td>
<td>-1.971+j0.920</td>
<td>-1.971-j0.920</td>
</tr>
<tr>
<td>4.5</td>
<td>-4.561+j15.07</td>
<td>-4.561+j15.07</td>
<td>-1.971+j0.920</td>
<td>-1.971-j0.920</td>
</tr>
</tbody>
</table>
Although other shapes such as the bell, Gaussian and trapezoid which are used to describe the membership functions, can also be selected. The universe of $u_{dc, err}$ is set as $[-10V, 10V]$, the universe of $du_{dc, err}/dt$ is set as $[-4, 4]$, and the universe of $\Delta k_{pdc}$ is set as $[-1.5, 1.5]$.

Further, fuzzifier performs a mapping from crisp inputs and output to their fuzzy sets. The universes of $u_{dc, err}$ and $du_{dc, err}/dt$ on their fuzzy sets are defined as $\{-3, -2, -1, 0, 1, 2, 3\}$, and the universe of $\Delta k_{pdc}$ on a fuzzy set is defined as $\{-3, -2, -1, 0, 1, 2, 3\}$. The corresponding fuzzy subsets are defined as {negative big (NB), negative median (NM), negative small (NS), zero (ZO), positive small (PS), positive median (PM), positive big (PB)}. The membership functions are shown in Fig. 10. In fuzzy set theory, the fuzzy sets are characterized by their triangular membership functions, which assign to each element a number in the interval 0 to 1. This represents the grade of membership. The steeper the shape of a triangle, the higher the control sensitivity in the corresponding universe. In the universe of flat shapes, the control system will be more robust. Thus, when we design the triangle shapes of output membership, the steeper triangle is adopted in the universe of smaller error, and the flatter triangle is used in the universe of larger error. Generally, the variable universe means that input or output universes can change according to the changing of their variables. However, based on the above motivational experiments and analysis, the output power of WTG is a major impact factor of the oscillation phenomena in this wind-diesel system. $i_d$ can characterize the variation of output power. Furthermore, in order to obtain adequate control parameters for adapting the conditions of different

**TABLE 4. Fuzzy control rules.**

<table>
<thead>
<tr>
<th>$\frac{du_{dc, err}}{dt}$</th>
<th>NB</th>
<th>NM</th>
<th>NS</th>
<th>ZO</th>
<th>PS</th>
<th>PM</th>
<th>PB</th>
</tr>
</thead>
<tbody>
<tr>
<td>$u_{dc, err}$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NB</td>
<td>PB</td>
<td>PB</td>
<td>PM</td>
<td>PM</td>
<td>PS</td>
<td>PS</td>
<td>ZO</td>
</tr>
<tr>
<td>NM</td>
<td>PB</td>
<td>PB</td>
<td>PM</td>
<td>PS</td>
<td>PS</td>
<td>ZO</td>
<td>NS</td>
</tr>
<tr>
<td>NS</td>
<td>PM</td>
<td>PM</td>
<td>PM</td>
<td>PS</td>
<td>ZO</td>
<td>NS</td>
<td>NS</td>
</tr>
<tr>
<td>ZO</td>
<td>PS</td>
<td>PS</td>
<td>ZO</td>
<td>NS</td>
<td>NS</td>
<td>NM</td>
<td>NM</td>
</tr>
<tr>
<td>PS</td>
<td>PS</td>
<td>PS</td>
<td>ZO</td>
<td>NS</td>
<td>NM</td>
<td>NM</td>
<td>NM</td>
</tr>
<tr>
<td>PM</td>
<td>PS</td>
<td>ZO</td>
<td>NS</td>
<td>NM</td>
<td>NM</td>
<td>NB</td>
<td>NB</td>
</tr>
<tr>
<td>PB</td>
<td>ZO</td>
<td>NS</td>
<td>NM</td>
<td>NM</td>
<td>NM</td>
<td>NB</td>
<td>NB</td>
</tr>
</tbody>
</table>

WTG output power, considering the characteristics of linear relationship of the wind-diesel system in Fig. 7, we propose a contraction-expansion factor $\alpha$ in output universe of the fuzzy PI controller as shown in (11).

$$\alpha = (1 - \frac{i_d}{i_{d, max}}) + \varepsilon,$$  

where $\varepsilon$ is a sufficiently small positive number, $\varepsilon = 10^{-4}$. The design of $\alpha$ should follow the principle of duality, monotonicity, coordination, normality and zero avoidance. The contraction-expansion factor can be defined as the adjustment of language control variable universe. Its output universe is transformed into $[-1.5\alpha, 1.5\alpha]$, and new membership function is shown in Fig. 11.

