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Small-Signal Stability Analysis and Optimal Parameters Design of Microgrid Clusters

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ABSTRACT The two-layer distributed control architecture, including the microgrid (MG) control layer and MG cluster (MGC) control layer, can be used for interconnecting multiple MGs to form the MGC. However, the coupling among multiple elements and the interaction between two control layers may introduce new low-damping oscillatory modes and even reduce the stability margin. Unfortunately, the detailed small-signal stability analysis and stability enhancement method of the MGC with the two-layer distributed control strategy have not been reported. To fill this gap, this paper first presents a unified small-signal dynamic model of the MGC. Subsequently, a comprehensive small-signal stability analysis based on the model is presented to analyze: 1) the mechanism of coupling/interaction among MGs and multiple control layers; 2) the participation factors of the low-damping modes; and 3) the sensitivity of the distributed control parameters. Moreover, the design of the distributed control parameters is formulated as an optimization problem, where the particle swarm optimization is employed to search for an optimal combination of parameters to enhance system stability. Finally, the stability assessment and time-domain simulation are carried out to validate the effectiveness of the proposed method.

INDEX TERMS Distributed control, hierarchical control, microgrid cluster, particle swarm optimization, small-signal stability.

I. INTRODUCTION In recent years, the microgrid (MG) has experienced rapid development because it is an effective solution for the reliable integration of distributed generation (DG) units, energy storage systems, and loads [1]--[3]. Meanwhile, with the increasing application of MGs, interconnecting MGs to form a microgrid cluster (MGC) is considered as an effective option of enabling maximum utilization of renewable sources, suppressing stress and aging of the components in MGs [4] or even operating as an island to serve more area when a major outage happened [5].

The three-level hierarchical control architecture including primary control, secondary control and tertiary control is widely investigated for a single MG to realize its voltage/frequency regulation, power balance and load sharing [6], [7]. However, for a MGC, the two-layer architecture is commonly adopted, in which the classical MG three-level control is modified and embedded into the MG-control layer, and a MGC-control layer is employed to overlook the resources and realize coordination of multiple MGs [8]--[10]. For the two-layer control architecture of MGC, there are centralized or distributed ways to perform the control actions. Due to the advantages of reliability, reconfigurability and low communication investment, the distributed control method gains a lot of concerns for the MGC [11]--[15]. Based on the distributed communication network, each DG unit or MG unit only requires its own and the neighbor’s information to realize control objectives. The existing two-layer distributed control methods for the MGC mainly focus on realization of the steady-state objectives, e.g., (i) elimination of system frequency deviations [12], [15], (ii) regulation of system voltage,
The main contributions of this paper include:

1. A two-layer distributed control strategy. The focus is on stability analysis and enhancement method of the MGC and MG control layer should be optimized jointly.
2. A comprehensive stability analysis of the MGC based on its small-signal dynamic model to reveal the coupling mechanism among multiple MGs, control interaction between different control layers, and the impact of control parameters on stability.
3. An accurate power sharing among MGs [11], [14].

However, the dynamic characteristics of the MGC may be undesirable in terms of the system damping, response time, stability margin, and so on [16], [17]. First, the interaction between two control layers and the dynamic coupling among multiple MGs may introduce new low-damping modes, which lead to oscillatory responses or even destabilize the system. Moreover, compared with the centralized method, the neighboring communication characteristic of the distributed control method may result in a more significant interaction/coupling among DG or MG units. Therefore, a detailed small-signal stability analysis for the MGC is of significant importance. In [16], a small-signal modeling method for the MGC is proposed, in which each MG is simplified as a DG unit without considering its internal dynamics. Thus, the simplification in [16] will inevitably lead to analysis errors. In [17], a detailed small-signal dynamic model of a PV-based MGC is proposed and the analysis results indicate that the coupling among MGs will weaken the system stability. However, only decentralized primary control is employed with each DG in [17], which means the impact of other control layers, especially the impact of interaction between different control layers cannot be studied. To the best of our knowledge, a comprehensive small-signal stability analysis of the MGC considering detailed models and distributed control method has not been reported before.

Furthermore, although many methods have been proposed to enhance the stability of a single MG [18]–[21], to the best of our knowledge, the stability enhancement via optimal control parameters design for the MGC has not been reported before. Compared with a single MG, the complicated interactions/couplings in a MGC with the two-layer distributed control strategy are strongly associated with multiple control parameters. Therefore, the control parameters of both the MGC and MG control layer should be optimized jointly.

Motivated by the aforementioned limitations, this paper focuses on stability analysis and enhancement method of the MGC with the two-layer distributed control strategy. The main contributions of this paper include:

1. A comprehensive stability analysis of the MGC based on its small-signal dynamic model to reveal the coupling mechanism among multiple MGs, control interaction between different control layers, and the impact of control parameters on stability;
2. A formulation of the control parameters optimal design problem considering both MG-control layer and MGC-control layer and a particle swarm optimization (PSO) approach to jointly optimize multiple control parameters to enhance the system stability.

This paper also presents time-domain simulation validations of the MGC small-signal dynamic model to ensure an accurate and reliable stability analysis result. Eigenvalue analysis and time-domain simulation are provided to verify the effectiveness of the proposed parameters optimization method.

The rest of the paper is organized as follows. Section II describes the unified small-signal dynamic model of the MGC with the two-layer distributed control method. Section III presents the stability analysis of the MGC based on the small-signal dynamic model. Section IV formulates the control parameters optimization problem and the PSO based solution method. Case studies are presented in Section V to validate the effectiveness and of the proposed stability enhancement method. Section VI concludes the paper.

II. SMALL-SIGNAL DYNAMIC MODEL OF THE MGC WITH THE TWO-LAYER DISTRIBUTED CONTROL STRATEGY

In this section, the two-layer distributed control method for the MGC is presented. Based on it, the small-signal dynamic model is provided.

A. TWO-LAYER DISTRIBUTED CONTROL FRAMEWORK FOR MGC

The two-layer distributed control framework includes (i) primary and distributed secondary control levels in the MG-control layer, (ii) tertiary and distributed quaternary control levels in the MGC-control layer.

- The primary control (PC) level is responsible for controlling the local power, voltage, and current of DGs.
- The distributed secondary control (DSC) level is introduced to adjust the voltage phasor of the point of common coupling (PCC) in the MG by controlling the PCC voltage magnitude and frequency at the reference values received from the tertiary control level.
- The tertiary control (TC) level manages the power flow through PCC of each MG by sending commands to the secondary control level.
- The distributed quaternary control (DQC) level supervises the entire MGC and controls the critical bus voltage and system frequency as desired values.

A schematic diagram of the two-layer distributed control framework is presented in Fig. 1.
Within an arbitrary MGk, each DG unit communicates with its neighbors to formulate the lower distributed communication network Gk. Then, each MG is represented by an agent and communicates with its neighbors to formulate the upper distributed communication network G. Note that each MG agent needs to communicate with at least one DG unit inside this MG, as shown by the red dashed lines in Fig. 1, to realize the coordination between two control layers.

The corresponding control objectives are summarized as follows:

(i) The system frequency $\omega_{\text{sys}}$ is controlled as the desired value $\omega_{\text{sys}}^*$. 
(ii) The critical bus voltage $V_c$ is restored to the desired value $V_c^*$. Note that the critical bus can be selected according to the operation requirement and only one critical bus is selected in this paper.
(iii) The active and reactive power through PCC of each MG are shared among them based on their capacities, i.e.,
\[
P_{\text{PCC1}}/P_{n\text{MG1}} = \ldots = P_{\text{PCCm}}/P_{n\text{MGm}}
\]
\[
Q_{\text{PCC1}}/Q_{n\text{MG1}} = \ldots = Q_{\text{PCCm}}/Q_{n\text{MGm}}
\]
where $P_{n\text{MGk}}$, $Q_{n\text{MGk}}$, $P_{\text{PCCk}}$, $Q_{\text{PCCk}}$ are active and reactive power capacities, respectively, with $k \in M$, $M = \{1, 2, \ldots, m\}$. 
(iv) Within each MG, the output active and reactive power of each DG are shared among them based on their capacities, i.e.,
\[
P_{ki}/P_{mk1} = \ldots = P_{kni}/P_{mknk}
\]
\[
Q_{ki}/Q_{mk1} = \ldots = Q_{kni}/Q_{mknk}
\]
where $P_{mk1}$, $Q_{mk1}$, $P_{ki}$, $Q_{ki}$ are active and reactive power capacities, output active and reactive power of DGi in MGk, respectively, with $i \in N_k$, $N_k = \{1, 2, \ldots, n_k\}$.

B. MG LAYER CONTROLLERS AND SMALL-SIGNAL DYNAMIC MODELING

In the MG-control layer, the droop method is adopted as the primary control. The distributed secondary control is designed based on distributed cooperative control [22], [23] and then implemented through the communication network $G_k$ which is modeled by a digraph in the graph theory [24]. The associated adjacency matrix with $G_k$ is $A^k = \{a_{ij}^k\}$. Assume for an arbitrary MGk, the internal DG units are considered as nodes in $G_k$, as shown in Fig. 1.

1) PRIMARY CONTROLLER (PC) AND DISTRIBUTED SECONDARY CONTROLLER (DSC)

The PC is based on the droop method [25], [26] which consists of the power controller, inner voltage controller, and current controller, as shown in Fig. 2. The power controller is
\[
\omega_{ki} = \omega_n - D_{pk1}P_{ki} + \Omega_{ki}
\]
\[
E_{odki} = V_n - D_{Qdk1}Q_{ki} + \lambda_{ki} + h_{ki}
\]
\[
E_{oqki} = 0
\]
where $\omega_{ki}$ is the angular frequency of DGi in MGk, $\omega_n$ is the rated angular frequency, $V_n$ is the rated voltage of the low voltage (LV) network, $E_{odki}$ is the $d$-axis voltage reference, and the $q$-axis voltage reference $E_{oqki}$ is set to be zero. $E_{odki}$ and $E_{oqki}$ are provided to the inner voltage controller. $D_{pk1}$ and $D_{Qdk1}$ are active and reactive power droop coefficients, respectively. $\Omega_{ki}$, $\lambda_{ki}$ and $h_{ki}$ are the distributed secondary control variables.

The DSC is based on a distributed frequency and voltage control method for MG introduced in our previous work [27]. More details can be found in [27]. The only modification of the DSC in this paper is controlling the angular

![FIGURE 2. A block diagram of the two-layer distributed control method.](image-url)
frequency $\omega_{\text{PCC}}$ and PCC voltage $V_{\text{PCC}}$ as $\omega_{\text{MG}}$ and $V_{\text{PCC}}^\ast$ received from the TC instead of controlling them as rated frequency and voltage in [27]. This modification can embed the MG-layer control into the overall control architecture of the MGC.

2) SMALL-SIGNAL DYNAMIC MODEL OF MG $k$

The reference frame of DG$_{11}$, namely DG$_1$ in MG$_1$, is selected as the common $DQ$-frame of the entire MGC. Thus, the phase angle $\delta_{kl}$ of DG$_{kl}$ can be defined as

$$\dot{\delta}_{kl} = \omega_k - \omega_g$$

where $\omega_g$ is the rotating frequency of the common $DQ$-frame and equal to $\omega_{11}$, and $\delta_{kl}$ is the rotating frequency of local $dq$-frame of DG$_{kl}$.

By modeling the dynamics of PCs, DSCs, lines and loads inside MG$_k$, the model of MG$_k$ can be obtained [27], i.e.,

$$[\Delta S_{\text{MG}k}] = A_{\text{MG}k} [\Delta S_{\text{MG}k}] + B_{\text{MG}k} \Delta V_{\text{PCC}k}^\ast + C_{\text{MG}k} [\Delta \psi_{\text{PCC}DQ_k}]$$

where $\Delta S_{\text{MG}k} = [\Delta X_{\text{DG}k}, \Delta i_{\text{line}DQ_k}, \Delta i_{\text{load}DQ_k}, \Delta \psi_{1k}]^T$, $\Delta X_{\text{DG}k}$ refers to the state variables of all DG units in MG$_k$ and $\Delta X_{\text{DG}k} = [\Delta X_{\text{DG}1k}, \Delta X_{\text{DG}2k}, \ldots, \Delta X_{\text{DG}kn_k}]^T$, $\Delta X_{\text{DG}1k} = [\Delta \psi_{1k}, \Delta p_{1k}, \Delta q_{1k}, \Delta \Omega_{1k}, \Delta \lambda_{1k}, \Delta \delta_{1k}, \Delta \delta_{\text{load}1k}]^T$, $i_{\text{load}1k}$, $i_{\text{load}1k}$ are the $d$-axis and $q$-axis component of DG output current $i_{\text{load}1k}$ in Fig.2. $\Delta \psi_{1k}$ is a state variable introduced by the PCC voltage controller, $\Delta V_{\text{PCC}k}^\ast$ and $\Delta \psi_{\text{PCC}DQ_k}$ are coupling states which reflect the interactions among the MGs and other MGs. $A_{\text{MG}k}$, $B_{\text{MG}k}$ and $C_{\text{MG}k}$ are parameter matrices. Therefore, as indicated by (8), the dynamics of PCs, DSCs, loads and lines are modeled and the detailed modeling process can be found in [27].