Rule base consists of a collection of fuzzy IF-THEN rules. According to engineering experience, the fuzzy rules formulated in this paper are shown in Table 4.
defuzzifier maps output fuzzy set to a crisp value. Here, we use the weighted average method to obtain $\Delta k_{pdc}$ as shown in (12).

$$M_{\text{avg}} = \frac{1}{n} \sum_{i=1}^{n} U(u_i)$$

(12)

where $M_{\text{avg}}$ is the crisp output of the fuzzy system, $u_i$ ($i = 1, 2, ..., n$) is an element of output fuzzy set, and $U(u_i)$ is the corresponding membership function value. When $u_{\text{dc}}$, changes, $\Delta k_{pdc}$ is adjusted by the fuzzy PI controller, which ensures that $u_{\text{dc}}$ tracks $u_{\text{dc,ref}}$ stably. Compared with the existing GSPI controller, the variable universe fuzzy PI controller adapts WTG to the conditions of different wind speeds, and exhibits better robustness in suppressing $u_{\text{dc}}$ oscillation.

V. EXPERIMENT

Experimental platform and its specific control block diagram are shown in Fig. 1 and Fig. 2 respectively. The variable universe fuzzy PI controller is verified below in three cases. Different wind speeds are set, and the power of load and diesel generator are constant. The experimental results are shown in Fig. 12 and Fig. 13.

A. CASE 1: $V_w = 0$ m/s

In this case, PMSG does not generate power to SSC, and GSC utilizes isolated grid power to stabilize DC-link voltage. GSPI controller exhibits poor performances in Fig. 5. The experimental results adopted the variable universe fuzzy PI controller are shown in Fig. 12(a), (d), and (g). Due to the adjustment $\Delta k_{pdc}$, the deviation of $u_{\text{dc}}$ and $u_{\text{dc,ref}}$ in Fig. 12(a) is less than that in Fig. 5(d), which shows that $u_{\text{dc}}$ can stably track $u_{\text{dc,ref}}$ based on the fuzzy controller. The oscillations of $i_d$ and $i_{\text{d,ref}}$ in Fig. 12(d) are also weakened, and $i_q$ is around zero. $u_{\text{d}}$ and $u_{\text{i}}$ in Fig. 12(g) are more stable than those in Fig. 5(j). Fig. 13(a) and (b) show the curves of $P_e$, $f_{\text{err}}$ and $u_{\text{dc}}$. It can be seen that the oscillations of $f_{\text{err}}$ and $u_{\text{dc}}$ are smaller than those in Fig. 6(a) and (b), and $P_e$ is also around zero. Compared with the GSPI controller, the overall oscillation amplitude of $u_{\text{dc}}$ is lowered by nearly 10 V. The oscillation amplitude of $f_{\text{err}}$ is reduced by up to 0.175 Hz. The wind-diesel system is relatively more stable.

B. CASE 2: $V_w = 8$ m/s

In this case, the WTG operates in the MPPT mode. Fig. 12(b), (e), and (h) show the experimental results with the fuzzy PI controller. $u_{\text{dc}}$ and $u_{\text{dc,ref}}$ in Fig. 12(b) are more stable than those in Fig. 5(h), and its oscillation amplitudes are similar to those in Fig. 12(a). $i_d$ in Fig. 12(e) is close to -0.17 pu. The adjustable range of $\Delta k_{pdc}$ has already been narrowed according to equation (11). Fig. 13(c) and (d) show the curves of $P_e$, $f_{\text{err}}$, $u_{\text{dc}}$ when $V_w = 8$ m/s. Compared with Fig. 7(c) and (d), it can be seen that the power oscillation of GSC is reduced, the oscillation amplitudes of $f_{\text{err}}$ and $u_{\text{dc}}$ are also decreased, and the system stability is enhanced.

C. CASE 3: $V_w = 12$ m/s

In this case, WTG is in the rated power operating condition. Fig. 12(c), (f) and (i) show the experimental results with the variable universe fuzzy PI controller. In Fig. 12(b), $u_{\text{dc}}$ tracks $u_{\text{dc,ref}}$ tightly. According to equation (11), $i_d$ is close to $i_{d,\text{max}}$, and $\alpha$ is small when $V_w = 12$ m/s. When $u_{\text{dc}}$ changes, $\Delta k_{pdc}$ has a small adjustment. The fuzzy PI controller plays a fine-tuning role, and the initial parameters play the main role. Our expected target is achieved. Fig. 13(e) and (f) show the curves of $P_e$, $f_{\text{err}}$, $u_{\text{dc}}$ when $V_w = 12$ m/s. Compared with Fig. 7(e) and (f), it can be seen that $P_e$ and $u_{\text{dc}}$ are stable.

VI. CONCLUSIONS

Oscillation causes of the isolated grid are researched, and an adaptive fuzzy PI controller is proposed. The theoretical analysis and experimental results show that the control parameters of DC-link voltage controller and wind speed are related to the oscillations, and more especially $k_{pdc}$ has large influences on the stability of frequency and WTG output power. Thus, only $k_{pdc}$ is adjusted by the fuzzy PI controller. Besides, with decreasing wind speed, the oscillation is more severe. By building the extension factor of the output universe with $i_d$, the adjustment of $k_{pdc}$ is increased at low wind speeds and decreased at high wind speeds. Compared with the state-of-the-art GSPI controller, the oscillation amplitude of isolated
plays a certain inhibitory effect on system oscillation. The proposed fuzzy PI controller reduces the oscillation amplitude of DC-link voltage substantially.

REFERENCES


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