C. MGC LAYER CONTROLLERS AND SMALL-SIGNAL DYNAMIC MODELING

In the MGC-control layer, the TCs and DQCs are employed to realize objective (i) - (iii).

1) TERTIARY CONTROLLER (TC)

The TC is a local controller which is responsible for regulating the active and reactive power through PCC of each MG. To ensure the plug-and-play characteristic of MGs, each MG is considered as a droop-controlled node, given by,

$$\omega_{\text{MG}k} = \omega_n - D_{\text{pk}} P_{\text{PCC}k}$$

$$V_{\text{PCC}k} = V_n - D_{\text{Qk}} Q_{\text{PCC}k}$$

where $\omega_{\text{MG}k}$ and $V_{\text{PCC}k}$ are the angular frequency and voltage reference values, $D_{\text{pk}}$ and $D_{\text{Qk}}$ are the active and reactive droop coefficients of MG$_k$, respectively.

$$D_{\text{pk}} = D_{\text{max}} / P_{\text{mMG}k}, D_{\text{Qk}} = D_{\text{max}} / Q_{\text{mMG}k}$$

where $D_{\text{max}}$ and $D_{\text{max}}$ are the maximum acceptable angular frequency and PCC voltage magnitude deviations, respectively.

2) DISTRIBUTED QUATERNARY CONTROLLER (DQC)

The DQC is responsible for regulating system frequency and critical bus voltage to the desired values. Besides, the inaccurate reactive power sharing problem due to unbalanced line impedance [28] is solved by DQC. The DQC is designed based on the concept of the distributed cooperative control [22], [23]. The communication network is denoted as $\hat{G}$ with the associated adjacency matrix $A = [\hat{a}_{ij}]$. Each MG is considered as a node in $\hat{G}$, as shown in Fig.1. For node $k$, the set of its neighbors is denoted as $H_k$.

The frequency/active power controller of DQC level aims at realizing objective (i) and (iii)-(1). The control variable $\Omega_k$ is introduced on (9), given by

$$\omega_{\text{MG}k} = \omega_n - D_{\text{pk}} P_{\text{PCC}k} + \Omega_k$$

where $\Omega_k$ consists of frequency control part $e_{\text{ok}}$ and active power sharing control part $e_{\text{pk}}$, which satisfies

$$\Omega_k = e_{\text{ok}} + e_{\text{pk}}$$

The updating laws of $e_{\text{ok}}$ and $e_{\text{pk}}$ are based on the distributed cooperative control theory and given as

$$e_{\text{ok}} = c_{\text{ok}} \left[ \sum_{l \in H_k} a_{kl} (\omega_{\text{MG}l} - \omega_{\text{MG}k}) + g_k (\omega_{\text{sys}} - \omega_{\text{MG}k}) \right]$$

$$e_{\text{pk}} = c_{\text{pk}} \sum_{l \in H_k} a_{kl} (D_{\text{pk}} P_{\text{PCC}l} - D_{\text{pk}} P_{\text{PCC}k})$$

where $c_{\text{ok}}$ and $c_{\text{pk}}$ are positive control gains, the pinning gain $g_k \geq 0$ is the weight of the edge by which the $k_{\text{th}}$ MG unit is connected to the reference. Eq. (14) is applied to synchronize the frequency $\omega_{\text{MG}k}$ of all MGs to the reference $\omega_{\text{sys}}$ to achieve objective (i). Similarly, objective (iii)-(1) will be realized by making $D_{\text{pk}} P_{\text{PCC}k}$ of all MGs equal, as indicated by (15). Note that $\omega_{\text{MG}k}$ is provided to the DSC of MG$_k$ as the frequency reference.

The critical bus voltage controller of DQC level is responsible for realizing objective (ii). A control variable $\lambda_k$ is added in (10), i.e.,

$$\hat{V}_{\text{PCC}k} = V_n - D_{\text{Qk}} Q_{\text{PCC}k} + \lambda_k$$

The updating law of $\lambda_k$ is given by

$$\dot{\lambda}_k = c_{\lambda k} \left[ \sum_{l \in H_k} a_{kl} \left( \hat{V}_{\text{PCC}l} - \hat{V}_{\text{PCC}k} \right) + g_k \left( V_{l}^\ast - \hat{V}_{\text{PCC}l} \right) \right]$$

where $c_{\lambda k}$ is a positive control gain. The dynamic process of (17) results in $\hat{V}_{\text{PCC}k}$ of all MGs converging to the common reference $V_i^\ast$. $V_i^\ast$ is generated through a PI controller such that $V_i$ recovers to its reference $V_i^\ast$ (objective (ii)), i.e.,

$$V_i^\ast = V_n + k_p (V_c^\ast - V_c) + k_i \int (V_c^\ast - V_c) \, dt$$

where $k_p$ and $k_i$ are the gains of the PI controller.

The reactive power controller of DQC level is introduced to solve the inaccurate reactive power sharing problem introduced by TC and realize objective (iii)-(2). A control variable $h_k$ is added to (16) to achieve accurate reactive power...
sharing, i.e.,

\[ V_{\text{PCC}}^* = V_n - D_{\text{Q}k}Q_{\text{PCC}} + \lambda_k + h_k \]  

(19)

where \( V_{\text{PCC}}^* \) is generated as the voltage reference of DSC in the MG-control layer, as shown in Fig. 2. Note that \( V_{\text{PCC}}^* \) in (16) is an intermediate variable, and \( V_{\text{PCC}}^* \) is the final value provided to DSC as the reference. This setting aims to realize the objectives of critical bus voltage control and reactive power sharing among MGs simultaneously. \( h_k \) is selected by

\[ \dot{h}_k = c_{qk} \sum_{i \in L_k} a_{ij} (D_{Qi}Q_{\text{PCC}} - D_{Qk}Q_{\text{PCC}}) \]  

(20)

where \( c_{qk} \) is a positive control gain. Eq. (20) is used to make \( D_{Qk}Q_{\text{PCC}} \) of all MGs equal to each other to achieve objective (iii)-(2).

3) COMPLETE MODEL OF THE MG UNIT

The dynamics of PCs, DSCs, lines and loads of each MG in the MG-control layer have been modeled by (8). Therefore, in the MGC-control layer, each MG is considered as a black box and referred to the MG unit, and its corresponding model is about the dynamics of TCs and DQCs. By linearizing (12), (14)-(17), and (19)-(20) around an operating point, the small-signal dynamic model of MG unit \( k \) can be derived as

\[ \Delta \dot{X}_{\text{MG}k} = A_{\text{MG}k} \Delta X_{\text{MG}k} + B_{\text{MG}k} \Delta V_{\text{bDQ}k} + C_{\text{MG}k} \Delta \omega_g + \sum_{i \in H_k} F_{\text{MG}k} \Delta X_{\text{MG}i} + H_{\text{MG}k} \Delta v_{i}^* + I_{\text{MG}k} \Delta V_{\text{PCC}DQ} \]  

(21)

where \( \Delta V_{\text{bDQ}k} \) is the deviation of MV bus voltage \( v_{bk} \) in the common DQ-frame, \( A_{\text{MG}k}, B_{\text{MG}k}, C_{\text{MG}k}, F_{\text{MG}k} \) and \( H_{\text{MG}k} \) are parameter matrices. Note that \( F_{\text{MG}k} \) reflects the correlation between unit MG \( k \) and its neighbors \( MG_i, i \in H_k \). The state variables of each MG unit are

\[ \Delta X_{\text{MG}k} = [\Delta \delta_k, \Delta P_{\text{PCC}k}, \Delta Q_{\text{PCC}k}, \Delta \Omega_k, \Delta \lambda_k, \Delta h_k, \Delta i_{\text{PCC}DQ}, \Delta i_{\text{PCC}Q}]^T \]  

(22)

where \( \Delta i_{\text{PCC}DQ} \) and \( \Delta i_{\text{PCC}Q} \) represent the deviations of \( i_{\text{PCC}} \) in the DQ-frame.

4) CRITICAL BUS VOLTAGE CONTROLLER MODEL

State \( \psi \) is introduced to represent the dynamics of critical bus voltage controller (18), given by

\[ \psi = V_{c}^* - V_c \]  

(23)

where \( V_c \) is the magnitude which can be represented by \( v_{\text{CD}} \) and \( v_{\text{CB}} \). By linearizing (18) and (23), the model of the critical bus voltage controller can be obtained, i.e.,

\[ \Delta \dot{\psi} = -A_c [\Delta V_{\text{bDQ}}] \]  

(24)

\[ \Delta V_{c}^* = -k_p A_c [\Delta V_{\text{bDQ}}] + k_i \Delta \psi \]  

(25)

where \( \Delta v = [\Delta v_{\text{CD}}, \Delta v_{\text{CQ}}]^T \), and \( A_c \) is the parameter matrix.

5) MEDIUM VOLTAGE (MV) NETWORK AND LOAD MODELS

The RL feeder lines and the RL-type constant-impedance load are assumed in this paper. The small-signal dynamic model of MV network and load is similar to the LV network and load model in [29], and it can be derived as

\[ \Delta i_{\text{lineDQ}} = A_{net} [\Delta i_{\text{lineDQ}}] + B_{net} [\Delta V_{\text{bDQ}}] + C_{net} \Delta \omega_g \]  

(26)

\[ \Delta i_{\text{loadDQ}} = A_{load} [\Delta i_{\text{loadDQ}}] + B_{load} [\Delta V_{\text{bDQ}}] + C_{load} \Delta \omega_g \]  

(27)

where \( \Delta i_{\text{lineDQ}}, \Delta i_{\text{loadDQ}} \) and \( \Delta V_{\text{bDQ}} \) are deviations of all MV line currents, load currents and bus voltages, respectively. \( \Delta i_{\text{PCCDQ}} \) denotes \( \Delta i_{\text{PCCDQ}} \) of all the MG units. Then MV bus voltage deviations \( \Delta V_{\text{bDQ}} \) is represented as [29]

\[ \Delta V_{\text{bDQ}} = R_N (M_{\text{MG}} [\Delta i_{\text{PCCDQ}}] + M_{\text{net}} [\Delta i_{\text{lineDQ}}]) + M_{\text{load}} [\Delta i_{\text{loadDQ}}] \]  

(28)

Based on (28), the critical bus voltage \( V_c^* \) can be expressed in terms of \( \Delta i_{\text{PCCDQ}}, \Delta i_{\text{lineDQ}} \) and \( \Delta i_{\text{loadDQ}} \) and named as \( V_c^* \) expression.

6) COMPLETE MGC LAYER MODEL

Denote the state variables of all MG units in the MGC as \( X_{\text{MG}} \). Combine (21), (24), (26), (27) and replace \( \Delta V_r^*, \Delta V_{\text{bDQ}}, \Delta V_{\text{CQ}} \) with (25), (28) and \( \Delta V_{cDQ} \) expression. Then, the small-signal dynamic model of the MGC-control layer can be obtained, which is

\[ \Delta S_{\text{MG}} = A_{\text{MG}} [\Delta S_{\text{MG}}] + B_{\text{MG}} \Delta V_{\text{PCCDQ}} \]  

(29)

where \( \Delta S_{\text{MG}} = [\Delta X_{\text{MG}}, \Delta \psi, \Delta i_{\text{lineDQ}}, \Delta i_{\text{loadDQ}}]^T \), \( A_{\text{MG}}, B_{\text{MG}} \) are parameter matrices.

D. COMPLETE SMALL-SIGNAL DYNAMIC MODEL OF THE MGC

By combining \( m \) MG-control layer models (8) and MGC-control layer model (29) and then dealing with the coupling states \( \Delta V_{\text{PCC}DQ}, \Delta V_{\text{PCCQ}} \) and \( \Delta V_{\text{PCCDQ}} \), the complete MGC model can be obtained as

\[ \Delta S_{\text{sys}} = A_{\text{sys}} [\Delta S_{\text{sys}}] \]  

(30)

where \( \Delta S_{\text{sys}} = [\Delta S_{\text{MG}1}, \ldots, \Delta S_{\text{MGm}}, \Delta S_{\text{MGc}}]^T \).

The system dynamics and stability can be evaluated based on the state matrix \( A_{\text{sys}} \) in (30), as given in Section III.
control parameters are given in Appendix. Fig. 4 shows the communication networks of MG-control layer and MGC-control layer, which are assumed to have the same topology and adjacency matrix. From Fig. 4, only one root node receives reference values.

**A. SMALL-SIGNAL DYNAMIC MODEL VALIDATION BASED ON TIME-DOMAIN SIMULATION**

Based on the aforementioned typical 40-bus MGC, a time-domain validation of the small-signal dynamic model (solid line) against the non-linear model (dashed line) established in PSCAD/EMTDC is presented in Fig. 5. Load 1 suffers a step change from 150kW + 45kVar to 175kW + 65kVar at \( t = 2 \) s.

The good agreement between the solid line and dashed line in terms of frequency, voltage, active and reactive power in Fig. 5 demonstrates the accuracy and the validity of the small-signal dynamic model. The small differences during the transient are mainly due to the linearization error and the ignorance of voltage and current controller, Fig. 2, in the modeling process.

**B. INFLUENCE OF INTERCONNECTING MGS ON SYSTEM STABILITY**

1) **THE IMPACT OF INTERCONNECTION OF MG**

As illustrated in Section II, the tertiary control is responsible for interconnecting MGs as an islanded MGC. Fig. 6 presents the comparison of eigenvalue spectrums between a single MG and the MGC in Fig. 3. Note that (i) the single MG is employed with PC and DSC and operated as an island, and (ii) the MGC consists of four single MGs with PC and DSC which are interconnected with each other through TC level.

Fig. 6 indicates that the interconnection of MGs through TC will complicate the system dynamic behavior and reduce the system stability margin.

2) **THE IMPACT OF DISTRIBUTED QUATERNARY CONTROL LEVEL**

Based on the tertiary control, the distributed quaternary control is introduced to realize frequency, critical bus voltage and accurate power sharing objectives among MGs, as described at Section II. However, the neighboring communication and distributed control algorithm may further deteriorate the system dynamic performance. Fig. 7 presents a comparison of
such that the overall participation for MG-control layer states in mode $i$ is defined as

$$
\eta_{MG,i} = \frac{\| \rho_{MG,i} \|}{\| \rho_i \|} \quad (32)
$$

where $\| \cdot \|$ denotes the $L_1$-norm. Similarly, the overall participation for MGC-control layer states in mode $i$ is given by

$$
\eta_{MGC,i} = \frac{\| \rho_{MGC,i} \|}{\| \rho_i \|} \quad (32)
$$

Obviously, $\eta_{MG,i} + \eta_{MGC,i} = 1$. We define that when the MG-control layer and MGC-control layer states have a fair participation, namely $\eta_{MG,i} = \eta_{MGC,i} = 0.5$, the coupling degree is the strongest. Therefore, $C_{layer,i}$ is defined as

$$
C_{layer,i} = \sqrt{\eta_{MG,i} \times \eta_{MGC,i}} / (\eta_{MG,i} + \eta_{MGC,i})/2 
$$

(33)

where $\sqrt{\eta_{MG,i} \times \eta_{MGC,i}}$ implies a penalty. The more deviations from 0.5 of $\eta_{MG,i}$ or $\eta_{MGC,i}$, the smaller this value is. Obviously, $C_{layer,i} \in [0, 1]$ and the larger the value is, the stronger the MG and MGC layer couples.

The coupling degree among MGs is quantified by another index $C_{MG,i}$. The participation degree factor $\eta_{MG,i}$ represents participation of MG$_k$ in MG layer, given by

$$
\eta_{MG,i} = \frac{\| \rho_{MG,i} \|}{\sum_{k=1}^{m} \| \rho_{MG,k} \|} 
$$

(34)

Due to $\sum_{k=1}^{m} \eta_{MG,i} = 1$, we define that (i) when each MG has a fair participation, namely $\eta_{MG,1} = \eta_{MG,2} = \ldots = \eta_{MG,m} = \frac{1}{m}$, the coupling is the strongest, and (ii) when only one arbitrary MG$_k$ participates in mode $i$, namely $\eta_{MG,k} = 1$, the coupling is the weakest.

Therefore, $C_{MG,i}$ is defined as

$$
C_{MG,i} = 1 - \frac{m^m}{m^m} \times \prod_{k=1}^{m} \eta_{MG,k} - \frac{1}{m} \quad (35)
$$

where $m^m$ means that the more deviations from $\frac{1}{m}$ of $\eta_{MG,i}$, the smaller this value is. Obviously, $C_{MG,i}$ will be 1 in the strongest coupling situation. The scaling factor $\frac{m^m}{m^m} - 1$ is applied to convert $C_{MG,i}$ to be 0 in the weakest coupling situation.

Then, the comprehensive coupling degree index $C_i$ considering layer coupling $C_{layer,i}$ and MG coupling $C_{MG,i}$ is defined as

$$
C_i = 0.5 \times C_{layer,i} + 0.5 \times C_{MG,i} 
$$

(36)

2) PARTICIPATION FACTOR ANALYSIS

The low-frequency eigenvalue spectrum of the test MGC considering the two-layer distributed control strategy is shown in Fig. 8. Table 1 provides the dominant low-frequency modes, which are categorized as group A, B, C, and D according to their damping.

**TABLE 1.** Dominant low-frequency modes and corresponding damping ratios.

<table>
<thead>
<tr>
<th>Group</th>
<th>Damping</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>&lt;0.1</td>
</tr>
<tr>
<td>B</td>
<td>0.1–0.2</td>
</tr>
<tr>
<td>C</td>
<td>0.2–0.4</td>
</tr>
<tr>
<td>D</td>
<td>0.4–0.8</td>
</tr>
</tbody>
</table>
Modes 1, 2, 3 and 4 are respectively selected as the representative modes of group A, B, C, and D and marked with red in Fig. 8. Their corresponding participation factors of the system state variables are shown in Fig. 9. Participation factors of other modes are similar to the corresponding representative modes and thus not presented. Fig. 10 shows the damping ratio $\zeta_i$ and coupling degree $C_i$ of modes $1 \sim 4$. The analysis results of Fig. 9 and Fig. 10 are summarized as follows.

(i) Modes 1, 2, 3 are inter-MG modes which means these modes are associated with multiple MGs as shown in Fig. 9 (a), (b), and (c). Mode 1 is affected by the states of MG$1 \sim MG_4$ and mode 2 is associated with MG$1$ and MG$3$. For mode 3, its difference from modes 1 and 2 is that the participation of MGC-control layer further enhances the inter-MG coupling for mode 1 and 2 but not for mode 3. Moreover, Fig. 9(d) indicates that mode 4 is a MG local mode, which is only affected by the states of MG$4$.

(ii) The coupling degree has a strong relationship with the mode damping. As indicated in Fig. 10, the stronger the coupling degree is, the less damped the mode is.

(iii) Fig. 9 indicates that the MG-control layer states $(\Delta \delta_{ki}, \Delta P_{ki}, \Delta Q_{ki}, \Delta \omega_{ki}, \Delta \lambda_{ki}, \Delta h_k)$ and MGC-control layer states $(\Delta \delta_k, \Delta P_k, \Delta Q_k, \Delta \omega_k, \Delta \lambda_k, \Delta h_k)$ contribute to modes 1-4 in different proportions. Since the MG-control layer states associate with DSCs and MGC-control layer states associate with DQCs of (14), (15), (17), and (20), the impact of DSC and DQC parameters should be carefully analyzed.

D. IMPACT OF CONTROL PARAMETERS ON SYSTEM STABILITY

In this part, the impacts of control parameters are analyzed in two aspects: (i) ratio of DSC and DQC parameters; (ii) sensitivity analysis of DSC and DQC parameters.

1) IMPACT OF THE RATIO OF DSC AND DQC PARAMETERS
The DSC control parameter $C_{w_1}, C_{p_1}, C_{v_1}, C_{q_1}$ are chosen as (500, 50, 20 and 50). Note that $C_{w_k}$, $C_{p_k}$ are the parameters of distributed secondary frequency controller, and $C_{v_k}$, $C_{q_k}$ are the parameters of distributed secondary voltage controller. More details can be found in [27]. The DQC parameters are set as $C_{w_k} = \gamma * C_{w_1}, C_{p_k} = \gamma * C_{p_1}, C_{v_k} = \gamma * C_{v_1}, C_{q_k} = \gamma * C_{q_1}$. Fig. 11 presents the traces of low-frequency eigenvalues when $\gamma$ varies from 0.1 to 5.
Fig. 11 indicates that a relatively smaller $\gamma$ leads to a more stable system while a large value of $\gamma$ may destabilize the system. Therefore, it can be deduced that the interaction between MG-control layer and MGC-control layer has a strong impact on the system stability.

**Remark 1:** The DSC and DQC parameters are related with the response time of MG and MGC control layer, respectively. Thus, the ratio $\gamma$ actually describes the time-scale separation degree of the MG and MGC control layer. As shown by the red arrow in Fig. 2, the DSC in MG-control layer tracks the reference values from TC and DQC in MGC-control layer. It should be noted that the time constant of TC is much smaller compared with DQC and thus can be ignored in the response time of MG-control layer. Therefore, if the reference values from the DQC in MGC-control layer vary too fast, namely the response time of MGC-control layer is much smaller than that of MG-control layer, the DSC cannot follow the references and then the system becomes unstable.

2) SENSITIVITY ANALYSIS OF PARAMETERS ON STABILITY

As shown in Table 1, the damping of modes in group A is much smaller than that of MG-control layer, the DSC cannot ensure the response time of MGC-control layer. Therefore, if the ratio $\gamma$ increases from 5 to 150.

**IV. OPTIMAL DESIGN OF DISTRIBUTED CONTROL PARAMETERS**

In this section, the selection of DSC and DQC parameters is formulated as an optimization problem and solved by the particle swarm optimization (PSO) algorithm [30].

**A. PROBLEM FORMULATION**

In order to enhance the MGC stability margin and damping characteristics, the objective function of the optimization problem aims to (i) move the real part $\sigma$ of eigenvalues to a relatively far area from the imaginary axis and (ii) increase their damping ratio $\zeta$ as much as possible. The comprehensive assessment index $J$ is defined as

$$J = J_{att} + J_{osc}$$  (37)

where $J_{att}$ and $J_{osc}$ are assessment indices with respect to attenuation modes and oscillation modes, respectively. Note that the imaginary part of an attenuation mode is zero, and the imaginary part of an oscillation mode is non-zero.

As the damping ratio $\zeta$ and real part $\sigma$ are in different dimensions, they cannot be readily applied in (37). Therefore, variables $f_\sigma$ and $f_\zeta$ are introduced to normalize $|\sigma|$ and $\zeta$ within the range of 0 to 1. The normalized function $f_\sigma$ is [31]

$$f_\sigma = 1 - e^{-\frac{1}{2}(\mu - \mu_0)}, \mu \geq \mu_0$$  (38)

where $\mu_0$ and $\tau$ determine the function as shown in Fig. 13. A pre-specified point $(\mu_\sigma, 0.95)$ on the plot of Fig. 13 is used to determine $\tau$ for (38), i.e.,

$$\tau = \frac{\mu_0 - \mu_\sigma}{\ln 0.95}$$  (39)

Based on (38), $|\sigma|$ and $\zeta$ can be normalized as

$$f_{|\sigma|} = 1 - e^{-\frac{1}{|\sigma|}(\mu - \mu_0, |\sigma|)}, |\sigma| \geq \mu_0, |\sigma|$$  (40)

$$f_\zeta = 1 - e^{-\frac{1}{\zeta}(-\mu_0, \zeta)}, \mu \geq \mu_0, \zeta$$  (41)
where \( f_{\sigma_j} \) and \( f_{\zeta_j} \) are the normalization values for \(|\sigma|\) and \(\zeta\) of mode \(j\), \(\mu_0_{\sigma_j}\), \(\mu_0_{\zeta_j}\), \(\tau_s|\sigma_j|\) and \(\tau_s|\zeta_j|\) are the corresponding parameters.

Therefore, the assessment indices \( J_{att} \) and \( J_{osc} \) can be represented as

\[
J_{att} = \sum_{\rho=1}^{\alpha} w_{\rho} f_{|\sigma_{\rho}|}
\]

\[
J_{osc} = \sum_{\mu=1}^{\beta} w_{\mu} (f_{|\sigma_{\mu}|} + f_{\zeta_{\mu}})
\]

where \(\alpha\) is the total number of attenuation modes, \(w_{\rho}\) is the weighting factor and satisfies \(\sum_{\rho=1}^{\alpha} w_{\rho} = 1\), \(\beta\) is the total number of oscillation modes, and \(w_{\mu}\) is the weighting factor and satisfies \(\sum_{\mu=1}^{\beta} w_{\mu} = 1\).

To optimize the system stability margin and damping, index \(J\) must be maximized. Therefore, the optimization problem is formulated as

\[
\max J = J_{att} + J_{osc}
\]

\[
\begin{align*}
|\lambda I - A_{sys}| & = 0, \\
C_{w_{\text{DG}}} & \leq C_{w_{\text{DG}}} \leq C_{w_{\text{DG}}}, \\
C_{p_{\text{DG}}} & \leq C_{p_{\text{DG}}} \leq C_{p_{\text{DG}}}, \\
C_{v_{\text{DG}}} & \leq C_{v_{\text{DG}}} \leq C_{v_{\text{DG}}}, \\
C_{q_{\text{DG}}} & \leq C_{q_{\text{DG}}} \leq C_{q_{\text{DG}}}, \\
C_{w_{\text{MG}}} & \leq C_{w_{\text{MG}}} \leq C_{w_{\text{MG}}}, \\
C_{p_{\text{MG}}} & \leq C_{p_{\text{MG}}} \leq C_{p_{\text{MG}}}, \\
C_{v_{\text{MG}}} & \leq C_{v_{\text{MG}}} \leq C_{v_{\text{MG}}}, \\
C_{q_{\text{MG}}} & \leq C_{q_{\text{MG}}} \leq C_{q_{\text{MG}}},
\end{align*}
\]

where \(\lambda\) is the eigenvalue of \(A_{sys}\), \(I\) is the identity matrix. The control parameters of MG-control layer (\(C_{v_{ki}}, C_{p_{ki}}, C_{v_{ki}}, C_{q_{ki}}\)) and MGC-control layer (\(C_{w_{k}}, C_{p_{k}}, C_{v_{k}}, C_{q_{k}}\)) are chosen as optimization variables. To simplify analysis, the DSC parameters of each DG unit are represented by \(C_{w_{DG}}, C_{p_{DG}}, C_{v_{DG}}, C_{q_{DG}}\), and the DQC parameters are represented by \(C_{w_{MG}}, C_{p_{MG}}, C_{v_{MG}}, C_{q_{MG}}\). They are constrained by the corresponding lower limits and upper limits as shown in (44).

**B. PSO IMPLEMENTATION**

Problem (44) is a non-linear and non-convex optimization problem, which also includes eigenvalues constraints. Thus, PSO is adopted to solve this problem to obtain the optimal distributed control parameters. Fig. 14 depicts the computational flowchart of the method. The overall optimization process can be described in the following steps:

- **Step 1** (Initialization): generate a random particle population and generate randomly initial velocities and positions for each particle.
- **Step 2** (Obtain Eigenvalues): choose the first particle and calculate the corresponding eigenvalues via matrix \(A_{sys}\) in (30). Note that the position vector of each particle consists of DSC and DQC parameters.
- **Step 3** (Obtain \(\sigma\) and \(\zeta\) and Normalization): obtain the real part \(\sigma\) of attenuation modes and oscillation modes, and calculate the damping ratio \(\zeta\) of the oscillation modes. Then, normalize \(\sigma\) and \(\zeta\) by (40) and (41), respectively.
- **Step 4** (Calculate \(J\) for Each Particle \(i\) at Iteration \(k\)): calculate \(J_{att_i}\) and \(J_{osc_i}\) by (42) and (43), respectively. Then, the final objective function \(J_i^k\) can be obtained by (44).
- **Step 5** (Individual Best Updating): update \(J_i^k\) for each particle in the population. If \(J_i^k > J_{i,\text{best}}\), then update the individual best \(J_{i,\text{best}} = J_i^k\) and go to the next step; else do not update and go to the next step.
- **Step 6** (Global Best Updating): Search for the maximum value \(J_{\text{max}}\) among the individual best \(J_{i,\text{best}}\). If \(J_{\text{max}} > J_{g,\text{best}}\),
then update global best as $J_{g,best} = J_{max}$ and go to the next step; else do not update and go to the next step.

*Step 7) (Stopping Criteria):* The search process will be terminated if the number of iterations is greater than a pre-specified number.

### V. CASE STUDY

To evaluate the proposed optimal parameter design method, stability assessment and time-domain simulation studies in the PSCAD/EMTDC platform are carried out based on the 40-bus MGC shown in Fig. 3 and Fig. 4. The parameters are given in Appendix.

#### A. STABILITY ASSESSMENT

Based on the optimal design method introduced at Section IV, the MG-control layer and MGC-control layer parameters are optimized and the results are given in Appendix. The convergence performance of the PSO method, shown in Fig. 15, indicates that the objective value converges to the maximum value 2.61 around the 20th iteration, which shows a good convergence performance of the PSO based method.

![Figure 15. Convergence result of the PSO-based distributed control parameter optimization.](image)

**TABLE 2.** Coupling degree comparison before and after optimization.

<table>
<thead>
<tr>
<th></th>
<th>Before optimization</th>
<th>After optimization</th>
</tr>
</thead>
<tbody>
<tr>
<td>$C_{ave}$</td>
<td>0.9403</td>
<td>0.5654</td>
</tr>
<tr>
<td>$C_l$</td>
<td>0.9992</td>
<td>0.9395</td>
</tr>
</tbody>
</table>

#### B. TIME-DOMAIN SIMULATION RESULTS

This subsection is organized into two studies. Study 1 evaluates the stability enhancement effect with the optimally designed two-layer distributed controllers. Study 2 validates the robustness of the proposed method under sudden load changes.

1) STUDY 1: STABILITY ENHANCEMENT EVALUATION

The PCs are initially engaged and the DSCs and TCs are activated at $t = 1.5s$. DQCs are employed at $t = 3s$. Fig. 17 and Fig. 18 present the active and reactive power outputs of MGs and DGs under initial control parameters and

![Figure 16. Comparison of eigenvalue spectrum before and after optimization.](image)

![Figure 17. Study 1: active and reactive output of MG1-MG4. (a) and (b): before optimization; (c) and (d): after optimization.](image)
optimal control parameters, respectively. Note that only the output power of DGs in MG₄ is presented for simplification. Fig. 19 shows the comparison results of system frequency and critical bus voltage. Comparisons of Fig. 17, 18 and 19 reveal that the system stability is enhanced by the optimally designed control parameters.

Moreover, considering the four control objectives in Section II, Fig. 17, 18, and 19 indicate that the optimal design of control parameter does not interfere with the system steady-state performance, because the control strategy can achieve objective (i): restoration of the system frequency to the rated value 50 Hz, Fig. 19(a), objective (ii): restoration of the PCC voltage to the rated value 1 p.u., Fig. 19(b), objective (iii): accurate active and reactive power sharing among MGs with the ratios of $P_{PCC1}/P_{PCC4}$ being 1:2:1:1 and $Q_{PCC1}/Q_{PCC4}$ being 1:1.5:1:1.5, Fig. 17(c) and (d), and objective (iv): accurate active and reactive power sharing among DGs within MG₄ with the ratios of $P_{41}/P_{44}$ being 1:1:1:1 and $Q_{41}/Q_{44}$ being 1:1:1:1, Fig. 18(c) and (d).

Remark 2: with the optimal control parameters, the overshoot of active and reactive power responses is decreased and the corresponding settling time is decreased. However, due to the coupling/interaction among MGs and multiple control layers, a certain degree of oscillation still exists. A possible way to further mitigate the oscillation is to introduce supplementary controllers. This is beyond the scope of this paper and will be investigated in future work.

2) STUDY 2: SUDDEN LOAD CHANGE

To evaluate the system dynamic performance when suffering sudden load changes, 50% of load 1 is switched off at $t = 2.5s$ and load 7 is switched off at $t = 3.5s$. The reactive power outputs of MGs under initial control parameters and optimal control parameters are presented in Fig. 20(a) and (b), respectively. The reactive power outputs of DGs in MG₄ under initial control parameters and optimal control parameters are presented in Fig. 21(a) and (b), respectively.

Comparisons in Fig. 20 and 21 indicate that the controller with optimal parameters can mitigate the oscillations and improve the system stability, which validates the robustness of the controllers with optimal parameters under significant load changes.

VI. CONCLUSIONS

This paper presents a detailed small-signal stability analysis and optimal control parameters design method for MGC with the two-layer distributed control strategy. The small-signal stability analysis reveals that (i) the interconnection of MGs and the neighboring communication of distributed control algorithm may introduce new low-damping modes to the system, (ii) the coupling degree of a mode has an opposite relationship with its damping ratio, (iii) the mode damping is affected by multiple parameters of both MG and MGC control layer. Based on the small-signal dynamic model, the design of MG and MGC layer control parameters is formulated as an optimization problem and the optimal control parameters are solved by PSO algorithm. Eigenvalue analysis and
time-domain simulation on a test MGC system validate that with the proposed optimal control parameter design method, the stability performance of the MGC is improved.

APPENDIX

Table 3 provides the electrical parameters of the test MGC in Fig. 3. Table 4 provides the parameters of PCs and TCS. Tables 5 and 6 provide the control parameters of DSCs and DCQCs before and after optimization, respectively.

TABLE 3. Electrical parameters of MGC.

<table>
<thead>
<tr>
<th>Line</th>
<th>MV line: 0.069+j0.099Ω</th>
<th>LV line: 0.284+j0.083Ω</th>
</tr>
</thead>
<tbody>
<tr>
<td>MV load:</td>
<td>Load=150kW+45kvar</td>
<td>Load=75kW+22.5kvar</td>
</tr>
<tr>
<td>Load:</td>
<td>Load=25kW+7.5kvar</td>
<td>Load=20kW+5kvar</td>
</tr>
<tr>
<td>Transformer</td>
<td>Loaded=15kW+7.5kvar,Load=12kW+5kvar</td>
<td></td>
</tr>
<tr>
<td>Coupling</td>
<td>Transformer</td>
<td>Lc=0.1mH</td>
</tr>
</tbody>
</table>

TABLE 4. Parameters of PCs and TCS.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>DGs in MG, and MG4</th>
<th>DGs in MG, and MG4</th>
<th>MG1, MG3</th>
<th>MG1, MG3</th>
</tr>
</thead>
<tbody>
<tr>
<td>(D_{Q1}/D_{Q2}) (Hz/kW - 10^{-7})</td>
<td>16.67</td>
<td>20</td>
<td>5.56</td>
<td>6.67</td>
</tr>
<tr>
<td>(D_{Q1}/D_{Q2}) (kV/kvar - 10^{-3})</td>
<td>0.7775</td>
<td>0.5183</td>
<td>0.26</td>
<td>0.173</td>
</tr>
<tr>
<td>(P_{max}/P_{MG}) (kW)</td>
<td>60</td>
<td>50</td>
<td>120</td>
<td>100</td>
</tr>
<tr>
<td>(Q_{max}/Q_{MG}) (kvar)</td>
<td>20</td>
<td>30</td>
<td>40</td>
<td>60</td>
</tr>
</tbody>
</table>

TABLE 5. Parameters of DSCs and DCQCs before optimization.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>DSC level</th>
<th>DQC level</th>
</tr>
</thead>
<tbody>
<tr>
<td>(c_{uk1}/c_{uk})</td>
<td>490</td>
<td>3018</td>
</tr>
<tr>
<td>(c_{ph1}/c_{ph})</td>
<td>85</td>
<td>3243</td>
</tr>
<tr>
<td>(c_{uk1}/c_{uk})</td>
<td>28</td>
<td>58</td>
</tr>
<tr>
<td>(c_{ph1}/c_{ph})</td>
<td>10</td>
<td>26</td>
</tr>
</tbody>
</table>

TABLE 6. Parameters of DSCs and DCQCs after optimization.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>DSC level</th>
<th>DQC level</th>
</tr>
</thead>
<tbody>
<tr>
<td>(c_{uk1}/c_{uk})</td>
<td>550</td>
<td>2530</td>
</tr>
<tr>
<td>(c_{ph1}/c_{ph})</td>
<td>45</td>
<td>2640</td>
</tr>
<tr>
<td>(c_{uk1}/c_{uk})</td>
<td>20</td>
<td>15</td>
</tr>
<tr>
<td>(c_{ph1}/c_{ph})</td>
<td>90</td>
<td>23</td>
</tr>
</tbody>
</table>

REFERENCES


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